



Review

# Underwater Undulating Propulsion Biomimetic Robots: A Review

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**Abstract:** The traditional propeller-based propulsion of underwater robots is inefficient and poorly adapted to practice. By contrast, underwater biomimetic robots show better stability and maneuverability in harsh marine environments. This is particularly true of undulating propulsion biomimetic robots. This paper classifies the existing underwater biomimetic robots and outlines their main contributions to the field. The propulsion mechanisms of underwater biomimetic undulating robots are summarized based on theoretical, numerical and experimental studies. Future perspectives on underwater biomimetic undulating robots are also presented, filling the gaps in the existing literature.

**Keywords:** underwater biomimetic robots; undulating propulsion robots; undulating propulsion mechanism; experimental study

## 1. Introduction

Underwater robots have an important role to play in future marine development and underwater activities and have broad application prospects and great potential value [1–5]. Researchers have designed various underwater robots for underwater missions, such as remotely operated vehicles (ROVs) and autonomous underwater vehicles (AUVs) [6,7] (Figure 1). Traditional underwater robots are composed of rigid materials and most are propelled by propellers [8,9]. However, propeller propulsion is unsuitable for implementation in harsh marine environments as it can damage aquatic life or the seabed or even become trapped in weeds [10,11]. In addition, the low efficiency and stability of propeller-driven craft in low-speed attitude adjustment conditions greatly limit the applications of propeller propulsion. Therefore, novel underwater propulsion methods are desired and are currently being investigated [7].

At present, increasing attention is being paid to bionics-based propulsion mechanisms. This propulsive method is validated in marine environments as its principle is inspired by various marine organisms. The soft bodies, good flexibility and strong environmental adaptability of marine organisms inspire new ideas for the development of underwater robots [12]. After a long period of evolution, fish have adapted to exploit the principle of hydrodynamics to move forward using tail fins or pectoral fins [13–15], which has become the best way to move in water [16,17]. The propulsion method employed by fish can maintain high maneuverability and change posture according to the changing environment. Inspired by the fish propulsion method, the first underwater bionic robot RoboTuna [18] was unveiled in 1994, and various types of underwater bionic robots continue to emerge. Equipped with various propulsion methods, underwater robots present positive development trends and broad application prospects [19–23]. The term underwater biomimetic robot generally refers to robots that imitate the structure, function, or type of movement of fish species [24]. They have the basic movement characteristics of biomimetic fish and are continuously being optimized and improved on this basis. They have diverse functions, strong environmental adaptability and stability [25]. Undulating propulsion biomimetic robots are propelled by the undulating of pectoral fins, caudal fins and the body, an approach that has superior



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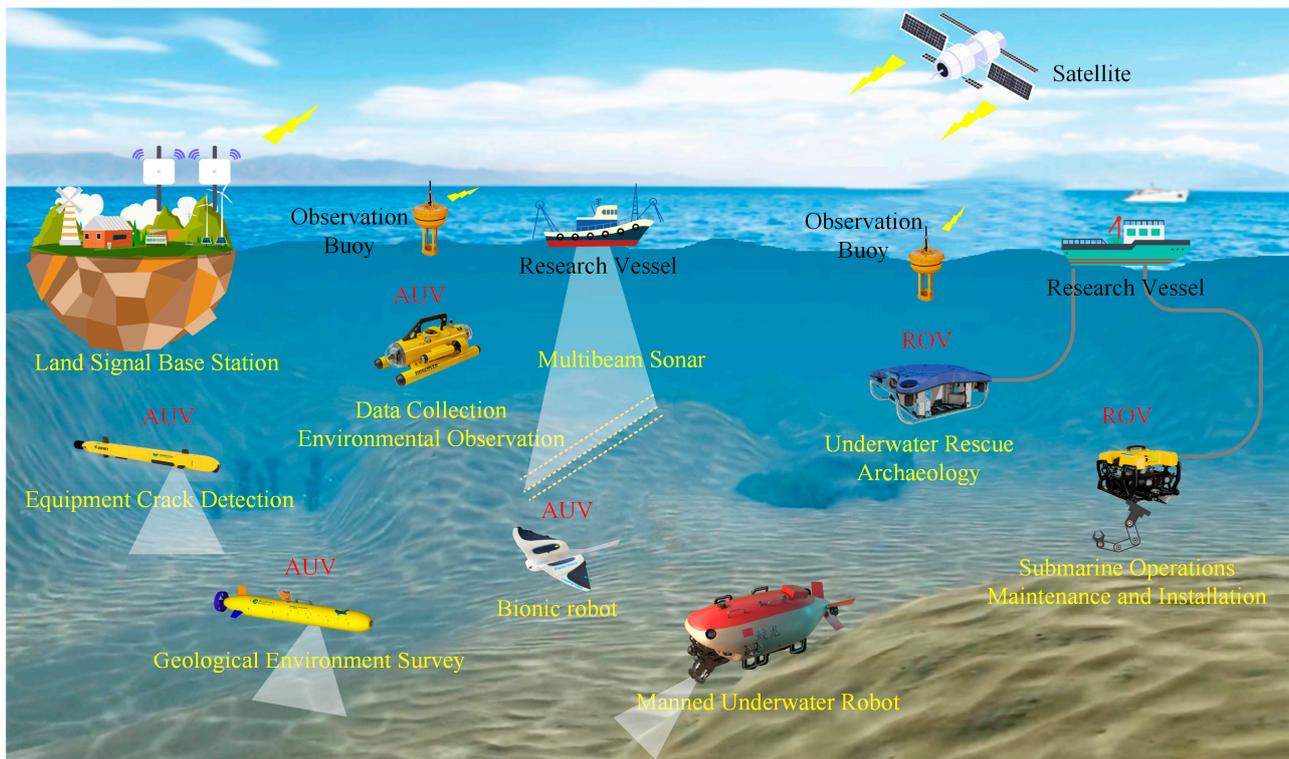
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motion performance and can realize multiple motion modes [26]. In summary, undulating propulsion underwater biomimetic robots are increasingly favored by scholars due to their good maneuverability and stability. Distinct from previous reviews [7,27–37], this work provides a review of undulating propulsion biomimetic robots, especially the different types of propulsion mechanisms. The review is organized as follows: In Section 2, the swimming patterns of fish are described. In Section 3, an overview of existing underwater robots with undulating propulsion is presented. In Section 4, the propulsion mechanisms of undulating propulsion underwater robots are described. In Section 5, the limitations and perspectives of fluctuation-propelled underwater robots are outlined.



**Figure 1.** Overview of ROV and AUV application scenarios.

## 2. The Swimming Mode of Fish

Starting from the morphological function of fish, there are many swimming modes of fish in nature, the most authoritative classification of which, based on the organ of propulsion, was first proposed by Breder and Webb [38]. There are two main categories of propulsion methods, body caudal fin (BCF) propulsion and median paired fin (MPF) propulsion. In 1978, Lindsey [39] classified the different families of fish species according to their mode of propulsion, which provided the essential foundation for the improvement of the overall performance of undulating propulsion biomimetic robots.

Figure 2 shows the fish species that employ BCF mode propulsion [32]. For this propulsion mode, the main body types are anguilliform, subcarangiform, carangiform, thunniform and ostraciiform, and the representative fish species for these body types are the eel, trout, herring, tuna and longhorn cowfish, respectively. Fish employing BCF mode propulsion gradually transition from undulating to oscillatory propulsion according to their different driving methods, as shown by the dashed line in Figure 2. In the figure, the first three propulsion modes are undulating and the last two are oscillatory. BCF propulsion modes are characterized by a high swimming speed—swordfish can reach a speed of 110 km/h—and good energy efficiency—tuna can maintain 90% energy efficiency while swimming for a long time [40]. Fish with the anguilliform body type employ fluctuations of the whole body and tail fin. This type of fish has a slender body and a faster swimming

speed. Subcarangiform and carangiform fish species are relatively similar; the difference is that the former uses 1/2 of their body length for fluctuations, while the latter uses only about 1/3 of their body length for propulsion [41,42]. Compared with the anguilliform model, the fluctuation range is small, but the caudal fluctuation frequency is high. The propulsion of thunniform fish comes from the tail fin [43]. Based on hydrodynamic models, thunniform propulsion has been estimated to produce mechanical efficiencies in the range of 80–90% [18,44,45]. The fastest fish (tuna, dolphin) use this propulsion mode [46–49]. Fish species with the ostraciiform body type adopt an oscillatory propulsion mode. This type of fish simply oscillates the caudal fin, which induces only a small thrust; thus, the speed of travel is relatively slow [50].

