



Article

Micromagnetic Simulation of Vortex Development in Magnetic Bi-Material Bow-Tie Structures

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Abstract: Magnetic vortex structures are of high technological relevance due to their possible application in magnetic memory. Moreover, investigating magnetization reversal via vortex formation is an important topic in basic research. Typically, such vortices are only investigated in homogeneous magnetic materials of diverse shapes. Here, we report for the first time on micromagnetic simulation of vortex formation in magnetic bow-tie nanostructures, comprising alternating parts from iron and permalloy, investigated for two different thicknesses and under different angles of the external magnetic field. While no vortex was found in pure permalloy square, nanoparticles of the dimensions investigated in this study and in case of iron only a relatively thick sample allowed for vortex formation, different numbers of vortices and antivortices were found in the bow-tie structures prepared from both materials, depending on the angular field orientation and the sample thickness. By stabilizing more than one vortex in a confined nanostructure, it is possible to store more than one bit of information in it. Our micromagnetic simulations reveal that such bi-material structures are highly relevant not only for basic research, but also for data storage applications.

Keywords: magnetic nanostructures; micromagnetic simulation; bow-tie structure; vortex; magnetization reversal; iron, permalloy; lithography

1. Introduction

Magnetic nanostructures can be produced with typical thicknesses of a few nanometers up to tens of nm and with lateral dimensions in the range of some 10 nm to several micrometers, applying lithographic techniques [1,2], pulsed electrodeposition [3] or self-assembly methods [4]. Such nanostructures are generally of high interest since the configurational anisotropy due to the shape of the nanoparticles can be in a similar order of magnitude as magneto-crystalline and magneto-elastic anisotropies, giving rise to new effects caused by the superposition of all these anisotropies [5–8].

Magnetic nano-dots were especially investigated by diverse research groups, since they often enable the formation of a vortex which can be used for data storage [9,10]. One advantage of such vortex states is the reduction of stray fields and thus of interactions with neighboring nanoparticles [11,12], although such interactions are not fully suppressed [13]. Flux-closed vortex states can be created in round, elliptical or square nano-rings without a core region, again reducing stray fields [14–18], while nano-dots of different shapes with a core region may enable formation of more magnetic states [19–22].

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A former simulation of round iron (Fe) nanodots revealed nucleation of one or even two vortices during magnetization reversal, depending on the lateral dimensions of the nanodot and its thickness, but also several dimensions and aspect ratios in which no vortex state could be reached [23]. These vortices were often accompanied by antivortices, which are typically unstable and tend to annihilate at the edges of a nanostructure [24]. In square Fe nanodots, seven different magnetization reversal processes were found for different orientations of the external magnetic field, five of which contained one or more vortex states [25]. Similarly, dynamic simulations of rectangular nanostructures showed one or two resonance frequencies for different aspect ratios [26]. While square magnetic nanostructures of pure ferromagnetic or ferromagnetic/antiferromagnetic materials are sometimes reported in the literature [6,27–30], no investigations of bi-material square nanodots have been performed yet to the best of our knowledge.

Here, we report on square bow-tie structures (Figure 1), comprising alternating triangles of iron and permalloy (Py), which show unexpected vortex formation in comparison with square nanodots of both pure materials. Our micromagnetic simulations underline the new possibilities, which may be opened by such bi-material structures in basic research and technological applications. An overview of the possible production of such structures is given in Materials and Methods.

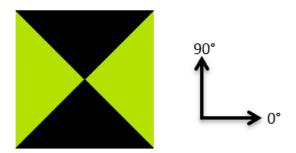


Figure 1. Sketch of the bow-tie structure under examination consisting of iron (**black**) and permalloy (**green**) as well as orientation of the external magnetic field angles.

2. Results and Discussion

Firstly, Figure 2 depicts typical magnetization states during the reversal process from positive to negative saturation and hysteresis loops of pure Fe nanoparticles of 15 nm and 30 nm thickness, respectively. Simulations of the other angles under examinations revealed no qualitative differences and are thus not shown here.

In all graphical representations of the magnetization in the sample, the red color indicates a local magnetization orientation to the right, while the blue color shows magnetic moments oriented to the left. In the hysteresis loops, the longitudinal magnetization component M_L is defined as parallel to the external magnetic field, while the transverse magnetization component M_T depicts the hysteresis curve perpendicular to it.

While the Fe particle with thickness 15 nm shows magnetization reversal via a meander state, as already reported in Ref. 25 and also typical in thin-film systems [31], a vortex state is formed for a thickness of 30 nm, indicated by the "jump" in the hysteresis loop at –16 mT (Figure 2). The vortex state is here thus only reached after remanence, which can be different for slightly modified field orientations or geometries [25].

