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# A Scenario-Based Optimization Model for Planning Sustainable Water-Resources Process Management under Uncertainty

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Abstract: Discrepancies between water demand and supply are intensifying and creating a need for sustainable water resource process management associated with rapid economic development, population growth, and urban expansion. In this study, a scenario-based interval fuzzy-credibility constrained programming (SIFCP) method is developed for planning a water resource management system (WRMS) that can handle uncertain information by using interval values, fuzzy sets, and scenario analysis. The SIFCP-WRMS model is then applied to plan the middle route of the South-to-North Water Diversion Project (SNWDP) in Henan Province, China. Solutions of different water distribution proportion scenarios and varied credibility levels are considered. Results reveal that different water-distribution proportion scenarios and uncertainties used in the SIFCP-WRMS model can lead to changed water allocations, sewage discharges, chemical oxygen demand (COD) emissions, and system benefits. Results also indicate that the variation of scenarios (i.e., from S2 to S3) can result in a change of 9% over the planning horizon for water allocation in the industrial sector. Findings can help decision-makers resolve conflicts among economic objective, water resource demand, and sewage discharge, as well as COD emissions.

**Keywords:** programming; scenario analysis; South-to-North Water Diversion Project of China; uncertainty; water-resources process management

# 1. Introduction

## 1.1. Motivation

A safe and reliable water supply is a basic condition for human settlements, standard of living, economic growth and ecological environment improvement. Global water resource issues are becoming increasingly serious owing to rapid economic development, population growth, and urban expansion [1]. Disparities between increased demand and limited water supply are, thus, intensifying and putting great pressure on sustainable water resource management [2,3]. When water shortages occur, residents' living standards, economic development, and the ecological environment may be affected [4,5]. Any individual water-related activity may affect processes within a water resource system [6,7]. These issues have forced decision-makers to take great efforts to improve water resource utilization efficiency and alleviate the pressure on the water supply, such as the Global Water Partnership (GWP), International Hydrological Programme (IHP), and International Water Resources Association (IWRA), as well as the



Water Diversion Project (WDP) [8]. The WDP is indispensable in relieving excessive pressure on water resources and promoting the sustainable increase of the local economy and has been widely used in China for projects that include the South-to-North Water Diversion Project (SNWDP) [9,10]. However, the water resource management system (WRMS) is a large, complex, dynamic, and nonlinear system that involves multiple water-receiving areas and multiple water users [11,12]. Each water-receiving area includes diverse elements from hydrogeological, economic, social, and environmental aspects. Any water user (e.g., agricultural, industrial, domestic, and ecological) in each water-receiving area has different water resource requirements and competes for resources in every planning period [13]. Therefore, effective system analysis methods are desired for planning WRMS and raising water utilization efficiency corresponding to such complexities and uncertainties.

## 1.2. Literature Review

Previously, many works were introduced for planning WRMS problems, such as linear programming, dynamic programming, and artificial intelligence-based algorithms (abbreviated as LP, DP, and AI, respectively) [14–18]. For example, Castelletti et al. [14] proposed artificial neural networks (ANNs) for addressing the dynamic problems of the reservoir network's management problems in a real-world case study of the River Piave. Bi et al. [15] utilized genetic algorithms (GAs) for optimizing water distribution systems, in which the efficiency of GAs was increased by using heuristic domain knowledge in the sampling of the initial population. Veintimilla-Reyes et al. [16] employed a mixed integer linear programming (MILP) approach to distribute water resources under different temporal and spatial variations. Abdulbaki et al. [17] presented an integer linear programming (ILP) model to optimize the allocation of water resources, in which conventional water treatment costs, wastewater costs, desalination costs, and pumping and transportation costs were represented with an integer variable. Robert et al. [18] introduced a DP approach that embedded different year and season decision stages to optimize an irrigation water system. Generally, the above studies mainly focused on dealing with WRMS problems when their system components were deterministic. However, some coefficients are not deterministic because of various uncertainties existing in WRMS, such as the randomness of available water (e.g., stream flow, precipitation, and climate change), the imprecision in modeling parameters (e.g., uncertainty of data acquisition and data utilization), and the fuzziness of system objectives and constraints [19–22]. Therefore, robust optimization techniques are indispensable for planning WRMS problems in response to the associated complexities and uncertainties.

