

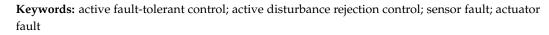


# Article Active Fault-Tolerant Control for Near-Space Hypersonic Vehicles

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**Abstract:** Due to the harsh working environment, Near-Space Hypersonic Vehicles (NSHVs) have the characteristics of frequent faults, which seriously affect flight safety. However, most researches focus on active fault-tolerant control for actuator faults. In order to fill the gap of active fault-tolerant control for sensor faults, this paper presents an Active Fault-Tolerant Control (AFTC) strategy for NSHVs based on Active Disturbance Rejection Control (ADRC) combined with fault diagnosis and evaluation. With the proposed AFTC strategy, both sensor faults and actuator faults can be compensated within 0.5 s. Wavelet packet decomposition and Kernel Extreme Learning Machine (KELM) are associated to ensure the high accuracy and real-time ability of fault diagnosis. Simulation results show that the proposed fault diagnosis method can significantly reduce the divergence of diagnosis results by up to 98%. The fault information is used to generate tolerant compensation, which is combined with the ADRC to achieve AFTC. Statistical results indicate that AFTC has significantly lower static error than ADRC. The proposed AFTC method endows NSHVs with the ability to complete missions even when various types of faults appear. Its advantages are demonstrated in comparison with other fault diagnosis and tolerant control methods.



# 1. Introduction

In recent years, Near-Space Hypersonic Vehicles (NSHVs) have become the central issue in aerospace. However, due to the severe near-space flight environment, NSHVs are prone to various types of small faults with concurrency [1,2]. Moreover, in the dynamic closed-loop system, small faults are easily amplified into significant faults, leading to serious consequences. The existence of the closed-loop control strategy causes fault deterioration, which can mask early features [3]. Therefore, the design of a high-quality fault-tolerant control strategy is urgently needed and becomes a new hotspot [4,5].

Fault-tolerant control methods for complex nonlinear systems are divided into Passive Fault-Tolerant Control (PFTC) and Active Fault-Tolerant Control (AFTC) [6]. A PFTC system is designed by experts, which can accommodate prescribed faults using its robustness, without the knowledge of faults [7,8]. Active Disturbance Rejection Control (ADRC) is widely used in PFTC for its simple structure and outstanding performance in anti-disturbance and actuator fault tolerance. Zhang et al. [9] designed a double closed-loop ADRC for the quadrotor UAV, and the total disturbances are estimated and compensated by ESO which can improve the anti-disturbance ability.

On the contrary, an AFTC strategy requires the fault information to reconstruct the controller. The fault information is provided by an onboard fault diagnosis and evaluation unit. Compared with PFTC, the addition of fault information makes AFTC more adaptable, and makes it possible to solve sensor faults. And that's why AFTC has become a new



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). research focus [5,10–12]. Xu et al. [13] developed an adaptive fault-tolerant control method for hypersonic vehicles considering unexpected elevator faults, uncertain parameters, and external disturbances. Wu et al. [14] used a fault diagnosis unit, based on the long short-term memory neural network, to diagnose actuator faults, and the fault tolerance was realized both in the control allocation and control layers. However, the papers above focus on the actuator faults, but neglect fault tolerance for sensor faults. For the severe flight environment, actuator faults and sensor faults are common for NSHVs. Therefore, both of these faults are considered in this paper.

For NSHVs, both PFTC and AFTC have been widely studied. The former needs the system to be strong enough in face of faults, but cannot well handle significant faults. The latter has higher fault tolerance ability for obvious faults. However, study on the AFTC concentrates mainly on actuator faults, relying on the correct sensors' feedback. Table 1 shows the capabilities of different control methods. It's evident that sensor faults should also be taken into consideration for AFTC [15–17].