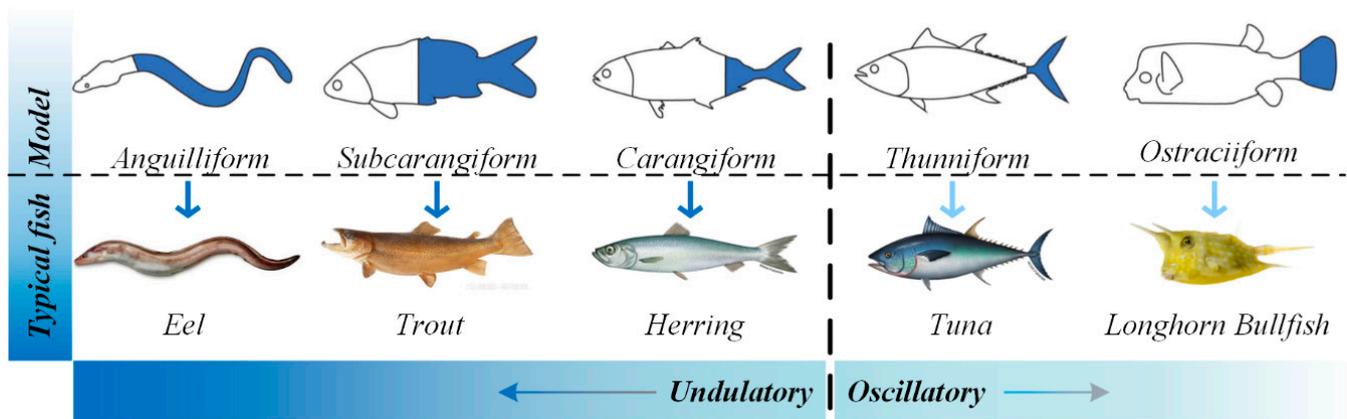


Figure 2. BCF propulsion mode [29].

Figure 3 shows the fish that employ MPF mode propulsion [32]. The main body types seen are rajiform, diofontiform, amiiform, gymnotiform, balistiform tetraodontidae and labriform, and the corresponding representative fish species are the stingray, puffer fish, bowfin fish triggerfish, yellowfin puffer and wrasse, respectively. The first five body types employ undulating propulsion, and the latter two employ oscillatory propulsion. As shown by the dotted line in Figure 3, most of the fish that employ MPF mode propulsion exhibit undulating propulsion. Rajiform fish species have soft and wide pectoral fins in a triangular shape and use the large fluctuations of the pectoral fins to generate driving power [51]. The most representative diodontiform fish species is the puffer fish. The puffer fish utilizes fluctuation of the pectoral fins on both sides of its body to propel [52]. Compared with rajiform fish species, the pectoral fins of diodontiform fish are smaller; thus, the traveling speed is slower. Amiiform fish generally have very long dorsal fins, which leads to larger amplitude waves during undulations, enabling larger movements [53]. Gymnotiform fish are similar to amiiform fish, except that their propelling fins are on the lower side of their bodies, and the power to move is generated through the oscillatory movement of the anal fin [54]. Balistiform fish generate the driving force using their dorsal and anal fins [55]. Balistiform-based locomotion has a very high propulsive efficiency compared to BCF propulsion modes. And compared to propulsion arising from the undulation of a slender fin, balistiform-based locomotion allows more maneuverability [56].

Overall, it appears that BCF-based propulsion permits a higher travel speed than MPF-based propulsion, and uses the rapid oscillation of wings to obtain efficient propulsion [56]. For example, in terms of BCF mode, the average swimming speed of Chinook salmon is 0.6 m/s, and their maximum swimming speed can exceed 6 m/s [57]. The swordfish, with its carangiform body type, has a swimming speed close to 2 m/s, and its maximum speed can even reach 27 m/s [58]. Conversely, with MPF mode, the average swimming speed of the fish is relatively slow. For example, the average swimming speed of the common stingray is 0.81 m/s, and its maximum speed is only 13 m/s [59]. It can be seen that most of the fish employing BCF-based propulsion swim faster than fish employing MPF-based propulsion. Different fish species have different morphological functions, which guarantee

their survival. Researchers should study the morphological functions of fish species for use as the inspiration for bionics-based propulsion systems.

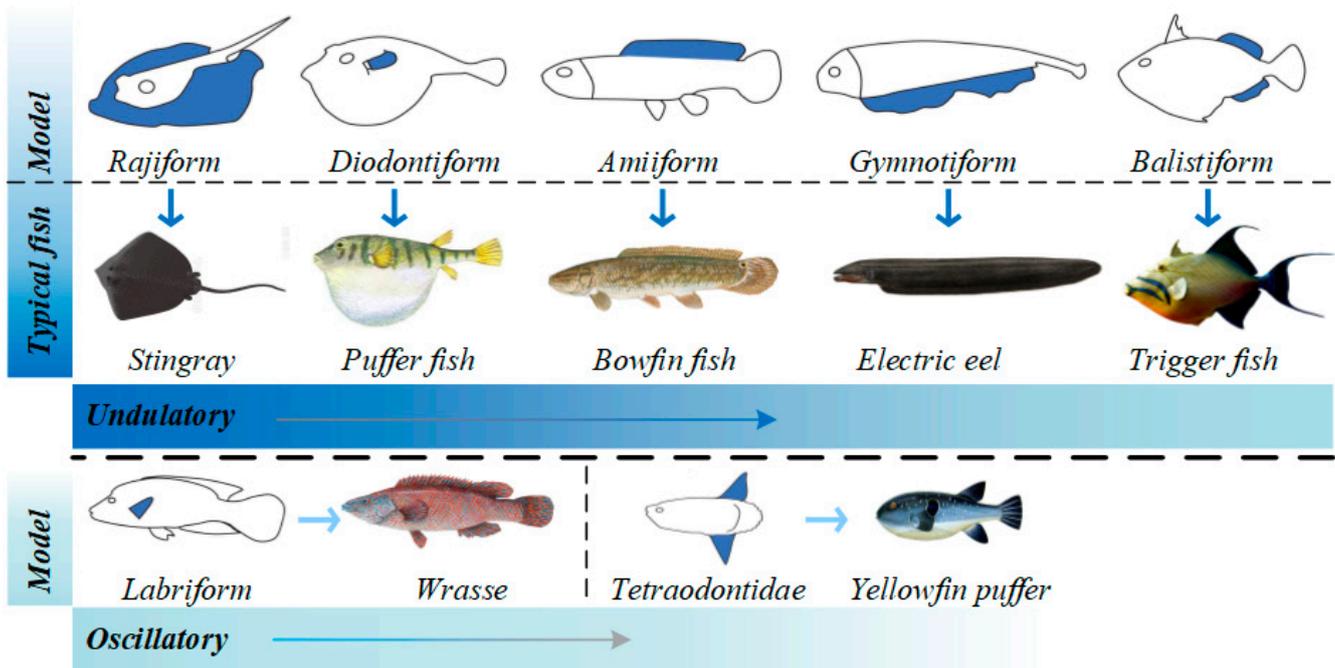


Figure 3. MPF propulsion mode [29].

