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Impact of Newly Measured Nuclear Reaction Rates on ²⁶Al Ejected Yields from Massive Stars

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Abstract: Over the last three years, the rates of all the main nuclear reactions involving the destruction and production of 26 Al in stars (26 Al(n, p) 26 Mg, 26 Al(n, α) 23 Na, 26 Al(p, γ) 27 Si and 25 Mg(p, γ) 26 Al) have been re-evaluated thanks to new high-precision experimental measurements of their crosssections at energies of astrophysical interest, considerably reducing the uncertainties in the nuclear physics affecting their nucleosynthesis. We computed the nucleosynthetic yields ejected by the explosion of a high-mass star (20 M_{\odot} , Z = 0.0134) using the FRANEC stellar code, considering two explosion energies, 1.2×10^{51} erg and 3×10^{51} erg. We quantify the change in the ejected amount of ²⁶Al and other key species that is predicted when the new rate selection is adopted instead of the reaction rates from the STARLIB nuclear library. Additionally, the ratio of our ejected yields of ²⁶Al to those of 14 other short-lived radionuclides (36Cl, 41Ca, 53Mn, 60Fe, 92Nb, 97Tc, 98Tc, 107Pd, 126Sn, 129I, ³⁶Cs, ¹⁴⁶Sm, ¹⁸²Hf, ²⁰⁵Pb) are compared to early solar system isotopic ratios, inferred from meteorite measurements. The total ejected 26 Al yields vary by a factor of \sim 3 when adopting the new rates or the STARLIB rates. Additionally, the new nuclear reaction rates also impact the predicted abundances of short-lived radionuclides in the early solar system relative to ²⁶Al. However, it is not possible to reproduce all the short-lived radionuclide isotopic ratios with our massive star model alone, unless a second stellar source could be invoked, which must have been active in polluting the pristine solar nebula at a similar time of a core-collapse supernova.

Keywords: evolved stars; stellar evolution; stellar interiors; nucleosynthesis; supernovae



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1. Introduction

The synthesis occurring in stars (and related explosions) of the radioactive nuclide 26 Al, characterized by a half-life of 0.72 Myr, plays a pivotal role in enhancing our comprehension of the genesis of our solar system and the evolution of stars and galaxies, and is a subject of interest in both γ -ray astrophysics and cosmochemistry [1,2]. An excess of 26 Mg, the daughter isotope of 26 Al, is found in meteoritic calcium–aluminium-rich inclusions (CAIs), the first solids to form in the protosolar nebula. This observation provides evidence for the injection of live 26 Al during the early stages of the Solar System [3,4]. Consequently, unraveling the origin of 26 Al is imperative for a comprehensive understanding of the birth of the Sun and our planetary system. Additionally, the distinctive 26 Al emission of the diffuse 1809 keV line within our Galaxy, as observed by γ -ray telescopes [5], serves as a direct tracer of ongoing nucleosynthesis processes enriching the interstellar medium, with its spatial distribution

indicating that outflows from massive Wolf–Rayet stars (with masses exceeding $25\,\mathrm{M}_\odot$ [6,7]) and core-collapse supernovae are the principal loci for $^{26}\mathrm{Al}$ production [8], contributing to approximately 70% of the observed live $^{26}\mathrm{Al}$ in the Milky Way [9,10].

²⁶Al is generated during three distinct phases in the life cycle of massive stars: (i) H core burning in Wolf–Rayet stars, characterized by strong mass loss leading to the expulsion of highly ²⁶Al-enriched layers within the H convective core; (ii) explosive C/Ne burning; and (iii) C/Ne convective shell burning during pre-supernova stages. In the latter phase, the fraction of ²⁶Al that survives the subsequent explosion is ejected [11,12].

Other contributors to the presence of ²⁶Al in the Galactic environment include nova explosions [13]. Novae play a role in supplying up to 30% of the live ²⁶Al observed in the Milky Way [14,15]. Further minor sources are found in Asymptotic Giant Branch (AGB) stars, representing the concluding phase in the life cycle of low- and intermediate-mass stars [16], and Type-I X-ray bursts (assuming enough mass can actually be ejected from the accreting neutron star). In this last case, one of the main channels producing ²⁶Al is the nuclear reaction chain $^{22}{\rm Mg}(\alpha,p)^{25}{\rm Al}(\beta^+)^{25}{\rm Mg}(p,\gamma)^{26}{\rm Al}$, whose reaction rate uncertainty can significantly impact the modeled light curve shape [17]. Across all these sources, ²⁶Al is generated through the $^{25}{\rm Mg}(p,\gamma)^{26}{\rm Al}$ nuclear reaction, and it is mainly destroyed (apart from its β + decay into 26 Mg) by 26 Al $(p, \gamma)^{27}$ Si [11] and, if an efficient neutron source is available, by the neutron-induced nuclear reactions 26 Al $(n, p)^{26}$ Mg and 26 Al $(n, \alpha)^{23}$ Na [18]. The rates of all these key nuclear reactions have been re-evaluated by several authors over the last two years. Both the $^{25}{\rm Mg}(p,\gamma)^{26}{\rm Al}$ and the $^{26}{\rm Al}(p,\gamma)^{27}{\rm Si}$ nuclear reaction rates have been recently re-computed by the authors of Ref. [2], who presented a re-evaluation based on the most recent nuclear data and included the deep underground direct measurement performed by the LUNA collaboration [19]. Additionally, the 25 Mg(p, γ) 26 Al nuclear reaction was also re-studied by the authors of Ref. [20], who derived a new reaction rate based on the results of a complete experimental investigation of the 92, 130, and 189 keV resonances (interms of center of mass energy) with the Jinping Underground Nuclear Astrophysics (JUNA) lab. Finally, the authors of Ref. [21] determined a new rate for both the 26 Al $(n, p)^{26}$ Mg and 26 Al $(n, \alpha)^{23}$ Na nuclear reactions, of which they presented re-evaluations primarily based on high-precision measurements from the n_TOF-CERN facility ([22–24]), supplemented by theoretical calculations and a previous experiment [25] at higher neutron energies, to cover the full range of relevant stellar temperatures.