An AFTC system usually consists of three parts: a PFTC unit, a fault diagnosis and evaluation unit, and a controller reconstruction unit [18,19]. The use of PFTC is to track the control instruction and implement passive fault tolerance before the controller is reconstructed when there are faults. The key point of fault diagnosis and evaluation unit is to get information about faults. To some extent, the accuracy of fault diagnosis and evaluation decides the effect of AFTC. Thus, different methods have been researched explosively. Currently, the widely used methods are mainly divided into two categories, namely model-based methods and data-driven methods [20]. Model-based methods rely on the mathematical of models, which are unsuitable for complex nonlinear systems such as NSHVs. Meanwhile, in data-driven methods, machine-learning methods are generally used, such as neural networks or classifiers. The advantage is that accurate models are not required, which are more beneficial for complex systems [21]. To achieve AFTC, the fault diagnosis and evaluation unit should gives types and severity of faults to the subsequent controller. Meanwhile, it should have the capability of real-time computing. Considering noises and various types of faults, higher requirements are put forward for fault diagnosis.

Method	Anti-Interference	Actuator Fault Tolerance	Sensor Fault Tolerance
PFTC	$\checkmark$	partly	
Previous AFTC	$\checkmark$	$\checkmark$	
AFTC proposed	$\checkmark$	$\checkmark$	$\checkmark$

Table 1. Capability of different control methods.

Above all, although plenty of researches have focused on Fault Tolerant Control (FTC) or fault diagnosis, there are still some problems that need to be solved: (1) most of the PFTC-adopted researches are helpful for actuator faults depending on the correct sensors' feedback, but cannot handle sensor faults [17,22,23]; (2) plenty of researchers focus on faults classification, ignoring the requirement of faults identification [24,25]. Motivated by the aforementioned challenges and demands, this paper proposes a novel Active Disturbance Rejection Control and Kernel Extreme Learning Machine (ADRC-KELM) based AFTC scheme for NSHVs with actuator faults and sensor faults.

The main contribution of this paper is to introduce a novel method for fault diagnosis, evaluation and AFTC algorithm for NSHVs. The introduction of sliding window and KELM enables faults diagnosis less than 0.5 s. Furthermore, the joint time-frequency analysis makes fault identification possible. Finally, the AFTC endows NSHVs with the ability to complete missions in the face of multiple faults.

The remainder of this paper is organized as follows. In Section 2, model of NSHVs, the Reaction Control System (RCS), and an ADRC controller are proposed. Details of ADRC-KELM based AFTC are addressed in Section 3. In Section 4, results of various simulations are illustrated and analyzed. Finally, Section 5 draws the conclusion.

## 2. Nonlinear Model of NSHV with Closed-Loop Faults

In this section, a nonlinear model is provided. The nonlinear model established under ideal conditions lays the foundation for flight simulation experiments. The PFTC is established for disturbance rejection and uncertainty suppression. Main ideas and implementation of the AFTC method are briefly described in Figure 1.

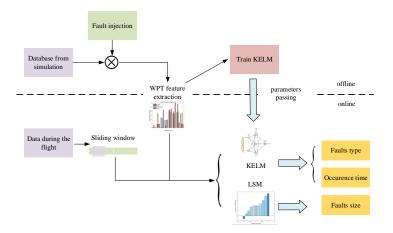


Figure 1. Flowchart of the AFTC.

The AFTC method is composed of two parts: online and offline. The task of the offline part is to train KELM for obtaining an efficient classifier. First, simulation results of different states constitute the database. Then Wavelet Packet Transformation (WPT) is used to extract features to train the KELM. For the online part, a sliding window is adopted to realize real-time fault diagnosis. And the trained parameters are passed to classify faults. Finally, joint time-frequency analysis of the residual signal is employed to identify fault sizes.

As shown in Figure 2a, the studied NSHV has delta wings, foldable horizontal canards, a vertical tail, and the RCS. Due to the low atmospheric density, the aerodynamic rudder surface efficiency is insufficient, which makes it difficult to meet the control requirements. Therefore, RCS is adopted to complete attitude control.