Over the past decades, research has focused on WRMS for handling complexities and uncertainties such as interval-parameters programming (IPP), fuzzy programming (FP), and scenario analysis (SA) methods [23–28]. For instance, Maqsood et al. [23] used an IPP method for planning WRMS, in which agricultural and industrial water demands presented as interval numbers were solved. Safavi et al. [25] analyzed various water demand-supply scenarios in the Zayandehrud River basin in Iran using an existing and calibrated model. Autovino et al. [26] presented a SA approach to optimize the irrigation scheme for orchards by testing various irrigation water amounts and systems. Zhang et al. [28] introduced a fuzzy-confidence constraint programming method to evaluate various monthly inflows and rainfall amounts and optimize crop water resources.

#### 1.3. Research Gap

Generally, the IPP approach proposed by Maqsood et al. [23] can deal with inconclusive coefficients that are presented as interval numbers, while it can hardly reflect the subjective attitudes toward the decision-makers owing to unknown membership distribution functions [29]. The FP method formulated by Zhang et al. [28] can effectively address precise parameters using fuzzy sets; however, it is incapable of handling different scenarios [30]. SA proposed by Safavi et al. [25] and Autovino et al. [26] can handle uncertainties using various modeled scenarios, while many scenarios are required for accurate modeling of any uncertainty [27,31]. Moreover, in practical WRMS planning issues, some parameters, such as water resource demand for each water user, are based on the experts' and

stakeholders' subjective inference, and the predicted results may be changed by the meteorological, social, economic, and human conditions. These parameters may be presented as dual uncertainties, which results in a dilemma for the optimization approaches to solve such WRMS issues. Thus, robust optimization techniques are indispensable because they integrate the advantages of IPP, FP, and SA into one approach for jointly addressing the associated complexities and uncertainties in WRMS management problems.

## 1.4. Innovation and Organization

The purpose of this study is to develop a scenario-based interval fuzzy-credibility constrained programming (SIFCP) approach for multi-uncertainty reflection in the WRMS. SIFCP combines the advantages of fuzzy-credibility constrained programming (FCP), IPP, and SA into one framework. Compared to IPP, FCP, and SA, SIFCP can handle single uncertainties presented as interval, fuzzy, and modeled information, and cope with dual uncertainties presented as interval-fuzzy parameters or interval-scenarios. A SIFCP-WRMS model is formulated to plan the middle route of SNWDP in Henan Province, China. In SIFCP-WRMS, four scenarios with different water distribution proportions were considered for examining the variations of water resources allocation schemes. Summarily, SIFCP-WRMS model has advantages of: (a) reflecting dual uncertainties expressed as interval-fuzzy parameters and interval-scenarios; and (b) balancing adjustment of the conflict among system benefit, water resource demand-supply balance, and sewage discharge, as well as chemical oxygen demand (COD) emission. Results can provide decision support for achieving effective schemes of water resource allocation with a cost-efficient and uncertainty-averse manner.

The paper's organization is as follows: Section 1 is the introductory section, which includes the study's motivation, literature review, and research gap, as well as the innovation and contribution; Section 2 shows the whole process for formulating the SIFCP-WRMS model that consists of the two subsections (SIFCP method development and SIFCP-WRMS modelling formulation); Section 3 depicts the application of SIFCP-WRMS model into a real case of the middle route of the SNWDP in China, wherein three subsections, 'Statement of problems', 'Data collection', and 'Result analysis' are included; and, finally, Section 4 illustrates the conclusions and outlook of this study.

## 2. Development of SIFCP-WRMS Model

#### 2.1. SIFCP Method Development

A decision-maker has a responsibility to allocate water resources within a maximum system benefit and a minimum sewage discharge in a long-term planning period [32]. In practical water resource management (WRM) problems, the water resources' demand may be different from each sector in every period, and the proportion of each water-user sector may be previously unknown. Such uncertainties could bring about complexities in WRM related to the system satisfaction. FCP has advantages of reflecting tradeoffs between system performance and failure risk related to the credibility constraints (i.e., constraints of water resource demand in each water-user) through using fuzzy sets [33]. Additionally, various scenarios can also be modeled by the SA approach. Integrating SA into FCP, a general scenario-based fuzzy-credibility constrained programming (SFCP) model can be presented as:

$$\operatorname{Min} E = \sum_{j=1}^{n} c_j x_j \tag{1a}$$

subject to:

$$Cr\left\{\sum_{j=1}^{n} a_{ij} x_j \le \widetilde{b}_i\right\} \ge \lambda_i, \, i = 1, \, 2, \, \dots, \, m \tag{1b}$$

$$x_j \ge 0, \ j = 1, 2, \dots, n$$
 (1c)

where  $x_j$  are decision variables;  $c_j$  and  $a_{ij}$  are coefficients; and  $\tilde{b}_i$  are right-hand side coefficients. *Cr* is the credibility measure which was extensively used in many research fields [34–36]. Let  $\xi$  be a fuzzy variable with membership function u and let r be real numbers [32]. The credibility of  $r \leq \xi$  is expressed by the followed fuzzy sets:

$$Cr(r \le \xi) = \begin{cases} 1 & \text{if } r \le \underline{t} \\ \frac{2t - \underline{t} - r}{2 \times (t - \underline{t})} & \text{if } \underline{t} \le r \le t \\ \frac{r - \underline{t}}{2 \times (t - \underline{t})} & \text{if } t \le r \le \underline{t} \\ 0 & \text{if } r \ge \underline{t} \end{cases}$$
(2)