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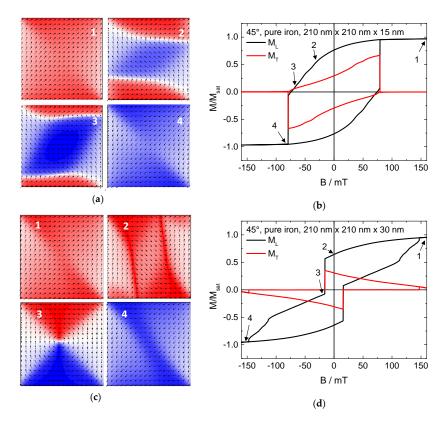


Figure 2. Snapshots of the magnetization reversal process and hysteresis loops of pure iron nanoparticles, simulated for an external field orientation of 45° , for a thickness of (\mathbf{a},\mathbf{b}) 15 nm or (\mathbf{c},\mathbf{d}) 30 nm, respectively. In all graphs, the longitudinal magnetization M_L is detected parallel to the magnetic field, while the transverse magnetization M_T is perpendicular to it.

For permalloy, the symmetric 45° orientation—i.e., the external magnetic field is oriented along 45°, resulting in the same situation as if the sample had been rotated by this angle—shows domain wall states, while the other orientations reveal magnetization reversal via meander states for both thicknesses (Figure 3). The Py nanoparticle does not exhibit any vortex state for the dimensions and field orientations examined in this study.

While three of the four particles modelled from pure materials did not show any vortex states, this changes by forming the bow-tie structure. The following figures depict snapshots of magnetization reversal states and hysteresis loops detected for field orientations of 30° , 45° and 60° , respectively.

Snapshots of the magnetization reversal process for the thinner sample (15 nm) are depicted in Figure 4a. Here, starting from positive saturation, firstly the typical aforementioned meander state is formed, before a double-vortex state is reached, finally leading to negative saturation. The first "jump" in the hysteresis loops in Figure 4b corresponds to the start of this double-vortex state. Generally, such steps along the hysteresis loops indicate the possibility that vortex states or domain walls are nucleated.

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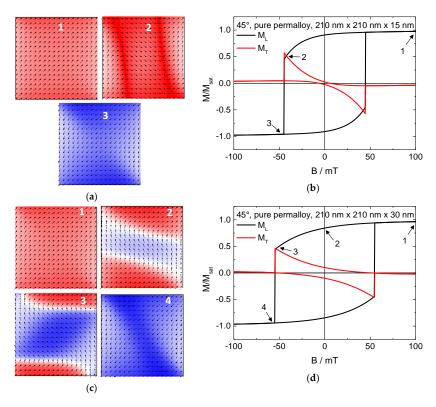


Figure 3. Snapshots of the magnetization reversal process and hysteresis loops of pure permalloy nanoparticles, simulated for an external field orientation of 30°, for a thickness of (**a,b**) 15 nm or (**c,d**) 30 nm, respectively.

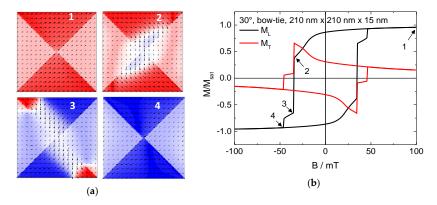


Figure 4. (a) Snapshots of the magnetization reversal process and (b) hysteresis loops of bow-tie nanoparticles, simulated for an external field orientation of 30° and a thickness of 15 nm.

For a thickness of 30 nm, magnetization reversal comprises more intermediates states, as visible in the snapshots in Figure 5a and indicated by the large amount of steps along the slopes of the hysteresis curves for this case (Figure 5b).

Starting again at positive saturation, the already known meander state is formed. Next, a double-vortex state is visible, as it was simulated earlier for pure Fe nanoparticles of similar dimensions [25]. In the next step, two more vortex-antivortex pairs are created which have not yet been found in pure Fe nanodots. While both vortex cores are firstly trapped at the border between Fe and Py, the first vortex pair starts moving into the Fe region now, while the second vortex pair moves slightly into the Py region. It should be mentioned that the newly formed antivortex, opposite to previous literature reports [24], does not visibly move to one of the nanoparticle edges. With the external magnetic field becoming more and more negative, firstly the second vortex-antivortex pairs vanish, before the first vortex pair also vanishes, and magnetization reversal is finished.

