

## Article

# Configuration Optimization of a Shell-and-Tube Heat Exchanger with Segmental Baffles Based on Combination of NSGAI and MOPSO Embedded Grouping Cooperative Coevolution Strategy

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**Abstract:** A design indicators prediction model using the Bell-Delaware method for a shell-and-tube heat exchanger with segmental baffles (STHX-SB) is constructed and validated by experiment. The average errors of heat transfer capacity and tube-side pressure drop are 8.52% and 7.92%, respectively, and the predicted weight is the same as the weight obtained by Solidworks commercial software, which indicates the model's reliability. Parametric influences of the outside diameter of the heat dissipation tube, clearance between heat dissipation tubes, heat dissipation tube length, and tube bundle bypass flow clearance on heat transfer capacity per tube-side pressure drop and heat transfer capacity per weight are studied, and it indicates that whether the interaction between factors is considered or not, both heat transfer capacity per tube-side pressure drop and heat transfer capacity per weight are the most sensitive to outside diameter of heat dissipation tube and the least sensitive to heat dissipation tube length based on the Sobol' method. To avoid falling into local optima due to algorithm convergence being too fast and to improve the reliability of solving complex optimization problems, Non-Dominated Sorted Genetic Algorithm II (NSGAI) and Multi-Objective Particle Swarm Optimization (MOPSO) embedded grouping cooperative coevolution (NSGAI-MOPSO-GCC) is proposed to optimize the studied four configuration parameters to maximize heat transfer capacity per tube-side pressure drop and heat transfer capacity per weight for STHX-SB, simultaneously. Compared with the original structure, heat transfer capacity per tube-side pressure drop and heat transfer capacity per weight of the chosen solutions separately increased by 57.66% and 4.63%, averagely, and in the optimization comparison of NSGAI, MOPSO, and NSGAI-MOPSO-GCC, NSGAI-MOPSO-GCC has the best performance, which shows that the proposed method is effective and feasible and can supply beneficial solutions and valuable guidance for heat exchanger design and improvement.



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## 1. Introduction

As widely used mechanical devices in various kinds of industrial fields like aerospace, automotive, food, chemical, energy, and so on, heat exchangers have the ability to transfer heat from the fluid of lower temperature to the fluid of higher temperature [1,2]. As heat exchangers have the advantages of high efficiency and reliability, they are frequently adopted in lubricating oil systems in aero-engines to heat fuel and cool lubricating oil simultaneously, which can improve fuel combustion efficiency, prevent fuel from freezing, ensure sufficient cooling of bearings, and guarantee smooth low-temperature cold start of

aero-engines. Therefore, pursuing comprehensive high performance for heat exchangers is meaningful and significant in engineering applications [3], and thus numerous studies on heat exchanger configuration optimization have been conducted.

The traditional optimization design of heat exchangers is mainly through gradually changing configuration parameters to meet the requirements of both designers and users in iterative design processes. Although using this research and development process could ultimately achieve the optimization goal, it consumes a lot of costs and time, and may not ultimately lead to a particularly excellent design solution. As various optimization algorithms have been developed well in these years, using optimization algorithms to achieve optimal design of heat exchangers for better characteristic indicators has been increasingly widely used, and its effectiveness and applicability have been increasingly recognized by many researchers. Up to now, in terms of optimization design of heat exchangers, good results have been achieved by adopting many classic and newly developed optimization algorithms, like Non-Dominated Sorted Genetic Algorithm II (NSGAI) [4,5], Multi-Objective Particle Swarm Optimization (MOPSO) [6], Taguchi approach [7], Differential Evolution (DE) [8], Falcon Optimization Algorithm (FOA) [9], Jaya [10], Topology optimization [11], and so on. In the research of Seema Singh et al. [12], three classic optimization algorithms and three newly developed optimization algorithms were adopted to optimize plate and frame heat exchanger structural parameters. There are two kinds of studies that can be divided based on the existing studies on heat exchanger design optimization using optimization algorithms: combining optimization algorithms and theoretical analysis, and combining optimization algorithms and numerical simulation.

In terms of combining optimization algorithms and theoretical analysis, parameters optimization was conducted by Yayun Zhang et al. [13] using Genetic Algorithm based on the proposed function models for a rectangular staggered fins heat exchanger. Vidyadhar H. Iyer et al. [14] proposed the Adaptive Range Genetic Algorithm to optimize a shell-and-tube heat exchanger in the aspects of design and economy based on theoretical design calculation. An optimization strategy of combining genetic algorithm with entransy theory was proposed by Jian wen et al. [15] to realize configuration optimization for a shell-and-tube heat exchanger with helical baffles. In the research of Hongyoung Lim et al. [16], for mobile air conditioning systems, a strategy of replacing a louver fin heat exchanger by one kind of bare tube heat exchanger as an evaporator was proposed, and the approximated assisted optimization method was adopted to optimize five independent design variables of bare tube heat exchanger based on theoretical calculation.

In terms of combining optimization algorithms and numerical simulation, for shell-and-tube heat exchangers with helical baffles, Jian Wen et al. [17] and Simin Wang et al. [18,19] both conducted numerical simulation to analyze performances, and obtained corresponding response surface functions for different structural parameters. Then, structural parameters multi-objective optimization was conducted using Genetic Algorithm. Moreover, a spiral-wound heat exchanger was also optimized by Simin Wang et al. [20] through applying this method. In the research of Xinting Wang et al. [21], numerical simulation was conducted for shell-and-tube heat exchangers separately with segmental baffles, continuous helical baffles, and staggered baffles to study their performances, and shell-and-tube heat exchanger with staggered baffles was chosen to be the one that has the best comprehensive performance through comparison. Then, Genetic Algorithm combining with artificial neural network was used to optimize the selected heat exchanger to pursue comprehensive optimum heat transfer rate and pressure drop. Paweł Ocloń et al. [22] optimized high-temperature fin-and-tube heat exchanger manifold shape using Particle Swarm Optimization and Continuous Genetic Algorithms based on numerical simulation. Hadi Keramati et al. [23] utilized Deep Reinforcement Learning and Boundary Representation combined with numerical simulation to optimize heat exchanger shape to enhance heat transfer and suppress flow resistance. In the research of Kizhakke Kodakkattu Saijal et al. [24], Genetic Algorithm was adopted to pursue heat transfer rate maximizing and pressure drop minimizing based on numerical simulation analysis. Finally, heat transfer rate per pressure drop was utilized

as one criterion to find a satisfactory optimization result. In the research of Chuangeng Tang et al. [25], two new cross-flow radiator structures were designed through Topology optimization, with the objective function aimed at achieving the minimum temperature difference and pressure drop. The influence of six channel heights was analyzed using the evaluation criterion Colburn coefficient per friction factor to obtain the result with the best heat dissipation ability.

Even though there already exist many studies about heat exchanger performance improvement, most of the researched heat exchangers are large-sized. Meanwhile, due to the light weight and few space occupation design requirements for airborne equipment, the heat exchangers adopted in aero-engines are usually small-sized, and their comprehensive high-performance design needs to be researched more. Thus, in this research, in order to provide a stable design theory base and promote engineering application for heat exchangers in the aerospace field, a small-sized shell-and-tube heat exchanger with segmental baffles (STHX-SB), which has been widely utilized in aero-engines, was studied. One design indicators prediction model adopting the Bell–Delaware method was constructed and validated by experiment. The influences of four structure parameters, which are significant in engineering applications, on design indicators were studied, and their global sensitivity indices were analyzed based on Sobol' method to reveal influential degrees. Then, in order to avoid falling into local optima due to algorithm convergence being too fast and to improve the reliability of solving complex optimization problem, based on the above research, one combination optimization method of NSGAI and MOPSO embedded grouping cooperative coevolution was proposed to optimize the analyzed four key configuration parameters to improve comprehensive performance for STHX-SB, which can provide beneficial solutions and valuable guidance for heat exchanger design and improvement.

## 2. Design Indicators Prediction Model Construction

### 2.1. STHX-SB Structure Description

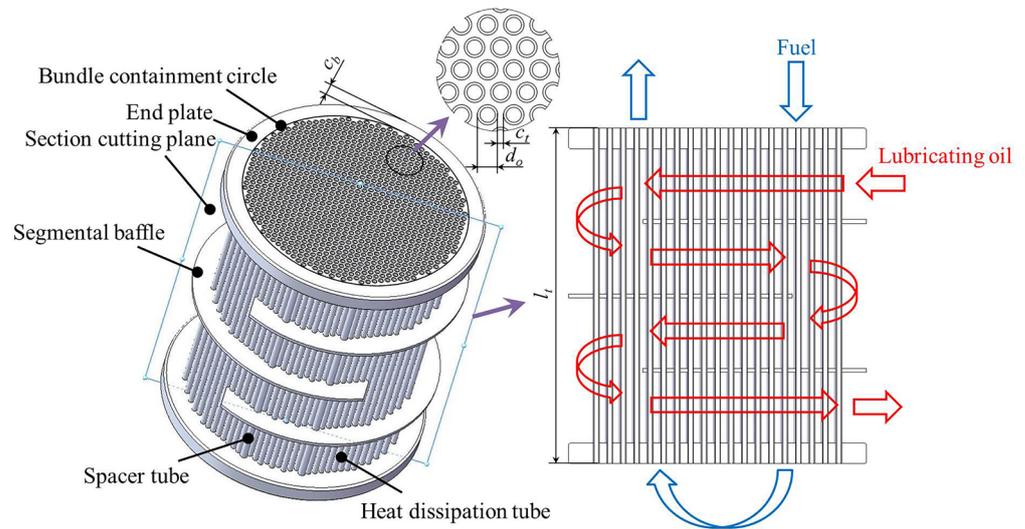
STHX-SB studied in this research is one kind of heat exchanger that is adopted in one turbine-shaft aero-engine to heat cold fuel by hot lubricating oil, which is smaller, lighter, and more compact compared with heat exchangers in many other industrial fields. STHX-SB is mainly composed of heat dissipation tubes, end plates, segmental baffles, and spacer tubes. In STHX-SB, uniformly distributed segmental baffles are located by spacer tubes, and two end plates are fixed with heat dissipation tubes ends. As shown in Figure 1, hot lubricating oil cross flows through outside heat dissipation tubes and cold fuel flows inside them, and then heat exchange can be realized between two fluids through tubes wall. The materials of heat exchanger, hot side fluid, and cold side fluid are aluminum alloy, lubricating oil 4050 [26], and fuel RP-3 [27], respectively. Main structural parameters and normal working conditions of STHX-SB are presented in Tables 1 and 2, separately.