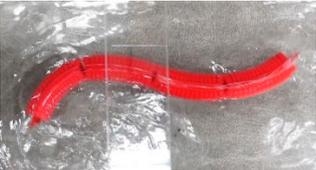
### 3. Classification of Undulating Propulsion Underwater Robots

Inspired by various morphological functions of fish species, underwater biomimetic robots have been designed and developed. On the basis of inheriting the characteristics of biomimetic objects, different materials and structures have been applied to optimize biomimetic robots. In this section, according to the requirements of application scenarios, the motion performance and travel efficiency of underwater biomimetic robots are highlighted. The corresponding underwater biomimetic robots are classified according to the biometric fish model that serves as their inspiration, and recent developments are also briefly presented.

#### 3.1. Anguilliform Biomimetic Robots

Anguilliform biomimetic robot fish, mainly inspired by the soft eel, have flexible joints and fluctuate their flexible bodies and tail fins to produce motion [60]. The AmphiBot II, which was designed by Alessandro Crespi, featured a maximum torque that was 3.5 times higher than that of the earlier AmphiBot I, which greatly enhanced its propulsion efficiency [61]. Salamandra Robotica II can crawl and swim both on land and in water. To further enhance the working capabilities of such robots, the Lampetra Project robot was proposed, which not only had muscle-like execution capabilities but also can work continuously for 5 h [62]. With the gradual maturation of the biomimetic robot design concept, the modular research method was applied in the Mamba Waterproof Snake Robot [63] and Multi-joint Underwater Robot [64], which not only facilitated the subsequent upgrading of the robots but also improved the propulsion efficiency. Details of the above-mentioned designs are presented in Table 1.

**Table 1.** Anguilliform biomimetic robots.

Robot	Date	Description	Main Contributions	Picture
Multi-Joint Underwater Robot [64]	2022	<ul style="list-style-type: none"> <li>● Modular design</li> <li>● Control system with 4 motion models</li> <li>● With controllable propellers</li> </ul>	<ul style="list-style-type: none"> <li>➤ First-generation prototype</li> <li>➤ Kinematic and dynamical models</li> </ul>	
Soft Eel Robot [65]	2022	<ul style="list-style-type: none"> <li>● 4 pairs of soft actuators</li> <li>● The maximum speed reaches 19 cm/s</li> </ul>	<ul style="list-style-type: none"> <li>➤ The frequency of robot muscle unit (0.83~1.67) Hz</li> </ul>	
Mamba Waterproof Snake Robot [63]	2014	<ul style="list-style-type: none"> <li>● Modularization and Reconfigurability</li> <li>● With a torque sensor in each joint</li> </ul>	<ul style="list-style-type: none"> <li>➤ Completion of the design based on strain gages</li> </ul>	
Salamandra Robotica II [66]	2013	<ul style="list-style-type: none"> <li>● Walk and swim</li> <li>● 4 legs and a driven spine</li> <li>● Only a single plane of motion</li> </ul>	<ul style="list-style-type: none"> <li>➤ Salamander-like robots</li> <li>➤ The movement patterns of salamander-like robots</li> </ul>	N/A

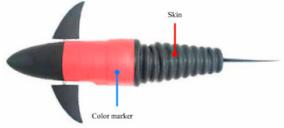
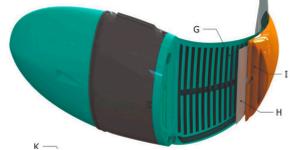
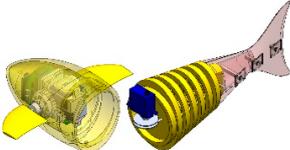
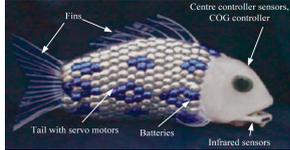
**3.2. Subcarangiform and Carangiform Biomimetic Robots**

Subcarangiform and carangiform fish have similar movement patterns. Robots with these forms have high undulating propulsion efficiency, fast swimming speed, and high application value, and hence, numerous studies have been conducted, as shown in Table 2. The G9fish was a relatively mature subcarangiform robotic fish [67]. Its design was derived from a set of mature underwater biomimetic robots motion modeling methods and it could realize two traveling modes, straight–line cruise and C–shaped sharp turn. Relying on mature motion modeling methods, the number of motion modes of biomimetic robots has constantly increased. Hydraulic Soft Robotic Fish could realize diving swimming and the Wire–Driven Robot Shark could realize ascending swimming and position–maintaining actions [68]. In addition, the Soft–Bodied Robotic Fish [69] could simulate escape response maneuvers and the Fabricated Bionic Robotic Fish [70] could actively avoid obstacles and quickly determine the shortest path to a target point. To further improve the kinematic performance of underwater robots, some scholars have focused their research on innovations in biomimetic materials. Compared with biomimetic robots with rigid structures such as ISplash–I [71], ISplash–II [72] and the Four–link Robotic Fish [73], the Biomimetic Fish Robot [74] used piezoelectric composites for the robot’s muscle structure. The Fabricated Bionic Robotic Fish utilized spring–based shape memory alloys as propulsion mechanisms, which not only improved its kinematic performance but also greatly enhanced its maneuverability [70].

**Table 2.** Subcarangiform and carangiform biomimetic robots.

Robot	Date	Description	Main Contributions	Picture
Untethered High–Performance Robotic Tuna [75]	2022	<ul style="list-style-type: none"> <li>● Inspired by tuna</li> <li>● Through mechanism optimization and steering strategies design</li> </ul>	<ul style="list-style-type: none"> <li>➤ Both high swimming speed and steering maneuverability</li> <li>➤ Novel design of redundant joints to increase the number of swimming patterns</li> </ul>	

Table 2. Cont.

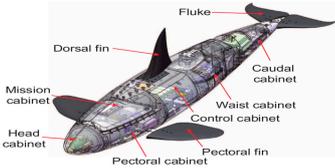
Robot	Date	Description	Main Contributions	Picture
Untethered Bioinspired Robotic fish [76]	2022	<ul style="list-style-type: none"> <li>● With high–frequency oscillation and a compliant passive mechanism</li> </ul>	<ul style="list-style-type: none"> <li>➤ An actuation system with a powerful output and a compact structure</li> </ul>	
Bio–inspired AUV [77]	2021	<ul style="list-style-type: none"> <li>● Inspired by a pink salmon</li> <li>● With numerical investigation results</li> </ul>	<ul style="list-style-type: none"> <li>➤ These hydrodynamic results are utilized to adapt a fish–like aquatic unmanned vehicle from conceptual design to working prototype</li> </ul>	
Four–link Carangiform Fish Robot [78]	2016	<ul style="list-style-type: none"> <li>● With a flexible multi–joint propulsion mechanism</li> <li>● Serve as the spine system of the fish body</li> </ul>	<ul style="list-style-type: none"> <li>➤ Move forward freely, avoid obstacles, and quickly find the shortest path to the target</li> </ul>	
Four–link Robotic Fish Large Pectoral Fin Control Surfaces [73]	2014	<ul style="list-style-type: none"> <li>● Multiple artificial control surfaces</li> <li>● Embedded vision system</li> <li>● Relies on the caudal fin and the secondary fins for propulsion</li> </ul>	<ul style="list-style-type: none"> <li>➤ Equipped with a monocular visual recognition system</li> <li>➤ Autonomous obstacle avoidance</li> </ul>	
Soft–bodied Robotic Fish [69]	2013	<ul style="list-style-type: none"> <li>● An autonomous soft robot</li> <li>● Quick escape response</li> <li>● An array of fluidic elastomer actuators</li> </ul>	<ul style="list-style-type: none"> <li>➤ Soft robots display independent, fast body movements like biological fish</li> </ul>	
Self–contained Hydraulic Fish [79]	2013	<ul style="list-style-type: none"> <li>● Soft fluidic elastomer robot</li> <li>● Three viable actuator morphologies</li> <li>● Internal channel structure</li> </ul>	<ul style="list-style-type: none"> <li>➤ Provided a new actuator design and manufacturing method</li> </ul>	
Improved ACP Robot Fish [80]	2012	<ul style="list-style-type: none"> <li>● A flexible caudal fin to provide thrust</li> <li>● Rigid head, articulated torso, and compliant caudal fin</li> <li>● With flow and pressure microelectromechanical sensors</li> </ul>	<ul style="list-style-type: none"> <li>➤ Utilizing low–cost MEMS sensor</li> <li>➤ Quantify the normal force of the propulsion element</li> </ul>	
G9fish [67]	2010	<ul style="list-style-type: none"> <li>● A new multi–joint robot fish swimming motion modeling method</li> <li>● An improved trajectory approximation</li> <li>● Tail with servo motors</li> </ul>	<ul style="list-style-type: none"> <li>➤ An error function for digital approximation</li> <li>➤ A lookup table for online optimization</li> </ul>	
Fabricated Bionic Robotic Fish [70]	2021	<ul style="list-style-type: none"> <li>● Spring–based shape memory alloys</li> <li>● Driven by a shape memory alloy (SMA) spring actuator</li> </ul>	<ul style="list-style-type: none"> <li>➤ Complete the undulating march of subcarangiform fish</li> <li>➤ Can realize the two–way shape memory effect</li> </ul>	N/A
ACP Robot Fish [81]	2018	<ul style="list-style-type: none"> <li>● Based on the Lighthill fish swimming model</li> <li>● Obtained the distribution law of thrust</li> </ul>	<ul style="list-style-type: none"> <li>➤ A manufacturing method of the biomimetic robot fish from theoretical model</li> </ul>	N/A