Figure 2b depicts the inertia coordinate  $ox_oy_oz_o$ , body coordinate  $ox_by_bz_b$ . Without loss of generality, only the longitudinal channel of the aircraft is considered. The reentry process of the NSHV can be modeled by the following equations:

$$\begin{aligned} \dot{x} &= v \cos \gamma \\ \dot{z} &= -v \sin \gamma \\ \dot{v} &= \frac{(-D - mg \sin \gamma - T_y \sin \alpha)}{\gamma} \\ \dot{\gamma} &= \frac{Y + T_y \cos \alpha - mg \cos \gamma}{mv} \\ \dot{\alpha} &= \omega_y - \dot{\gamma} \\ \dot{\omega} &= \frac{lT_y}{l_{yy}} \end{aligned}$$
(1)

where x, z denote the position of the NSHV in the inertia coordinate system. v is the velocity.  $\gamma, \alpha$  denote the trajectory inclination angle and the angle of attack, respectively. m is the mass of NSHV, which is regarded as a constant. g indicates the gravitational acceleration.  $D, T_y, Y$  are the aerodynamic drag, propulsion, and aerodynamic force, respectively.  $w_y$ represents the pitch angular rate.  $I_y$  denotes the moment of inertia for the y coordinate axes. l means the distance from the RCS to the center of mass. More details are cited from [1].

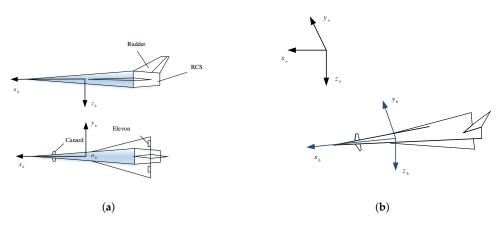


Figure 2. (a) Schematic drawing of NSHV; (b) the inertia and body coordinate.

# 2.1. NSHV Passive Fault-Tolerant Control

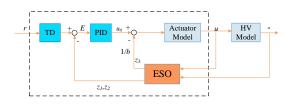
The construction of ADRC is designed as Figure 3. The Extended State Observer (ESO) can be regarded as a reference model, which is established as follow:

$$\begin{cases} e = z_1 - \theta \\ \dot{z}_1 = z_2 - \beta_1 e \\ \dot{z}_2 = z_3 - \beta_2 e + bu \\ \dot{z}_3 = -\beta_3 e \end{cases}$$
(2)

where  $z_1$ ,  $z_2$ ,  $z_3$  are observations of ESO, which are angle of attack, its differential, and the total disturbance. *e* is the residual signal.  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$  are the tunable parameters with different values, which are generally determined by the bandwidth of the observer and can affect tracking performance [26]. The Tracking Differentiator (TD) is defined as follows:

$$\begin{cases} a_1(k+1) = a_1(k) + T_s a_2(k) \\ a_2(k+1) = a_2(k) - T_s(\left(\frac{a_1(k)}{T^2} - a^*(k)\right) + \frac{2a_2(k)}{T_c}) & , \end{cases}$$
(3)

where  $a_1(k)$ ,  $a_1(k + 1)$  denote the estimated angle values of the current time and next time, respectively.  $a_2(k)$ ,  $a_2(k + 1)$  are the derivatives of  $a_1(k)$ ,  $a_1(k + 1)$ , respectively.  $a^*(k)$  represents the desired signal.  $T_s$  and  $T_c$  are the sampling time and the time constant, respectively. The larger  $T_s$ , the better noise filtering [27].



**Figure 3.** The construction of ADRC. *r* is the desired angle of attack.

#### 2.2. Description and Modeling of Actuator Faults and Sensor Faults

During the stage of reentry, for the low atmospheric density, RCS is necessary for attitude control. Actuators directly decide the performance of control. That's why FTC for actuators is widely studied. But for sensor faults, most researchers regard them as interference terms and their causes are ignored. Building on previous work, the fault mechanisms are summarized [3,28,29].

Stuck fault: The output maintains a certain value and no longer changes. For RCS, once the adjust venturi tubes are stuck, the thrust maintains a constant value. For sensors, it is usually caused by unstable signal transmission.

Gain variation fault: The output deviates from the desired value. Usually, gain is multiplied by the desired value. For RCS, this fault is mainly caused by the change of throat diameter due to ablation. For sensors, temperature change and parts aging usually cause a slight variation or static error.