**Table 1.** Structural parameters of STHX-SB.

Parameter	Value
Outside diameter of heat dissipation tube $d_o$	2.36 mm
Clearance between heat dissipation tubes $c_t$	0.64 mm
Heat dissipation tube length $l_t$	130 mm
Tube bundle bypass flow clearance $c_b$	7.5 mm
Baffle cut $P_c$	0.25
Baffles number $N_b$	3
Baffle diameter $d_b$	115 mm
Baffle thickness $t_b$	1.5 mm
End plates number $N_p$	2
Thickness of end plate $t_p$	8 mm
Spacer tube number between baffles $N_{s,b}$	4
Wall thickness of spacer tube $t_{s,w}$	0.305 mm
Wall thickness of heat dissipation tube $t_{t,w}$	0.305 mm
Shell passes number $Z_s$	1
Tube passes number $Z_t$	2
Shell/Tube-side inlet/outlet diameter $D_N$	20 mm

**Table 2.** STHX-SB normal working conditions.

Working Condition	Value
Flow rate of lubricating oil $q_o$	15 L/min
Inlet temperature of lubricating oil $T_o$	383 K
Fuel flow rate $q_f$	6 L/min
Fuel inlet temperature $T_f$	333 K



**Figure 1.** STHX-SB structure.

2.2. Design Indicators Calculation Model

2.2.1. Computation Equations

In engineering applications, heat exchanger efficiency and economy are two significant considerations. Thus, heat transfer capacity per tube-side pressure drop  $Q/\Delta P$  and heat transfer capacity per weight  $Q/G$  are two main indicators in STHX-SB configuration design. The higher these two design indicators, the better the comprehensive performance looks. Before predicting  $Q/\Delta P$  and  $Q/G$ ,  $Q$ ,  $\Delta P$ , and  $G$  need to be computed reliably. In this research,  $\epsilon$ -NTU relational expression and the Bell–Delaware method [28] were adopted in  $Q$  calculation, and the computation equations of  $Q$ ,  $\Delta P$ , and  $G$  are presented in Tables 3–5, respectively.

**Table 3.** Computation equations for heat transfer capacity [28–34].

Parameter	Equation	No.
Heat transfer capacity	$Q = \epsilon W_{\min}(t_1 - t_2)$	(1)
Heat transfer efficiency	$\epsilon = \frac{2}{1+C^* + \sqrt{1+C^{*2}}(1+e^{-NTU\sqrt{1+C^{*2}}})/(1-e^{-NTU\sqrt{1+C^{*2}}})}$	(2)
Heat capacity ratio	$C^* = W_{\min}/W_{\max}$	(3)
Number of transfer units	$NTU = \frac{KA}{W_{\min}}$	(4)
Total heat transfer coefficient	$K = \frac{\alpha_o \alpha_i}{\alpha_o + \alpha_i}$	(5)
Heat transfer coefficient of tube-side	$\alpha_i = 0.027 \frac{\lambda_i}{d_i} Re_i^{0.8} Pr_i^{1/3} (\frac{\mu_i}{\mu_{iw}})^{0.14}$ $(Re_i > 10,000, 0.7 < Pr_i < 16,700, l_t/d_i \geq 60),$ $\alpha_i = 0.027(1 - \frac{6 \times 10^5}{Re_i^{1.8}}) \frac{\lambda_i}{d_i} Re_i^{0.8} Pr_i^{1/3} (\frac{\mu_i}{\mu_{iw}})^{0.14}$ $(2300 \leq Re_i \leq 10,000, 0.7 < Pr_i < 16,700, l_t/d_i \geq 60),$	(6)
Heat transfer coefficient of shell-side	$\alpha_o = 1.86 \frac{\lambda_o}{d_o} (Re_o Pr_o \frac{d_o}{l_o})^{1/3} (\frac{\mu_o}{\mu_{ow}})^{0.14}$ $(Re_o < 2300, 0.6 < Pr_o < 6700, Re_o Pr_o l_o/d_o \geq 100).$	(7)

Table 3. Cont.

Parameter	Equation	No.
Baffle layout correction factor	$\begin{cases} J_c = 0.55 + 0.72F_c \\ F_c = 1 - \frac{\theta_{ctl}}{\pi} + \frac{\sin\theta_{ctl}}{\pi} \\ \theta_{ctl} = 2 \cos^{-1} \left( \frac{D_s - 2l_c}{D_{ctl}} \right) \\ D_{ctl} = D_{otl} - d_o \end{cases}$	(8)
Baffle leakage effect correction factor	$\begin{cases} J_l = 0.44(1 - r_s) + [1 - 0.44(1 - r_s)]e^{-2.2r_{lm}} \\ r_s = \frac{A_{o,sb}}{A_{o,sb} + A_{o,tb}} \\ r_{lm} = \frac{A_{o,sb} + A_{o,tb}}{A_{o,cr}} \end{cases}$	(9)
Tube bundle bypass correction factor	$\begin{cases} J_b = \begin{cases} 1, & N_{ss}^+ \geq 0.5 \\ e^{-Cr_b[1 - (2N_{ss}^+)^{\frac{1}{3}}]}, & N_{ss}^+ \leq 0.5 \end{cases} \\ C = \begin{cases} 1.35, & Re_o \leq 100 \\ 1.25, & Re_o > 100 \end{cases} \\ r_b = \frac{A_{o,bp}}{A_{o,cr}} \\ N_{ss}^+ = \frac{N_{ss}}{N_{r,cc}} \\ N_{r,cc} = \frac{D_s - 2l_c}{X_t} \end{cases}$	(10)
Correction factor for unequal span heat transfer	$\begin{cases} J_s = \frac{N_b - 1 + (L_i^+)^{(1-n)} + (L_o^+)^{(1-n)}}{N_b - 1 + L_i^+ + L_o^+} \\ L_i^+ = \frac{L_{bj}}{L_{bc}} \\ L_o^+ = \frac{L_{bo}}{L_{bc}} \\ n = \begin{cases} 0.6, & Re_o \geq 1000 \\ 1/3, & Re_o < 1000 \end{cases} \end{cases}$	(11)
Temperature gradient correction factor	$\begin{cases} J_r = \begin{cases} 1, & Re_o \geq 100 \\ \text{linear interpolation}, & 20 < Re_o < 100 \\ (10/N_{r,c})^{0.18}, & Re_o \leq 20 \end{cases} \\ N_{r,c} = N_{r,cc} + N_{r,cw} \end{cases}$	(12)

Table 4. Computation equations for tube-side pressure drop [28–34].

Parameter	Equation	No.
Tube-side pressure drop	$\Delta P = \Delta P_i + \Delta P_r + \Delta P_N$	(13)
On-way resistance	$\Delta P_i = \begin{cases} \frac{64}{Re_i} Z_t \frac{l_t}{d_i} \frac{\rho_i u_i^2}{2} \left( \frac{\mu_i}{\mu_{iw}} \right)^{-0.25}, & Re_i < 2000 \\ (0.014 + 1.56 Re_i^{-0.42}) Z_t \frac{l_t}{d_i} \frac{\rho_i u_i^2}{2} \left( \frac{\mu_i}{\mu_{iw}} \right)^{-0.14}, & Re_i \geq 2000 \end{cases}$	(14)
Elbow flow resistance	$\Delta P_r = 4 \frac{\rho_i u_i^2}{2} Z_t$	(15)
Inlet and outlet flow resistance	$\Delta P_N = 1.5 \frac{\rho_i u_i^2}{2}$	(16)

Table 5. Computation equations for weight.

Parameter	Equation	No.
Weight	$G = G_p + G_b + G_t + G_s$	(17)
Weight of end plates	$G_p = 0.25\pi(d_b^2 - N_t d_o^2) t_p N_p \rho_{al} \cdot 10^{-9}$	(18)
Weight of baffles	$G_b = \left\{ [0.25\pi - 0.25\arccos(1 - 2P_c)] + (0.5 - P_c) \sqrt{P_c(1 - P_c)} \right\} d_b^2 - 0.25\pi d_o^2 (N_t - N_{t,cut}) t_b N_b \rho_{al} \cdot 10^{-9}$	(19)
Weight of heat dissipation tubes	$G_t = 0.25\pi l_t (d_o^2 - d_i^2) N_t \rho_{al} \cdot 10^{-9}$	(20)
Weight of spacer tubes	$G_s = \pi(l_t - t_p N_p - t_b N_b) t_{s,w} (d_o + t_{s,w}) N_{s,b} \rho_{al} \cdot 10^{-9}$	(21)

### 2.2.2. Model Calculation Process

As temperature is changing with the flowing of fluid, fluid physical properties are not constant in the heat exchanger. In order to consider this influence in calculation, fluid average temperature was computed by arithmetic mean of inlet and outlet temperatures,

and heat dissipation tube wall temperature was computed by arithmetic mean of fluid temperatures of two sides. Meanwhile, outlet temperatures were not known before starting computation. Hence, in this research, one strategy of assuming heat transfer capacity and repeatedly correcting it through iterative calculation was utilized to calculate  $Q$ . The design indicators prediction model calculation process is depicted as follows:

- (1) Define heat exchanger working conditions and configuration parameters.
- (2)  $Q$  calculation.
  - (a) Assume STHX-SB heat transfer capacity  $Q_{as}$ .
  - (b) Compute fuel average temperature  $T_{f\_ave}$ , lubricating oil average temperature  $T_{o\_ave}$ , and heat dissipation tube wall temperature  $T_{t\_w}$  by Equations (22)–(24). In these equations,  $W_f$  and  $W_o$  are under the inlet temperatures of fuel and lubricating oil, respectively.

$$T_{f\_ave} = T_f + \frac{Q_{as}}{2W_f}, \quad (22)$$

$$T_{o\_ave} = T_o - \frac{Q_{as}}{2W_o}, \quad (23)$$

$$T_{t\_w} = \frac{T_{f\_ave} + T_{o\_ave}}{2}, \quad (24)$$

- (c) Compute heat transfer capacity  $Q$  by Equations (1)–(12). Unless otherwise required, the physical properties of fuel and lubricating oil are defaulted to the values under  $T_{f\_ave}$  and  $T_{o\_ave}$ , respectively.
- (d) If  $Q$  can fulfill the requirement depicted by Equation (25), output  $Q$ , otherwise utilize the computed  $Q$  in this iteration as  $Q_{as}$  in the next iteration and recompute from Step (b). Error  $E$  was set as 0.05 kW in this study.

$$|Q - Q_{as}| \leq E, \quad (25)$$

- (3) Compute  $\Delta P$  by Equations (13)–(16). Unless otherwise required, fuel physical properties are defaulted to the values under  $T_{f\_ave}$ .
- (4) Compute and output weight  $G$  by Equations (17)–(21).

