



# Proceeding Paper Catalytic Performance of Doped Ni<sub>2</sub>P Surfaces for Ammonia Synthesis <sup>+</sup>

Abdulrahman Almithn 匝

Department of Chemical Engineering, College of Engineering, King Faisal University, Al Ahsa 31982, Saudi Arabia; aalmithn@kfu.edu.sa

<sup>+</sup> Presented at the 4th International Electronic Conference on Applied Sciences, 27 October–10 November 2023; Available online: https://asec2023.sciforum.net/.

**Abstract:** Ammonia is a key ingredient in fertilizer production, but its synthesis using the conventional Haber–Bosch process over metal-based catalysts is energy intensive. Prior investigations revealed that metal catalysts suffer from a trade-off between N<sub>2</sub> activation and N\* binding strength, hindering their overall reactivity. Metal phosphide catalysts are promising alternatives to conventional metal catalysts due to their unique reactivity and stability. Here, we used DFT to study the catalytic performance of Ni<sub>2</sub>P catalysts doped with Fe and Ru for ammonia synthesis. We show that H-assisted N–N activation may provide a new route to circumvent the N<sub>2</sub> dissociation scaling relationships.

Keywords: ammonia synthesis; nitrogen dissociation; nickel phosphide

# 1. Introduction

Ammonia (NH<sub>3</sub>) holds a crucial position in various aspects of modern society. Its significance spans from agriculture to industry, making it an essential molecule for the global economy and sustainability efforts. It serves as a fundamental building block for the production of fertilizers, which are essential for enhancing crop yields and ensuring food security for a growing global population [1]. Additionally, ammonia finds applications in diverse sectors, including chemicals, pharmaceuticals, and even renewable energy storage. The Haber–Bosch process revolutionized agricultural productivity in the early 20th century by converting atmospheric nitrogen into ammonia over Fe-based catalysts and contributing to the large-scale production of synthetic fertilizers [2]. However, despite its immense importance, ammonia synthesis presents a range of formidable challenges.

The nitrogen  $(N_2)$  dissociation step is believed to be the rate-limiting step in ammonia synthesis [3–6]. Cleaving the strong  $N \equiv N$  bond requires high temperatures and pressures over the conventional ammonia synthesis catalysts (Fe and Ru). The surface intermediates  $(NH_x; x = 0-3)$  formed during ammonia synthesis often bind too strongly to most transition metal catalysts under ambient conditions; thus, elevated temperatures and pressures are necessary to maintain a favorable exergonic nature of the overall reaction [7]. The catalytic reduction of dinitrogen to ammonia under mild conditions is a long-standing challenge in catalysis. The goal is to find a catalyst that can bind the  $NH_x$  species weakly while also maintaining a low energy barrier for N<sub>2</sub> dissociation. Computational assessments using density functional theory (DFT), however, have revealed a significant limitation: the N–N transition state energy cannot be adjusted without influencing the binding energy of  $NH_x$  to the surface due to the presence of a Brønsted–Evans–Polanyi (BEP) scaling relationship for transition metal surfaces [8-11]. Decreasing the N<sub>2</sub> activation barrier also increases the binding strength of  $NH_x$ , thus hindering subsequent hydrogenation reactions and the production of NH<sub>3</sub>. These studies have concluded that the turnover rate for ammonia synthesis as a function of N\* binding energy for several transition metals



Citation: Almithn, A. Catalytic Performance of Doped Ni<sub>2</sub>P Surfaces for Ammonia Synthesis. *Eng. Proc.* 2023, *56*, 53. https://doi.org/ 10.3390/ASEC2023-15319

Academic Editor: Manoj Gupta

Published: 21 November 2023



**Copyright:** © 2023 by the author. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). follows a volcano-shaped curve, with Fe and Ru being the only metals that are close to the optimum.