Let  $\sum_{j=1}^{n} a_{ij}^{\pm} x_{j}^{\pm} = s_{i}^{\pm}$ . Thus, Equation (1b) can be represented as:

$$Cr\{s_i \le b_i\} \ge \lambda_i, \ i = 1, 2, \dots, m \tag{3}$$

Normally, a significant credibility level should be greater than 0.5 [37]. Therefore, based on the definition of credibility, we have the following for each  $1 \ge u_{\tilde{t}_i} \ge \lambda_i \ge 0.5$ :

$$\frac{2b_i - \underline{b}_i - s_i}{2 \times (b_i - \underline{b}_i)} \ge \lambda_i \tag{4}$$

In practical WRM problems, some economic parameters are affected by the socio-economic, political, legislation, and technical factors, which can be difficult to achieve as modeled scenarios or fuzzy sets, but can be presented as interval values using the IPP technique [38]. Through introducing IPP into SFCP, a SIFCP model can be formulated as follows:

$$Min E^{\pm} = \sum_{j=1}^{n} c_{j}^{\pm} x_{j}^{\pm}$$
(5a)

subject to:

$$Cr\left\{\sum_{j=1}^{n} a_{ij}^{\pm} x_{j}^{\pm} \le \widetilde{b}_{i}^{\pm}\right\} \ge \lambda_{i}^{\pm}, i = 1, 2, \dots, m$$

$$(5b)$$

$$\sum_{j=1}^{n} a_{ij}^{\pm} x_j^{\pm} \le b_i^{\pm}, \, i = m+1, \, m+2, \dots, \, K$$
(5c)

$$x_j \ge 0, \ j = 1, 2, \dots, n$$
 (5d)

According to Equation (4) and the transformation of  $\sum_{j=1}^{n} a_{ij}^{\pm} x_j^{\pm} = s_i^{\pm}$ , the SIFCP model can be converted into:

$$\operatorname{Min} E^{\pm} = \sum_{j=1}^{n} c_{j}^{\pm} x_{j}^{\pm}$$
(6a)

subject to:

$$\sum_{j=1}^{n} a_{ij}^{\pm} x_j^{\pm} \le b_i + \left(1 - 2\lambda_i^{\pm}\right) \times \left(b_i - \underline{b}_i\right), i = 1, 2, \dots, m$$
(6b)

$$\sum_{j=1}^{n} a_{ij}^{\pm} x_{j}^{\pm} \le b_{i}^{\pm}, \, i = m+1, \, m+2, \dots, \, K$$
(6c)

$$x_j \ge 0, \ j = 1, 2, \dots, n$$
 (6d)

where  $a_{ij}^{\pm} \in \{R^{\pm}\}^{m \times n}$ ,  $c_j^{\pm} \in \{R^{\pm}\}^{1 \times n}$ , and  $x_j^{\pm} \in \{R^{\pm}\}^{n \times 1}$ ;  $R^{\pm}$  represents interval numbers, where superscripts '-' and '+' represent the lower and upper bounds of the interval values, respectively. In this study, the two-step method (TSM) is used for obtaining the lower and upper bounds of the SIFCP model (i.e.,  $f_{opt}^{\pm} = \left[f_{opt}^{-}, f_{opt}^{+}\right]$  and  $x_{opt}^{\pm} = \left[x_{opt}^{-}, x_{opt}^{+}\right]$ ) under each scenario and each  $\lambda$  level [39].