It needs to be noted that in order to make calculation convenient, there are some simplifying assumptions of the calculation model: (1) the fluids in the heat exchanger are considered in steady state; (2) the default properties of fluids and solid are under average temperatures computed by Equations (22)–(24); (3) the radiative heat dissipation from heat exchanger to environment is neglected; (4) the heat exchanger is assumed to be new and free of dirt inside.

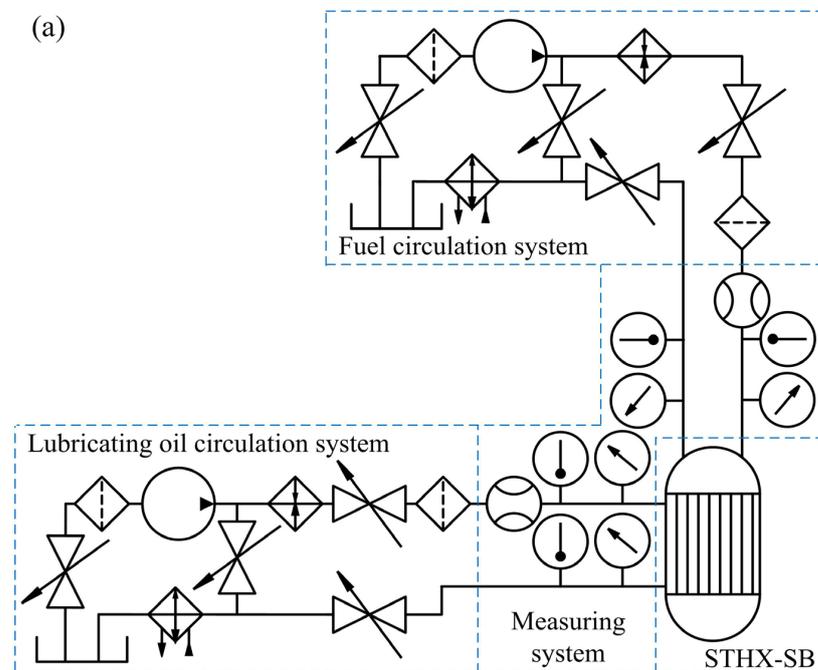
### 2.3. Experimental Verification

A thermodynamic characteristic and flow resistance experiment was conducted to verify the proposed model reliability. In this experiment, flow rate and inlet temperature of lubricating oil and flow rate of fuel as shown in Table 2 were used as constant operating conditions, and inlet temperature of fuel was changed from 318 K to 348 K with a changing step of 5 K. Lubricating oil 4050 [26] and fuel RP-3 [27] were used as test medium.

The experimental system adopted in this research contains fuel and lubricating oil circulation systems and a measuring system, as illustrated by Figure 2a. Fuel and lubricating oil circulation systems both contain oil pumps, oil tanks, radiators, heaters, regulating valves, filters, cut-off valves, and so on, which mainly provide the fluids that can meet the requirements of working conditions. The function of oil tanks is to store fuel or lubricating oil used in experimental systems. Cut-off valves are used to control the on/off of the entire fluid circuits. Filters are adopted to ensure that the fluid is clean, which can avoid the adverse effects on the experimental results caused by heat exchanger clogging. The function

of oil pumps is to provide sufficient power for fluid circulation and pressurize fluid. The function of heaters is to heat fluid to ensure that the fuel inlet temperature and lubricating oil inlet temperature of the test piece meet the requirements. The function of regulating valves is to regulate fuel flow, lubricate oil flow, and bypass the fluid circuit. Radiators are used to help dissipate excess fluid heat in the system through water cooling. The measuring system contains temperature sensors, pressure sensors, and flowmeters distributed in the experimental system, which is mainly used to measure the fluids values of temperature, pressure, and flow rate. Flowmeters are integrated in the test bench. The measuring range of temperature sensors is 218–473 K, and the basic error is calculated by Equation (26). The measuring range and basic error of pressure sensors in lubricating oil circulation system are 0–1 MPa and  $\pm 0.25\%$  FS, respectively. The measuring range and basic error of pressure sensors in fuel circulation system are 0–1 kPa and  $\pm 0.25\%$  FS, respectively.

$$E_{ts} = 0.3 + 0.005|t_{ts} - 273|, \quad (26)$$



**Figure 2.** Validation experiment: (a) experimental schematic drawing; (b) experiment photo.

The tested STHX-SB was connected in the experimental system through pipelines, as shown in Figure 2b. The recorded experimental  $Q$  and  $\Delta P$  were calculated by arithmetic mean of three groups of experimental data, and the three groups of experimental data of  $Q$  and  $\Delta P$  were computed by Equations (27) and (28) based on the corresponding groups of measured data of  $T_o'$ ,  $T_f'$ , and  $P_f'$ .

$$Q = \frac{\rho_o q_o c_{po}(T_o - T_o') + \rho_f q_f c_{pf}(T_f' - T_f)}{2}, \quad (27)$$

$$\Delta P = P_f - P_f', \quad (28)$$

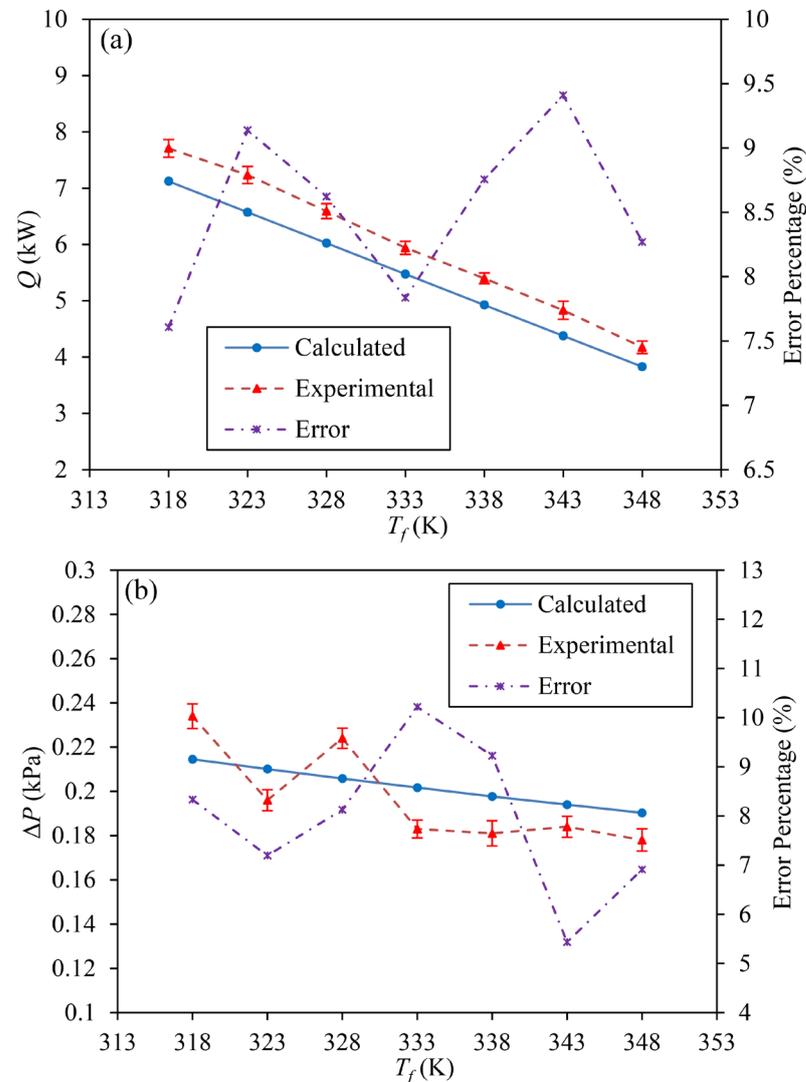
The recorded experimental data of  $Q$  and  $\Delta P$  were compared with the calculation results of the design indicators calculation model, as illustrated in Figure 3. The positive or negative deviation of the error bars of the experimental data shown in Figure 3 was calculated by the standard deviation based on the corresponding three groups of measurement results. It needs to be noted that in the process of standard deviation calculation, three groups of experimental data of  $Q$  and  $\Delta P$  need to be computed based on corresponding groups of the experimental data of  $T_o'$ ,  $T_f'$ , and  $P_f'$  by Equations (27) and (28) first, and then standard deviations of  $Q$  and  $\Delta P$  are calculated based on the computed three groups of experimental data of  $Q$  and  $\Delta P$ . The error percentages presented in Figure 3 are computed by Equation (29). In Equation (29),  $EP$ ,  $da_{ca}$ , and  $da_{ex}$  represent error percentage, calculation data, and experimental data, respectively.

$$EP = \frac{|da_{ca} - da_{ex}|}{da_{ex}} \cdot 100\%, \quad (29)$$

From the error bars shown in Figure 3, it could be found that the standard deviations of  $Q$  measurement results are 0.096–0.161 kW with the average standard deviation of 0.132 kW, and the standard deviations of  $\Delta P$  measurement results are 0.004–0.006 kPa with the average standard deviation of 0.005 kPa. Thus, it could be considered that the measurement uncertainty of this experiment is acceptable and the experimental data can be utilized in the following comparison. Then, from the comparison between calculation results and experimental data shown in Figure 3, it could be clearly seen that the results obtained by this design indicators calculation model are in good agreement with the experiment data. Compared with the experimental data, the error percentages of  $Q$  are 7.61–9.41% with the average value of 8.52%, and the error percentages of  $\Delta P$  are 5.43–10.22% with the average value of 7.92%.