A logical approach to catalyst design was suggested, involving the combination of metals positioned on opposite sides of the volcano to achieve the desired interaction with nitrogen intermediates. For example, combining Co, which binds N\* too weakly, with Mo, which binds N\* too strongly in the Co–Mo catalyst, leads to a material that has ammonia synthesis activity similar to that of Ru [12]. Many subsequent studies have focused on finding ways to circumvent the scaling relationship using different catalytic materials, such as metal nitrides [13], hydrides [14], and oxides [15]. Electrochemical N<sub>2</sub> reduction has also emerged as an alternative approach for synthesizing NH<sub>3</sub> at ambient conditions, but the development of efficient electrochemical catalysts remains a key challenge [16-18]. Here, we explore the catalytic performance of the  $Ni_2P$  catalyst doped with Fe and Ru for ammonia synthesis using DFT. We have previously shown that incorporating phosphorus atoms in nickel phosphide catalysts can alter the catalytic behavior of Ni atoms, leading to improved selectivity for various catalytic reactions [19–21]. The P atoms introduce weak binding surface sites that disrupt the metal ensembles. We also explore H-assisted N-N activation pathways involving diazene  $(N_2H_2)$  and hydrazine  $(N_2H_4)$  to weaken the N–N bond prior to activation.

### 2. Computational Methods

Periodic plane-wave DFT calculations were performed using the Vienna ab initio simulation package (VASP) [22–25] and the computational catalysis interface (CCI) [26]. The RPBE form of the generalized gradient approximation and PAW pseudopotentials were used [27–31]. The Ni<sub>2</sub>P(001) surface was constructed from bulk Ni<sub>2</sub>P, as described in more detail in our previous work [19]. Figure 1 shows the top and side views of the  $2 \times 2 \text{ Ni}_2\text{P}(001)$  surface used in this study. The bottom two atomic layers were constrained during geometric relaxation. Electronic energies were converged to within  $10^{-6}$  eV, and forces were converged to less than  $0.05 \text{ eVÅ}^{-1}$  with a *k*-point mesh of  $3 \times 3 \times 1$  [32,33]. Transition state structures were identified using the nudged elastic band (NEB) method and the dimer method [34–36]. The Ni<sub>2</sub>P(001) surface was modified by substituting a surface Ni atom (highlighted in Figure 1a) with either a Fe or Ru atom. This procedure mirrors the approach employed in a prior investigation using doped Ni<sub>2</sub>P surfaces [37]. The formation energies of doped Ni<sub>2</sub>P surfaces were calculated using the following formula:

$$E_f = E_{\rm M/Ni2P} + E_{\rm Ni} - E_{\rm Ni2P} - E_{\rm M} \tag{1}$$

where  $E_{\text{Ni}}$  and  $E_{\text{M}}$  are the energies of a single Ni atom and a single metal atom. The Ru–Ni<sub>2</sub>P surface has a formation energy of -2.050 eV compared to -1.129 eV for Fe–Ni<sub>2</sub>P, indicating that Ru–Ni<sub>2</sub>P is more stable. Additional calculations were run using the pure 3 × 3 Fe(110) and Ru(001) surfaces for comparison. Spin-polarized calculations were exclusively applied to the Fe(110) and Fe–Ni<sub>2</sub>P doped surfaces, as the energy discrepancy between spin-polarized and non-spin-polarized calculations exceeded  $10^{-3}$  eV.



**Figure 1.** The top (**a**) and side (**b**) views of the doped  $Ni_2P(001)$  surface model. Labels indicate different surface sites.