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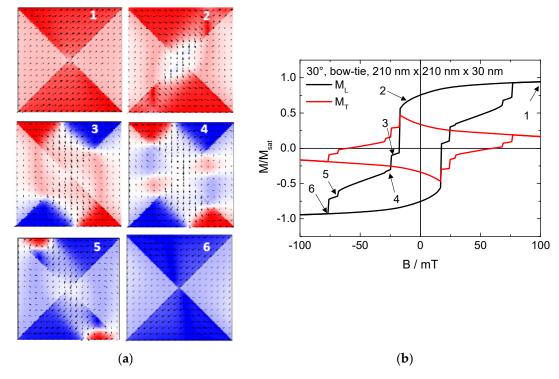


Figure 5. (a) Snapshots of the magnetization reversal process and (b) hysteresis loops of bow-tie nanoparticles, simulated for an external field orientation of 30° and a thickness of 30 nm.

For a sample orientation of 45°, there is interestingly no vortex state visible for the thinner sample, which is identical to the pure Fe and Py specimens, respectively (Figure 6).

The thicker sample, however, shows again an interesting magnetization reversal process, as indicated by the corresponding hysteresis loops (Figure 7) and clearly visible in the snapshots of this magnetization reversal process.

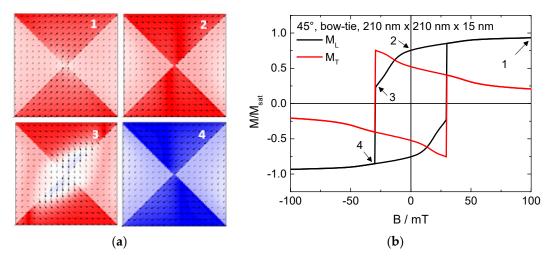


Figure 6. (a) Snapshots of the magnetization reversal process and (b) hysteresis loops of bow-tie nanoparticles, simulated for an external field orientation of 45° and a thickness of 15 nm.

Magnetization reversal again starts with a meander state, as seen before, this time leading to nearly fully symmetric vortices in the Fe areas. With the external magnetic field becoming more negative, these vortices start moving to the borders between both materials, while the antivortices propagate along the border from the middle of the Py areas to the middle of the Fe areas where they are more prominently visible due to the here chosen color code. Next, unexpectedly one of the vortices

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vanishes, resulting in an asymmetric situation. Such asymmetries are at first glance unusual, but can be found in many simulations due to small asymmetries of the geometry or the anisotropy distribution. Finally, the single vortex vanishes, and magnetization reversal is completed.

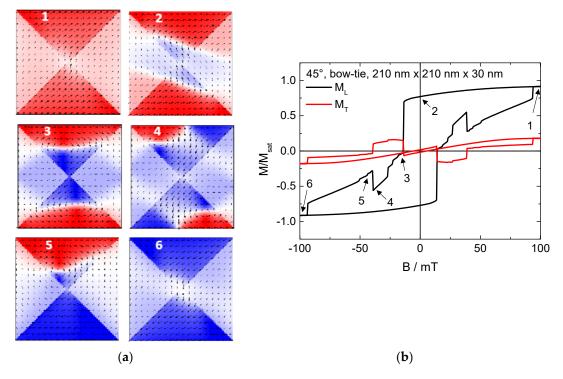


Figure 7. (a) Snapshots of the magnetization reversal process and (b) hysteresis loops of bow-tie nanoparticles, simulated for an external field orientation of 45° and a thickness of 30 nm.

Next, Figures 8 and 9 depict snapshots of the magnetization reversal as well as hysteresis loops for an external magnetic field orientation of 60° . For both thicknesses under examination, steps along the loops can be recognized, indicating vortex or domain wall states during magnetization reversal. While the sample of thickness 15 nm reverses magnetization without vortices, the thicker sample shows a double-vortex very similar to Figure 5 (Figure 9). The nearly identical states during magnetization reversal in the thicker samples for field orientations of 45° (Figure 7) and 60° (Figure 9) point out the strong influence of the configurational anisotropy, especially for small external magnetic fields counteracting the configurational anisotropy.

Generally, it can be stated that the bow-tie structure fully prevents formation of a vortex core in the middle of the sample. This results in all cases under examination in the formation of a symmetric double-vortex structure, with the vortex cores being formed either in the Fe area or near the border between both materials.

