



Article Giant Rotational Magnetocaloric Effect in Ni(*en*)(H₂O)₄·2H₂O: Experiment and Theory

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> **Abstract:** An experimental study of the rotational magnetocaloric effect in Ni(*en*)(H₂O)₄SO₄·2H₂O (*en* = ethylenediamine) single crystal is presented. The study was carried out at temperatures above 2 K and was associated with adiabatic crystal rotation between the easy plane and hard axis in magnetic fields up to 7 T. The magnetocaloric properties of the studied system were investigated by isothermal magnetization measurement. The experimental observations were completed with ab initio calculations of the anisotropy parameters. A large rotational magnetic entropy change $\approx 12 \text{ Jkg}^{-1}\text{K}^{-1}$ and $\approx 16.9 \text{ Jkg}^{-1}\text{K}^{-1}$ was achieved in 5 T and 7 T, respectively. The present study suggests a possible application of this material in low-temperature refrigeration since the adiabatic rotation of the single crystal in 7 T led to a cooldown of the sample from the initial temperature of 4.2 K down to 0.34 K. Finally, theoretical calculations show that S = 1 Ni(II)-based systems with easy-plane anisotropy can have better rotational magnetocaloric properties than costly materials containing rare-earth elements in their chemical structures.

Keywords: rotational magnetocaloric effect; entropy; adiabatic temperature change; magnetic anisotropy; crystal field

1. Introduction

Recently, the magnetocaloric effect (MCE) has become a focus of the physical and material science community [1–8]. The effort is motivated by a search for a more efficient and environmentally friendly alternative for refrigeration and air conditioning. The magnetic coolant represents one of the crucial components of a magnetic refrigerator. Apart from a pronounced magnetocaloric response, it must also meet specific criteria, e.g., a large density of magnetic entropy, nearly zero magnetic hysteresis, very small thermal hysteresis, small specific heat, large thermal conductivity, high chemical stability, low cost, availability, and simple sample synthesis [9].

The conventional MCE is based on the heating (normal MCE) or cooling (inverse MCE) of the system exposed to an increasing external magnetic field. Two parameters are essential for the quantitative expression of MCE, namely, the isothermal magnetic entropy change (ΔS_M) and the adiabatic temperature change (ΔT_{ad}) [4,10]. The mentioned parameters are influenced by the magnitude of external magnetic field change. Obviously, the efficient magnetic refrigerants for active MCE should have the given parameters in the relevant temperature and magnetic field ranges as large as possible. Designing materials with a large density of magnetic ions while keeping magnetic coupling weak [11,12] as well as tailoring critical behavior [13] have become conventional approaches in tuning magnetocaloric properties. Alternatively, properties of spin liquids in quantum spin chains [14] and localized excitations in geometrically frustrated magnets proved an enhanced magnetocaloric effect in these systems.



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In addition, in recent years, the topic of the rotational magnetocaloric effect has come to the forefront in the field of magnetic cooling [15-27]. The cooling of the sample is obtained by a simple rotation of the magnetocaloric material in a constant magnetic field from the easy to hard magnetization axis. The rotation of a magnetocaloric material changes its entropy, referred to as a rotational entropy change, ΔS_R . A large value of ΔS_R causes a significant temperature change during the rotation of the sample, and therefore the presence of the magnetic anisotropy of the system is a necessary condition for the observation of a large rotational MCE. It is important to note that all investigated systems with large rotational MCE contained rare-earth elements in their chemical structures. However, the single crystal preparation of these materials is money-, time-, and energy-consuming. For this reason, the given materials may not meet the important criteria for selecting appropriate magnetic refrigerants. It should be noted that the magnetocaloric properties of financially affordable S = 1 Ni(II)-based systems have been studied. Their properties can be tuned by magnetic dimensionality, exchange coupling, and single-ion anisotropy [28–30]. If the S = 1 Ni(II)-based systems are described within a model of a spin-1 paramagnet in a crystal field with a spin Hamiltonian $H = DS_z^2 + E(S_x^2 - S_y^2)$, where *D* and *E* represent uniaxial and in-plane anisotropy parameters, respectively, an inverse MCE can be observed for the easy-plane anisotropy [31]. Thus, considering the combination of normal and inverse MCE, a large rotational MCE can be expected, comparable to the rotational MCE observed in materials containing rare-earth elements in their chemical structures.