Outlier data fault: This kind of fault is a short-term fault. When it occurs, the output changes suddenly and returns to normal quickly without lasting effect, which is unique for sensor faults. This occurs when there is communication interference or other disturbances. Above all, the faults are summarized as follows:

$$O_{f,s} = O(t) + fal_{s}(O(t), t_{s})$$
  

$$O_{f,g} = O(t) + fal_{g}(O(t), K_{g}, t_{g}) ,$$
  

$$O_{f,o} = O(t) + fal_{o}(O(t), \delta, t_{o})$$
(4)

where O(t) is the output of sensors or actuators.  $O_{f,s}$ ,  $O_{f,g}$ ,  $O_{f,o}$  are outputs under the stuck fault, the gain variation fault, and the outlier data fault, respectively.  $t_s$ ,  $t_g$ ,  $t_o$  are the time of faults occur.  $K_g$ ,  $\delta$  are fault sizes, and  $fal(\cdot)$  is the fault model.

# 3. Construction of ADRC Based AFTC

Due to the existence of ESO, noise and disturbance are tolerated, to some extent. But when sensor faults occur, the PFTC cannot handle them. The information about sensor faults is needed for controller reconstruction to achieve AFTC. Thus, it is urgent to carry out fault identification to diagnose and identify sensor faults online.

## 3.1. Fault Diagnosis and Identification

## 3.1.1. Fault Diagnosis by WPT and KELM

According to (2), ESO can be regarded as a reference model. Therefore, the residual between the observation of ESO and the output of NSHV contains the fault information. Efficient feature extraction is beneficial for fault diagnosis and evaluation. However, in the stage of reentry, NSHVs are affected by the severe environment. Considering maneuver and disturbance, the signal is characterized as a non-stationary signal. WPT is adopted to extract features, for wavelet transform's unique advantages in processing non-stationary signals and its time-frequency feature processing ability. Sliding-window based feature extraction is adopted in view of real-time fault diagnosis. Figure 4a illustrates the structure of real-time fault identification.

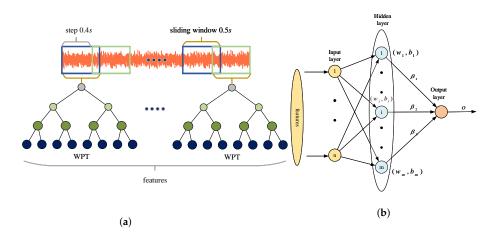


Figure 4. (a) Sliding-window based feature extraction; (b) structure of ELM.

Then, a classifier is used to classify sensor faults. Extreme Learning Machine (ELM) is a single hidden layer forward neural network, which has the advantage of calculation speed and accuracy. Figure 4b depicts the structure.

The output of ELM is  $O = \sum_{i=1}^{m} \beta_i g(W_i X_i + b_i)$ , where  $g(\cdot)$  is the activation function,  $W_i$  is the weight,  $b_i$  is the bias, and  $\beta_i$  is the output weight. The output can be represented by the matrix  $O = H\beta$ , where  $H, \beta$  are the hidden layer's output, and the output weights, respectively.

For ELM, once the  $W_i$ ,  $b_i$  is given, the  $\beta$  can be calculated by  $\hat{\beta} = H^+T$ , where  $H^+$  is the Moore-Penrose pseudoinverse of H, T is the target output. Usually, a positive value I/C is added, where C is a user-defined parameter for calculating the output weights. Then the formula is rewritten as  $\hat{\beta} = H^T (I/C + HH^T)^{-1}T$ . The output of ELM is  $y(x) = h(x)\hat{\beta}$ , where h(x) is the hidden layer [30].

Further, KELM is raised to overcome the dimension disaster.

$$\Omega_{ELM} = HH^T : \Omega_{ELMi,i} = h(x_i) \cdot (x_i) = K(x_i, x_i),$$
(5)

where  $K(x_i, x_j)$  is a kernel function. In this paper, the Radial Basis Function (RBF) kernel is used. Finally, the output of KELM is obtained [31]:

$$f(x) = \begin{bmatrix} K(x, x_1) \\ \vdots \\ K(x, x_N) \end{bmatrix}^{T} (I/C + \Omega_{ELM})^{-1}T$$
(6)

In this paper, the inputs of KELM are the features extracted by WPT and the outputs are types of sensor faults.