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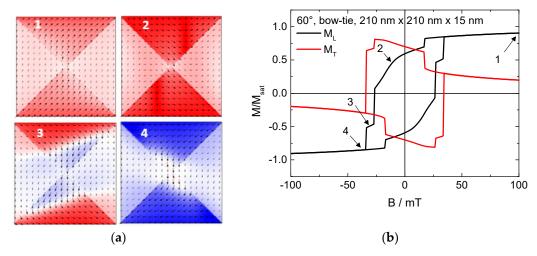


Figure 8. (a) Snapshots of the magnetization reversal process and (b) hysteresis loops of bow-tie nanoparticles, simulated for an external field orientation of 60° and a thickness of 15 nm.

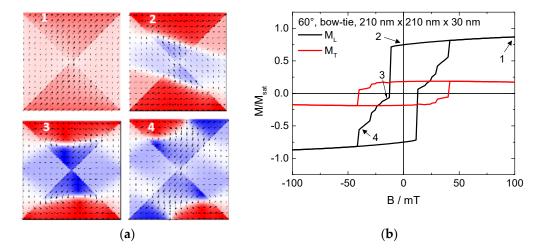


Figure 9. (a) Snapshots of the magnetization reversal process and (b) hysteresis loops of bow-tie nanoparticles, simulated for an external field orientation of 60° and a thickness of 30 nm.

Next, to enable storing more than one bit of information in such a structure, it is necessary to break this mirror symmetry by either modifying the thickness or—technologically easier—varying the Fe and Py areas, in this way possibly increasing the number of stable intermediate states with different vortex chirality. It should be mentioned that similar results have also been obtained by Nasirpouri et al., working with pyramidal and truncated icosahedral structures with nickel shell, which the authors also suggested using in multi-bit storage architecture [32].

Another highly interesting topic to be potentially combined with the here suggested bi-material structures are chiral magnets and skyrmions whose interactions with interfaces are of high interest in recent research. This means that instead of using vortices for data storage, as suggested here, skyrmions could be used for this purpose. The materials for such skyrmion-based structures, on the other hand, would be atomically-thin ferromagnets from materials like Fe or Co, typically on heavy-metal substrates like Pt or Pd, instead of the here used much thicker Fe/Py structures. Mulkers et al., e.g., pointed out the possibility to have multiple stable cycloidal states with different periods in laterally confined thin ferromagnetic films with Dzyaloshinskii-Moriya interaction (DMI) as well as stable skyrmions [33]. Even more interesting phenomena are reported by the same group, investigating heterochiral 2D structures, starting with spin canting at interfaces between regions with different DMI to strong domain pinning to improved skyrmion racetrack memory [34]. For the refraction of spin waves at such DMI interfaces in heterochiral magnetic films, a generalized Snell's law was setup which

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depends on an in-plane magnetic field, in this way giving rise to the critical incident angles and showing asymmetric Brewster angles at interfaces between regions with different DMI [35]. Most recently, the group investigated in detail the interaction of skyrmions with heterochiral interfaces and found deflection of the trajectory of ferromagnetic skyrmions which could be tuned by the spin-polarized current applied and the DMI difference on both sides of the interface, while AFM skyrmions were not deflected, but had a much higher speed [36]. Similar investigations should be carried out with the here proposed structures, too.

3. Materials and Methods

The nanoparticles under examination in this study are bow-tie structures, as depicted in Figure 1, consisting of Fe and Py parts. Lateral dimensions are 210 nm x 210 nm, the thickness is 15 nm or 30 nm. Such bow-tie structures are well known as electrodes [37].

There are two methods to produce bow-tie structures by electron beam lithography (EBL). The most common one starts with spin-coating a chip with PMMA resist. The PMMA is structured by EBL. After developing the resist (structures are cavities in the resist), metal is deposited on the substrate by sputtering or evaporation. Redundant metal and resist are removed by a lift-off process. An alternative is to metalize the chip firstly. Then structures are written by EBL and the resist is developed. Now the resist covers the structures and acts as an etch mask. Residual metal is dry etched and the resist is stripped. Bow tie structures remain, as visible in Figure 10.

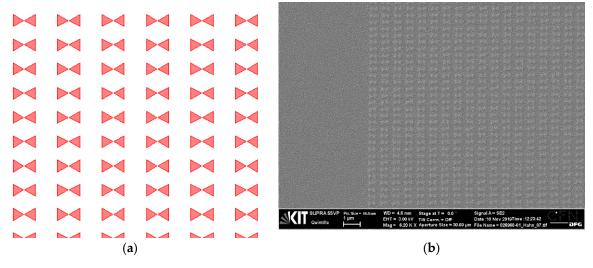


Figure 10. Single-material bow tie structures (**a**) as layout and (**b**) produced with an edge length of 200 nm with negative resist AR-N.