The title compound Ni(*en*)(H₂O)₄SO₄·2H₂O (*en* = ethylenediamine) (NEHS) has been identified as a spin-1 paramagnet with the nonmagnetic ground state introduced by the easy-plane anisotropy $D/k_{\rm B} = 11.6$ K with E/D = 0.1 and negligible exchange interactions $J \approx 0$ [32]. Analysis of the specific heat in zero magnetic field indicated the absence of a phase transition to a magnetically ordered state below 1.8 K as a direct consequence of the dominant influence of the crystal field on the magnetic properties of the studied system.

This work presents an experimental study of the rotational MCE in NEHS single crystal at temperatures above 2 K, associated with adiabatic crystal rotation between the easy plane and hard axis in magnetic fields up to 7 T. The experimental observations are completed with ab initio calculations of the anisotropy parameters. Besides that, theoretical simulations of the rotational MCE in the S = 1 paramagnet were performed, and the simulations were compared with experimental data. Based on the present results, the design of better magnetocaloric properties of financially affordable S = 1 Ni(II)-based systems is discussed.

2. Materials and Methods

The crystal structure of NEHS is a monoclinic, space group C 2/c with the unit cell parameters a = 9.523 Å, b = 12.185 Å, c = 11.217 Å, $\beta = 107.3^{\circ}$; and Z = 4 [33]. The crystal structure consists of [Ni(*en*)(H₂O)₄]²⁺ cations, [SO₄]²⁻ anions, and two molecules of water. These units are connected by a large number of hydrogen bonds [33]. NEHS single crystals were prepared in the form of blue prisms from an aqueous solution of nickel sulphate and *en* in stoichiometric amounts.

Isothermal magnetization curves were measured in a commercial superconducting quantum device (SQUID) magnetometer in magnetic fields up to 7 T in the temperature range from 2 K to 20 K. A single crystal of NEHS glued to a quartz holder with a mass of 2.58 mg and dimensions $3 \times 1 \times 0.3$ mm³ was used (Figure 1).





Ab initio calculations were performed using the computational package ORCA 5.0.1 [34]. The estimates of single-ion anisotropy parameters were based on the state-averaged complete-active-space self-consistent field wave functions (SA-CASSCF) with tight SCF convergence criteria, including the following N-electron valence second-order perturbation theory (NEVPT2) [35–39]. The active space was defined on metal-based *d*-orbitals for Ni(II) as CAS(8,5) and CAS(8,10). The state averaged approach was used with all 10 triplet and 15 singlet states equally weighted. The ZFS parameters were calculated through the quasi-degenerate perturbation theory [40–42]. Relativistic effects were taken into account by using the zeroth-order regular approximation [43,44] together with the corresponding segmented all-electron relativistic contracted version of the triple- ζ basis set Def2-TZVP [45] for all atoms. The calculations utilized the RI approximation and the chain-of-spheres (RIJCOSX) approximation to exact exchange [46–48].

3. Results

The single-ion anisotropy parameters, together with the orientations of local anisotropy axes of Ni(II) ions in NEHS [33], were predicted using ab initio calculations in ORCA on $[Ni(en)(H_2O)_4]^{2+}$ cation using atom positions as obtained from X-ray diffraction. The SA-CASSCF/NEVPT2 calculations yielded crystal field parameters $D/k_B = 11.5$ K, E/D = 0.07 with an average g-factor g = 2.22. This result is in excellent agreement with the values obtained from the analysis of the heat capacity in the zero magnetic field [32]. The crystal structure of a $[Ni(en)(H_2O)_4]^{2+}$ cation with the schematic orientation of the equatorial plane of the octahedron and local anisotropy axes predicted by SA-CASSCF/NEVPT2 calculations is shown in Figure 2. It can be seen that the local anisotropy Z-axis is parallel to the direction of the bond between the nickel ion and oxygen, which corresponds to the axis of the octahedron. On the other hand, the local anisotropy axes X and Y are located within the equatorial plane of the octahedron, with the X-axis passing along the bisector axis of the oxygen–nickel–oxygen angle while the Y-axis is oriented along the bisector axis of the oxygen–nickel–nitrogen angle.