## 2.2. SIFCP-WRMS Modelling Formulation

In this study, the incomplete economic parameters expressed as interval values can be tackled by IPP. Water resource demand for each water user based on subjective experience of experts and stakeholders can be solved by FCP. The scenarios of various future water distribution proportions are handled by SA. Based on the SIFCP method, a SIFCP-WRMS model can be formulated (see Figure 1). The framework of the SIFCP-WRMS model is divided into three parts: Section 1 is the identification of complexity and uncertainty in SIFCP-WRMS model; Section 2 is the entire development of SIFCP method; Section 3 describes the formulation and application of SIFCP-WRMS model, as well as strategies for decision-makers. The objective of SIFCP-WRMS model is to achieve the maximum system benefit within a series of constraints. The objective function is:

$$\operatorname{Max} f^{\pm} = \sum_{c=1}^{13} \sum_{u=1}^{3} \sum_{t=1}^{3} \left( R_{c,u,t}^{\pm} - C_{c,u,t}^{\pm} \right) \times W_{c,u,t}^{\pm}$$
(7)

Constraints mainly consist of water for urban life demand and supply, minimum proportion of ecology and environment water usage, as well as sewage discharge requirements. They can be depicted as follows:

(1) The constraint of total water resources availability:

$$\sum_{c=1}^{13} \sum_{u=1}^{3} W_{c,u,t}^{\pm} \le T_t^{\pm}$$
(8)

(2) The constraint of water resources for urban life demand:

$$Cr\{W_{c,1,t}^{\pm} \ge Demand_{c,1,t}^{\pm}\} \ge \lambda^{\pm}$$

$$W_{c,1,t}^{\pm} \ge Demand_{c,1,t}^{\pm} + (1 - 2\lambda^{\pm}) \times (Demand_{c,1,t}^{\pm} - Demand_{c,1,t}^{\pm})$$
(9)

(3) The constraint of minimum proportion for ecology and environment water usage:

$$Cr\left\{W_{c,3,t}^{\pm} \ge \sum_{u=1}^{3} W_{c,u,t}^{\pm} \times \widetilde{\alpha}_{c,t}^{\pm}\right\} \ge \lambda^{\pm}$$

$$W_{c,3,t}^{\pm} \ge \sum_{u=1}^{3} W_{c,u,t}^{\pm} \times \alpha_{c,t}^{\pm} + (1 - 2\lambda^{\pm}) \times \left(\alpha_{c,t}^{\pm} - \underline{\alpha}_{c,t}^{\pm}\right)$$
(10)

(4) The constraint of sewage discharge requirements:

$$\sum_{c=1}^{13} \sum_{u=1}^{3} W_{c,u,t}^{\pm} \times P_{c,u,t}^{\pm} \le Sew_{t}^{\pm}$$
(11)

(5) The constraint of COD emission limitation:

$$\sum_{c=1}^{13} \sum_{u=1}^{3} W_{c,u,t}^{\pm} \times P_{c,u,t}^{\pm} \left(1 - \eta_t^{\pm}\right) \le COD_t^{\pm}$$
(12)

(6) The constraint of water resources limitations for industry:

$$Cr\left\{\sum_{c=1}^{3} W_{c,u,t}^{\pm} \times (\widetilde{\beta}_{lb})_{c,t}^{\pm} \ge W_{c,3,t}^{\pm}\right\} \ge \lambda^{\pm}$$

$$\sum_{u=1}^{3} W_{c,u,t}^{\pm} \times ((\beta_{lb})_{c,t}^{\pm} + (1 - 2\lambda^{\pm}) \times ((\beta_{lb})_{c,t}^{\pm} - (\beta_{\underline{l}b})_{c,t}^{\pm})) \ge W_{c,3,t}^{\pm}$$

$$Cr\left\{\sum_{u=1}^{3} W_{c,u,t}^{\pm} \times (\widetilde{\beta}_{ub})_{c,t}^{\pm} \le W_{c,3,t}^{\pm}\right\} \ge \lambda^{\pm}$$

$$\sum_{u=1}^{3} W_{c,u,t}^{\pm} \times ((\beta_{ub})_{c,t}^{\pm} + (1 - 2\lambda^{\pm}) \times ((\beta_{ub})_{c,t}^{\pm} - (\beta_{\underline{l}b})_{c,t}^{\pm})) \le W_{c,3,t}^{\pm}$$
(13a)
$$(13b)$$

(7) Nonnegative constraint:

$$W_{c,\mu,t}^{\pm} \ge 0 \tag{14}$$

The specific nomenclature and abbreviation are shown in Nomenclature and Abbreviations. The detailed solution process of handling the SIFCP-WRMS model is depicted in Figure 2.



Figure 1. Formulation of the SIFCP-WRMS model.



Figure 2. The solution process of SIFCP-WRMS model.