In this work, we re-compute the ejected nucleosynthetic yields from a $20~\rm M_{\odot}$ massive star at solar metallicity including all the new rates of the $^{25}\rm Mg(p,\gamma)^{26}Al$, $^{26}\rm Al(p,\gamma)^{27}Si$, $^{26}\rm Al(n,p)^{26}\rm Mg$ and $^{26}\rm Al(n,\alpha)^{23}\rm Na$ key nuclear reactions involving $^{26}\rm Al$. The main characteristics of our stellar models are presented in Section 2.2. We apply the new rates in the calculation of full stellar and nucleosynthesis models, quantify the impact of the new nuclear reaction rates and compare the results to key observables in Section 3. Our conclusions are presented in Section 4.

2. Computational Methods

2.1. Simulation Setup

We used the 1D stellar code FRANEC (Frascati Raphson–Newton Evolutionary Code, presented in detail in [26,27]) to calculate the hydrostatic evolution of the models presented in this work. FRANEC solves the equations describing the physical and chemical evolution of a star in hydrostatic and thermal equilibrium, assuming spherical symmetry and applying a classical Raphson–Newton method. The adopted initial composition for the solar metallicity is the one provided by Asplund, 2009 [28] and corresponds to Z = 0.01345. For the simulations, we used an extended nuclear network, already adopted in Roberti et al. [29], including 525 nuclear species extending up to Bi and more than 3000 reactions, fully coupled to the solution of the equations that describe the evolution of the star. The explosion and the associated explosive nucleosyntheses have been computed by means of the HYPERION Lagrangian hydrodynamic flux limited diffusion radiation 1D code (extensively described in [30]). HYPERION solves the full system of hydrodynamic

equations governing the supernova evolution by means of the fully Lagrangian scheme of the piecewise parabolic method (PPM), a higher-order extension of Godunov's method, described by [31]. The nuclear network used for the explosion is the same as the one used for the hydrostatic evolution of the star.

2.2. Description of the Stellar Models

To evaluate the impact of the newly measured reaction rates on ²⁶Al, we calculated the evolution of a 20 M_{\odot} star at solar metallicity adopting three different reaction rate selections for the 25 Mg $(p,\gamma)^{26}$ Al, 26 Al $(p,\gamma)^{27}$ Si, 26 Al $(n,p)^{26}$ Mg and 26 Al $(n,\alpha)^{23}$ Na nuclear reaction, as summarised in Table 1. The nuclear reaction rates adopted in the STANDARD case are the same as in [29]; in particular, the $^{25}{
m Mg}(p,\gamma)^{26}{
m Al}$ and $^{26}{
m Al}(p,\gamma)^{27}{
m Si}$ reaction rates are both from [32], while the 26 Al $(n, p)^{26}$ Mg and 26 Al $(n, \alpha)^{23}$ Na reaction rates are from [33,34], respectively. In the LA-BA case abbreviation for "LAIRD-BATTINO"), the 26 Al $(n, p)^{26}$ Mg and 26 Al $(n,\alpha)^{23}$ Na reaction rates are both from [21], while the 25 Mg $(p,\gamma)^{26}$ Al and 26 Al $(p,\gamma)^{27}$ Si reaction rates are both from [2]. Most importantly, we extended both rates beyond 0.7 GK (the highest temperature provided by [2]) using the RATESMC code [32], including higher energy resonances beyond 484 keV based on the information presented in [32]. Our new high-temperature rates are presented in Tables 2-4. Finally, in the JU-LA-BA case (abbreviation for "JUNA-LAIRD-BATTINO") the reaction rates adopted are the same as in the LA-BA case, with the only exception of the $^{25}{\rm Mg}(p,\gamma)^{26}{\rm Al}$ reaction rate which is taken from [20]. Note that we do not attempt any extrapolation of the reaction rate in all the cases where the temperature grid is not extending up to 10 GK, but instead we adopt the value of the last available experimental point.