The first main reason for these errors is that the calculation is based on fluid average temperature of inlet and outlet. The temperature is changed continuously inside the heat exchanger, and thus the physical properties are changed continuously with the flowing of fluid. Meanwhile, the continuous changing of temperature and fluid physical properties cannot present directly by theory calculation formulae. To make the calculation convenient, the average temperature of inlet and outlet is used as the fluid average temperature, and the default fluid physical properties are obtained under this temperature. Even though this handling method is convenient, there exist some approximations, actually. The second main reason for these errors is that the heat exchange between the test article and the environment is neglected. As the profile of the heat exchanger is complex, it is not easy and convenient to consider the radiative heat dissipation from heat exchanger to environment. Thus, to make the calculation convenient, this part of heat loss is not considered in calculation. Apart from these two reasons that come from method principle, some other factors can also cause these errors, like the neglect of test article manufacturing error, the neglect of surface roughness of parts, and the inevitable experimental errors. Meanwhile, in engineering applications, the calculated error percentages are in acceptable range. Hence, it could be considered that the calculation model of  $Q$  and  $\Delta P$  is reliable.

In this research, the calculated  $G$  was compared with the data obtained by STHX-SB 3D model weighing using Solidworks commercial software (SOLIDWORKS 2020). It could be found that the  $G$  data obtained by these two ways are both 0.989 kg. So, it could be considered that the calculation model of weight is accurate.



**Figure 3.** Model validation: (a)  $Q$  calculation validation; (b)  $\Delta P$  calculation validation.

### 3. Parametric Study

In this research, outside diameter of heat dissipation tube  $d_o$ , clearance between heat dissipation tubes  $c_t$ , heat dissipation tube length  $l_t$ , and tube bundle bypass flow clearance  $c_b$ , as shown in Figure 1, were studied to explore their influences on  $Q/\Delta P$  and  $Q/G$  based on STHX-SB design indicators calculation model.

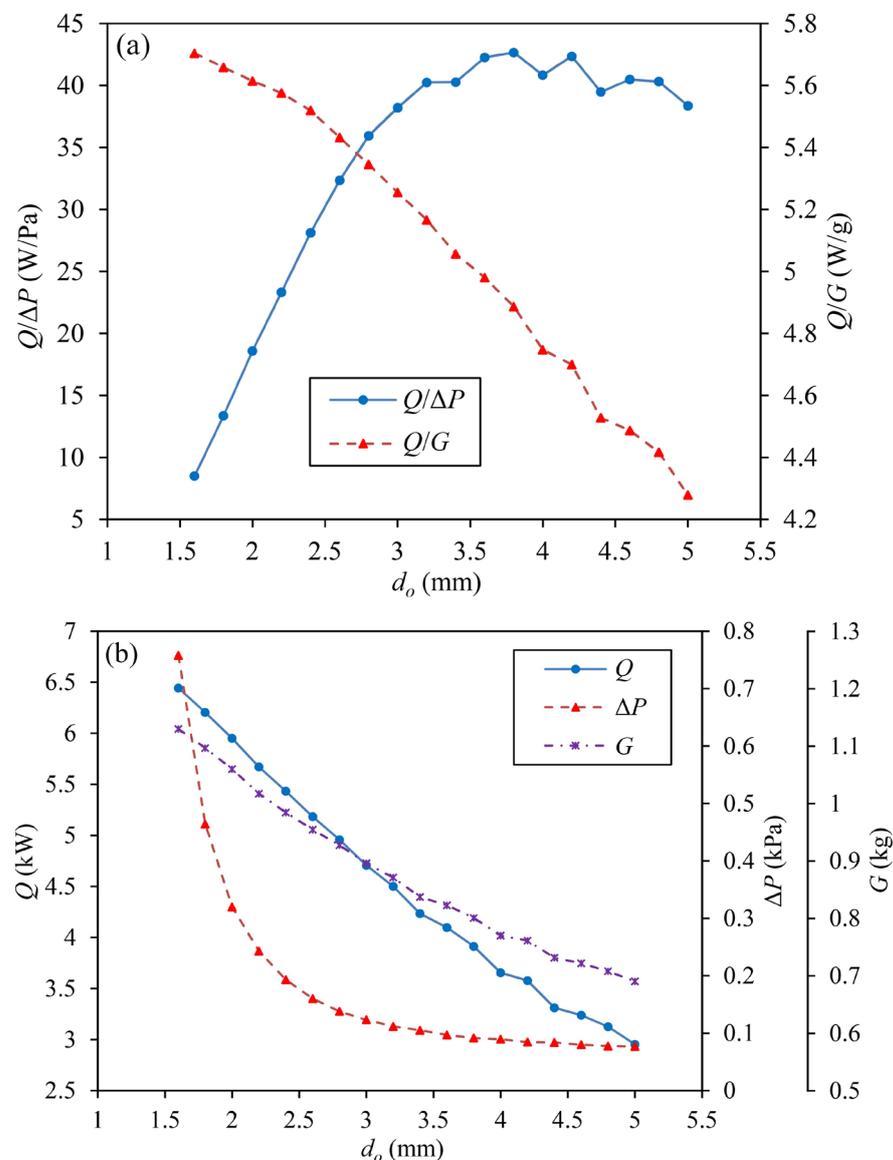
#### 3.1. Parametric Influences Analysis

##### 3.1.1. Influences of $d_o$

$d_o$  varied from 1.6 mm to 5 mm while other structural parameters remained unchanged. The influences of  $d_o$  are presented in Figure 4.

As depicted in Figure 4a, while  $d_o$  increases from 1.6 mm to 5 mm,  $Q/\Delta P$  increases from 8.50 W/Pa first, reaching its highest point of 42.66 W/Pa when  $d_o$  is 3.8 mm, and then generally reduces gradually to 38.37 W/Pa with slight oscillations, and  $Q/G$  decreases by 5.70–4.28 W/g. As  $d_o$  increases, heat dissipation tubes number decreases, and thus

both heat transfer area and heat dissipation tubes weight decrease, which can result in heat transfer attenuation and weight reduction. In addition, the increase of  $d_o$  can cause the growth of tube-side flow area, thus the flow rate of the fluid inside heat dissipation tubes decreases, which can attenuate heat transfer and reduce tube-side on-way resistance. Thus,  $Q$ ,  $\Delta P$ , and  $G$  are all decreased with the increase of  $d_o$ , as illustrated in Figure 4b. Meanwhile, the reduction effect on tube-side on-way resistance of  $d_o$  increasing is gradually weakening. So, the reduce rate of  $\Delta P$  is fast at the beginning and then gradually slow. Thus,  $Q/\Delta P$  increases first and then decreases slowly after the effects of  $Q$  and  $\Delta P$  reduce are almost equivalent. The slight oscillations of the  $Q/\Delta P$  decreasing process are caused by the heat dissipation tubes number changing. As the change of heat dissipation tubes number is not continuous, the  $Q/\Delta P$  line could be shaking, especially the variation effects of  $Q$  and  $\Delta P$  are not much different. Thus,  $Q/\Delta P$  increases first and then decreases slowly with slight oscillations, as shown in Figure 4a. Moreover, even though  $Q$  and  $G$  both decrease with the growth of  $d_o$ ,  $Q$  always decreases faster than  $G$ . Hence,  $Q/G$  decreases continuously as shown in Figure 4a.

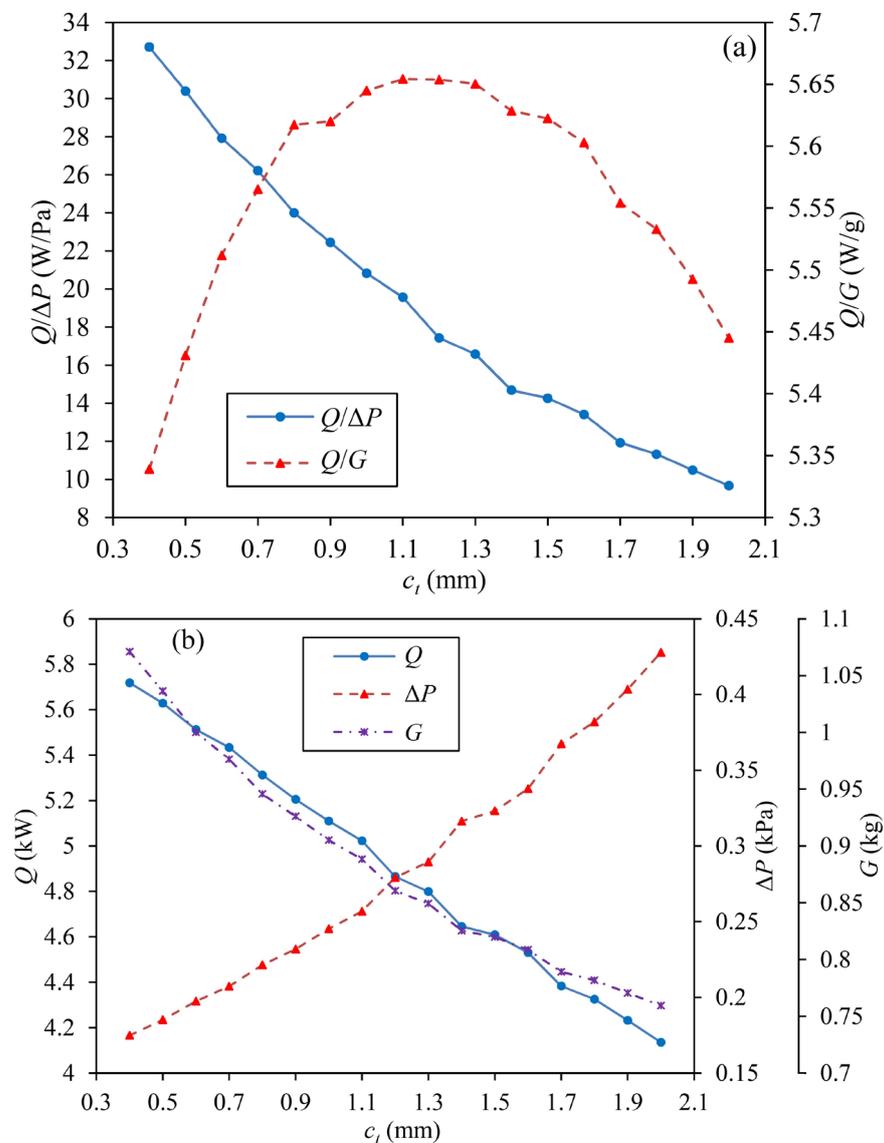


**Figure 4.** Influences of  $d_o$ : (a)  $Q/\Delta P$  and  $Q/G$  separately versus  $d_o$ ; (b)  $Q$ ,  $\Delta P$ , and  $G$  separately versus  $d_o$ .