# 3. Application

#### 3.1. Statement of Problems

Henan province, which is in Central China, covers an area of  $167 \times 10^3$  km<sup>2</sup> ( $110^{\circ}21'$  E– $116^{\circ}39'$  E,  $31^{\circ}23'$  N– $36^{\circ}22'$  N) (see Figure 3). The province includes 18 cities and is densely populated with a total population of 107.22 million. In addition, Henan Province is an important transportation and communication hub and material distribution center in China. It is also the most important province for agricultural and food production in China. In 2018, the GDP of the province was 48,05.586 billion RMB. There are more than 1500 rivers in this territory, which receive an average annual precipitation of 500–900 mm, and the amount of annual average water resource is 40.35 billion m<sup>3</sup>. However, the per capita water resource is about 383 m<sup>3</sup>, which is far lower than the international standard for extreme water shortage (500 m<sup>3</sup> per capita). The lack of water resources in Henan directly restricts the sustainable development of the local economy and society, as well as ecological protection. Thus, it is of great importance to encourage developing WDP to satisfy the local water shortage.



Figure 3. Study area.

The middle route of the SNWDP in China originates from the Danjiangkou Reservoir Taoyuan Canal in Xichuan County (Henan Province) and arrives at Tuancheng Lake in Beijing, covering a total length of 1267 km. As a water-receiving area, the total water distribution of the main canal of the province is 2.994 billion m<sup>3</sup>, excluding the allocated water in Danjiangkou Irrigation District and the total dry channel water loss. The water-receiving area of SNWDP in Henan includes 13 cities from south to north, including Dengzhou, Nanyang, Pingdingshan, Xuchang, Luohe, Zhoukou, Zhengzhou, Jiaozuo, Xinxiang, Hebi, Huaxian, Puyang, and Anyang. Water use department consumption is shown in Figure 1, which includes urban life water, industrial water, and ecological environment water. As the economy continues to grow and productivity levels continue to improve, water demand continues to increase, which aggravates the contradiction between water demand and supply.

## 3.2. Data Collection

The planning horizon includes three periods with each having one year (i.e., t = 1 represents the year 2020, t = 2 represents the year 2025, and t = 3 represents the year 2030). In this study, the system parameters from economic, technical, subjective, and observed or estimated aspects were collected from the Statistical Yearbook of Henan Province, survey questionnaires and expert consultations, Henan government official reports, as well as the Henan Province Water Resources Bulletin [40–42]. For instance, the future water resource demand for urban life are based on the water quota in terms of survey questionnaires and expert consultations; the future water resource demand for the industry are dependent on the water consumption per unit of output by means of the Statistical Yearbook of Henan Province. Additionally, four scenarios in relation to different water distribution proportions were considered. In detail, scenario 1 (S1) represents the basic scenario without any particular regulatory or political barriers; scenario 2 (S2) represents equal departmental water distribution proportion for each sector (i.e., 33% of urban life, 33% of industry, and 33% of ecology and environment); scenario 3 (S3) represents different departmental water distribution proportions for each sector (i.e., 50% of urban life, 25% of industry, and 25% of ecology and environment); and scenario 4 (S4) represents

different departmental water distribution proportion for each sector (i.e., 25% of urban life, 50% of industry, and 25% of ecology and environment). Tables 1 and 2 present the water supply situations in the South-to-North Water Transfer Middle Line Project within the scope of Henan Province.

Water-Receiving Area	2014	2015	2016
Dengzhou	0.500	7.543	18.237
Nanyang	5.691	40.197	57.249
Pingdingshan	56.668	19.390	26.324
Xuchang	46.076	63.851	78.539
Louhe	7.586	56.069	53.477
Zhouko	0.000	0.140	15.599
Zhengzhou	180.486	355.238	438.467
Jiaozuo	4.0165	11.318	14.347
Xinxiang	29.833	95.082	109.501
Hebi	17.127	36.709	50.334
Huaxian	0.000	0.030	9.902
Puyang	15.645	46.969	71.246
Anyang	0.000	5.322	30.134
Total	363.630	737.859	973.355

Table 1. Water supply pattern in each water-receiving city in 2014–2016 (10<sup>6</sup> m<sup>3</sup>).

Table 2. Water supply pattern in each water-receiving city under different departments by  $2016 (10^6 \text{ m}^3)$ .