## 3. Results and Discussion

#### 3.1. NH<sub>x</sub> Species Binding Energies

In this section, we investigate the preferred adsorption configuration and binding energies of different NH<sub>x</sub> species over Ni<sub>2</sub>P, as well as doped Fe–Ni<sub>2</sub>P and Ru–Ni<sub>2</sub>P catalysts. For the sake of comparison, we also included the binding energies over pure Fe(110) and Ru(001) surfaces. The binding energies shown in Table 1 are calculated with respect to the gas-phase species and bare surfaces (i.e.,  $\Delta E_{ads} = E_{species/surf} - E_{species(g)} - E_{surf}$ ). Diatomic nitrogen (N<sub>2</sub>) vertically adsorbs on the metal atop site (M<sub>1</sub>) over Ni<sub>2</sub>P with a binding energy of -25 kJ mol<sup>-1</sup>. This binding energy increases to -35 kJ mol<sup>-1</sup> for Fe–Ni<sub>2</sub>P and -50 kJ mol<sup>-1</sup> for Ru–Ni<sub>2</sub>P. For the NH<sub>x</sub>\* species, the binding strength increases as the number of hydrogen atoms bonded to the N atom decreases, i.e., NH<sub>3</sub>\* binds most weakly to the surface, whereas N\* has the highest binding energy. This reflects the increasing stability of the more saturated NH<sub>x</sub>\* species in the gas phase, and they coordinate with fewer metal atoms upon adsorption. For example, N\* and NH\* bind to the metal 3-fold (M<sub>3</sub>) site, whereas NH<sub>2</sub> and NH<sub>3</sub> bind to the bridging (M<sub>2</sub>) and atop (M<sub>1</sub>) sites, respectively (Figure 2).

**Table 1.** The binding energies ( $\Delta E_{ads}$  in kJ mol<sup>-1</sup>) of N<sub>2</sub>\*, H\*, and NH<sub>x</sub> (x = 0–3) over the catalytic surfaces examined in this study.

	Ni <sub>2</sub> P(001)		Fe-Ni <sub>2</sub> P(001)		Ru–Ni <sub>2</sub> P(001)		Fe(110)		Ru(001)	
Species	Mode	$\Delta E_{ads}$	Mode	$\Delta E_{ads}$	Mode	$\Delta E_{\rm ads}$	Mode	$\Delta E_{\rm ads}$	Mode	$\Delta E_{\rm ads}$
N <sub>2</sub> *	$M_1$	-25	$M_1$	-35	$M_1$	-50	$M_1$	-95	$M_1$	-34
H*	$M_3$	-222	M3	-240	M3	-246	M3	-288	M3	-262
N*	$M_3$	-375	M3	-435	M3	-445	$M_4$	-601	M3	-551
NH*	$M_3$	-325	M3	-353	M3	-365	M3	-528	M3	-437
NH <sub>2</sub> *	$M_2$	-224	M <sub>2</sub>	-235	M <sub>2</sub>	-256	M <sub>2</sub>	-326	M3	-213
NH <sub>3</sub> *	$M_1$	-60	M <sub>1</sub>	-50	M <sub>1</sub>	-74	M <sub>1</sub>	-109	$M_1$	-63



**Figure 2.** Adsorbed NH<sub>*x*</sub> (x = 0–3) species over Fe–Ni<sub>2</sub>P (**a**–**d**) and Ru–Ni<sub>2</sub>P (**e**–**h**) catalysts. The adsorption configuration and binding energies ( $\Delta E_{ads}$  in kJ mol<sup>-1</sup>) are shown beneath each image.

We also observe a general trend in binding energies across examined surfaces where the binding strength for each species generally increases as  $Ni_2P \rightarrow Fe-Ni_2P \rightarrow Ru-Ni_2P$  $\rightarrow Ru \rightarrow Fe$  with few exceptions. If we consider the N\* binding energy as a proxy for the catalytic activity towards N–N bond activation within N<sub>2</sub>, following the principles of Brønsted–Evans–Polanyi (BEP) scaling relations [8–11], it can be inferred that Ni<sub>2</sub>P is likely to exhibit weak activity. Conversely, Fe and Ru-doped Ni<sub>2</sub>P catalysts are expected to demonstrate higher activity compared to pure Ni<sub>2</sub>P, although falling short of the reactivity of Fe- and Ru-based catalysts. However, this also means that Fe- and Ru-based catalysts are more prone to deactivation due to the strongly bound N\* or NH\* than phosphide-based catalysts.