The field dependence of the magnetization of NEHS for the magnetic field parallel to the *Y*-axis is shown in Figure 3a. It can be seen that the value of the magnetization increases with increasing magnetic field for each temperature, but the magnetization does not reach its saturation value even at the lowest measured temperatures. On the other hand, the magnetization decreases with increasing temperature for all magnetic fields, which implicates a normal magnetocaloric effect for the orientation *B* | | *Y*.



Figure 2. The crystal structure of $[Ni(en)(H_2O)_4]^{2+}$ cation in NEHS with the schematic orientation of the equatorial plane of the octahedron and local anisotropy axes determined by ORCA calculations.



Figure 3. Magnetic-field dependence of the magnetization of NEHS for $B \parallel Y$ (**a**) and $B \parallel Z$ (**b**,**c**), temperature steps $\Delta T = 0.5$ K and 1 K for intervals 2–10 and 11–20 K, respectively.

A different situation was observed for the field dependence of the magnetization in the magnetic field parallel to the Z-axis (Figure 3b,c). The value of the magnetization increases

with increasing magnetic field for each temperature, but at temperatures between 2 and 5.5 K the magnetization increases with increasing temperature. At higher temperatures the isothermal magnetization curves for $B \mid \mid Z$ show the same behavior as the data for the orientation $B \mid \mid Y$.

For the analysis of the magnetocaloric effect of the system NEHS in both mentioned orientations, the magnetic entropy change was calculated using the Maxwell relation [49]:

$$\Delta S_M(T, \Delta B) = \int_{B_i}^{B_f} \frac{\partial M(T, B)}{\partial T} dB,$$
(1)

where $\Delta B = B_i - B_f$, while B_f and B_i stand for the final and initial magnetic fields, respectively. Due to the real conditions of the experiment, relation (1) can be replaced by:

$$\Delta S_M\left(\frac{T_j + T_{j+1}}{2}, B\right) = \sum_{j} \frac{\left(M_{j+1} - M_j\right)_B}{T_{j+1} - T_j} \Delta B,$$
(2)

where M_{i+1} and M_i are the magnetization values measured in the magnetic field B at temperatures T_{i+1} and T_i , respectively. The temperature dependence of the magnetic entropy change (Equation (2)) calculated for several B_f values and $B_i = 0$ T for the orientations $B \mid | Y$ and $B \mid | Z$ is shown in Figure 4. It can be seen that the normal MCE has been observed for the orientation $B \mid Y$ in a whole range of temperatures and magnetic fields. The maximum value of $-\Delta S_M$ is shifted towards high temperatures with increasing magnetic fields. A large magnetocaloric effect is observed around 6 K ($-\Delta S_{max} = 10.9 \text{ Jkg}^{-1}\text{K}^{-1}$ for 7 T). However, an interesting situation is observed in the temperature dependence of $-\Delta S_{\rm M}$ for the orientation $B \parallel Z$. Approximately below 7 K, an inverse magnetocaloric effect is observed for all magnetic field values, with $-\Delta S_M$ decreasing with increasing magnetic field. On the other hand, the temperature dependence of $-\Delta S_M$ above 7 K has a similar tendency as the data in the orientation $B \mid \mid Y$. Large inverse magnetocaloric effect is observed around 2 K ($-\Delta S_{max} = -14.5 \text{ Jkg}^{-1}\text{K}^{-1}$ for 7 T). Further analysis of the experimental data was performed using the model of the S = 1 paramagnet, including single-ion anisotropy with $D/k_{\rm B}$ = 11.6 K, E/D = 0.1, and g = 2.16 as obtained from the previous analysis of specific heat and susceptibility [32]. Corresponding theoretical prediction of the temperature dependence of $-\Delta S_{\rm M}$ for both field orientations is in excellent agreement with experimental data (Figure 4).



Figure 4. Temperature dependence of the isothermal entropy change in NEHS at different magnetic fields for $B \parallel Y$ (**a**) and $B \parallel Z$ (**b**). Symbols represent $-\Delta S_M$ values obtained from experimental magnetization curves; solid lines represent $-\Delta S_M$ values calculated for the S = 1 paramagnet with E/D = 0.1, $D/k_B = 11.6$ K and g = 2.16.