Water-Receiving Area	Water from SNWDP	Water for Urban Life	Water for Industry	Water for Ecology and Environment
Dengzhou	18.237	7.170	4.963	6.105
Nanyang	57.249	19.677	33.712	3.859
Pingdingshan	26.324	5.977	19.874	0.472
Xuchang	78.539	15.526	47.885	15.127
Louhe	53.477	14.473	32.938	6.065
Zhouko	15.599	10.675	4.647	0.277
Zhengzhou	438.467	222.954	169.908	3.417
Jiaozuo	14.347	3.741	9.136	1.470
Xinxiang	109.501	55.821	53.680	0.000
Hebi	50.334	21.659	23.913	4.762
Huaxian	9.902	8.771	1.131	0.000
Puyang	71.246	25.086	42.779	3.381
Anyang	30.134	8.931	12.470	8.732
Total	973.355	420.461	457.036	53.669

## 3.3. Result Analysis

The results of allocated water of SNWDP under each period and scenario are shown in Figure 4. Allocated water resources for cities and departments would vary with time. For example, in period 1 under S1 the allocated water for urban life, industry, ecology, and environment in Zhengzhou would be  $325.27 \times 10^6$  m<sup>3</sup>, 237.46  $\times 10^6$  m<sup>3</sup>, and  $55.56 \times 10^6$  m<sup>3</sup>, respectively; while the allocated water in period 2 would be  $408.38 \times 10^6$  m<sup>3</sup>, 288.65  $\times 10^6$  m<sup>3</sup>, and  $123.01 \times 10^6$  m<sup>3</sup>, respectively. This is because the proportion of urban life and industrial water distribution would change with the improvement of water-saving technology. Along with the awareness of the ecological environment protection of the whole society, the water consumption of the ecological environment would also increase. Results also indicated that scenarios would lead to changed allocation of water resources corresponding to departmental water distribution proportion for each sector. Figure 5 shows the proportion of allocated water for industry would decrease 9% from S2 to S3. That is because S2 mainly simulates the same proportion of water demand for each department. However, under S3, the proportion of allocated water for urban life and ecology and environment is 75%.



**Figure 4.** Allocated water under different scenarios in different departments and different periods (10<sup>6</sup> m<sup>3</sup>). Note: S1, Scenario 1; S2, Scenario 2; S3, Scenario 3; S4, Scenario 4; t1, period 1; t2, period 2; t3, period 3; 1, Dengzhou City; 2, Nanyang City; 3, Pingdingshan City; 4, Xuchang City; 5, Luohe City; 6, Zhoukou City; 7, Zhengzhou City; 8, Jiaozuo City; 9, Xinxiang City; 10, Hebi City; 11, Huaxian County; 12, Puyang City; 13, Anyang City.



**Figure 5.** Water distribution proportions under different scenarios in different departments (%). Note: S1, Scenario 1; S2, Scenario 2; S3, Scenario 3; S4, Scenario 4; 1, Dengzhou City; 2, NanyangCity; 3, Pingdingshan City; 4, Xuchang City; 5, Luohe City; 6, Zhoukou City; 7, Zhengzhou City; 8, Jiaozuo City; 9, Xinxiang City; 10, Hebi City; 11, Huaxian County; 12, Puyang City; 13, Anyang City.

Figure 6 shows the sewage discharge for each sector during various periods. Sewage emissions from the urban life of Zhengzhou would increase to  $227.69 \times 10^6$  m<sup>3</sup>,  $285.86 \times 10^6$  m<sup>3</sup>, and  $350.23 \times 10^6$  m<sup>3</sup> from periods 1–3 under S1. The increasing volume of sewage emission is mainly because of the rapid development of the urban population. Conversely, the sewage emissions from the urban life of Xinxiang would decrease by  $46.35 \times 10^6$  m<sup>3</sup> from S1–S2 in 2020. This is mainly because constraints are imposed on the water distribution proportion of each department. Eventually, sewage emissions from each department would change.



**Figure 6.** Amounts of sewage discharge under different scenarios in different departments and different periods (10<sup>6</sup> m<sup>3</sup>). Note: S1, Scenario 1; S2, Scenario 2; S3, Scenario 3; S4, Scenario 4; t1, period 1; t2, period2; t3, period3; 1, Dengzhou City; 2, Nanyang City; 3, Pingdingshan City; 4, Xuchang City; 5, Luohe City; 6, Zhoukou City; 7, Zhengzhou City; 8, Jiaozuo City; 9, Xinxiang City; 10, Hebi City; 11, Huaxian County; 12, Puyang City; 13, Anyang City.