### 3.1.2. Influences of $c_t$

$c_t$  varied from 0.4 mm to 2 mm while other structural parameters remained unchanged. The influences of  $c_t$  are presented in Figure 5.

As depicted in Figure 5a, while  $c_t$  increases from 0.4 mm to 2 mm,  $Q/\Delta P$  decreases by 32.71–9.67 W/Pa, and  $Q/G$  increases from 5.34 W/g first, reaching its highest point of 5.65 W/g when  $c_t$  is 1.1 mm, and then reduces continuously to 5.45 W/g. Heat dissipation tubes number reduces with the increase of  $c_t$ , which can result in the reduction of heat transfer area and heat dissipation tubes weight and the growth of flow rate of the fluid inside heat dissipation tubes. Thus, both  $Q$  and  $G$  decrease, and  $\Delta P$  increases, simultaneously, as illustrated in Figure 5b. As  $Q$  decreases and  $\Delta P$  increases with the growth of  $c_t$ ,  $Q/\Delta P$  decreases steadily, as depicted in Figure 5a. In addition, even though both  $Q$  and  $G$  decrease, the decrease rate of  $Q$  is lower than  $G$  at the beginning, and then the decrease rate of  $Q$  is higher than  $G$  after  $c_t$  grows to one point. Thus,  $Q/G$  increases first and then decreases after peaking at one point, as shown in Figure 5a.

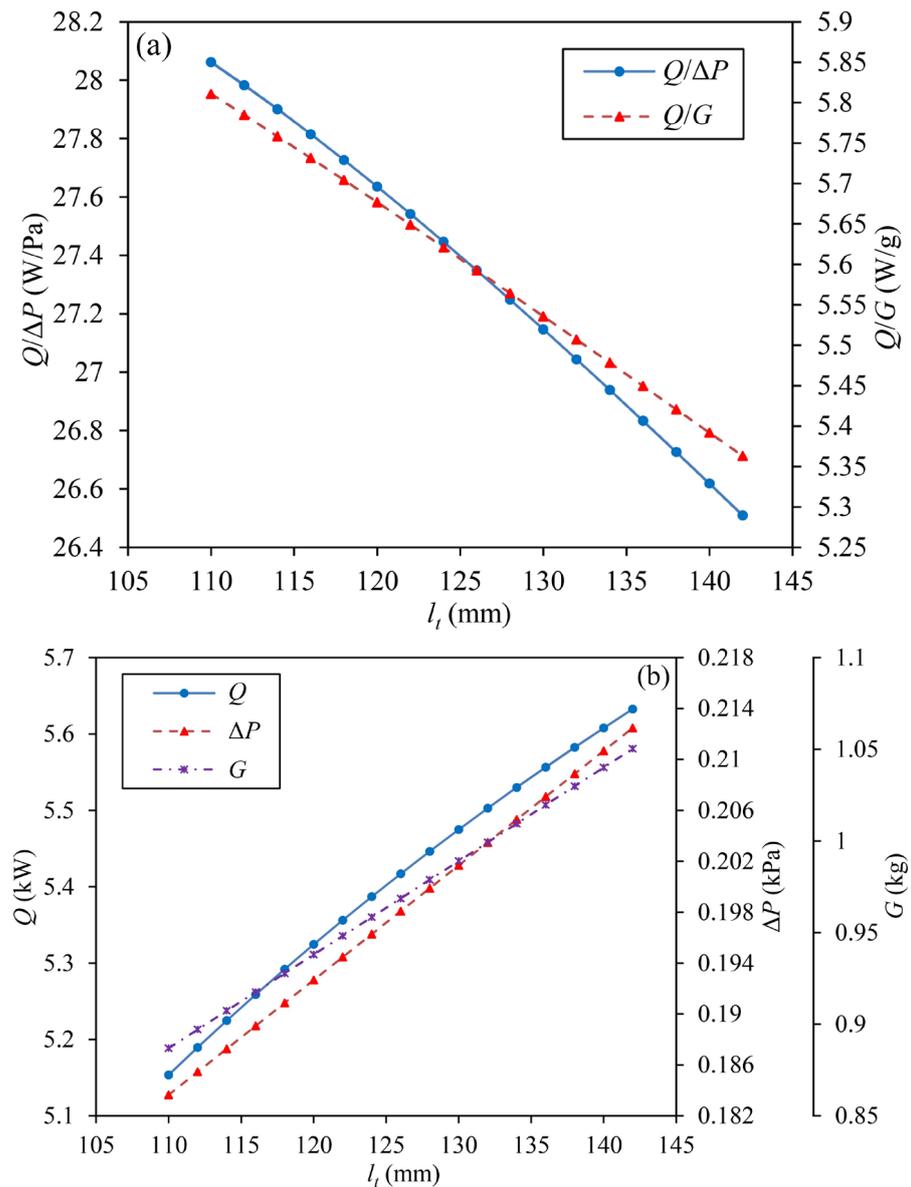


**Figure 5.** Influences of  $c_t$ : (a)  $Q/\Delta P$  and  $Q/G$  separately versus  $c_t$ ; (b)  $Q$ ,  $\Delta P$ , and  $G$  separately versus  $c_t$ .

### 3.1.3. Influences of $l_t$

$l_t$  varied from 110 mm to 142 mm while other structural parameters remained unchanged. The influences of  $l_t$  are presented in Figure 6.

As depicted in Figure 6a, while  $l_t$  increases from 110 mm to 142 mm,  $Q/\Delta P$  and  $Q/G$  decrease by 28.06–26.51 W/Pa and 5.81–5.36 W/g, respectively. Heat transfer area, tube-side on-way resistance, and heat dissipation tubes weight are all increased with the growth of  $l_t$ , which results in the growth of  $Q$ ,  $\Delta P$ , and  $G$ , as illustrated in Figure 6b. Meanwhile, the growth rate of  $Q$  is lower than  $\Delta P$  and  $G$ , which cause the continuously declining  $Q/\Delta P$  and  $Q/G$ , as depicted in Figure 6a.



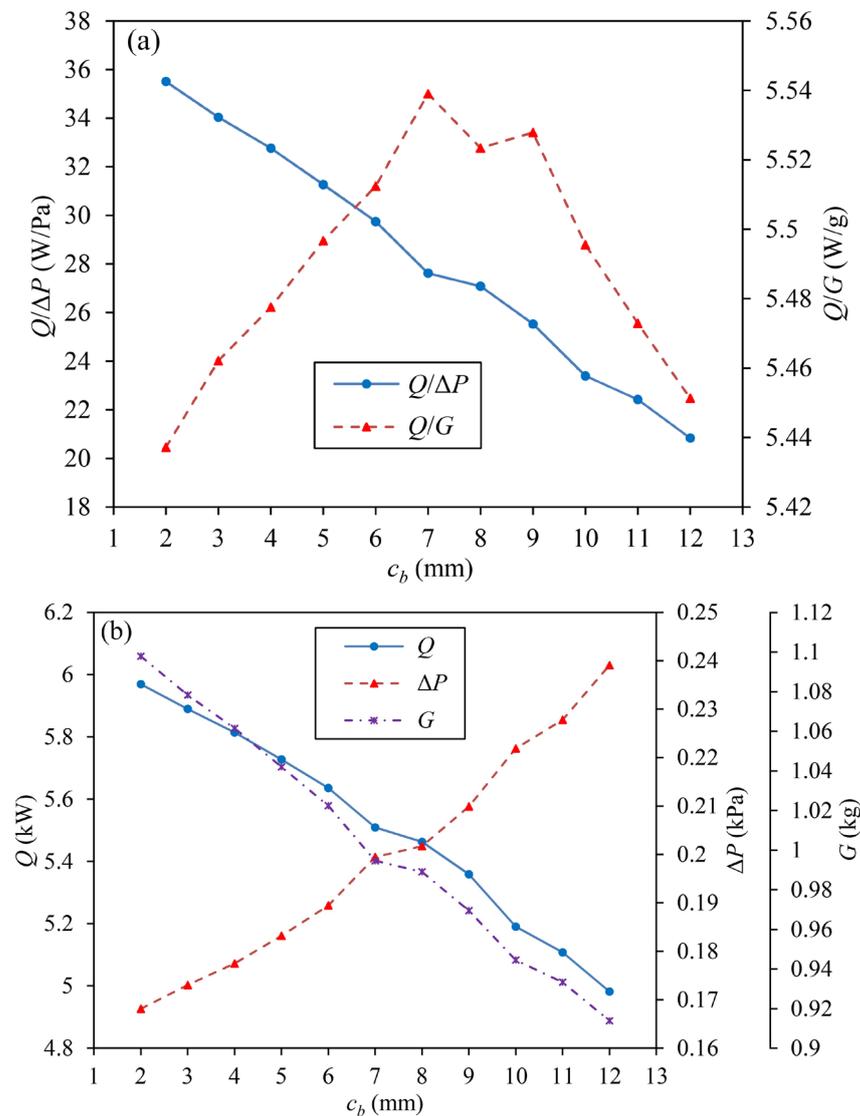
**Figure 6.** Influences of  $l_t$ : (a)  $Q/\Delta P$  and  $Q/G$  separately versus  $l_t$ ; (b)  $Q$ ,  $\Delta P$ , and  $G$  separately versus  $l_t$ .

### 3.1.4. Influences of $c_b$

$c_b$  varied from 2 mm to 12 mm while other structural parameters remained unchanged. The influences of  $c_b$  are presented in Figure 7.