#### 3.1.2. Joint Time-Frequency Analysis Based Fault Identification

Energy is extracted by WPT from the residual, and its expression is:

$$||f||^{2} = \int |f(x)|^{2} dx \tag{7}$$

In the low-frequency bands, the energy reflects the size of the sensor faults. Meanwhile, in the high-frequency ones, the energy is affected by sensor noise and the sensor faults. Least Square Method (LSM) is widely used in data fitting, for its simplicity and efficiency. And considering that the noise is concentrated in the high-frequency bands, it's more accurate to use the energy in low-frequency bands to fit the size of sensor faults.

#### 3.2. Policy of Controller Reconstruction

So far, Fault Diagnosis and Evaluation (FDE) is achieved by the proposed fault diagnosis method. And the whole AFTC structure is illustrated in Figure 5.

The AFTC is designed as:

$$\alpha_{AFTC}(t) = \begin{cases} \alpha(t), & 0 \le t \le t_f \\ \alpha(t), & t_f \le t \le t_d, \\ \alpha(t) + \Delta_{FDE}, & t_d \le t \end{cases}$$
(8)

where  $t_f$ ,  $t_d$  are the time when faults occur and the time when the FDE unit determines the faults, respectively.  $\alpha(t)$  is the output of the sensor.  $\Delta_{FDE}$  is the amount of compensation for sensor faults.

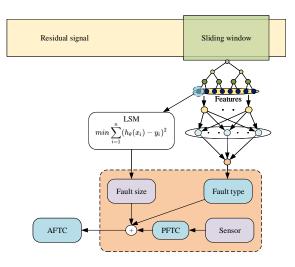


Figure 5. The structure of AFTC

# 4. Simulation Results

To verify the effectiveness of the proposed AFTC method, simulations under the standard condition and fault conditions are presented. The mid-term of reentry segment of NSHVs is selected. In this stage, the NSHV adopts a large angle of attack for decelerating. The simulation conditions are H = 33.5 km, v = 15 Ma,  $\alpha = 45^{\circ}$ , q = 0, and the angle of attack decreases to  $\alpha = 35^{\circ}$ , 2 s later, and the random noise  $\mu = 0.5^{\circ}$  is added to the data of the sensor. When the conditions are determined, the response is shown in the Figure 6.

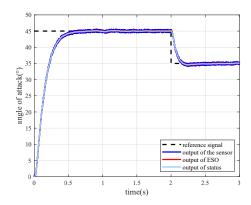


Figure 6. Angle of attack under fault-free.

The simulation shows that the NSHV can normally track the command with a raise time of 0.32 s, and the designed ESO observes the sensor output correctly under the fault-free condition. The sensor and actuator faults may occur at any time in the reentry process. To simplify the training process, faults are injected at 1.5 s during the simulation.

# 4.1. Simulations with Actuator Faults

According to the introduction of actuator faults model above, the gain variation fault  $K_g = 0.9$  and the stuck fault are injected separately.

It can be seen from Figure 7a,b that the designed PFTC has strong adaptability to the actuator gain variation fault. The steady-state time is only 0.2 s longer than the fault-free state. Meanwhile, the actuator stuck fault can be solved by redundant actuators, which is out of the range of this paper.