### 3.2. N–N Activation Reactions

Here, we examine the N–N bond cleavage reactions in N<sub>2</sub>\*, N<sub>2</sub>H<sub>2</sub>\*, and N<sub>2</sub>H<sub>4</sub>\*, as shown in Figure 3. Over the Ru(001) surface, adsorbed N<sub>2</sub>\* undergoes N–N bond activation with a forward activation barrier ( $\Delta E_a$ ) of 168 kJ mol<sup>-1</sup> to form two nitrogen atoms (2N\*) both adsorbed on separate 3-fold sites. This reaction is slightly endothermic with a reaction energy ( $\Delta E_{rxn}$ ) of 13 kJ mol<sup>-1</sup>. These results are consistent with previous studies on Ru(001) flat surfaces [38]. On both Fe-Ni<sub>2</sub>P and Ru-Ni<sub>2</sub>P surfaces, N<sub>2</sub>\* dissociates to 2N\* with a much larger activation barrier of 350 kJ mol<sup>-1</sup> and a highly endothermic reaction energy. This reaction starts with N<sub>2</sub>\* vertically adsorbed on the doped metal atom. After the N–N bond cleavage, the N\* atoms bind to nearby 3-fold sites. We have attempted this reaction and even the other H-assisted N–N bond activation reactions in N<sub>2</sub>H<sub>2</sub> and N<sub>2</sub>H<sub>4</sub> over the undoped Ni<sub>2</sub>P surface, but we were not able to identify stable transition states. The trends in N\* binding energy discussed in Section 3.1 indeed correlate with the calculated N–N bond activation barriers over these materials.



**Figure 3.** Reaction coordinate diagram for N–N bond activation in N<sub>2</sub>\*, N<sub>2</sub>H<sub>2</sub>\*, and N<sub>2</sub>H<sub>4</sub>\* over Fe–Ni<sub>2</sub>P (red), Ru–Ni<sub>2</sub>P (blue), and Ru (black). Images display the reactants, transition state, and product structures over Fe–Ni<sub>2</sub>P (top) and Ru–Ni<sub>2</sub>P (bottom).

We next examine the N–N bond activation reactions in diazine  $(N_2H_2)$  and hydrazine  $(N_2H_4)$  to investigate whether hydrogenating N<sub>2</sub> can weaken the N–N bond prior to its activation. Figure 3 shows that the activation barrier of the N–N bond in adsorbed N<sub>2</sub>H<sub>2</sub>\* dramatically decreased by more than 220 kJ mol<sup>-1</sup> over both Fe–Ni<sub>2</sub>P and Ru–Ni<sub>2</sub>P surfaces (121 and 129 kJ mol<sup>-1</sup>, respectively) compared to direct N<sub>2</sub>\* dissociation (350 kJ mol<sup>-1</sup>). Breaking the N–N bond in N<sub>2</sub>H<sub>4</sub> also exhibits a similar barrier of 128 kJ mol<sup>-1</sup> over Ru-Ni<sub>2</sub>P, but the barrier for this reaction over Fe-Ni<sub>2</sub>P increases to 143 kJ mol<sup>-1</sup>. We expect a similar decrease in the activation barrier of H-assisted N–N activation over a pure Ru(001) surface; however, the resulting NH\* also strongly binds to the surface (Table 1), which may render

the active sites inert. The more facile activation of the N–N bond in  $N_2H_2^*$  over both Fe–Ni<sub>2</sub>P and Ru-Ni<sub>2</sub>P-doped surfaces, coupled with the weaker binding of the product NH<sup>\*</sup>, may open the door for a promising pathway that avoids the current paradigm of direct  $N_2$  dissociation. However, it is important to note that further analysis of the hydrogenation reactions to produce  $N_2H_2$  and eventually NH<sub>3</sub> over these materials is necessary to fully ascertain the viability of this pathway.