### 3.3. Thunniform and Ostraciiform Biomimetic Robots

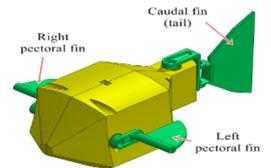
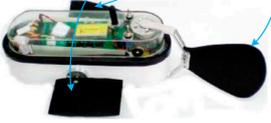
Thunniform and ostraciiform fish employ the oscillatory propulsion mode. Their traveling speed is fast; however, their mobility is inferior. There have been relatively few studies of this type of motion due to the limited number of application scenarios [82]. As shown in Table 3, the Miniature Robotic Fish took live fish as the biometric research object, studying the interaction between robotic fish and live fish to provide a basis for the study of fish habits [83]. The Gliding Robotic Dolphin combined the advantages of dolphins and underwater gliders, which not only increased the speed of the robots but also enabled the smooth gliding motion and attitude adjustment of the robot [84]. Although the Single–Motor–Actuated Robotic Fish [85] and Thunniform Robotic Fish [43] had a simple structure, they performed well in terms of motion and maneuverability.

Ostraciiform biomimetic robots have three propulsion modules, a tail fin and two pectoral fins. With the help of the CPG control network, the BoxyBot could swim in water and crawl on the ground [86]. The Boxfish–like Robot could swim in three dimensions and used a rolling motion for attitude control, which greatly enhanced its motion performance [87]. Details of the above–mentioned designs are provided in Table 4.

**Table 3.** Thunniform biomimetic robots.

Robot	Date	Description	Main Contributions	Picture
Single–Motor–Actuated Robotic Fish [85]	2016	<ul style="list-style-type: none"> <li>● Fewer joints</li> <li>● Mechanical design, motion analysis and attitude control</li> <li>● Controlled by a single motor</li> </ul>	<ul style="list-style-type: none"> <li>➤ Relies on simple mechanical structure and motion control to improve the overall motion performance</li> </ul>	
Gliding Robotic Dolphin [84]	2015	<ul style="list-style-type: none"> <li>● Combines the advantages of dolphins and underwater gliders</li> <li>● Gliding motions, dolphin–style double–jointed flapping swimming, and stable chest propulsion motions</li> </ul>	<ul style="list-style-type: none"> <li>➤ Rear–drive propulsion and fluke can realize dolphin–like fast swimming</li> <li>➤ Uses pectoral fins and fluke to realize attitude adjustment and smooth glide</li> </ul>	
Thunniform Robotic Fish [43]	2022	<ul style="list-style-type: none"> <li>● An elastic chord and a tail fin</li> <li>● Controlled by two motors</li> <li>● The tail fin part can provide a fixed amplitude</li> </ul>	<ul style="list-style-type: none"> <li>➤ Relationship between caudal fin frequency, oscillation amplitude and travel speed</li> </ul>	N/A
Mackerel Robot [88]	2013	<ul style="list-style-type: none"> <li>● The power, wakefield and propulsion speed of the robotic fish can be measured simultaneously</li> </ul>	<ul style="list-style-type: none"> <li>➤ Quantitative measurement of robotic fish propulsion efficiency achieved</li> </ul>	N/A

**Table 4.** Ostraciiform biomimetic robots.

Robot	Date	Description	Main Contributions	Picture
Boxfish Robot [86]	2017	<ul style="list-style-type: none"> <li>● With three micro–servo motors</li> <li>● Speed, thrust and hydrodynamic aspects</li> <li>● Three types of pectoral fins</li> </ul>	<ul style="list-style-type: none"> <li>➤ The combination of a quarter–circle pectoral fin and a triangular tail fin provides the fastest speed</li> </ul>	
Boxfish–like Robot [87]	2013	<ul style="list-style-type: none"> <li>● Multiple 3D swimming modes and roll attitude control</li> <li>● CPG control network</li> <li>● Inertial measurement unit</li> </ul>	<ul style="list-style-type: none"> <li>➤ CPG closed–loop control for robotic fish yaw and roll</li> </ul>	

**Table 4.** *Cont.*

Robot	Date	Description	Main Contributions	Picture
BoxyBot [89]	2007	<ul style="list-style-type: none"> <li>● Non–steady–state swimming and crawling</li> <li>● Three actuated fins</li> <li>● Swim in water and crawl on solid ground</li> </ul>	<ul style="list-style-type: none"> <li>➤ The CPG model can generate fin trajectories online</li> <li>➤ CPG change control parameters</li> </ul>	N/A

**3.4. Rajiform Biomimetic Robots**

Inspired by rajiform fish, some biomimetic robot fish employing the MPF propulsion modes have been proposed, as listed in Table 5. The skate is a typical rajiform with a flat body, wide pectoral fins and large fluctuating motions. Inspired by the skate’s soft body skeleton, the Self–Powered Soft Robot developed by Zhejiang University had high application value and consisted of a full–body soft structure without any rigid structure [90]. In addition, it used a dielectric elastomer material for its flutter wings, with electronic components integrated into a silicone body, and was successfully launched in a field test in the Marianas Trench down to a depth of 10,900 m. Other rajiform underwater biomimetic robots also demonstrated good kinematic performance, such as the IPMC Manta Ray [91], the Manta Ray Robot [92] and the Bionic Fin Manta Ray [93]. The difference between these three robots is their material implementation, that is, IPMC Manta Ray was made of ionic polymer metal composite materials, the Manta Ray Robot was made of three flexible materials, and the Bionic Fin Manta Ray was made of flexible PVC material. Both the Soft Body Single–Dual Actuator Ray [94] and the Cartilage Structure Underwater Robot [95] were inspired by stingrays, with the former being made of silicon–based cartilage and the latter being made of steel.