Table 1. Schematic view of the references adopted for the three reaction rate selections presented in this work.

Nuclear Reaction	STANDARD	JU-LA-BA	LA-BA
25 Mg(p, γ) 26 Al	Iliadis et al., 2010 [32]	Zhang et al., 2023 [20]	Laird et al., 2023 [2]
26 Al $(p,\gamma)^{27}$ Si	Iliadis et al., 2010 [32]	Laird et al., 2023 [2]	Laird et al., 2023 [2]
26 Al $(n,p)^{26}$ Mg	Caughlan & Fowler 1988 [33]	Battino et al., 2023 [21]	Battino et al., 2023 [21]
26 Al $(n,\alpha)^{23}$ Na	Angulo et al., 1999 [34]	Battino et al., 2023 [21]	Battino et al., 2023 [21]

Table 2. 25 Mg(p, γ) 26 Al reaction rates for temperatures higher than 0.7 GK on the ground state of 26 Al in units of [cm³/mol s].

T[GK]	Lower Limit	Median Rate	Upper Limit
0.700	1.027×10^{2}	1.078×10^{2}	1.136×10^{2}
0.800	1.933×10^{2}	2.022×10^{2}	2.121×10^{2}
0.900	3.195×10^{2}	3.333×10^{2}	3.488×10^{2}
1.000	4.810×10^{2}	5.011×10^2	5.240×10^{2}
1.250	1.026×10^{3}	1.068×10^{3}	1.118×10^{3}
1.500	1.740×10^{3}	1.811×10^{3}	1.897×10^{3}
1.750	2.586×10^{3}	2.689×10^{3}	2.815×10^{3}
2.000	3.532×10^{3}	3.667×10^{3}	3.831×10^{3}
2.500	5.615×10^{3}	5.809×10^{3}	6.039×10^{3}
3.000	7.804×10^{3}	8.047×10^{3}	8.329×10^{3}
3.500	9.946×10^{3}	1.023×10^4	1.055×10^{4}
4.000	1.193×10^{4}	1.225×10^4	1.261×10^{4}
5.000	1.520×10^4	1.559×10^4	1.600×10^{4}
6.000	1.748×10^{4}	1.792×10^{4}	1.839×10^{4}
7.000	1.890×10^{4}	1.938×10^{4}	1.989×10^{4}
8.000	1.966×10^{4}	2.017×10^{4}	2.071×10^{4}
9.000	1.994×10^{4}	2.047×10^4	2.103×10^{4}
10.000	1.989×10^{4}	2.043×10^{4}	2.100×10^{4}

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Table 3. 25 Mg(p, γ) 26 Al reaction rates for temperatures higher than 0.7 GK on the isomeric state of 26 Al in units of [cm 3 /mol s].

T[GK]	Lower Limit	Median Rate	Upper Limit
0.700	2.887×10^{1}	3.054×10^{1}	3.237×10^{1}
0.800	5.899×10^{1}	6.232×10^{1}	6.610×10^{1}
0.900	1.043×10^{2}	1.102×10^{2}	1.171×10^{2}
1.000	1.661×10^{2}	1.756×10^{2}	1.870×10^{2}
1.250	3.944×10^{2}	4.169×10^{2}	4.451×10^{2}
1.500	7.198×10^{2}	7.593×10^{2}	8.101×10^{2}
1.750	1.125×10^{3}	1.183×10^{3}	1.259×10^{3}
2.000	1.592×10^{3}	1.668×10^{3}	1.767×10^{3}
2.500	2.631×10^{3}	2.741×10^{3}	2.881×10^{3}
3.000	3.705×10^{3}	3.843×10^{3}	4.016×10^{3}
3.500	4.720×10^{3}	4.883×10^{3}	5.079×10^{3}
4.000	5.626×10^{3}	5.807×10^{3}	6.020×10^{3}
5.000	7.033×10^3	7.240×10^{3}	7.474×10^{3}
6.000	7.930×10^{3}	8.154×10^{3}	8.400×10^{3}
7.000	8.428×10^{3}	8.660×10^{3}	8.910×10^{3}
8.000	8.641×10^{3}	8.873×10^{3}	9.124×10^{3}
9.000	8.660×10^{3}	8.890×10^{3}	9.135×10^{3}
10.000	8.550×10^{3}	8.776×10^{3}	9.015×10^{3}

Table 4. 26 Al(p, γ) 27 Si reaction rates for temperatures higher than 0.7 GK on the ground state of 26 Al in units of [cm 3 /mol s].