#### 4. Conclusions

In this work, we investigated the binding energies of various NH<sub>x</sub> species and the N–N bond activation energy over Ni<sub>2</sub>P catalysts doped with Fe and Ru using DFT. Our results indicate that the NH<sub>x</sub> species with fewer hydrogen atoms bind more strongly to the catalytic surfaces, and the binding strength generally increases as Ni<sub>2</sub>P  $\rightarrow$  Fe–Ni<sub>2</sub>P  $\rightarrow$  Ru–Ni<sub>2</sub>P  $\rightarrow$  Ru  $\rightarrow$  Fe. This trend is reflected in the relative activity of these catalytic surfaces towards direct N<sub>2</sub>\* dissociation, with Ru being the most active and Ni<sub>2</sub>P the least active surface. However, we show that hydrogenating the N<sub>2</sub>\* prior to N–N bond cleavage can dramatically decrease the activation barrier over doped Ni<sub>2</sub>P surfaces. These findings suggest that the H-assisted N–N bond activation may play a crucial role in reducing the activation energy required for ammonia synthesis over these surfaces without a concomitant increase in the binding strength of the NH<sub>x</sub> species. Further investigation into the underlying mechanisms of this catalytic process could potentially lead to enhanced strategies for nitrogen activation and ammonia synthesis.

Funding: This research received no external funding.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Data are contained within the article.

Conflicts of Interest: The author declares no conflict of interest.

#### References

- Erisman, J.W.; Sutton, M.A.; Galloway, J.; Klimont, Z.; Winiwarter, W. How a Century of Ammonia Synthesis Changed the World. Nat. Geosci. 2008, 1, 636–639. [CrossRef]
- Smil, V. Enriching the Earth: Fritz Haber, Carl Bosch, and the Transformation of World Food Production; MIT Press: Cambridge, MA, USA, 2004; ISBN 0262693135.
- 3. Boudart, M. Kinetics and Mechanism of Ammonia Synthesis. *Catal. Rev.* **1981**, 23, 1–15. [CrossRef]
- 4. Honkala, K.; Hellman, A.; Remediakis, I.N.; Logadottir, A.; Carlsson, A.; Dahl, S.; Christensen, C.H.; Nørskov, J.K. Ammonia Synthesis from First-Principles Calculations. *Science* 2005, 307, 555–558. [CrossRef]
- 5. Schlögl, R. Catalytic Synthesis of Ammonia—A "Never-Ending Story"? Angew. Chem. Int. Ed. 2003, 42, 2004–2008. [CrossRef]
- Ertl, G. Surface Science and Catalysis—Studies on the Mechanism of Ammonia Synthesis: The P. H. Emmett Award Address. *Catal. Rev.* 1980, 21, 201–223. [CrossRef]
- Vojvodic, A.; Medford, A.J.; Studt, F.; Abild-Pedersen, F.; Khan, T.S.; Bligaard, T.; Nørskov, J.K. Exploring the Limits: A Low-Pressure, Low-Temperature Haber–Bosch Process. *Chem. Phys. Lett.* 2014, 598, 108–112. [CrossRef]
- Logadottir, A.; Rod, T.H.; Nørskov, J.K.; Hammer, B.; Dahl, S.; Jacobsen, C.J.H. The Brønsted-Evans-Polanyi Relation and the Volcano Plot for Ammonia Synthesis over Transition Metal Catalysts. J. Catal. 2001, 197, 229–231. [CrossRef]
- Munter, T.R.; Bligaard, T.; Christensen, C.H.; Nørskov, J.K. BEP Relations for N<sub>2</sub> Dissociation over Stepped Transition Metal and Alloy Surfaces. *Phys. Chem. Chem. Phys.* 2008, 10, 5202. [CrossRef]
- Nørskov, J.K.; Bligaard, T.; Hvolbæk, B.; Abild-Pedersen, F.; Chorkendorff, I.; Christensen, C.H. The Nature of the Active Site in Heterogeneous Metal Catalysis. *Chem. Soc. Rev.* 2008, 37, 2163. [CrossRef]
- 11. Medford, A.J.; Vojvodic, A.; Hummelshøj, J.S.; Voss, J.; Abild-Pedersen, F.; Studt, F.; Bligaard, T.; Nilsson, A.; Nørskov, J.K. From the Sabatier Principle to a Predictive Theory of Transition-Metal Heterogeneous Catalysis. J. Catal. 2015, 328, 36–42. [CrossRef]
- 12. Jacobsen, C.J.H.; Dahl, S.; Clausen, B.G.S.; Bahn, S.; Logadottir, A.; Nørskov, J.K. Catalyst Design by Interpolation in the Periodic Table: Bimetallic Ammonia Synthesis Catalysts. *J. Am. Chem. Soc.* **2001**, *123*, 8404–8405. [CrossRef]
- Zeinalipour-Yazdi, C.D.; Hargreaves, J.S.J.; Catlow, C.R.A. Nitrogen Activation in a Mars–van Krevelen Mechanism for Ammonia Synthesis on Co<sub>3</sub>Mo<sub>3</sub>N. J. Phys. Chem. C 2015, 119, 28368–28376. [CrossRef]
- 14. Wang, P.; Chang, F.; Gao, W.; Guo, J.; Wu, G.; He, T.; Chen, P. Breaking Scaling Relations to Achieve Low-Temperature Ammonia Synthesis through LiH-Mediated Nitrogen Transfer and Hydrogenation. *Nat. Chem.* **2017**, *9*, 64–70. [CrossRef]