**Table 5.** Rajiform biomimetic robots.

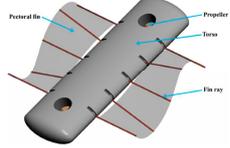
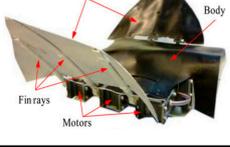
Robot	Date	Description	Main Contributions	Picture
Cartilage Structure Underwater Robot [95]	2021	<ul style="list-style-type: none"> <li>● Inspired by stingrays</li> <li>● Silicon–based cartilage and soft tissue</li> </ul>	<ul style="list-style-type: none"> <li>➤ Cartilage structure can improve efficiency</li> <li>➤ The stiffness gradient is important for locomotion performance</li> </ul>	
Manta Ray Robot [92]	2021	<ul style="list-style-type: none"> <li>● Inspired by the manta ray</li> <li>● Modular design</li> <li>● The flapping wing consists of three different soft materials</li> </ul>	<ul style="list-style-type: none"> <li>➤ Simple pitching and rolling and continuous and stable swimming</li> <li>➤ As the frequency increases, the swimming speed increases</li> </ul>	
Hybrid Manta Ray Robot [96]	2021	<ul style="list-style-type: none"> <li>● Driven by two pectoral fins and two vertical propellers</li> <li>● The hydrodynamics of the torso are analyzed</li> </ul>	<ul style="list-style-type: none"> <li>➤ Combined with Fluid mechanics, the 6–DOF motion mode of the robot is analyzed</li> </ul>	
RoMan–II [97]	2012	<ul style="list-style-type: none"> <li>● Multi–fin thruster based on CPG</li> <li>● With flexible membrane propulsion</li> <li>● Motors distributed on both sides</li> </ul>	<ul style="list-style-type: none"> <li>➤ Determined the framework of the CPG control method</li> </ul>	

Table 5. Cont.

Robot	Date	Description	Main Contributions	Picture
Self-powered Soft Robot [90]	2021	<ul style="list-style-type: none"> <li>Inspired by deep-sea snails</li> <li>A high-pressure-resistant soft robot</li> <li>With dielectric elastomer materials and electronic components</li> </ul>	<ul style="list-style-type: none"> <li>The whole body is soft</li> <li>Can swim in deep seas</li> <li>The electronic components and soft actuators have good pressure resilience</li> </ul>	N/A
Bionic Fin Manta Ray [93]	2015	<ul style="list-style-type: none"> <li>Inspired by the manta ray</li> <li>Passive flexibility of the pectoral fins</li> <li>The servo motor actively oscillates</li> </ul>	<ul style="list-style-type: none"> <li>Passive flexible pectoral fins</li> <li>A simple and efficient propulsion structure</li> </ul>	N/A
IPMC Manta Ray [91]	2012	<ul style="list-style-type: none"> <li>Ionomer metal composites</li> <li>IPMC as artificial muscles</li> <li>Equipped with a lightweight, compact Li-ion polymer battery</li> </ul>	<ul style="list-style-type: none"> <li>The pectoral fins can produce up to 100% tip deflection and 40° twist</li> </ul>	N/A

### 3.5. Amiiiform Biomimetic Robots

The Amiiiform differs from the gymnotiform in that its undulating propulsion mechanism is a dorsal fin. As shown in Table 6, RoboGnilos [98] and the Bio-inspired Amphibious Robot [99] were inspired by *Gymnarchus Niloticus*. The former had an undulating dorsal fin above the body and the latter had undulating fins symmetrically distributed on both sides of the body.

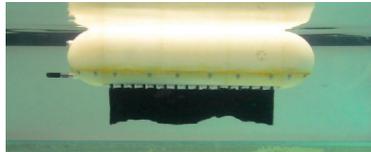
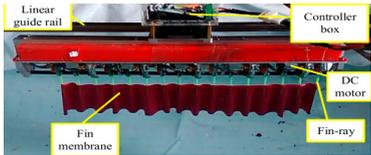
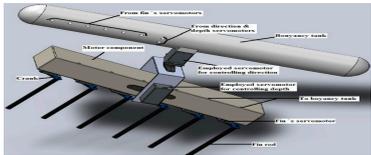
Table 6. Amiiiform biomimetic robots.

Robot	Date	Description	Main Contributions	Picture
Bio-inspired Amphibious Robot [99]	2021	<ul style="list-style-type: none"> <li>Inspired by <i>Gymnarchus Niloticus</i></li> <li>The undulating fins are placed on both sides</li> <li>Swimming and crawling brushless motor-driven rigid fin rays</li> </ul>	<ul style="list-style-type: none"> <li>Mechanical method to create fins by applying force to pristine flexible membranes achieved</li> </ul>	
RoboGnilos [98]	2009	<ul style="list-style-type: none"> <li>Inspired by <i>Gymnarchus Niloticus</i></li> <li>Modular independent motors</li> <li>A multi-joint dynamic system</li> </ul>	<ul style="list-style-type: none"> <li>Establishing a qualitative relationship between dynamical performance and undulating parameters</li> </ul>	
Dorsal Undulation Fin Robot [100]	2016	<ul style="list-style-type: none"> <li>Two kinds of biomimetic undulating fins</li> <li>Two kinds of propulsion devices</li> <li>Fixed undulating and independent drive mode</li> </ul>	<ul style="list-style-type: none"> <li>Prototypes guided by dynamic and kinematic models</li> </ul>	N/A

### 3.6. Gymnotiform Biomimetic Robots

Gymnotiform and anguilliform fish are similar, but gymnotiform fish are propelled by undulating ventral and anal fins, while anguilliform fish are propelled by undulating body and caudal fins. As shown in Table 7, most of the gymnotiform biomimetic robots were inspired by the black ghost knife fish, such as the NKF-II [101], Gymnotiform Undulating Fin Robot [102] and Undulatory Fin Propulsion Bio-Inspired Robot [103]. The Robotic Knifefish was inspired by the South American electric knife fish, and its key drive parameters were investigated for the undulating propulsion of the ribbon fin [104].

**Table 7.** Gymnotiform biomimetic robots.

Robot	Date	Description	Main Contributions	Picture
Undulatory Fin Propulsion Bio-Inspired Robot [103]	2018	<ul style="list-style-type: none"> <li>● Forward swimming, reverse movement, diving, maintaining a position and vertical swimming</li> <li>● Equipped with 16 DC motors</li> </ul>	<ul style="list-style-type: none"> <li>➤ Fin kinematics, hydrodynamics and thrust generation of undulating fin propulsion</li> </ul>	
Gymnotiform Undulating Fin Robot [102]	2018	<ul style="list-style-type: none"> <li>● Inspired by the South American black ghost knife fish</li> <li>● A polyester film surface and DC motor</li> </ul>	<ul style="list-style-type: none"> <li>➤ Equations of force generated by continuous and discontinuous sine waves</li> </ul>	
Knifefish Robot [105]	2011	<ul style="list-style-type: none"> <li>● Inspired by knife fish</li> <li>● With 6 servo motors</li> <li>● The fins are operated by wireless remote control</li> </ul>	<ul style="list-style-type: none"> <li>➤ The influencing factors of fin propulsion efficiency and thrust</li> </ul>	
Robotic Knifefis [104]	2011	<ul style="list-style-type: none"> <li>● Inspired by South American electric knife fish</li> <li>● A custom-printed circuit board</li> </ul>	<ul style="list-style-type: none"> <li>➤ Focus on the key driving parameters of ribbon fin propulsion</li> </ul>	N/A

### 3.7. Labriform Biomimetic Robots

Labriform biomimetic robotic fish employ the oscillatory propulsion mode, as shown in Table 8. Related underwater biomimetic robots use the oscillating travel of the pectoral and caudal fins, but to date, there have been few studies published. The Pectoral Fin and Dual Caudal Fin Robot used the tail fin as the main propeller and was capable of free swimming and active obstacle avoidance [106]. The Flexible Pectoral Fin Joint Labriform Robot used the rigid pectoral fin as the main propulsion structure, which was connected by flexible feather joints to enhance motion performance [107].