T[GK]	Lower Limit	Median Rate	Upper Limit
0.700	4.640×10^{1}	5.050×10^{1}	5.500×10^{1}
0.800	8.020×10^{1}	8.730×10^{1}	9.520×10^{1}
0.900	1.220×10^{2}	1.330×10^{2}	1.450×10^{2}
1.000	1.710×10^{2}	1.860×10^{2}	2.020×10^{2}
1.250	3.170×10^{2}	3.420×10^{2}	3.700×10^{2}
1.500	4.880×10^{2}	5.230×10^{2}	5.610×10^{2}
1.750	6.730×10^{2}	7.160×10^{2}	7.640×10^{2}
2.000	8.600×10^{2}	9.120×10^{2}	9.680×10^{2}
2.500	1.210×10^{3}	1.280×10^{3}	1.350×10^{3}
3.000	1.500×10^{3}	1.580×10^{3}	1.670×10^{3}
3.500	1.720×10^{3}	1.820×10^{3}	1.920×10^{3}
4.000	1.880×10^{3}	1.990×10^{3}	2.100×10^{3}
5.000	2.040×10^{3}	2.160×10^{3}	2.300×10^{3}
6.000	2.050×10^{3}	2.170×10^{3}	2.320×10^{3}
7.000	1.960×10^{3}	2.080×10^{3}	2.210×10^{3}
8.000	1.830×10^{3}	1.930×10^{3}	2.050×10^{3}
9.000	1.680×10^{3}	1.780×10^{3}	1.880×10^{3}
10.000	1.550×10^{3}	1.630×10^{3}	1.730×10^{3}

In this work, we focused on non-magnetic and non-rotating massive star models simulations, as we plan to extend our analysis to rotating models in a follow-up study. The physics inputs and assumptions are the same as used in [27,29]; in the following, we briefly recall the main relevant features. The convective zones are treated using the mixing length theory (MLT), and their borders are defined according to the Ledoux criterion in H-burning regions and to the Schwarzschild criterion elsewhere. Semiconvection is taken into account, as discussed in [35]. The MLT and semiconvection parameters are $\alpha_{\text{MLT}} = 2.1$ and $\alpha_{\text{semi}} = 0.02$, respectively. The convective boundary mixing (CBM), implemented as 0.2 H_{P} of overshooting, is considered only at the edge of the H convective core during the main sequence (MS). Mass loss has been included following the prescriptions of [36,37] for the Blue Super Giant (BSG) phase, [38,39] for the Red Super Giant (RSG) phase, and [40]

for the Wolf-Rayet phase (WR). We also included the dynamical mass loss caused by the approach of the luminosity of the star to the Eddington limit by removing all the zones where the Eddington factor $\Gamma = L_{\rm rad}/L_{\rm EDD} > 1$. The explosion is triggered through a thermal bomb, i.e., by depositing a certain amount of thermal energy at the edge of the Fe core in the pre-supernova model. The injected energy is such that to achieve a final kinetic energy of the ejecta (measured at infinity) of 1.2×10^{51} erg, the typical kinetic energy assumed for SN 1987A and widely used in the literature [41-44] is employed. The final mass-cut (that defines the remnant mass) is determined by the total amount of fallback $\sim 10^7$ s after the core-collapse and corresponds to 2.58 M_{\odot} , in agreement with other 20 M_{\odot} CCSN models available in literature [12,45,46]. We calculate an additional CCSN model, imposing a final kinetic energy of 3×10^{51} erg, to study the effect of a more energetic explosion on the production of ²⁶Al. In this case, the explosion energy is high enough to completely eject all the layers above the Fe core. The mass-cut is therefore chosen so that the ejecta contain 0.07 M_{\odot} of ⁵⁶Ni, to match the amount of ⁵⁶Ni estimated from SN 1987A, and it is 1.86 M_{\odot} . Finally, we did not include any "mixing and fall back" prescriptions in any of our CCSN simulations (see, e.g., [47,48]). A summary of the main properties of the reference model is reported in Table 5. The final structure is instead shown in Figure 1. We remind the reader that the explosive nucleosynthesis depends only on the temperature and density in the post-shock zones, and we use the following definition (e.g., [49–51]):

- Complete Si burning (Si_c): $T_{\text{shock}} > 5 \text{ GK}$;
- Incomplete Si burning (Si_i): $5 \text{ GK} > T_{\text{shock}} > 4 \text{ GK}$;
- Explosive O burning (O): $4 \text{ GK} > T_{\text{shock}} > 3.3 \text{ GK}$;
- Explosive Ne burning (Ne): $3.3 \text{ GK} > T_{\text{shock}} > 2.1 \text{ GK}$;
- Explosive C burning (C): $2.1 \text{ GK} > T_{\text{shock}} > 1.9 \text{ GK}$.

Table 5. Summary of the key characteristics of the presupernova (PSN) and explosive models presented in this work.