Figure 5. Isothermal entropy changes resulting from the rotation of NEHS single crystal between the *Y* and *Z* axes in constant magnetic fields (symbols). Lines represent $-\Delta S_R$ values calculated for the *S* = 1 paramagnet with E/D = 0.1, $D/k_B = 11.6$ K and g = 2.16. Inset: Field dependence of $-\Delta S_{R,max}$.

The isothermal rotational entropy change as a result of the isothermal rotation of NEHS single crystal in constant magnetic field from the initial sample position $B \mid \mid Z$ to the position $B \mid \mid Y$ yields from the relation:

$$\Delta S_R = \Delta S_M(B \parallel Y) - \Delta S_M(B \parallel Z). \tag{3}$$

The resulting isothermal rotational entropy change is shown in Figure 5. The maximal value of $-\Delta S_{R,max}$ increases with increasing magnetic field and is shifted to lower temperatures. However, high values, $-\Delta S_R \approx 12 \text{ Jkg}^{-1}\text{K}^{-1}$ and $-\Delta S_R \approx 16.9 \text{ Jkg}^{-1}\text{K}^{-1}$, are achieved in 5 T and 7 T, respectively. It should be mentioned again that the temperature dependence of $-\Delta S_R$ is in excellent agreement with the theoretical prediction.

The temperature dependence of the total (i.e., magnetic and lattice) entropy in NEHS was used for the calculation of the adiabatic temperature change $-\Delta T_{ad,R}$, associated with sample rotation in constant magnetic field from the initial sample position $B \mid \mid Y$ to the position $B \mid \mid Z$ under adiabatic conditions. The total entropy in the zero magnetic field was calculated from the experimental specific heat data from Ref. [32]. The temperature dependence of the total entropy in different magnetic fields for both orientations was calculated as the difference between the total entropy of NEHS in zero magnetic field and the absolute values of $\Delta S_{\rm M}$ obtained from experimental magnetization curves (Figure 6). The unavailable experimental d of the total entropy for the S = 1 paramagnet with E/D = 0.1, $D/k_{\rm B} = 11.6$ K, g = 2.16 with included lattice entropy of NEHS taken from Ref. [32]. It can be seen that the mentioned model perfectly describes the experimental d of the total entropy in magnetic fields to the total entropy in magnetic fields for B $\mid \mid Z$.

The temperature dependence of the adiabatic temperature change $-\Delta T_{ad,R}$, calculated from the total entropy, is shown in Figure 7. The maximal value of $-\Delta T_{ad,R}$ is shifted to higher temperatures with an increasing magnetic field. Rotation of the crystal from position $B \parallel Y$ to position $B \parallel Z$ in 5 T and 7 T at the initial temperature of 6.5 K and 8.4 K leads to $-\Delta T_{ad,R} \approx 3.55$ K and 6.95 K, respectively. If the initial temperature of 4.2 K is considered, the rotation of the crystal in conditions mentioned above in 5 and 7 T leads to cooling of the samples to 1.4 K and 0.34 K, respectively, which suggests the applicability of this material in low-temperature refrigeration. Examples of conventional and rotational magnetocaloric properties of selected magnetic refrigerants compared with the studied system NEHS are given in Table 1. One can conclude that NEHS is not a very suitable



material in conventional magnetocaloric applications; however, in rotational MCE it is competitive with expensive materials containing rare-earth metal ions.

Figure 6. Temperature dependence of the total (i.e., magnetic and lattice) entropy in NEHS at different magnetic fields for $B \mid \mid Y$ (**a**) and $B \mid \mid Z$ (**b**). Symbols represent the total entropy calculated as the difference between the total entropy of NEHS in zero magnetic field (calculated from the experimental specific heat) and the absolute values of $\Delta S_{\rm M}$ obtained from experimental magnetization curves. Lines represent the total entropy of NEHS. Inset: Temperature dependence of specific heat of NEHS in zero magnetic field taken from Ref. [32].