To obtain bi-material bow tie structures, a so-called bilayer process is necessary, a well-known process for structures with edge lengths of several 100 nm. The alignment precision of the e-beam process is approx. 20 nm, thus with a designed gap of 50 nm between the materials, a gap in the range of 30–70 nm can be expected. Recently, the writing accuracy as well as the necessary gap between both materials are being optimized.

Our recent simulations concentrate on individual nano-elements, before in a future simulation arrays of these structures will be modeled. Recent simulations of iron nanoparticles revealed that for inter-particle distances similar to the particle diameters, the influence of interactions with neighboring particles is relatively small [38,39], so that simulating individual elements firstly can be expected to be sufficient for a first comparison with the experiment.

The angles of the external magnetic field were chosen as 30° , 45° , and 60° ; the field is oriented in the plane of the nanostructure. As a comparison, pure Fe and Py nanoparticles of identical dimensions were modelled.

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Simulations were performed with the micromagnetic simulator OOMMF (Object Oriented MicroMagnetic Framework) [40]. In this program, finite differences are used for meshing, and the Landau-Lifshitz-Gilbert (LLG) equation of motion is solved dynamically [41].

OOMMF offers the possibility to create bi-material maps in different ways, using the eXtensible Solver. Here, material regions were defined by an image file (Figure 1), using the function ImageAtlas. The material parameters for Fe (Py) were chosen according to typical literature values: magnetization at saturation $M_{S,Fe} = 1700 \times 10^3$ A/m ($M_{S,Py} = 796 \times 10^3$ A/m), exchange constant $A_{Fe} = 21 \times 10^{-12}$ J/m ($A_{Py} = 10.5 \times 10^{-12}$ J/m), magneto-crystalline anisotropy constant $K_{1,Fe} = 48 \times 10^3$ J/m³ ($K_{1,Py} = 0.5 \times 10^3$ J/m³). Along the borders, these values were averaged between the values of the single materials.

It should be mentioned that computing on graphical processing units (GPUs), e.g., with the free GPU-accelerated micromagnetic solver Mumax based on the Nvidia CUDA toolkit, can be used to reach higher performance and can be used for larger-scale, more detailed simulations [42].

The crystallographic orientations in the single parts of the mesh are chosen arbitrarily, as would be the case for a sputtered sample. This means that in each of the cubic "grains", an arbitrary crystallographic orientation is chosen which varies with each new simulation, unlike the larger patches with well-defined differing crystallographic orientations used for simulations of amorphous ferrimagnets [43]. Opposite to the large magneto-crystalline anisotropy of cobalt which causes severe modifications from one simulation to the next for such an approach [1], here subsequent simulations showed approximately identical hysteresis loops which were dominated by the configurational anisotropy and not influenced by the arbitrary crystallographic orientation nor by the starting configuration. The material parameters are constant inside the "grains", no special parameters are taken into account at the grain boundaries inside either material. A quasi-static case was modelled by setting the Gilbert damping constant $\alpha = 0.5$ for both materials, the mesh size was chosen as 3 nm³ for the whole sample. Simulations were typically performed in the range between \pm 200 mT in steps of 0.4 mT; if minor loops were found, the field ranges were correspondingly increased to investigate proper full hysteresis loops. All simulations are started from a fully saturated state of the magnetization along the corresponding angle.

4. Conclusions

Square magnetic bow-tie nanostructures, comprised of iron and permalloy, were investigated by micromagnetic simulations for the first time. Depending on the orientation with respect to the external magnetic field and on the sample thickness, in most cases two or four vortices were found, while the typical single-vortex state which is often visible in round or square nanodots of different materials and dimensions was fully suppressed by the bi-material structure. These findings underline the opportunities given by such bi-material nanostructures in data storage and transport, allowing for storing more than one bit of information in a nanoparticle which contains more than one separately controllable vortex.

Next, preparation of such bow-tie bi-material structures by e-beam lithography will be optimized, and experimental investigations of the nanostructures will be compared with the simulated results. Finally, simulations and experimental verifications are necessary to evaluate possibilities to influence the vortices solely, in this way enabling storage of more than one bit of information in such a magnetic nanoparticle.

Author Contributions: Conceptualization, D.S. and A.E.; methodology, D.S.; validation, I.J.J., T.B., L.H. and A.E.; formal analysis, D.S., T.B. and A.E.; investigation, D.S.; writing—original draft preparation, A.E., T.B. and L.H.; writing—review and editing, all authors; visualization, D.S., C.D. and A.E. All authors have read and agreed to the published version of the manuscript.

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