Mass-loss scheme	Vink [36,37], de Jaeger [38] , Nugis [40], van Loon [39]	
Convection criteria	Ledoux in H burning zones, Schwarzschild elsewhere	
$lpha_{ m MLT}$	2.1	
$lpha_{ m semi}$	0.02	
CBM	$0.2 H_{\rm P}$ of overshooting (H burning)	
Initial mass	$20~M_{\odot}$	
Initial metallicity	1.345×10^{-2} (Asplund 2009 [28])	
Initial H mass fraction	0.721	
Initial ⁴ He mass fraction	0.265	
¹² C mass fraction (He exhaustion)	0.286	
CO core (He exhaustion)	$4.91~M_{\odot}$	
Lifetime (PSN)	9.87 Myr	
Total Mass (PSN)	$7.46~\dot{M_{\odot}}$	
$\log T_{\rm eff}$ (PSN)	4.30	
$\log L/L_{\odot}$ (PSN)	5.31	
Explosion scheme	Thermal bomb [30]	
Thermal energy injected	2.61×10^{51} erg, 4.41×10^{51} erg	
Explosion energy (at infinity)	1.20×10^{51} erg, 3.00×10^{51} erg	
Remnant mass	$2.58~M_{\odot}$, $1.86~M_{\odot}$	

 26 Al in CCSNe is usually produced between explosive Ne and C zones. In our models, 26 Al is synthesized at temperatures between 2.60 and 1.74 GK. It is clearly visible in Figure 2, which shows the 25 Mg(p, γ) 26 Al nuclear reaction rate ratio between [2,20], how, in this temperature range, the rate from [2] is very close to the rate from [20], while it is between two and three factors lower at the lowest temperatures. This is mainly due to the shifted resonance energy computed when taking the atomic binding into account, as described in [2], while this effect was not included by [20].

Below $T_{\rm shock} = 1.9$ GK, the temperature is too low on the typical explosion timescale (\sim 1 s) to activate other major explosive burning stages, and therefore, the matter is ejected without any further reprocessing. However, some secondary processes may still occur, such as the neutron burst in the He shell, required to explain Mo and Zr anomalies in pre-solar silicon carbide grains [52].

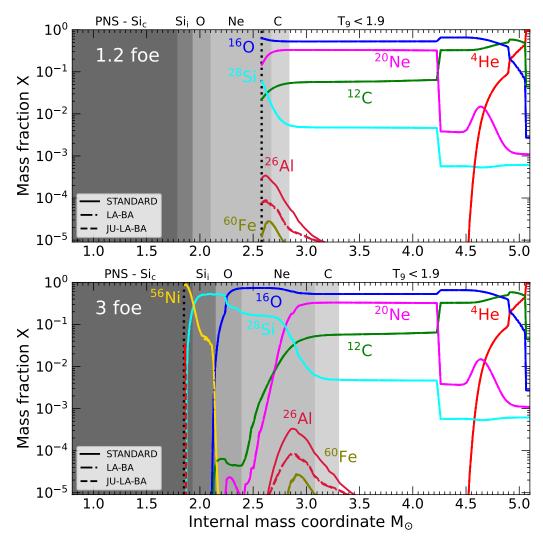


Figure 1. Abundances in mass fraction of key nuclear species as a function of the internal mass coordinate in the CCSN models exploding with 1.2×10^{51} erg (**upper** panel) and 3×10^{51} erg (**lower** panel). The gray shaded areas represent each explosive burning stage (see text); the vertical dotted line identifies the location of the mass-cut. The zone below the mass-cut contains the proto-neutron star (PNS), plus the fallback of the zone exposed to the explosive nucleosynthesis, depending on the explosion energy.

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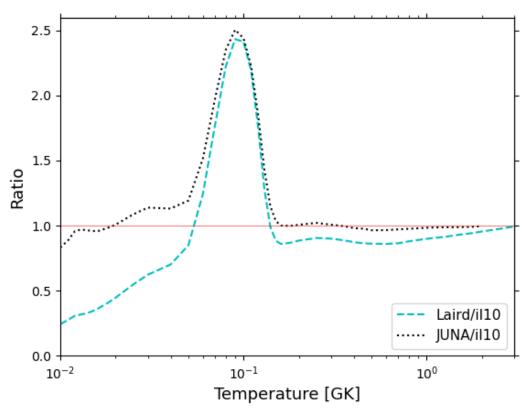


Figure 2. Comparison of [2,20] vs. [32] 25 Mg(p, γ) 26 Al nuclear reaction rate ratio as a function of temperature.

3. Results

3.1. Impact of New Nuclear Reaction Rates on the Ejected Yields

We re-computed the complete nucleosynthesis fully coupled to the structural evolution of our massive star model, using the three network settings described in Section 2.2. The resulting ejected yields for Ne, Na, Mg, Al and Si stable isotopes and ²⁶Al and ⁶⁰Fe (i.e., the species most affected by the newly measured reaction rates we test in this work) are presented in Table 6. Only minor differences are present between the LA-BA and JU-LA-BA cases. Indeed, the total rate of the 25 Mg(p, γ) 26 Al between 2.60 and 1.74 GK from Laird et al., 2023 [2] is very close to the rate from JUNA [20], differing on average by about 4%. Since the only difference between the JU-LA-BA and LA-BA cases is the different 25 Mg(p, γ) 26 Al reaction rate, this causes the small difference of the same order between the two cases in the final ²⁶Al abundance, being 4% lower in LA-BA compared to JU-LA-BA. Larger differences are instead present between the STANDARD case and both the JU-LA-BA and LA-BA cases, due to the different 26 Al $(n, \alpha)^{23}$ Na and 26 Al $(n, p)^{26}$ Mg reaction rates adopted. In particular, the ²⁶Al ejected yields change by a factor between 2 and 3 depending on the explosion energy. This is consistent with the results of [21], who noticed how the final abundance of ²⁶Al produced in their supernova simulations was about a factor of 2 lower when their 26 Al $(n,\alpha)^{23}$ Na and 26 Al $(n,p)^{26}$ Mg reaction rates were adopted (as in JU-LA-BA and LA-BA) instead of those from [33,34] (as in STANDARD).