Figure 7. Adiabatic temperature change as a function of the initial temperature, i.e., cooling NEHS single crystal during the adiabatic rotation from the position $B \mid \mid Y$ to the orientation $B \mid \mid Z$ in the constant magnetic fields (symbols). Lines represent the results of the extrapolation of total entropy data for orientation $B \mid \mid Z$ below 2 K. The dashed line represents the theoretical prediction of the adiabatic temperature change in the mentioned rotation conditions for NEHS single crystal in the critical magnetic field B_c (see text below).

System ——	$-\Delta S_M^{max}$ (Jkg $^{-1}$ K $^{-1}$)		$-\Delta S_M{}^R$ (Jkg $^{-1}K^{-1}$)		
	<i>B</i> = 5 T	$B = 7 \mathrm{T}$	$B = 5 \mathrm{T}$	$B = 7 \mathrm{T}$	- Keterences
Ni(en)(H ₂ O) ₄ SO ₄ ·2H ₂ O	7.6, -8	10.9, -14.5	12	16.9	This work
HoNiGe ₃	13.9	≈ 16	12.3	≈ 13	[23]
NdGa	-	21.1	-	16.6	[22]
Tb ₂ CoMnO ₆	-7.5	-17.3	20.8	20.5	[21]
<i>h</i> -ErMnO ₃	20.5	22.7	17	20	[20]
o-DyMnO ₃	14.6	17.25	14.2	16.3	[19]
HoMn ₂ O ₅	10	13.1	10	12.43	[18]
TbMn ₂ O ₅	12.35	13.35	≈ 12	13.14	[17]
GdVO ₄	≈ 44	56.03	$\approx\!8$	10.1	[16]
DyScO ₃	21.18	21.91	21.61	22.41	[15]
TbScO ₃	23.71	24.71	23.63	24.58	[50]

Table 1. Examples of conventional and rotational magnetocaloric properties of selected potential refrigerants.

As already mentioned, the system NEHS was identified as a spin-1 paramagnet with the nonmagnetic ground state induced by the easy-plane anisotropy with $D/k_{\rm B} = 11.6$ K and E/D = 0.1. For this system, there is a critical value of the magnetic field B_c equal to $\sqrt{(D^2 - E^2)}/(g\mu_B)$ when the energy levels cross, and the character of the ground state changes. For the description of the rotational magnetocaloric effect of the S = 1paramagnet with easy-plane anisotropy, the temperature dependence of the isothermal entropy change was calculated for magnetic fields applied parallel and perpendicular to the easy plane. For simplicity, only parameter D was considered. It can be seen (Figure 8a) that the normal MCE is observed for orientation $B \mid \mid$ easy plane in the whole range of temperatures and magnetic fields. The maximum value of $-\Delta S_{\rm M}$ is shifted towards low temperatures with decreasing magnetic field. Different behavior is observed for magnetic fields parallel to the hard axis. For temperatures $k_{\rm B}T/D < 0.5$, an inverse magnetocaloric effect is observed for all considered magnetic field values, while the $-\Delta S_{\rm M}$ acquires the maximum value equal to ≈ -5.76 Jmol⁻¹K⁻¹ in the critical magnetic field. However, the magnitude of the inverse magnetocaloric effect begins to decrease with magnetic fields above B_c at temperatures below $k_B T/D \approx 0.5$. Normal MCE is observed at temperatures above $k_{\rm B}T/D \approx 0.5$ for all values of the magnetic field, while $-\Delta S_{\rm M}$ is larger with the increasing magnetic field. The resulting isothermal rotational entropy change for the mentioned model is shown in Figure 8b. The largest rotational MCE is observed in the critical magnetic field, $-\Delta S_R \approx 5.76 \text{ Jmol}^{-1}\text{K}^{-1}$, at temperatures below $k_B T/D \approx 0.15$. In higher magnetic fields exceeding B_c , the isothermal rotational entropy change decreases and the maximum of $-\Delta S_{\rm R}$ is shifted to higher temperatures.