**Table 8.** Labriform biomimetic robots.

Robot	Date	Description	Main Contributions	Picture
Wrasse Robot [108]	2009	<ul style="list-style-type: none"> <li>● Double pectoral fins</li> <li>● Each actuator is differentially controlled</li> </ul>	<ul style="list-style-type: none"> <li>➤ Higher flapping frequency does not necessarily result in higher swimming speed</li> </ul>	
Pectoral Fin and Dual Caudal Fin Robot [106]	2016	<ul style="list-style-type: none"> <li>● Inspired by insect wings and fish fins</li> <li>● Two tail fins</li> <li>● Two pectoral fins</li> </ul>	<ul style="list-style-type: none"> <li>➤ Multifunctional maneuvering motion, motion switching and obstacle avoidance</li> </ul>	N/A

## 4. Undulating Propulsion Underwater Robot Propulsion Mechanisms

Exploring the propulsion mechanisms of underwater biomimetic robots is essential for the development of new prototypes and the continuous refinement of existing types. Researchers have investigated propulsion mechanisms by three main methods: theoretical analysis, numerical simulation and experimental testing. The main findings are presented below.

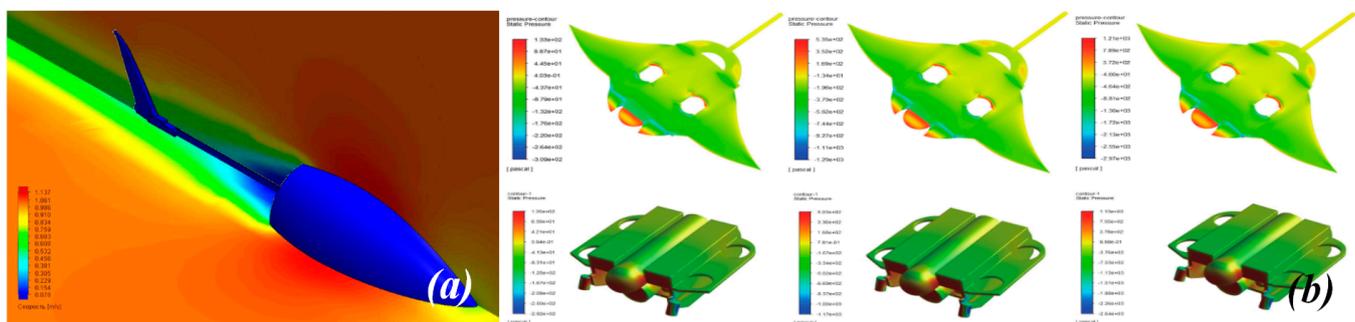
### 4.1. Theoretical and Numerical Simulation Studies

British scholar James Gray observed the daily food intake and swimming distance of dolphins in 1936 and found that the work done by dolphins swimming was seven times the

energy provided by the food they ate, which was called ‘Gray’s problem’ [109]. Gray pioneered the study of biomimetic fish. In 1952, the British physicist Geoffrey Taylor proposed an analytical model based on the resistance theory [110]. He used the ‘static fluid theory’ to solve the dynamics of fish movement. The theory considered the influence of viscous force but the effect of fluid inertial force was ignored, and hence, it was only suitable for small Reynolds number conditions. In 1955, Hancock [109] built on this achievement and put forward the ‘large-scale resistance theory’; however, the effect of fluid inertial force was still ignored. In 1960, Lighthill [111] derived an initial mathematical model of the propulsion mechanism of trevally fish; inspired by the ‘slender body theory’, he successfully applied the theory to the hydrodynamic analysis of fish swimming and then, in 1970, proposed the ‘large-oscillatory slender body theory’ according to the oscillatory amplitude of fish fins [112]. In 1960, Wu et al. [113–115] proposed the ‘two-dimensional undulating plate theory’, in which the research object was simplified into a flexible two-dimensional thin plate with zero thickness and simultaneously considered the inertia, leading-edge suction and wake spread. In 1971, based on the theory of two-dimensional plate fluctuations, the ‘unsteady two-dimensional undulating plate theory’ was proposed, and it was successfully used to analyze the motion performance of flat crescent-shaped fishes. In 1977, Chopra [116] studied the changes in shape of fish fins of different shapes when swimming and developed the ‘two-dimensional resistance theory’, which was considered to consist of the ‘large-oscillatory resistance theory’ and the ‘large-oscillatory slender body theory’. In 1991, Cheng et al. [117] simplified the fish model into a three-dimensional elastic plate and proposed the ‘three-dimensional undulating plate theory’.

With the application of the digital particle imaging tester (DPIT) to the research of fish propulsion mechanisms, studies have become focused on the relationship between eddy currents and fish swimming [118]. In 1994, Stamhuis [119] first applied DPIT technology to study live fish and analyze the changes in the surrounding flow field when the fish swam. Triantfyllou [120] observed that jets appeared behind the body when fish swam, and put forward the ‘jet propulsion theory’. Recently, with the mature application of simulation software and fluid dynamics software, CFD is used increasingly for kinematics and dynamics analysis [121].

Wai Pik Lau [122] derived a propulsion model for underwater biomimetic robots based on elongated body theory and created a simulation model for kinematic analysis. The Mackerel Robot designed by Li Wen used this simulation model to analyze the relationship between amplitude, efficiency and propulsion speed [88]. As shown in Figure 4, a simulation of the kinematic body drag distribution of a robot fish was carried out by Iliya Mitin et al. [43]. Finite element analysis of the kinematics and hydrodynamics of a robot fish was carried out by Qimeng Liu et al. [92].



**Figure 4.** Simulations of some biomimetic robotic fish. (a) Thunniform Robotic Fish [43] (b) Manta Ray Robot [92].

There is still a certain gap between theoretical derivation, numerical simulation results and actual testing of robot fish due to factors such as the material, structure, and operating environment of underwater biomimetic robots. Although simulation results can be utilized

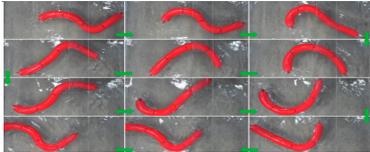
as a reference for mechanism exploration, it is still of critical importance to carry out an experimental study of the prototype.

4.2. Experimental Studies on the Propulsion Mechanism

4.2.1. Experimental Studies of Anguilliform Robots

As shown in Table 9, the Multi-joint Underwater Robot was tested in a river and the curves of lateral motion and longitudinal motion were obtained. The overall motion curve was smooth, which verified the good motion performance of the robot in the river [64]. The soft eel robot was tested in a water tank in the laboratory. With the help of high-speed cameras, it was found that swimming efficiency was dependent on both body fluctuations and body posture in situ [65]. The Lampetra Project has conducted experiments both in a laboratory tank and on land. They found that the robot was able to autonomously avoid different obstacles and swim continuously at the speed of a real creature for 5 h. The robot has a length of 0.99 m and a velocity of 0.3 m/s. For an anguilliform robot, this is a relatively high swimming speed [62]. Experiments on Salamandra Robotica II also showed that changing the curvature of the body can control the trajectory of the robot [66].

Table 9. Anguilliform biomimetic robots: experimental research.