As described in Figure 7a, while  $c_b$  increases from 2 mm to 12 mm,  $Q/\Delta P$  decreases by 35.51–20.84 W/Pa, and  $Q/G$  increases from 5.44 W/g first, reaching its highest point of 5.54 W/g when  $c_b$  is 7 mm, then experiencing a small oscillation on the point that  $c_b$  is

8 mm, and then reduces to 5.45 W/g gradually. As  $c_b$  grows, heat dissipation tubes number declines, which can result in the reduction of heat transfer area and heat dissipation tubes weight and the increase of flow rate of the fluid inside heat dissipation tubes. Thus, both  $Q$  and  $G$  decline, and  $\Delta P$  grows, simultaneously, as illustrated in Figure 7b. As  $Q$  decreases and  $\Delta P$  increases,  $Q/\Delta P$  decreases continuously with the growth of  $c_b$ , as depicted in Figure 7a. In addition, even though both  $Q$  and  $G$  decline, the decline rate of  $Q$  is lower than  $G$  at the beginning, and then the decline rate of  $Q$  is higher than  $G$  after  $c_b$  grows to one point. Thus,  $Q/G$  should increase first and then decrease. Meanwhile, the change of heat dissipation tubes number is not continuous, which results in  $Q/G$  line oscillation, especially when decline rates of  $Q$  and  $G$  are close, the oscillation phenomenon could become more severe. Hence, an oscillation occurs during the process of  $Q/G$  line reaching peak and gradually declining thereafter, as shown in Figure 7a.



**Figure 7.** Influences of  $c_b$ : (a)  $Q/\Delta P$  and  $Q/G$  separately versus  $c_b$ ; (b)  $Q$ ,  $\Delta P$ , and  $G$  separately versus  $c_b$ .

### 3.2. Sensitivity Analysis

#### 3.2.1. Sensitivity Analysis Using Sobol' Method

The Sobol' method [35,36] is one kind of widely employed global sensitivity analysis method based on variance, which can give out first-order sensitivity index that reflects a single input's contribution to output and total sensitivity index that reflects the contribution

of not only current input but also the interaction between current input and others to output. In this research, the Sobol’ method was adopted to analyze the influence contributions of  $d_o$ ,  $c_t$ ,  $l_t$ , and  $c_b$  on  $Q/\Delta P$  and  $Q/G$ , as depicted by the following procedures:

- (1) Set input parameters as  $d_o$ ,  $c_t$ ,  $l_t$ , and  $c_b$  and output parameters as  $Q/\Delta P$  and  $Q/G$ .
- (2) Set feasible region for input parameters and sampling size for Monte Carlo discretization.
- (3) Generate Sobol’ sequence and obtain sampling points using it.
- (4) Compute  $Q/\Delta P$  and  $Q/G$  for sampling points based on STHX-SB design indicators calculation model.
- (5) Calculate first order sensitivity indices and total sensitivity indices of  $Q/\Delta P$  and  $Q/G$  for  $d_o$ ,  $c_t$ ,  $l_t$ , and  $c_b$  utilizing Equations (30)~(35) [35–37].

$$S_i = \frac{D_i}{D_{tot}}, \quad \text{for } 1 \leq i \leq s, \tag{30}$$

$$S_{i\_tot} = \frac{D_{i\_tot}}{D_{tot}}, \quad \text{for } 1 \leq i \leq s, \tag{31}$$

$$D_{tot} = \int f^2(x)dx - f_0^2 \approx \frac{1}{N} \sum_{k=1}^N f^2(x_k) - f_0^2, \tag{32}$$

$$D_i = D_{tot} - \frac{1}{2} \int [f(x) - f(x_i, x'_{-i})]^2 dx dx'_{-i} \approx D_{tot} - \frac{1}{2N} \sum_{k=1}^N [f(x_k) - f(x_{ik}, x'_{-ik})]^2, \tag{33}$$

$$D_{i\_tot} = \frac{1}{2} \int [f(x) - f(x'_i, x_{-i})]^2 dx dx'_{-i} \approx \frac{1}{2N} \sum_{k=1}^N [f(x_k) - f(x'_{ik}, x_{-ik})]^2, \tag{34}$$

$$f_0 = \int f(x)dx \approx \frac{1}{N} \sum_{k=1}^N f(x_k), \tag{35}$$

### 3.2.2. Sensitivity Analysis Results

In this research, the feasible region for input parameters was set as shown by Equation (36).  $N$  was set as 100,000. The obtained sensitivity indices of  $Q/\Delta P$  and  $Q/G$  for  $d_o$ ,  $c_t$ ,  $l_t$ , and  $c_b$  are shown in Figure 8.

$$\left\{ \begin{array}{l} 1.6 \text{ mm} \leq d_o \leq 5 \text{ mm} \\ 0.4 \text{ mm} \leq c_t \leq 2 \text{ mm} \\ 110 \text{ mm} \leq l_t \leq 142 \text{ mm} \\ 2 \text{ mm} \leq c_b \leq 12 \text{ mm} \end{array} \right. \tag{36}$$

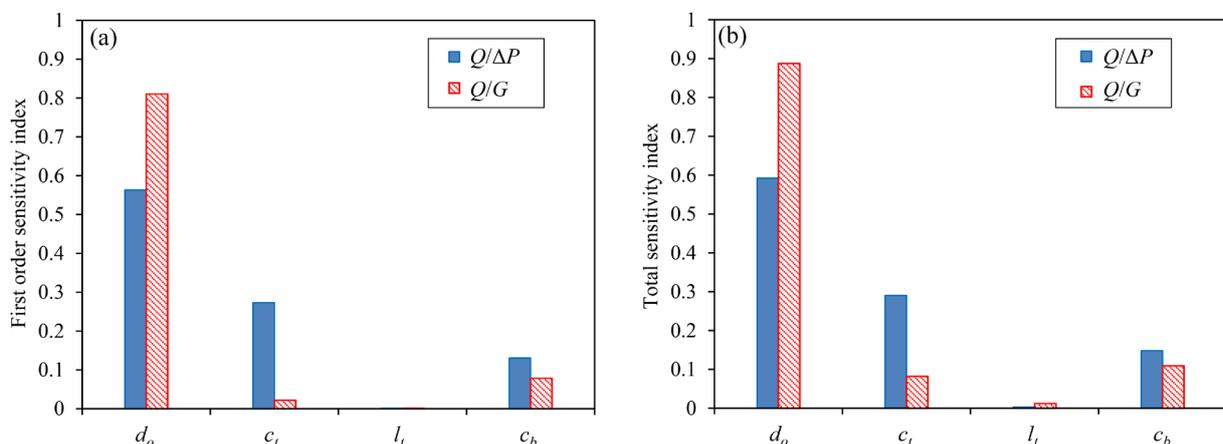


Figure 8. Sensitivity analysis results: (a) first-order sensitivity indices; (b) total sensitivity indices.

It could be found from Figure 8 that for these two kinds of indices, the indices of  $Q/\Delta P$  for  $d_o$  are both the highest followed by  $c_t, c_b, l_t$ , and the indices of  $Q/G$  for  $d_o$  are both the highest followed by  $c_b, c_t, l_t$ . Thus, it can be considered that whether the interaction between factors is considered or not, both  $Q/\Delta P$  and  $Q/G$  are the most sensitive to changes in  $d_o$  and the least sensitive to changes in  $l_t$ .

#### 4. Configuration Optimization

##### 4.1. Configuration Optimization Method

###### 4.1.1. Problem Presentation

According to previous parametric study, it is obvious that the changing of  $Q/\Delta P$  and  $Q/G$  is in connection with the variation of  $d_o, c_t, l_t$ , and  $c_b$ . Hence, in order to improve STHX-SB comprehensive performance,  $d_o, c_t, l_t$ , and  $c_b$ , as shown in Figure 1, were optimized to maximize  $Q/\Delta P$  and  $Q/G$ , simultaneously. This problem is formulated by Equation (37).

$$\begin{cases} \text{Max} & Q/\Delta P, Q/G \\ \text{S.t.} & 1.6 \text{ mm} \leq d_o \leq 5 \text{ mm} \\ & 0.4 \text{ mm} \leq c_t \leq 2 \text{ mm} \\ & 110 \text{ mm} \leq l_t \leq 142 \text{ mm} \\ & 2 \text{ mm} \leq c_b \leq 12 \text{ mm} \end{cases} \quad (37)$$

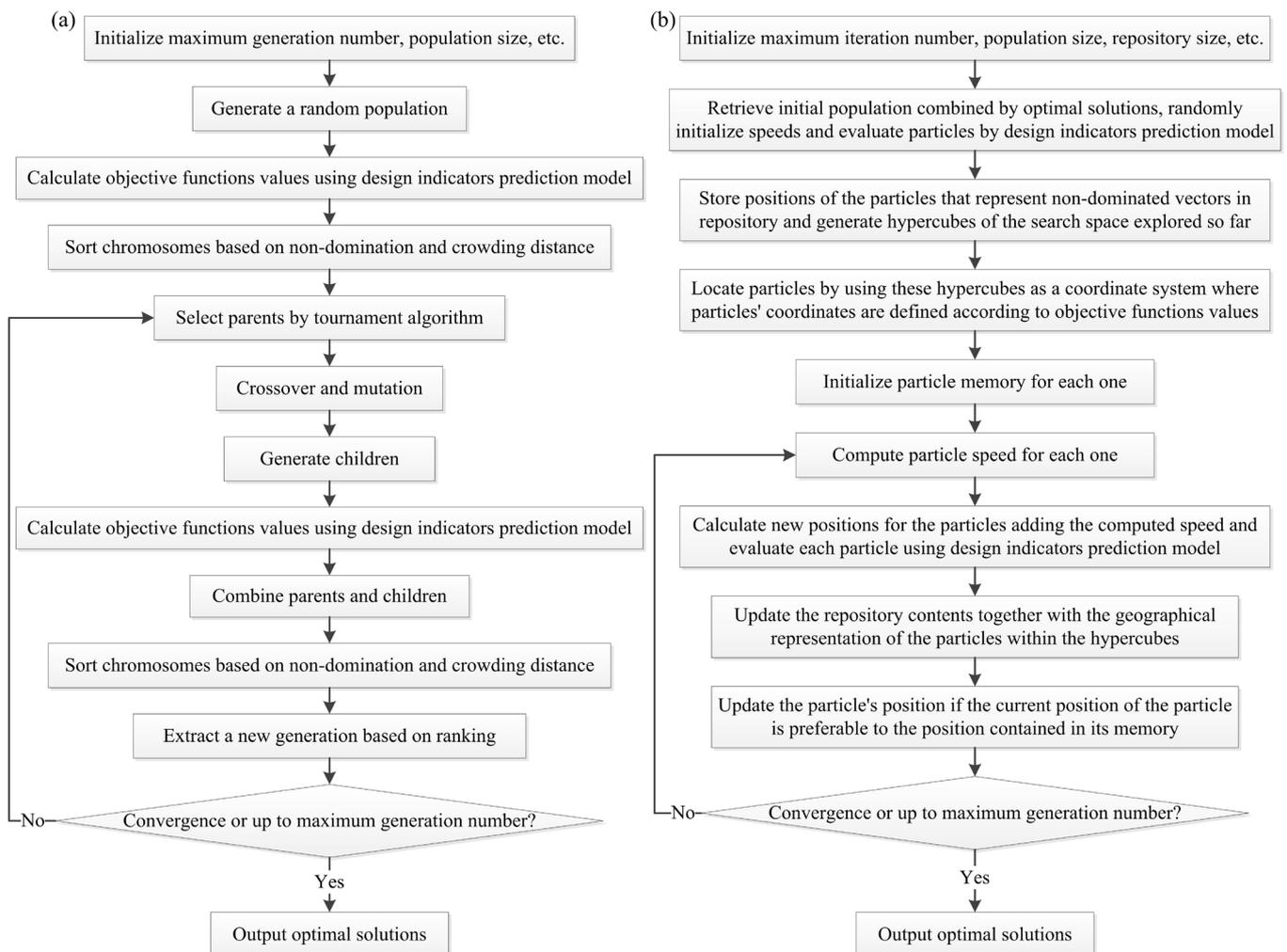
###### 4.1.2. Combination Optimization of NSGAI and MOPSO Embedded Grouping Cooperative Coevolution