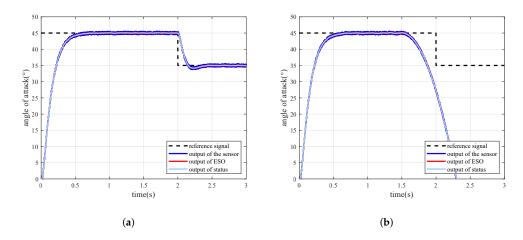
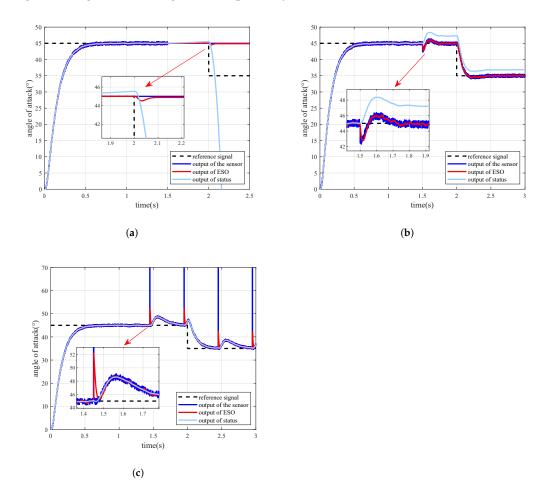


Figure 7. (a) Angle of attack under the gain variation fault; (b) angle of attack under the stuck fault.

## 4.2. Simulations with Sensor Faults

The angle of attack of sensor fault states is compared with that of the fault-free state. The results of the stuck fault, gain variation faults and the outlier data fault are shown in Figure 8a, Figure 8b and Figure 8c, respectively.



**Figure 8.** (a) Angle of attack under the stuck fault; (b) angle of attack under the gain variation fault; (c) angle of attack under the outlier data fault (the maximum outputs of the outlier data are  $90^{\circ}$ ).

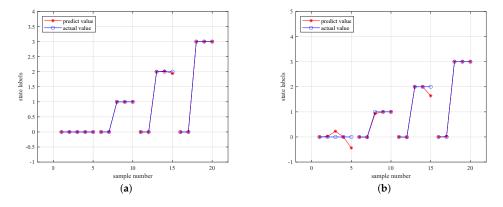
The results show that the designed PFTC cannot handle sensor faults, although it has better performance in actuator faults. The NSHV cannot follow flight instructions properly

because of the presence of faulty sensors. Sensor faults can reduce the flight quality and even seriously imperil the safety of NSHV.

#### 4.3. Simulations of the Proposed Fault Diagnosis Method

As our previous work showed, the energy distributions of diverse faults in different bands are various [3]. The energy caused by faults of different sizes shows a positive correlation with fault sizes, which can also get from the definition of energy (7).

For online FDE, a sliding window is adopted, with a 0.5 s sliding window and 0.4 s step time. The simulation result is shown in Figure 9a, where the labels 0, 1, 2, and 3 respectively represent the fault-free state, the stuck fault, the gain validation fault, and the outlier data fault.



**Figure 9.** (**a**) Results of fault diagnosis using the method proposed; (**b**) results of fault diagnosis using the contrast method.

To verify effectiveness of the proposed method, feature extraction and classification performed on the sensor output directly are adopted as the contrast method. It can be seen from results in Figure 9b that the contrast algorithm has greater uncertainty, especially in the fault-free state. This is because in the proposed method, the ESO estimates the total disturbance and counteracts the external interference, which is beneficial to improve the accuracy.

The distribution of multiple simulations is displayed in Figure 10a,b and Table 2. The Mean Squared Error (MSE) results show that except the outlier data fault, the proposed algorithm reduces the distribution of diagnostic results by up to 98%. The lower MSE indicates that the proposed method is more reliable. Although the MSE of the outlier data fault is slightly larger, the results of both methods are good enough in the diagnosis of the outlier data fault.

Furthermore, in terms of AFTC, it is necessary to know not only types of sensor faults but also sizes of faults. Energy in the low-frequency bands reflects sizes of the sensor fault. Under gain variation faults, as shown in Figure 11a, there is a quadratic correlation between the energy in the first band and gains, and the coefficients are calculated by LSM.

Fault Type	MSE Using the Proposed Method	MSE Using the Contrast Method
fault-free state	0.00021	0.01092
stuck fault	0.00022	0.00471
gain validation fault	0.0114	0.01536
outlier data fault	0.00026	0.00016

Table 2. Distribution of results.