Robot	Test Objectives	Test Conclusions	Picture
Multi-Joint Underwater Robot [64]	<ul style="list-style-type: none"> <li>● Obtained the horizontal motion and vertical motion curves</li> </ul>	<ul style="list-style-type: none"> <li>➤ Overall motion control results are satisfactory</li> </ul>	
Soft Eel Robot [65]	<ul style="list-style-type: none"> <li>● Images of frequency and motion posture were obtained</li> </ul>	<ul style="list-style-type: none"> <li>➤ Swimming efficiency depends both on thrust generated and on in situ body position</li> </ul>	
Salamandra Robotica II [66]	<ul style="list-style-type: none"> <li>● Analyzed the relationship between attitude and speed</li> </ul>	<ul style="list-style-type: none"> <li>➤ The speed increases monotonously with the frequency</li> <li>➤ Changing the curvature of the body can control the trajectory</li> </ul>	N/A

4.2.2. Experimental Studies of Subcarangiform and Carangiform Robots

As shown in Table 10, G9fish demonstrated that biomimetic modeling with the approximation function was feasible. It has a length of 0.52 m and a speed of 0.2 m/s. [67]. Experiments with the Biomimetic Fish Robot showed that the shape and oscillating frequency of the tail fin directly affected the swimming speed, and the robot reached the highest swimming speed at the natural frequency of the driving tail system [74]. Experiments with the ACP Robot Fish proved that materials used in soft biomimetic robots needed to have different bending moments [81]. The Hydraulic Soft Robotic Fish was a flexible biomimetic robot that could achieve continuous body deformation in water, and it relied on the manufacture of soft drives, utilizing the creation of arbitrary fluid passages to achieve a wide range of continuous curved profiles [68]. The parameters of the Fabricated Bionic Robotic Fish [70], ISplash-I [71] and ISplash-II [72] were verified through experiments, and their speed in the tank was close to that of real fish, showing good motion performance. In particular, ISplash-I can reach 0.85 m/s, which is a relatively high speed [71]. According to experiments with the CPG-based Biomimetic Robotic Fish, the forward speed of the robot increased with the oscillating amplitude and frequency of the body [123].

**Table 10.** Anguilliform biomimetic robots: experimental research.

Robot	Test Objectives	Test Conclusions	Picture
Untethered High-Performance Robotic Tuna [75]	<ul style="list-style-type: none"> <li>◆ Speed Performance</li> <li>◆ Steering Performance</li> </ul>	<ul style="list-style-type: none"> <li>➤ Can achieve both high swimming speed (2.26 m/s) and steering maneuverability with 0.48 BL (body lengths) turning radius</li> </ul>	
Untethered Bioinspired Robotic Fish [76]	<ul style="list-style-type: none"> <li>◆ Free-swimming and dynamic model validation</li> <li>◆ Pitch maneuvers</li> <li>◆ Leaping motion tests</li> </ul>	<ul style="list-style-type: none"> <li>➤ Speed of 3.8 BL/s</li> <li>➤ Achieves high pitch maneuvers by performing an agile front flip motion with a radius of 0.4 BL and an average angular velocity of 439°/s</li> </ul>	
G9fish [67]	<ul style="list-style-type: none"> <li>◆ Two traveling modes, cruising straight line and C-shaped sharp turn</li> </ul>	<ul style="list-style-type: none"> <li>➤ The relative tail motion and approximation error functions have good performance</li> </ul>	
Bio-inspired AUV [77]	<ul style="list-style-type: none"> <li>◆ The performance of the motor and AUV was tested</li> </ul>	<ul style="list-style-type: none"> <li>➤ Accomplishes turns at a body-length-to-turn-radius ratio of 1:1, at a swimming velocity of 1.5 BL/s</li> </ul>	
Soft-bodied Robotic Fish [69]	<ul style="list-style-type: none"> <li>◆ A simulated escape response exercise</li> <li>◆ Compared the kinematics and controllability</li> </ul>	<ul style="list-style-type: none"> <li>➤ Agonistic duration has strong authority over escape angle and minimal authority over linear escape velocity</li> </ul>	
Improved ACP Robot Fish [80]	<ul style="list-style-type: none"> <li>◆ The lateral acceleration was measured with flow and pressure MEMS sensors and analyzed by video</li> </ul>	<ul style="list-style-type: none"> <li>➤ The force of the propulsion unit near the tail fin has increased by 31% and the frequency of fluctuations has doubled</li> </ul>	
Four-link Carangiform Fish Robot [78]	<ul style="list-style-type: none"> <li>◆ Free-swimming test under randomly set obstacles</li> </ul>	<ul style="list-style-type: none"> <li>➤ Overcame plane obstacles and semi-closed obstacles</li> <li>➤ Determines the shortest path to the target area under the condition of obstacles</li> </ul>	
Four-link Robotic Fish Large Pectoral Fin Control Surfaces [73]	<ul style="list-style-type: none"> <li>◆ Validation of the electromechanical design and swimming performance</li> </ul>	<ul style="list-style-type: none"> <li>➤ Robot fish realizes autonomous obstacle avoidance and three-dimensional swimming</li> </ul>	
Fabricated Bionic Robotic Fish [70]	<ul style="list-style-type: none"> <li>◆ The swimming speed and the angle of fin oscillation were measured</li> </ul>	<ul style="list-style-type: none"> <li>➤ Forward swimming velocity is 24.5 mm/s.</li> <li>➤ The maximum force generated during fin oscillation is 0.39 N</li> </ul>	N/A
ACP Robot Fish [81]	<ul style="list-style-type: none"> <li>◆ Comparing locomotion properties with the kinematics</li> </ul>	<ul style="list-style-type: none"> <li>➤ Use materials with different bending stiffnesses for the compliant parts in different swimming models</li> </ul>	N/A

### 4.2.3. Experimental Studies of Thunniform Robots

As shown in Table 11, researchers analyzed the motion speed of Thunniform Robotic Fish and the mechanical characteristics of the tail fin and it was found that speed increases with increasing vibration frequency of the tail fin [43]. The vortex field behind the Miniature Robotic Fish’s movement and on both sides of its body was analyzed and it was found that non-static water flow would attract live fish [83]. The relationship between the amplitude, efficiency and travel speed of the Mackerel Robot was studied to determine the optimal propulsion efficiency of the robot. It has a length of 0.588 m and a speed of 0.3 m/s [88]. The Single-Motor-Actuated Robotic Fish has a length of 0.37 m and a speed of 1.14 m/s, and, thus, it travels relatively fast [85].

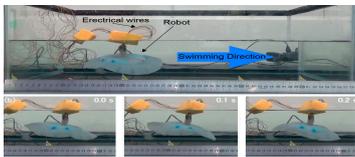
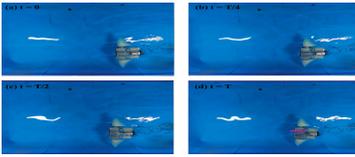
**Table 11.** Thunniform biomimetic robots: experimental research.

Robot	Test Objectives	Test Conclusions	Picture
Gliding Robotic Dolphin [84]	<ul style="list-style-type: none"> <li>Carried out a hydrodynamic analysis of the gliding motion</li> </ul>	<ul style="list-style-type: none"> <li>The robot can spiral and glide gently</li> <li>Obtained the hydrodynamic coefficients</li> </ul>	
Single-Motor-Actuated Robotic Fish [85]	<ul style="list-style-type: none"> <li>The speed was measured when going straight and turning</li> </ul>	<ul style="list-style-type: none"> <li>The maximum forward swimming speed is 1.14 m/s, and the speed is about 90 degrees/s during normal turns</li> </ul>	
Thunniform Robotic Fish [43]	<ul style="list-style-type: none"> <li>Studied the relationship between the moving speed and the shock dynamics of the caudal fin</li> </ul>	<ul style="list-style-type: none"> <li>The speed increases with the increase in the vibration frequency of the caudal fin, but there will be a certain threshold</li> </ul>	N/A
Mackerel Robot [88]	<ul style="list-style-type: none"> <li>Analyzed the relationship between amplitude, efficiency and propulsion speed</li> </ul>	<ul style="list-style-type: none"> <li>The optimal thrust efficiency is in the range of Strouhal number (St) <math>0.3 \leq St \leq 0.325</math></li> </ul>	N/A

### 4.2.4. Experimental Studies of Rajiform Robots

As shown in Table 12, Self-Powered Soft Robots achieved good results in physical tests. Relevant experimental researches were not only completed in lakes but also at a depth of 10,900 m in the Mariana Trench, and the robot swam autonomously in the deep sea at 3224 m in the South China Sea. Thus, experiments proved that underwater biomimetic robots can work in the deep sea, a result that has high application value [90]. Experimental tests of the Cartilage Structure Underwater Robot were similarly successful, although only in laboratory tanks, and the cartilage structure showed extremely high undulating propulsion efficiency [95]. The Manta Ray Robot achieved simple pitch and roll motion patterns in the tank, very close to the motion performance of live fish [92]. The swimming speed of IPMC Manta Ray is 0.067 BL/s, and the mobile power consumption is below 2.5 W [91].