The critical field for NEHS can be estimated as $B_c \approx 7.95$ T. The theoretical prediction of the temperature dependence of the adiabatic temperature change $-\Delta T_{ad,R}$ for this magnetic field value was calculated, as depicted in Figure 7. Apparently, in the critical field the $-\Delta T_{ad,R}$ reaches a maximum at T = 9.7 K and $-\Delta T_{ad,R} \approx 9.5$ K. At liquid helium temperatures (i.e., the initial temperature of 4.2 K), the rotation leads to $-\Delta T_{ad,R} \approx 4.18$ K, suggesting the applicability of this material in low-temperature cooling at the critical magnetic field.

The aforementioned theoretical calculations show that the largest rotational magnetocaloric effect is observed at the critical magnetic field B_c . If B_c is equal to 1, 2, 3, 4, 5, or 6 T, the parameter D/k_B must be equal to 1.45, 2.90, 4.35, 5.81, 7.26, and 8.71 K, respectively, to achieve a similar effect for spin-1 systems with easy-plane anisotropy (neglecting in-plane anisotropy parameter *E*).



Figure 8. (a)Temperature dependence of the isothermal entropy change for the S = 1 paramagnet with easy-plane anisotropy for $B \parallel i$ easy plane (dotted lines) and $B \parallel i Z$ (solid lines) at different magnetic fields; (b) isothermal entropy changes resulting from the rotation of S = 1 paramagnet with easy-plane anisotropy between the easy plane and hard axis in constant magnetic fields. The critical magnetic field B_c was calculated using relation $B_c = D/(g\mu_B)$.



Figure 9. Theoretical prediction of an adiabatic temperature change as a function of the initial temperature, i.e., cooling of the S = 1 paramagnet with the stated values of single-ion anisotropy and g = 2.16 during the adiabatic rotation from the easy plane to the hard axis in the constant critical magnetic fields. The lattice specific heat of NEHS was considered in the calculations.

Suppose the considered systems have a lattice specific heat comparable to the NEHS system. In that case, it is possible to calculate the adiabatic temperature change as a function of the initial temperature during the rotation of a single crystal from the easy plane to the hard axis in adiabatic conditions in the mentioned critical magnetic fields (Figure 9). The maximal values of $-\Delta T_{ad,R}$ shift to higher temperatures with increasing critical magnetic fields, and the rotation leads to $-\Delta T_{ad,R} \approx 4.18$ K at an initial temperature of 4.2 K for critical magnetic fields higher than 3 T.

To date, the largest rotational MCE has been observed in the system of HoNiSi in the magnetic field 5 T, where $-\Delta S_{\rm R} = 26.7 \, \text{Jkg}^{-1} \text{K}^{-1}$ [51]. Theoretical calculations show that the same value of rotational magnetic entropy change in the magnetic field of 5 T has a

spin-1 magnet with a nonmagnetic ground state introduced by easy-plane anisotropy with $D/k_{\rm B} = 7.26$ K and with a molecular mass of 215.73 g.mol⁻¹. Such theoretical estimates could help find financially affordable S = 1 Ni(II)-based systems with better magnetocaloric properties than materials containing rare-earth elements in their chemical structures.

4. Conclusions

This work presents an experimental study of the rotational magnetocaloric effect in Ni(*en*)(H₂O)₄SO₄·2H₂O single crystal at temperatures above 2 K, associated with adiabatic crystal rotation between the easy plane and hard axis in magnetic fields up to 7 T. The magnetocaloric properties of the studied system were investigated by isothermal magnetization measurement. The experimental observations were completed with ab initio calculations of the anisotropy parameters. The calculations enabled determination of the single-ion anisotropy parameters together with the orientations of local anisotropy axes of Ni(II) ions. The calculated values of the single-ion anisotropy parameters are in excellent agreement with the values obtained from previous analysis of heat capacity. A large rotational magnetic entropy change $\approx 12 \text{ Jkg}^{-1}\text{K}^{-1}$ and $\approx 16.9 \text{ Jkg}^{-1}\text{K}^{-1}$ was achieved in 5 and 7 T, respectively.

The present study reveals that adiabatic rotation of the crystal in 7 T starting at the initial temperature of 4.2 K leads to the cooling of the sample down to 0.34 K, which suggests a possible application of this material in low-temperature refrigeration.

Finally, our simulations show that S = 1 Ni(II)-based systems with easy-plane anisotropy can have better rotational magnetocaloric properties than costly materials containing rareearth elements in their chemical structures.

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