From previous parametric studies, it is not difficult to be found that the influences of  $d_o, c_t, l_t$ , and  $c_b$  on  $Q/\Delta P$  and  $Q/G$  are nonlinear and conflicted in most cases. Simultaneous changings of  $d_o, c_t, l_t$ , and  $c_b$  can result in complicated simultaneous variations of  $Q/\Delta P$  and  $Q/G$ , which can make satisfactory optimal solutions hard to pick out utilizing simple parametric study only. When encountering this kind of situation, adopting multi-objective optimization theory can be a feasible solution.

To avoid the problem of falling into local optima due to algorithm convergence being too fast and to improve the reliability of solving multidimensional large-scale complex optimization problems, a cooperative coevolution method that embeds grouping optimization strategy into multi-objective optimization theory was proposed, which groups configuration parameters according to their contributions to performance indicators and then realizes initial optimization of grouping and secondary optimization after merging various groups based on a strategy of multi-objective optimization algorithm driving design indicators prediction model. NSGAI [38] and MOPSO [39] are two classic and significant optimization methods. However, NSGAI has the limitation of lower convergence and MOPSO has the limitation of easily trapping into local optima. Thus, in this research, NSGAI was adopted in the initial optimization of grouping and MOPSO was adopted in the secondary optimization after merging various groups in the process of cooperative coevolution, which can realize complementary deficiencies between NSGAI and MOPSO. Ultimately, one combination optimization method of NSGAI and MOPSO embedded grouping cooperative coevolution (NSGAI-MOPSO-GCC) can be proposed. The procedures of STHX-SB configuration optimization based on NSGAI-MOPSO-GCC are presented as follows:

- (1) Define design parameters, feasible region, and optimization objectives.
- (2) Retrieve Sobol' sensitivity analysis results in parametric study.
- (3) Group design parameters according to the contributions of design parameters to objective functions. In this research, this procedure is conducted as follows:
  - (a) Select 50% of the design parameters that the first objective function is more sensitive to.
  - (b) Select 50% of the design parameters that the second objective function is more sensitive to.

- (c) Combine the design parameters selected in Step (a) and Step (b) as the first group.
  - (d) Select 50% of the design parameters that the first objective function is less sensitive to.
  - (e) Select 50% of the design parameters that the second objective function is less sensitive to.
  - (f) Combine the design parameters selected in Step (d) and Step (e) as the second group.
- (4) Optimize the design parameters in the first group and the second group, respectively, based on a strategy of NSGAI driving design indicators prediction model. NSGAI optimization flow is depicted by Figure 9a.
  - (5) Combine the optimal solutions of the two groups as initial population and optimize the design parameters shown by Equation (37) based on a strategy of MOPSO driving design indicators prediction model. MOPSO optimization flow is depicted by Figure 9b.



**Figure 9.** Optimization flows of NSGAI and MOPSO: (a) NSGAI; (b) MOPSO.

The illustration of STHX-SB configuration optimization flow based on NSGAI-MOPSO-GCC is depicted in Figure 10.

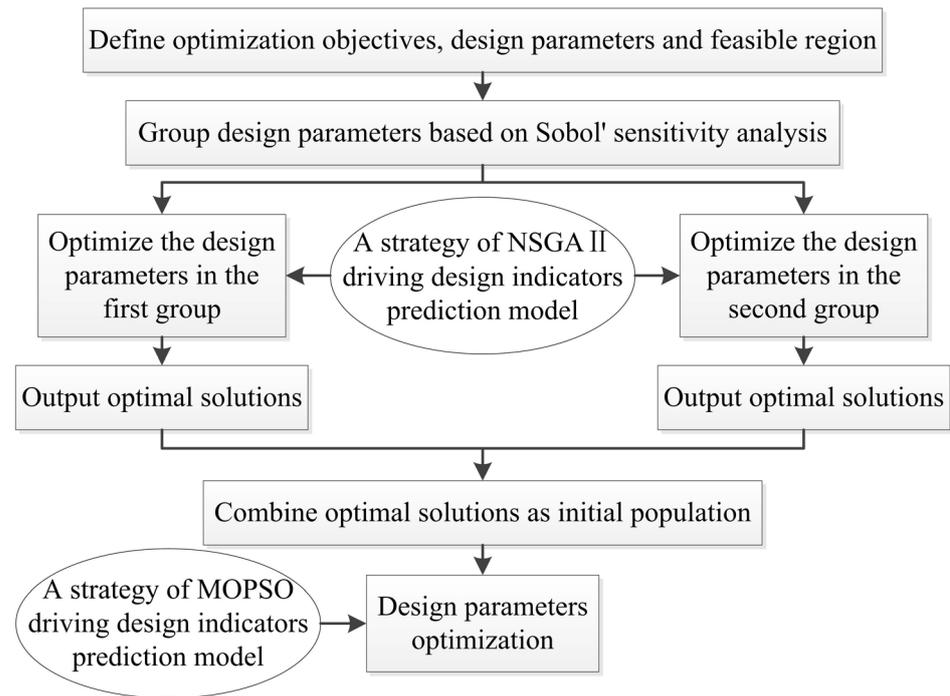


Figure 10. Flowchart of STHX-SB configuration optimization based on NSGAI-MOPSO-GCC.

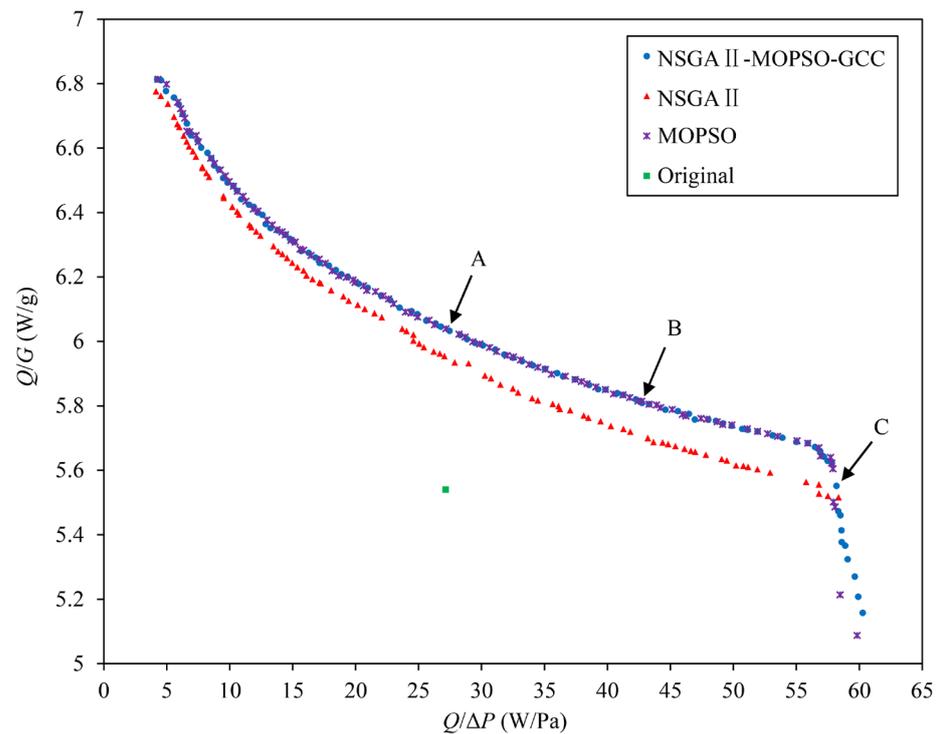
4.2. Optimization Results

According to the previous Sobol' analysis in this research,  $Q/\Delta P$  is the most sensitive to  $d_o$  and then followed by  $c_t, c_b, l_t$ , and  $Q/G$  is the most sensitive to  $d_o$  and then followed by  $c_b, c_t, l_t$ . Thus,  $d_o, c_t$ , and  $c_b$  were arranged in the first group of the design parameters that the objective functions are more sensitive to, and  $c_t, l_t$ , and  $c_b$  were arranged in the second group of the design parameters that the objective functions are less sensitive to. Population size and maximum generation number of NSGAI in NSGAI-MOPSO-GCC were 100 and 50, respectively. Repository size, population size, and maximum iteration number of MOPSO in NSGAI-MOPSO-GCC were 100, 200, and 50, respectively. The obtained optimal solutions by NSGAI-MOPSO-GCC are shown by Figure 10, and it is not hard to be found that some Pareto optimal solutions obtained by NSGAI-MOPSO-GCC can achieve higher  $Q/\Delta P$  and higher  $Q/G$  simultaneously compared with the original configuration. Three solutions were chosen from them, as shown in Figure 11 and Table 6.

Table 6. Optimal solutions comparison.