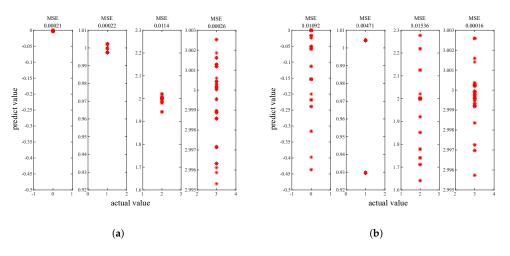
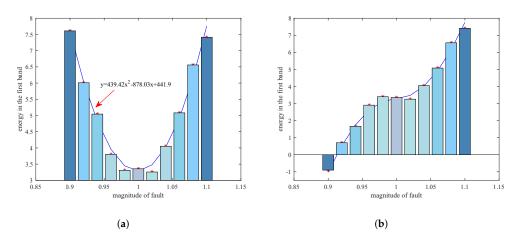


Figure 10. (a) Distribution of results using the method proposed; (b) distribution of results using the contrast method.



**Figure 11.** (a) Energy in the first band under different gain variation faults; (b) the relationship between the energy and the gain, considering the fault direction.

It should be noticed that the energy is symmetrically distributed, which is determined by the definition of residual energy. It can be solved by joint time-frequency analysis of the residual signal. Then, the energy can be redefined as:

$$E = sign(K_g - 1)(p_1K_g^2 + p_2K_g + p_3) + 2(K_g < 1) \cdot (p_1 + p_2 + p_3),$$
(9)

where  $K_g$  is the gain of the gain variation fault,  $p_1$ ,  $p_2$ ,  $p_3$  are the coefficients calculated by LSM. The result is shown in Figure 11b.

According to (9), the gains can be solved by the energy:

$$x = \frac{-p_2 + \xi(r)sqrt(p_2^2 - 4p_1p_3)}{2p_1},$$
(10)

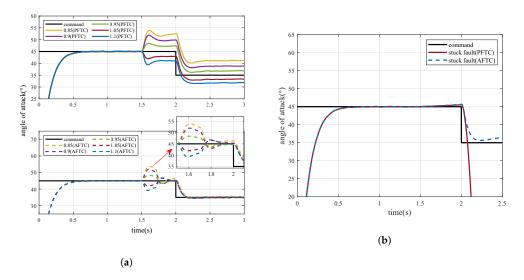
where  $\xi(r)$  is the sign of the residual signal. Above all, the fault identification with diagnosis delay less then 0.5 s is realized.

## 4.4. Simulations of AFTC

Once sensor faults occur during the flight, the fault diagnosis and identification unit generates information about the faults. According to the information, the strategy reconstruction is carried out by the AFTC proposed. The simulation results of different gain variation faults are described in Figure 11b and Table 3.

It can be seen that, when sensor faults occur, the PFTC strategy cannot counteract the wrong measurements. However, the NSHV adopted the proposed AFTC strategy can still follow the command correctly. The control command can be tracked correctly 0.4s after the fault occurs.

As the Figure 12b illustrates, under the stuck fault, the output of ESO is used as feedback to achieve security control to some extent. Compared with the PFTC strategy, the AFTC strategy has a stronger fault tolerant ability to the stuck fault. Command tracking can be maintained after the fault occurs, although it slowly diverges.



**Figure 12.** (a) Comparison of PFTC and AFTC under the gain variation faults; (b) comparison of PFTC and AFTC under the stuck fault.

Fault Size	Static Error Using PFTC (°)	Static Error Using AFTC (°)
k = 0.85	6.28	0.49
k = 0.9	3.76	-0.33
k = 0.95	1.71	-0.2
k = 1	0	0
k = 1.05	-1.82	0.14
k = 1.1	-3.31	-0.14

Table 3. Comparison of the control effects of PFTC and AFTC.