- Vojvodic, A.; Calle-Vallejo, F.; Guo, W.; Wang, S.; Toftelund, A.; Studt, F.; Martínez, J.I.; Shen, J.; Man, I.C.; Rossmeisl, J.; et al. On the Behavior of Brønsted-Evans-Polanyi Relations for Transition Metal Oxides. *J. Chem. Phys.* 2011, 134, 244509. [CrossRef]
- Choi, C.; Back, S.; Kim, N.-Y.; Lim, J.; Kim, Y.-H.; Jung, Y. Suppression of Hydrogen Evolution Reaction in Electrochemical N<sub>2</sub> Reduction Using Single-Atom Catalysts: A Computational Guideline. ACS Catal. 2018, 8, 7517–7525. [CrossRef]
- Liu, C.; Li, S.; Li, Z.; Zhang, L.; Chen, H.; Zhao, D.; Sun, S.; Luo, Y.; Alshehri, A.A.; Hamdy, M.S.; et al. Ambient N<sub>2</sub>-to-NH<sub>3</sub> Fixation over a CeO<sub>2</sub> Nanoparticle Decorated Three-Dimensional Carbon Skeleton. *Sustain. Energy Fuels* 2022, *6*, 3344–3348. [CrossRef]
- Wang, F.; Zhang, L.; Wang, T.; Zhang, F.; Liu, Q.; Zhao, H.; Zheng, B.; Du, J.; Sun, X. In Situ Derived Bi Nanoparticles Confined in Carbon Rods as an Efficient Electrocatalyst for Ambient N<sub>2</sub> Reduction to NH<sub>3</sub>. *Inorg. Chem.* 2021, 60, 7584–7589. [CrossRef]
- 19. Witzke, M.E.; Almithn, A.; Conrad, C.L.; Hibbitts, D.D.; Flaherty, D.W. Mechanisms and Active Sites for C–O Bond Rupture within 2-Methyltetrahydrofuran over Ni, Ni<sub>12</sub>P<sub>5</sub>, and Ni<sub>2</sub>P Catalysts. *ACS Catal.* **2018**, *8*, 7141–7157. [CrossRef]
- Almithn, A.; Alhulaybi, Z. A Mechanistic Study of Methanol Steam Reforming on Ni<sub>2</sub>P Catalyst. *Catalysts* 2022, 12, 1174. [CrossRef]
- 21. Almithn, A.; Alghanim, S.N.; Mohammed, A.A.; Alghawinim, A.K.; Alomaireen, M.A.; Alhulaybi, Z.; Hossain, S.S. Methane Activation and Coupling Pathways on Ni<sub>2</sub>P Catalysts. *Catalysts* **2023**, *13*, 531. [CrossRef]
- 22. Kresse, G.; Hafner, J. Ab Initio Molecular Dynamics for Liquid Metals. Phys. Rev. B 1993, 47, 558–561. [CrossRef]
- 23. Kresse, G.; Hafner, J. Ab Initio Molecular-Dynamics Simulation of the Liquid-Metal–Amorphous-Semiconductor Transition in Germanium. *Phys. Rev. B* 1994, 49, 14251–14269. [CrossRef]
- 24. Kresse, G.; Furthmüller, J. Efficient Iterative Schemes for Ab Initio Total-Energy Calculations Using a Plane-Wave Basis Set. *Phys. Rev. B* **1996**, *54*, 11169–11186. [CrossRef]
- 25. Kresse, G.; Furthmüller, J. Efficiency of Ab-Initio Total Energy Calculations for Metals and Semiconductors Using a Plane-Wave Basis Set. *Comput. Mater. Sci.* **1996**, *6*, 15–50. [CrossRef]