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Table 6. Total explosive ejected yields (in M_{\odot}) of ²⁶Al and other key species of our models for different selections of nuclear reaction rates (see main text for more details).

Species	STANDARD	JU-LA-BA	LA-BA
	$1.2 imes 10^{51} ext{ erg}$		
²⁰ Ne	5.60×10^{-1}	5.60×10^{-1}	5.60×10^{-1}
²³ Na	1.07×10^{-2}	1.07×10^{-2}	1.07×10^{-2}
$^{24}{ m Mg}$	9.32×10^{-2}	9.32×10^{-2}	9.33×10^{-2}
25 Mg	1.66×10^{-2}	1.66×10^{-2}	1.66×10^{-2}
$^{26}\mathrm{Mg}$	1.65×10^{-2}	1.65×10^{-2}	1.65×10^{-2}
²⁶ Al	7.02×10^{-5}	2.75×10^{-5}	2.65×10^{-5}
²⁷ Al	1.14×10^{-2}	1.13×10^{-2}	$1.14 imes 10^{-2}$
²⁸ Si	2.13×10^{-2}	2.14×10^{-2}	2.13×10^{-2}
²⁹ Si	3.17×10^{-3}	3.17×10^{-3}	3.18×10^{-3}
$^{30}\mathrm{Si}$	1.96×10^{-3}	1.94×10^{-3}	1.95×10^{-3}
⁶⁰ Fe	1.19×10^{-5}	1.19×10^{-5}	1.17×10^{-5}
	$3 imes 10^{51} \mathrm{erg}$		
²⁰ Ne	4.79×10^{-1}	4.79×10^{-1}	4.79×10^{-1}
²³ Na	8.80×10^{-3}	8.79×10^{-3}	8.79×10^{-3}
$^{24}{ m Mg}$	9.81×10^{-2}	9.78×10^{-2}	9.82×10^{-2}
$^{25}\mathrm{Mg}$	1.44×10^{-2}	1.44×10^{-2}	1.44×10^{-2}
$^{26}\mathrm{Mg}$	1.44×10^{-2}	1.44×10^{-2}	1.44×10^{-2}
²⁶ Al	9.68×10^{-5}	3.36×10^{-5}	3.26×10^{-5}
²⁷ Al	1.20×10^{-2}	1.19×10^{-2}	1.20×10^{-2}
28 Si	2.82×10^{-1}	2.82×10^{-1}	2.82×10^{-1}
²⁹ Si	4.99×10^{-3}	5.03×10^{-3}	5.03×10^{-3}
$^{30}\mathrm{Si}$	6.94×10^{-3}	6.88×10^{-3}	6.89×10^{-3}
⁶⁰ Fe	1.14×10^{-5}	1.14×10^{-5}	1.12×10^{-5}

3.2. Comparison to Ess Ratios

The early Solar System (ESS) was enriched in short-lived radionuclides (SLRs, with half-lives ranging between 0.1 and 100 Myr) at the time of its formation 4.6 Gyrs ago [4]. This evidence is gleaned from the examination of meteorite compositions, wherein excesses of daughter isotopes originating from radioactive nuclei are detected. While the majority of SLRs possess half-lives long enough (exceeding approximately 2 Myr) to be adequately explained by their production in the Galaxy [53], isotopes with shorter half-lives (such as ²⁶Al, ³⁶Cl and ⁴¹Ca) defy explanation through galactic chemical evolution (GCE) processes alone. Consequently, the presence and abundance of these isotopes necessitate one or more additional local stellar sources, potentially originating from the same molecular cloud as the Sun. These local sources would have directly enriched the protosolar nebula from which the Sun formed or the pre-existing proto-planetary disk (for comprehensive reviews of various scenarios, see, e.g., [4]).

We compared the yields of each of our stellar model to ESS abundances, as outlined in [4] and Lawson et al. (in prep). In order to probe the formation of the Solar System, we consider isotopes that have half-lives comparable to the time frame of the formation of the Solar System from its molecular cloud (approx. 15 Myrs, [54]), and compare their abundances with the ejected yields from our models. The aim is to test the hypothesis that a core-collapse supernova event could have produced all the SLRs in the proportion needed to reproduce their ESS abundances measured in calcium—aluminium-rich inclusions (CAIs, the first solids to have formed in the protosolar nebula), hence shaping the environment for the birth of the Sun. SLR daughter and reference signatures can be detected in meteoritic samples and are further used to estimate the abundances of SLRs in the ESS [4,55]. A list of these SLRs, daughter isotopes, reference isotopes, half-lives, mean lifetime and ESS abundance ratios can be found in Table 7. The nucleosynthesis of the SLRs in both massive star and CCSN are detailed in [12].