Figure 7 shows COD from the sewage of various departments under different periods and scenarios. Generally, the emission of COD would change as the scenario changed. For instance, in period 1 under S2 the COD from the sewage of allocated water for urban life, industry, ecology, and environment in Zhengzhou would be  $6.28 \times 10^3$  tonnes,  $1.95 \times 10^3$  tonnes, and  $0.80 \times 10^3$  tonnes, respectively; while the COD from sewage of allocated water resources under S3 would be  $9.75 \times 10^3$ tonnes,  $1.81 \times 10^3$  tonnes, and  $0.77 \times 10^3$  tonnes, respectively. Variations in COD emission are mainly because constraints would be imposed on the water distribution proportion of each department while there is a changing demand for water resources in various departments. It was demonstrated that the COD from the sewage of allocated water resources for different cities and departments would vary with time. For instance, COD of the sewage from the ecology and environment of Zhengzhou would increase by 471.81 tonnes under S1. Awareness of a need for protection of the ecological environment protection will occur, but in addition, water consumption of the ecological environment would also increase. Figure 8 shows the proportion of COD emission from each department under different scenarios. For example, under S1, the COD emission from urban life, industry, ecology and environment of Zhengzhou would contribute 79.86%, 18.10%, and 2.04%, respectively, in period 1, while they would account for 79.08%, 17.36%, and 3.56% COD emission, respectively, in period 2. In summary, the proportion of COD emission for each department is dependent on the needs of various departments for water resources under different scenarios.



**Figure 7.** Amounts of COD emission under different scenarios in different departments and different. periods (10<sup>3</sup> tonnes). Note: S1, Scenario 1; S2, Scenario 2; S3, Scenario 3; S4, Scenario 4; t1, period 1; t2, period2; t3, period3; 1, Dengzhou City; 2, Nanyang City; 3, Pingdingshan City; 4, Xuchang City; 5, Luohe City; 6, Zhoukou City; 7, Zhengzhou City; 8, Jiaozuo City; 9, Xinxiang City; 10, Hebi City; 11, Huaxian County; 12, Puyang City; 13, Anyang City.



**Figure 8.** COD emission proportions under different scenarios in different departments (%). Note: S1, Scenario 1; S2, Scenario 2; S3, Scenario 3; S4, Scenario 4; 1, Dengzhou City; 2, Nanyang City; 3, Pingdingshan City; 4, Xuchang City; 5, Luohe City; 6, Zhoukou City; 7, Zhengzhou City; 8, Jiaozuo City; 9, Xinxiang City; 10, Hebi City; 11, Huaxian County; 12, Puyang City; 13, Anyang City.

Figure 9 shows the system benefits under different credibility ( $\lambda = 1$ , 0.9, 0.8, 0.7) levels and different scenarios. Generally, the system benefits would decrease with rising  $\lambda$  levels and change with different scenarios. For instance, when  $\lambda = 0.9$ , the system cost would be [3.55, 4.00] × 10<sup>12</sup> RMB¥ under S4 and [3.23, 3.61] × 10<sup>12</sup> RMB¥ under S3. This is because different scenarios would correspond to the water allocation proportion of different departments, thus leading to different benefits of the overall system. Additionally, different credibility levels would generate reactions for the proportion of the allocation water for each department. For instance, the system benefits in S1 would be [3.57, 4.02] × 10<sup>12</sup> RMB¥ under  $\lambda = 1$ , while it would be [3.61, 4.06] × 10<sup>12</sup> RMB¥ under  $\lambda = 0.7$ . This is because higher  $\lambda$  levels would be imposed on the price factors. Figure 10 shows the proportion of the allocated water, sewage and COD from urban life, industry, ecology, and environment under each credibility and scenario. Generally, the allocated water, sewage and COD would increase with decreased  $\lambda$  levels. This is mainly because the constraints would impose on the water distribution proportion and lead to changes in sewage and COD emissions from each department.



**Figure 9.** System benefits under different  $\lambda$  levels and scenarios (10<sup>12</sup> RMB¥). Note:  $\lambda = 1, 0.9, 0.8, 0.7$ ; S1, Scenario 1; S2, Scenario 2; S3, Scenario 3; S4, Scenario 4.



**Figure 10.** Water allocation, COD emission, and sewage discharge under different  $\lambda$  levels in S1. Note:  $\lambda = 1, 0.9, 0.8, 0.7; S1$ , Scenario 1; 1, Dengzhou City; 2, Nanyang City; 3, Pingdingshan City; 4, Xuchang City; 5, Luohe City; 6, Zhoukou City; 7, Zhengzhou City; 8, Jiaozuo City; 9, Xinxiang City; 10, Hebi City; 11, Huaxian County; 12, Puyang City; 13, Anyang City.