- 26. Kravchenko, P.; Plaisance, C.; Hibbitts, D. A New Computational Interface for Catalysis. ChemRxiv 2019, preprint.
- 27. Hammer, B.; Hansen, L.B.; Nørskov, J.K. Improved Adsorption Energetics within Density-Functional Theory Using Revised Perdew-Burke-Ernzerhof Functionals. *Phys. Rev. B* **1999**, *59*, 7413–7421. [CrossRef]
- Perdew, J.P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* 1996, 77, 3865–3868. [CrossRef]
- 29. Zhang, Y.; Yang, W. Comment on "Generalized Gradient Approximation Made Simple". Phys. Rev. Lett. 1998, 80, 890. [CrossRef]
- 30. Blöchl, P.E. Projector Augmented-Wave Method. Phys. Rev. B 1994, 50, 17953–17979. [CrossRef]
- 31. Kresse, G.; Joubert, D. From Ultrasoft Pseudopotentials to the Projector Augmented-Wave Method. *Phys. Rev. B* 1999, *59*, 1758–1775. [CrossRef]
- 32. Monkhorst, H.J.; Pack, J.D. Special Points for Brillouin-Zone Integrations. Phys. Rev. B 1976, 13, 5188–5192. [CrossRef]
- 33. Pack, J.D.; Monkhorst, H.J. "Special Points for Brillouin-Zone Integrations"—A Reply. Phys. Rev. B 1977, 16, 1748–1749. [CrossRef]
- Henkelman, G.; Jónsson, H. Improved Tangent Estimate in the Nudged Elastic Band Method for Finding Minimum Energy Paths and Saddle Points. J. Chem. Phys. 2000, 113, 9978–9985. [CrossRef]
- Henkelman, G.; Jónsson, H. A Dimer Method for Finding Saddle Points on High Dimensional Potential Surfaces Using Only First Derivatives. J. Chem. Phys. 1999, 111, 7010–7022. [CrossRef]
- Jónsson, H.; Mills, G.; Jacobsen, K.W. Nudged Elastic Band Method for Finding Minimum Energy Paths of Transitions. In Classical and Quantum Dynamics in Condensed Phase Simulations; World Scientific: Singapore, 1998; pp. 385–404.
- 37. Wang, G.; Shi, Y.; Mei, J.; Xiao, C.; Hu, D.; Chi, K.; Gao, S.; Duan, A.; Zheng, P. DFT Insights into Hydrogen Activation on the Doping Ni<sub>2</sub>P Surfaces under the Hydrodesulfurization Condition. *Appl. Surf. Sci.* **2021**, *538*, 148160. [CrossRef]
- Dahl, S.; Logadottir, A.; Egeberg, R.C.; Larsen, J.H.; Chorkendorff, I.; Törnqvist, E.; Nørskov, J.K. Role of Steps in N<sub>2</sub> Activation on Ru(0001). *Phys. Rev. Lett.* 1999, 83, 1814–1817. [CrossRef]

**Disclaimer/Publisher's Note:** The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.