Parameters	$d_o$ (mm)	$c_t$ (mm)	$l_t$ (mm)	$c_b$ (mm)	$Q/\Delta P$ (W/Pa)	$Q/G$ (W/g)
Original	2.36	0.64	130	7.5	27.14	5.54
Solution A	2.26	0.93	110	2.1	27.45	6.03
Solution B	2.70	0.74	110	2.0	42.74	5.81
Solution C	3.39	0.40	115	2.0	58.18	5.55

As illustrated in Table 6,  $Q/\Delta P$  of solutions A, B, and C increases separately by 1.14%, 57.48%, and 114.37%, and simultaneously,  $Q/G$  of solutions A, B, and C increases separately by 8.84%, 4.87%, and 0.18%, compared with the original structure. For the selected solutions, the average improvement percentages of  $Q/\Delta P$  and  $Q/G$  are 57.66% and 4.63%, respectively. Thus, through NSGAI-MOPSO-GCC, maximizing  $Q/\Delta P$  and  $Q/G$  simultaneously can be realized reliably.



**Figure 11.** Optimal solutions.

In addition, optimization comparison among NSGAI-MOPSO-GCC and two classic optimization methods including NSGAI and MOPSO was also conducted. In order to ensure comparability, population size and maximum generation number of NSGAI were both set as 100, and repository size, population size, and maximum iteration number of MOPSO were separately set as 100, 200, and 100. The comparison results are depicted in Figure 10, and it can be clearly seen that  $Q/\Delta P$  and  $Q/G$  values of almost all of the optimal points obtained by NSGAI-MOPSO-GCC and MOPSO are higher than the values obtained by NSGAI, which indicates that NSGAI has the lowest convergence rate among them. Moreover, even though many of the optimal points obtained by MOPSO almost overlap with the optimal points obtained by NSGAI-MOPSO-GCC, there still exist some optimal points searched by NSGAI-MOPSO-GCC that are not found by MOPSO, especially the optimal solutions in the  $Q/\Delta P$  range of higher than 57.92 W/Pa, which indicates that the searching capability of MOPSO is lower than NSGAI-MOPSO-GCC as MOPSO has the limitation of easily trapping into local optima. Thus, it can be concluded that among these three optimization methods, NSGAI-MOPSO-GCC performs the best, followed by MOPSO, and then NSGAI. Hence, based on the analysis above, it can be considered that the proposed method of STHX-SB configuration optimization based on NSGAI-MOPSO-GCC is valid and feasible, which can supply beneficial and valuable guidance in engineer applications of heat exchanger.

## 5. Conclusions

In this research, one design indicators prediction model for STHX-SB based on the Bell–Delaware method was constructed to calculate  $Q$ ,  $\Delta P$ , and  $G$ , and the model reliability was validated. Based on a design indicators prediction model, a parametric study was conducted to research the influences of  $d_o$ ,  $c_t$ ,  $l_t$ , and  $c_b$  on  $Q/\Delta P$  and  $Q/G$  and analyze the sensitivity indices of  $d_o$ ,  $c_t$ ,  $l_t$ , and  $c_b$  for  $Q/\Delta P$  and  $Q/G$  utilizing the Sobol' method. Based on the design indicators prediction model and Sobol' sensitivity analysis theory, one combination optimization method of NSGAI-MOPSO-GCC was proposed for STHX-SB to optimize  $d_o$ ,  $c_t$ ,  $l_t$ , and  $c_b$  to maximize  $Q/\Delta P$  and  $Q/G$  simultaneously. Comparison between three selected optimal solutions and the original configuration was conducted. In addition,

optimization effects among NSGAI-MOPSO-GCC and two classic optimization algorithms including NSGAI and MOPSO were compared. Below are the main conclusions:

- (1) Compared with experimental data, the error percentages of  $Q$  are 7.61–9.41% with the average value of 8.52%, and the error percentages of  $\Delta P$  are 5.43–10.22% with the average value of 7.92%. The values of  $G$  predicted by the proposed model and weighed by Solidworks commercial software are the same. So, the proposed design indicators prediction model is validated to be reliable and valid.
- (2) Through parametric influences analysis, it can be found that  $Q/\Delta P$  grows first and then declines slightly with slight oscillations with the increase of  $d_o$ , and it reduces with the increase of anyone of  $c_t$ ,  $l_t$ , and  $c_b$ .  $Q/G$  decreases with the increase of anyone of  $d_o$  and  $l_t$ , and it rises first and then reduces with the increase of  $c_t$ . As  $c_b$  grows,  $Q/G$  increases first, experiencing a small oscillation after peaking at a point, and then reduces.
- (3) Through Sobol' sensitivity analysis, it can be found that whether the interaction between factors is considered or not,  $Q/\Delta P$  is the most sensitive to  $d_o$  and then followed by  $c_t$ ,  $c_b$ ,  $l_t$ , and  $Q/G$  is the most sensitive to  $d_o$  and then followed by  $c_b$ ,  $c_t$ ,  $l_t$ .
- (4) For the selected solutions, the average improvement percentages of  $Q/\Delta P$  and  $Q/G$  separately are 57.66% and 4.63%, compared with the original structure, and through the comparison among the three optimization algorithms, it can be found that NSGAI-MOPSO-GCC performs the best, followed by MOPSO, and then NSGAI, which illustrates that the proposed method of STHX-SB configuration optimization based on NSGAI-MOPSO-GCC is valid and feasible, and can supply beneficial and valuable guidance for heat exchanger design and improvement.

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**Conflicts of Interest:** The authors declare no conflict of interest.

## Nomenclature

### Latin Letters

$A$	heat transfer area, $m^2$
$A_{o,bp}$	bypass area of a cross flow section in shell-side, $m^2$
$A_{o,cr}$	flow area of a cross flow section in shell-side, $m^2$
$A_{o,sb}$	leakage area between shell and baffle, $m^2$
$A_{o,tb}$	leakage area between tubes and baffle, $m^2$
$C^*$	heat capacity ratio
$c_b$	tube bundle bypass flow clearance, m
$c_p$	specific heat capacity, $kJ/(kg \cdot K)$
$c_t$	clearance between heat dissipation tubes, m
$D_i$	variance of $f(x)$ for factor $x_i$
$D_{i,tot}$	total variance of $f(x)$ for factor $x_i$
$D_N$	shell/tube-side inlet/outlet diameter, m
$D_{otl}$	tube bundle containment diameter, m
$D_s$	inner diameter of heat exchanger shell, m
$D_{tot}$	total variance of $f(x)$

$d_b$	baffle diameter, m
$d_i$	inner diameter of heat dissipation tube, m
$d_o$	outside diameter of heat dissipation tube, m
$da_{ca}$	calculation data
$da_{ex}$	experimental data
$E$	heat transfer capacity calculation error, kW
$E_{ts}$	basic error of temperature sensor, K
$EP$	error percentage
$FS$	full scale
$G$	weight, kg
$G_b$	baffles weight, kg
$G_p$	end plates weight, kg
$G_s$	spacer tubes weight, kg
$G_t$	heat dissipation tubes weight, kg
$J_b$	tube bundle bypass correction factor
$J_c$	baffle layout correction factor
$J_l$	baffle leakage effect correction factor
$J_r$	temperature gradient correction factor
$J_s$	correction factor for unequal span heat transfer
$K$	total heat transfer coefficient, kW/(m <sup>2</sup> ·K)
$L_{bc}$	baffle spacing in shell-side middle section, m
$L_{b,i}$	baffle spacing near shell-side inlet, m
$L_{b,o}$	baffle spacing near shell-side outlet, m
$l_c$	chord height of baffle cut, m
$l_t$	heat dissipation tube length, m
$N$	sampling size for Monte Carlo discretization
$N_b$	baffles number
$N_p$	end plates number
$N_{r,c}$	effective number of tube rows for fluid crossing through in a baffle section
$N_{r,cc}$	effective number of tube rows for fluid crossing through in a cross flow section
$N_{r,cw}$	effective number of tube rows for fluid crossing through in a baffle window
$N_{ss}$	pairs number of bypass baffles of a cross flow section in shell-side
$N_{s,b}$	spacer tube number between baffles
$N_t$	heat dissipation tubes number
$N_{t,cut}$	number of the heat dissipation tubes in a baffle window
$NTU$	number of transfer units
$P_c$	baffle cut
$P_f$	fuel inlet pressure, kPa
$P_f'$	fuel outlet pressure, kPa
$Pr$	Prandtl number
$Q$	heat transfer capacity, kW
$Q_{as}$	assumed heat transfer capacity, kW
$q_f$	fuel flow rate, L/min
$q_o$	flow rate of lubricating oil, L/min
$Re$	Reynolds number
$S_i$	first order sensitivity index for factor $x_i$
$S_{i,tot}$	total sensitivity index for factor $x_i$
$s$	sensitivity analysis parameters number
$T_f$	fuel inlet temperature, K
$T_f'$	fuel outlet temperature, K
$T_{f,ave}$	fuel average temperature, K
$T_o$	inlet temperature of lubricating oil, K
$T_o'$	lubricating oil outlet temperature, K
$T_{o,ave}$	oil average temperature, K
$T_{t,w}$	heat dissipation tube wall temperature, K
$t_b$	baffle thickness, m
$t_p$	thickness of end plate, m
$t_{s,w}$	wall thickness of spacer tube, m

$t_{ts}$	temperature measured by temperature sensor, K
$t_{i\_w}$	wall thickness of heat dissipation tube, m
$t_1$	hot side inlet temperature, K
$t_2$	cold side inlet temperature, K
$u$	fluid velocity, m/s
$u_N$	fluid velocity of inlet/outlet, m/s
$W$	heat capacity, kW/K
$X_l$	tube pitch parallel to the shell-side fluid flow in cross flow zone, m
$x_i$	one independent random point uniformly distributed with $x'_i$
$x'_i$	one independent random point uniformly distributed with $x_i$
$x_{-i}$	parameter combination complementary to $x_i$
$Z_s$	shell passes number
$Z_t$	tube passes number
Greek Symbols	
$\alpha$	heat transfer coefficient, kW/(m <sup>2</sup> ·K)
$\Delta P$	tube-side pressure drop, kPa
$\Delta P_i$	on-way resistance, kPa
$\Delta P_N$	inlet and outlet flow resistance, kPa
$\Delta P_r$	elbow flow resistance, kPa
$\varepsilon$	heat transfer efficiency
$\lambda$	heat conductivity, kW/(m·K)
$\mu$	fluid viscosity, Pa·s
$\rho$	density, kg/m <sup>3</sup>
Subscripts	
$al$	aluminium alloy
$f$	fuel
$i$	tube-side
$id$	ideal
$max$	maximum
$min$	minimum
$o$	shell-side
$w$	tube wall

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