In order to calculate the contribution of ejecta from a model to the ESS, we must take into account the effect of dilution and radioactive decay. We can calculate a dilution factor (f) for each model, defined by

$$f = \frac{M_{SLR}^{ESS}}{M_{SLR}^*} \tag{1}$$

Here, M_{SLR}^{ESS} is the observed abundance of a reference SLR and M_{SLR}^* is the total ejected mass of the SLR from the model.

Table 7. The full list of SLRs considered in this work, listed with reference isotopes, $T_{1/2}$, τ , and ESS ratios. Data gathered from [4]. If no error is given, the value is an upper limit.

SLR	Daughter	Reference	T _{1/2} (yr)	τ (yr)	ESS Ratio
²⁶ Al	²⁶ Mg	²⁷ Al	7.170×10^{5}	1.034×10^{6}	$(5.23 \pm 0.13) \times 10^{-5}$
³⁶ Cl	36 S	³⁵ Cl	3.010×10^{5}	4.343×10^{5}	$(2.44 \pm 0.65) \times 10^{-5}$
⁴¹ Ca	$^{41}\mathrm{K}$	40 Ca	9.940×10^{4}	1.434×10^{5}	$(4.6 \pm 1.9) \times 10^{-9}$
53 Mn	⁵³ Cr	⁵⁵ Mn	3.740×10^{6}	5.396×10^{6}	$(7 \pm 1) \times 10^{-6}$
⁶⁰ Fe	$^{60}\mathrm{Ni}$	⁵⁶ Fe	2.620×10^{6}	3.780×10^{6}	$(1.01 \pm 0.27) \times 10^{-8}$
⁹² Nb	$^{92}\mathrm{Zr}$	⁹² Mo	3.470×10^{7}	5.006×10^{7}	$(3.2 \pm 0.3) \times 10^{-5}$
⁹⁷ Tc	⁹⁷ Mo	98 Ru	4.210×10^{6}	6.074×10^{6}	$< 1.1 \times 10^{-5}$
⁹⁸ Tc	⁹⁸ Ru	98 Ru	4.200×10^{6}	6.059×10^{6}	$< 6 \times 10^{-5}$
¹⁰⁷ Pd	107 Ag	¹⁰⁸ Pd	6.500×10^{6}	9.378×10^{6}	$(6.6 \pm 0.4) \times 10^{-5}$
¹²⁶ Sn	¹²⁶ Te	¹²⁴ Sn	2.300×10^{5}	3.318×10^{5}	$< 3 \times 10^{-6}$
$^{129}{ m I}$	¹²⁹ Xe	$^{127}\mathrm{I}$	1.570×10^{7}	2.265×10^{7}	$(1.28 \pm 0.03) \times 10^{-4}$
^{135}Cs	¹³⁵ Ba	¹³³ Cs	2.300×10^{6}	3.318×10^{6}	$< 2.8 \times 10^{-6}$
146 Sm	¹⁴² Nd	144 Sm	6.800×10^{7}	9.810×10^{7}	$(8.28 \pm 0.44) \times 10^{-3}$
¹⁸² Hf	^{182}W	$^{180}{ m Hf}$	8.900×10^{6}	1.284×10^{7}	$(1.018 \pm 0.043) \times 10^{-4}$
²⁰⁵ Pb	²⁰⁵ Tl	²⁰⁴ Pb	1.730×10^7	2.496×10^{7}	$(1.8 \pm 1.2) \times 10^{-3}$

We use 26 Al to define the f for each model ejecta, as the 26 Al/ 27 Al ratio is very well established [56,57]. A time delay is then applied to the ejecta to account for the time between the ejection of the SLRs by the stellar source and its incorporation into the CAIs. The decrease in the abundance of the radioactive species is then calculated using the radioactive decay equation

$$M_{SLR}(t) = M_{SLR}(t_0)e^{-\frac{ln(2)\Delta t}{T_{1/2}}}$$
 (2)

In this equation, the initial mass of the isotope $(M_{SLR}(t_0))$ is decayed by the half-life of the SLR $(T_{1/2})$. This provides the final decayed abundance of the ejecta $(M_{SLR}(t))$ after a time delay.

The SLR yields of each model are decayed using a time delay of 2.5 Myr. This is a good representative value [4], determined by examining the decay profiles of each SLR (with a dilution f calculated using 26 Al, Lawson et al. in prep).