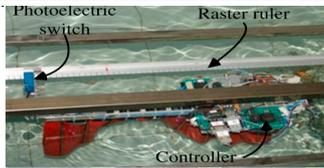
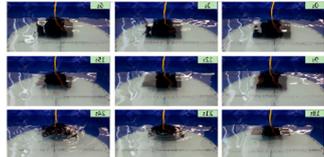
**Table 12.** Rajiform biomimetic robots: experimental research.

Robot	Test Objectives	Test Conclusions	Picture
Cartilage Structure Underwater Robot [95]	<ul style="list-style-type: none"> <li>Robots without cartilage and combined with soft cartilage materials were designed for experiments</li> </ul>	<ul style="list-style-type: none"> <li>Incorporating cartilage structures into the fins improves swimming efficiency. A reasonable arrangement of soft and hard structures is important</li> </ul>	
Manta Ray Robot [92]	<ul style="list-style-type: none"> <li>Tested the motion performance of the robot prototype</li> </ul>	<ul style="list-style-type: none"> <li>Can realize simple pitch and roll motion patterns</li> <li>Can swim forward steadily</li> </ul>	
Self-Powered Soft Robot [90]	<ul style="list-style-type: none"> <li>Verify pressure resilience of electronics and soft actuators</li> </ul>	<ul style="list-style-type: none"> <li>Activated in a field test at a depth of 10,900 m in the Mariana Trench</li> <li>Free swimming at a depth of 3224 m in the South China Sea</li> <li>The pressure resilience of the electronic components and soft actuators is reliable</li> </ul>	N/A
IPMC Manta Ray [91]	<ul style="list-style-type: none"> <li>Analyzed the fins in terms of wing tip deflection, twist angle, and power consumption</li> </ul>	<ul style="list-style-type: none"> <li>The swimming speed of the robot is 0.067 BL/s, and the mobile power consumption is below 2.5 W</li> </ul>	N/A
Bionic Fin Manta Ray [93]	<ul style="list-style-type: none"> <li>Tested the motion performance of fins with different thicknesses</li> </ul>	<ul style="list-style-type: none"> <li>The simple drive method of the design can produce a good propulsion effect</li> </ul>	N/A

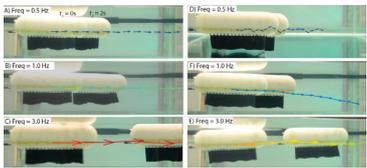
4.2.5. Experimental Studies of Amiiiform and Gymnotiform Robots

In the RoboGnilos undulating propulsion experiment, inclined fin rays produced higher speed and efficiency than vertical fin rays. The Bio-inspired Amphibious Robot could realize three-dimensional swimming in the water and could crawl on the ground [99]. Its motion frequency was 0.5 Hz to 2.5 Hz, and the speed and thrust increased with frequency both underwater and on the ground. The Undulatory Fin Propulsion Bio-Inspired Robot was able to perform various swimming movements like a live fish, and the swimming efficiency was studied [103]. Details of experimental studies of amiiiform and gymnotiform robots are presented in Tables 13 and 14.

**Table 13.** Amiiiform biomimetic robots: experimental research.

Robot	Test Objectives	Test Conclusions	Picture
RoboGnilos [98]	<ul style="list-style-type: none"> <li>Analyzed the influence of morphological parameters on undulating dynamics</li> </ul>	<ul style="list-style-type: none"> <li>Verified the convenience and effectiveness of the modular motor drive structure</li> </ul>	
Bio-inspired Amphibious Robot [99]	<ul style="list-style-type: none"> <li>Tested the motion performance in water and on the ground</li> </ul>	<ul style="list-style-type: none"> <li>Excellent undulating and flapping motion</li> </ul>	
Dorsal Undulation Fin Robot [100]	<ul style="list-style-type: none"> <li>Experimental testing of robotic fish locomotor performance</li> </ul>	<ul style="list-style-type: none"> <li>The proposed kinematic and dynamic models are effective for properties of undulating motion</li> </ul>	N/A

**Table 14.** Gymnotiform biomimetic robots: experimental research.

Robot	Test Objectives	Test Conclusions	Picture
Undulatory Fin Propulsion Bio-Inspired Robot [103]	<ul style="list-style-type: none"> <li>◆ Tested each movement mode of the robot</li> <li>◆ Measured the swimming speed and azimuth angle</li> </ul>	<ul style="list-style-type: none"> <li>➤ Can complete forward swimming, reverse movement, diving, maintaining position and vertical swimming like a live fish</li> </ul>	
Robotic Knifefis [104]	<ul style="list-style-type: none"> <li>◆ Determined how to decompose the force generated by a robotic fin into thrust and drag terms</li> </ul>	<ul style="list-style-type: none"> <li>➤ Measured surge and heave forces and swimming speed as a function of fin frequency, amplitude, and undulating number</li> </ul>	N/A

### 5. Limitations and Future Perspectives

The use of undulating propulsion for underwater robots plays a significant role in harsh marine environments. Although there have been many achievements, there are still some limitations in terms of motion performance, energy utilization and environmental perception. Firstly, the motion performance and maneuverability of undulating propulsion underwater biomimetic robots still need to be enhanced. Recent studies have mainly been conducted in stable fluid environments and how to deal with the impact of harsh water environments still needs to be supplemented and improved. Secondly, improving the energy utilization of underwater biomimetic robots is required for engineering applications, especially solving the energy consumption problem of long-term motion. Thirdly, how to improve robotic perception is the key to expanding the application of robots. Biomimetic robots usually rely on a few simple sensors to perceive the surrounding environment, but they cannot perceive the surrounding environment in harsh conditions as real fish can. Research on undulating propulsion underwater biomimetic robots is still in its infancy and needs continuous optimization in many aspects.

With the further development of biomimetics and material science, underwater biomimetic robots will achieve breakthroughs. Undulating propulsion underwater biomimetic robots will also have new prospects. These prospects include: (1) Given the complexity of the operating environment and tasks, future underwater biomimetic robots will need to not only possess the ability to swim but also possess other abilities, such as underwater grasping, sampling, transport, etc. (2) Increased biological similarity: underwater biomimetic robots will be closer in shape and movement to biological fish, and the degree of simulation and biological similarity will be continuously improved. (3) Improvement of movement efficiency and operation efficiency: with the improvement in control methods and battery technology, it is believed that future underwater biomimetic robots will have higher movement efficiency and operation efficiency. To sum up, future undulating propulsion underwater biomimetic robots will get closer to the form and function of natural organisms, and their motion performance and operating ability will also be continuously enhanced. At the same time, they will have a wider range of applications, including underwater exploration, underwater rescue, submarine engineering, underwater archaeology and aquarium-based entertainment.

### 6. Conclusions

Underwater biomimetic robots have strong operability, stability and mobility in the complex marine environment, all of which play a significant role in underwater exploration, rescue, mining, maintenance and scientific research. This paper provides a brief introduction to fish-based biometric propulsion. Existing underwater biomimetic robots are classified and the main achievements in this field are outlined, as well as the characteristics and advantages of each type. The main propulsion mechanisms of current underwater biomimetic robots are presented mainly through the content of experimental studies, em-

phasizing the importance of experimental studies to the discipline. The limitations and prospects of underwater biomimetic robots are also outlined, demonstrating that, in the future, underwater biomimetic robots will be developed with multiple functionalities and high bio-similarity and operational efficiency.

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