## 5. Conclusions

In this paper, a novel AFTC control strategy is proposed for NSHVs with actuator and sensor faults. An ADRC controller is adopted for command tracking and uncertainty compensation. To obtain accurate and real-time fault information, an estimation unit using ESO combined with KELM is presented. The ESO in ADRC is creatively used to generate residual signals to extract the features of different faults. Then, joint time-frequency analysis is adopted to estimate the sizes of faults. Combined ADRC with controller reconstruction strategy, AFTC is finally achieved. Actuator and sensor faults are discussed and analyzed to verify the effectiveness of the proposed reconfigurable control method. Simulation results show that the introduction of sliding window and KELM realizes real-time fault diagnosis, and the joint time-frequency analysis method makes fault identification possible. Finally, the NSHV adopted the proposed method can track the command precisely under the actuator and sensor faults. This paper provides new ideas for advanced active faulttolerant control, especially for sensor faults. **Author Contributions:** Conceptualization, J.S. and K.Z.; methodology, K.Z. and S.A.; software, K.Z.; validation, K.Z., S.A. and Y.L.; formal analysis, J.S. and X.X.; investigation, K.Z. and X.X.; resources, K.Z. and Y.L.; data curation, J.S.; writing—original draft preparation, K.Z.; writing—review and editing, K.Z.; visualization, K.Z.; supervision, J.S.; project administration, J.S.; funding acquisition, J.S. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

## Abbreviations

The following abbreviations are used in this manuscript:

AFTC	Active Fault-Tolerant Control
NSHV	Near-Space Hypersonic Vehicle
ADRC	Active Disturbance Rejection Control
KELM	Kernel Extreme Learning Machine
PFTC	Passive Fault-Tolerant Control
AFTC	Active Fault-Tolerant Control
FTC	Fault Tolerant Control
RCS	Reaction Control System
WPT	ThenWavelet Packet Transformation
ESO	Extended State Observer
TD	Tracking Differentiator
RBF	Radial Basis Function
LSM	Least Square Method
FDE	Fault Diagnosis and Evaluation
MSE	Mean Squared Error
Symbols	
x	horizontal position, m
z	vertical position, m
υ	velocity, m/s
$\gamma$	trajectory inclination angle, rad
α	angle of attack, rad
т	mass of NSHV, kg
8	gravitational acceleration, m/s <sup>2</sup>
D	aerodynamic drag, N
$T_y$	propulsion, N
Ŷ	aerodynamic force, N
$w_y$	pitch angular rate, rad/s
$I_y$	moment of inertia for the <i>y</i> coordinate axes, kg $\cdot$ m <sup>2</sup>
1	distance from the RCS to the center of mass, m
е	residual signal, rad
$z_1$	observation of the angle of attack, rad
$z_2$	observation of angular velocity of attack, rad/s
Z3	observation of total disturbance

*z*<sub>3</sub> observation of total disturbance

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$\beta_1, \beta_2, \beta_3$	tunable parameters
$a_1(k)$	estimated angle values of the current time, rad
$a_1(k+1)$	estimated angle values of the next time, rad
$a_2(k)$	derivative of $a_1(k)$ , rad/s
$a_2(k+1)$	derivative of $a_1(k+1)$ , rad/s
$a^*(k)$	desired signal, rad
$T_s$	sampling time, s
$T_c$	time constant, s
O(t)	output of sensors or actuators
$O_{f,s}$	output under the stuck fault
$O_{f,g}$	output under the gain variation fault
$O_{f,o}$	output under the outlier data fault
$t_s$	time of stuck fault occur, s
$t_g$	time of gain variation fault occur, s
$t_o$	time of outlier data fault occur, s
$K_g$	gain variation fault size
δ	outlier data fault size
$fal(\cdot)$	the fault model
0	output of ELM
т	number of neurons
β	the output weights
$g(\cdot)$	activation function
$W_i$	weights of neurons
$b_i$	biases of neurons
$X_i$	inputs of ELM
H	hidden layer's output
$H^+$	Moore-Penrose pseudoinverse of H
Т	target output
С	user-defined parameter
$K(\cdot)$	kernal function
$\alpha_{AFTC}$	Control instruction of AFTC
$\alpha(t)$	output of the sensor
$\Delta_{FDE}$	amount of compensation
$t_f$	time of fault occur
t <sub>d</sub>	time when the fault is diagnosed
$p_1, p_2, p_3$	coefficients calculated by LSM
$\xi(r)$	sign of the residual signal

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