

## Supplementary Materials

### Engineered Biomaterials for Reducing Phosphorus and Nitrogen Levels from Downstream Water of Aquaculture Facilities

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#### Nomenclature

##### Indices

<i>a</i>	Set of collection sites
<i>b</i>	Set of conversion sites
<i>bs</i>	Biomaterial storage
<i>c</i>	Set of biomaterial storage sites
<i>col</i>	Collection
<i>d</i>	Set of bio-oil storage sites
<i>di</i>	Distribution
<i>dr</i>	Dryer
<i>e</i>	Set of water treatment sites
<i>gr</i>	Grinding
<i>os</i>	Bio-oil storage
<i>ppb</i>	Parts per billion
<i>pyr</i>	Pyrolysis
<i>t</i>	Set of time

##### Parameters

$C_{C-col}$	Annual capital cost of collection (\$/yr)
$C_{C-bs}$	Annual capital cost of biomaterial storage (\$/yr)
$C_{C-dr}$	Annual capital cost of drying (\$/yr)
$C_{C-gr}$	Annual capital cost of grinding (\$/yr)
$C_{C-os}$	Annual capital cost of bio-oil storage (\$/yr)
$C_{C-pyr}$	Annual capital cost of pyrolysis (\$/yr)
$C_{C-di}$	Annual capital cost of distribution (\$/yr)
$C_{C-wt}$	Annual capital cost of water treatment (\$/yr)
$C_{V-col}$	Annual variable cost of collection (\$/yr)
$C_{V-bs}$	Annual variable cost of biomaterial storage (\$/yr)
$C_{V-dr}$	Annual variable cost of drying (\$/yr)
$C_{V-gr}$	Annual variable cost of grinding (\$/yr)
$C_{V-os}$	Annual variable cost of bio-oil storage (\$/yr)
$C_{V-pyr}$	Annual variable cost of pyrolysis (\$/yr)
$C_{V-di}$	Annual variable cost of distribution (\$/yr)
$C_{V-wt}$	Annual variable cost of water treatment (\$/yr)
<i>D</i>	Distance (km)
<i>EP</i>	Total pathway eutrophication (kg PO <sub>4</sub> eq.)
<i>EP<sub>N2O</sub></i>	Eutrophication potential of N <sub>2</sub> O (kg PO <sub>4</sub> eq./kg N <sub>2</sub> O)

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$EP_P$	Eutrophication potential of P (kg PO <sub>4</sub> eq./kg P)
$EP_{EF}$	Eutrophication potential for all processes (kg PO <sub>4</sub> /ton)
$EP_{EFN2O}$	N <sub>2</sub> O eutrophication potential of all processes (kg N <sub>2</sub> O/ ton)
$EP_{EFP}$	P eutrophication potential of all processes (kg P/ton)
$ER_{CH4}$	Emissions rate of CH <sub>4</sub> (kg CO <sub>2</sub> eq./kg CH <sub>4</sub> )
$ER_{CO2}$	Emissions rate of CO <sub>2</sub> (kg CO <sub>2</sub> eq./kg CO <sub>2</sub> )
$ER_{N2O}$	Emissions rate of N <sub>2</sub> O (kg CO <sub>2</sub> eq./kg N <sub>2</sub> O)
$M_{bc}$	Mass of produced biomaterial (metric ton)
$M_p$	Mass of raw pinewood (metric ton)
$MS_{EF}$	GHG emissions factor for biomaterial production process (kg CO <sub>2</sub> eq. per ton)
$MS_{EFCH4}$	CH <sub>4</sub> emission factor for biomaterial production process (kg CH <sub>4</sub> per ton)
$MS_{EFCO2}$	CO <sub>2</sub> emission factor for biomaterial production process (kg CO <sub>2</sub> per ton)
$MS_{EFN2O}$	N <sub>2</sub> O emission factor for biomaterial production process (kg N <sub>2</sub> O per ton)
$MS_{GWP}$	Biomaterial production GWP (kg CO <sub>2</sub> eq.)
$TR_{EF}$	GHG emissions factor for biomaterial transportation (kg CO <sub>2</sub> eq. per ton-mile)
$TR_{EFCH4}$	CH <sub>4</sub> emission factor for biomaterial transportation (kg CH <sub>4</sub> per ton-mile)
$TR_{EFCO2}$	CO <sub>2</sub> emission factor for biomaterial transportation (kg CO <sub>2</sub> per ton-mile)
$TR_{EFN2O}$	N <sub>2</sub> O emission factor for biomaterial transportation (kg N <sub>2</sub> O per ton-mile)
$TR_{GWP}$	Biomaterial transportation GWP (kg CO <sub>2</sub> eq.)
$U_{pyr}$	Annual pyrolysis utilization (metric ton/yr)
$U_{dr}$	Annual drying equipment utilization (metric ton/yr)
$U_{gr}$	Annual grinder utilization (metric ton/yr)
$U_{wt}$	Annual water treatment utilization (metric ton/yr)
$U_{os}$	Annual bio-oil storage equipment utilization (metric ton/yr)
$U_{bs}$	Annual biomaterial storage equipment utilization (metric ton/yr)
$U_{col}$	Annual handling equipment utilization (metric ton/yr)
$U_{di}$	Annual distribution utilization (metric ton/yr)
$US_{EF}$	GHG emissions factor for upstream processes (kg CO <sub>2</sub> eq. per ton)
$US_{EFCH4}$	CH <sub>4</sub> emission factor for upstream processes (kg CH <sub>4</sub> per ton)
$US_{EFCO2}$	CO <sub>2</sub> emission factor for upstream processes (kg CO <sub>2</sub> per ton)
$US_{EFN2O}$	N <sub>2</sub> O emission factor for upstream processes (kg N <sub>2</sub> O per ton)
$US_{GWP}$	Upstream processes GWP (kg CO <sub>2</sub> eq.)

### Decision Variables

$B_{bct}$	Integer variable for biomaterial mass from conversion site b to storage site c during time period t (metric ton)
$B_{cet}$	Integer variable for biomaterial mass from storage site c to water treatment site e during time period t (metric ton)
$BN_{cet}$	Continuous variable for biomaterial mass from conversion site b to water treatment site e during time period t (metric ton)
$O_{bat}$	Integer variable for bio-oil mass from conversion site b to storage site d during time period t (metric ton)
$PN_{abt}$	Continuous variable for pinewood mass from collection site a to conversion site b during time period t (metric ton)
$Z_{abt}$	Binary variable for forest residue from collection site a to conversion site b during time period t