## 4. Conclusions and Outlook

In this study, a scenario-based interval fuzzy-credibility constrained programming (SIFCP) method has been developed by integrating fuzzy-credibility constrained programming (FCP), interval-parameter programming (IPP), and scenario analysis (SA). SIFCP can handle uncertain information by using interval values, fuzzy sets and scenario analysis. Then, a SIFCP-WRMS model is formulated. The method was applied to the optimal allocation of water resources in the South-to-North Water Transfer Project within the scope of the Henan province. Different scenarios associated with varied water-allocation proportions have also been examined. SIFCP-WRMS model has advantages of: (a) tackling multi-uncertainty presented as interval-fuzzy parameters and interval-scenarios; (b) identifying the desired water-allocation strategies under different water-distribution proportion scenarios; and (c) making adjustments to the tradeoffs among system cost, water resource demand, and sewage discharge, as well as COD emission.

Several findings in association with water allocation, sewage discharge, COD emission, and system benefit are achieved. Firstly, results disclose that different water -distribution proportion scenarios can lead to changed water allocations, sewage discharges, COD emissions, and system benefits, and the proportion of allocated water for the industry would decrease 9% from S2 to S3 over the planning horizon. Secondly, results also reveal that uncertainties associated with different  $\lambda$  levels can result in varied solutions of allocated water and system benefits. Summarily, the achieved system benefit would change 20.44% based on the joint impacts of scenarios and uncertainties.

Although SIFCP-WRMS has its effectiveness in solving dual uncertainties presented as interval-fuzzy parameters or interval-scenarios, and the results can provide useful strategies for planning the WRMS under the conflict of economic objective, water demand, and sewage discharge, in this study, only one water source (i.e., water from the Water Diversion Project) was considered, and the other water sources, such as surface water, groundwater, and reclaimed water would be further considered to improve the applicability of the SIFCP-WRMS model [43,44]. Moreover, the flow of natural surface water is affected by a variety of factors from climate, topographic, and other aspects, thus, the stochastic programming should be integrated into the SIFCP-WRMS model [45–48].

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## Nomenclature

±	The interval value with lower and upper bounds
~	Fuzzy sets
	City, with <i>c</i> = 1 for Dengzhou City, 2 for Nanyang City, 3 for Pingdingshan City, 4 for Xuchang City,
С	5 for Luohe City, 6 for Zhoukou City, 7 for Zhengzhou City, 8 for Jiaozuo City, 9 for Xinxiang City, 10
	for Hebi City, 11 for Huaxian County, 12 for Puyang City, 13 for Anyang City
t	Planning period, $t = 1$ is 2020, 2 is 2025, 3 is 2030
и	Department, with $u = 1$ for urban life, 2 for industry, 3 for ecology and environment
$f^{\pm}$	System benefits in planning periods (10 <sup>12</sup> RMB¥)
$R_{c,u,t}^{\pm}$	Benefit coefficient (RMB¥/m <sup>3</sup> )
$C_{c,u,t}^{\pm}$	Cost coefficient (RMB¥/m <sup>3</sup> )
$W_{c.u.t}^{\pm}$	The amount of water allocated to u users in s cities in planning period $(10^6 \text{ m}^3)$
$T_t^{\pm}$	The total amount of available water $(10^6 \text{ m}^3)$
$Demand_{c,1,t}^{\pm}$	Water for urban life $(10^6 \text{ m}^3)$
$\alpha_{c,t}^{\pm}$	The minimum proportion of ecology and environment water usage
$P_{c.u.t}^{\pm}$	The sewage discharge coefficient
$Sew_t^{\pm}$	The maximum sewage discharge (10 <sup>6</sup> m <sup>3</sup> )
$\eta_t^{\pm}$	COD removal rate
$COD_t^{\pm}$	The allocation total of COD (tonnes)
$(\beta_{lb})_{c,t}^{\pm}$	The minimum proportion of industry water usage
$(\beta_{ub})_{c,t}^{\pm}$	The maximum proportion of industry water usage

## Abbreviations

AI	Artificial intelligence
ANNs	Artificial neural networks
COD	Chemical oxygen demand
DP	Dynamic programming
FCP	Fuzzy-confidence constraint programming
FP	Fuzzy programming
GAs	Genetic algorithms
GWP	Global water partnership
IHP	International Center for Integrated Water resource management
ILP	Integer linear programming
IPP	Interval-parameters programming
IWRA	International water resources association
LP	Linear programming
MILP	Mixed integer linear programming
S1	Scenario 1
S2	Scenario 2
S3	Scenario 3
S4	Scenario 4
SA	Scenario analysis
SFCP	Scenario-based fuzzy-credibility constrained programming

SIFCP	Scenario-based interval fuzzy-credibility constrained programming
SNWDP	South-to-North Water Diversion Project
TSM	Two-step method
WDP	Water Diversion Project
WRM	water resource management
WRMS	water resource management system

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