In Figure 3, we present the ESS abundance predicted by our 1.2×10^{51} erg explosive model for each SLR once decayed using Equation (2) and diluted using 26 Al to calculate f. In order to fully replicate the ESS abundances, each isotope should lie on (or potentially below) the dashed threshold line. Any SLR above this threshold are overproduced and require an additional 26 Al source. SLRs below the threshold may be polluted by an additional event or through galactic chemical evolution (GCE) contributions. We separate the top and bottom panels of Figure 3 into isotopes with lower/equal and greater half-lives than 60 Fe, respectively. Isotopes in the top panel have the shortest half-lives, and therefore, their ratio to 26 Al should ideally lie very close to the ESS value, since there would not be enough time for GCE to fill the gap in case of very low values (which can instead play a role for the longer-lived isotopes in the bottom panel). The models presented in this work are plotted as single points (a blue diamond for the standard model, blue hexagon

for JU-LA-BA and a red star for LA-BA) and are compared to the 23 models with initial mass 20 M_{\odot} of [12] (covering an explosion range of 0.53–8.86 \times 10 51 erg and remnant mass range of 1.74–3.40 M_{\odot}), which are plotted as box-plots and represent the impact of different stellar physics inputs. As the LA-BA and JU-LA-BA models have less 26 Al, they have an increased $M_{\rm model}/M_{\rm ESS}$ across all isotopes.

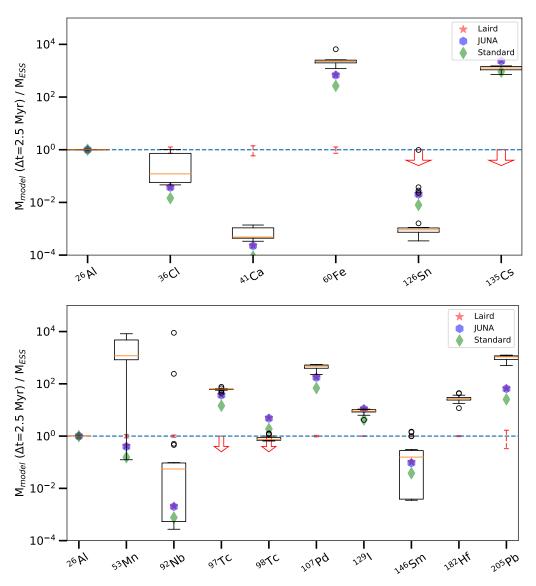


Figure 3. Ratio of decayed model ejecta, M_{model} , and ESS observation, M_{ESS} , for each isotope examined. Within these figures, the horizontal dashed line represents the threshold value of 1. The red error bars represent the error in the ESS ratio of the SLR in question; if the ESS ratio is given as an upper limit, a downward arrow is used. The isolation time for each model is given in the x-axis label as Δt , and f is calculated using 26 Al. Box-plots in these plots are the $20~M_{\odot}$ ejecta of [12]. The upper panel shows isotopes with $T_{1/2} \leq 2.620 \times 10^6~\rm yr$ (the $T_{1/2}$ of 60 Fe), and the lower panel shows isotopes with $T_{1/2} \geq 2.620 \times 10^6~\rm yr$. In line with the definition of a box-plot, the box size shows the range of values between the 25th and the 75th percentile of all the models in the dataset. The error bars on the box-plot denote the lower (upper) quartiles and are given by subtracting (adding) to the position of the 25th (75th) percentile 1.5 times the interquartile range (i.e., the box size). All values above (below) these thresholds are plotted as outliers. Outlying models outside the outer quartiles are shown as small circles for both decayed and undecayed results, using the same colour scheme as the boxes.

Starting with the isotopes with half-lives less than 2.62 Myr (the $T_{1/2}$ of 60 Fe, top panel of Figure 3), 36 Cl is underproduced in the stellar models presented in this work. However, considering the range of 36 Cl/ 26 Al covered by [12] models, it might be in agreement with the observed ESS values if different explosion energies are considered. 41 Ca and 126 Sn are both underproduced, even considering different stellar physics inputs. A similar case is represented by 60 Fe and 135 Cs, which are overproduced in both our models and in those by [12]. Considering the isotopes with half-lives longer than 2.62 Myr (bottom panel of Figure 3), 53 Mn, and 98 Tc are in agreement within nuclear and stellar uncertainties with their ESS values, while 92 Nb and 146 Sm are underproduced, but could be brought into agreement with ESS values by GCE contributions. On the other hand, 97 Tc, 107 Pd, 129 I, 182 Hf and 205 Pb are all overproduced.

Therefore, we notice how, even considering the most recent and up-to-date nuclear physics input, only 5 out of the 14 SLRs considered here are consistent with their observed ESS values. Two potential solutions could be represented by either a different astrophysical scenario that is able to perform better against observations, or an additional pollution event producing more 26 Al and less of the overproduced SLRs (such as 60 Fe) that happened close in time (within about 2.5 Myr) and space to a core-collapse supernova.

4. Conclusions

In this work, we computed the evolution of a high-mass star ($20 \, {\rm M}_{\odot}$, Z = 0.01345) and the nucleosynthetic yields ejected by its explosion at two different energies, 1.2×10^{51} erg and 3×10^{51} erg. We included all the updated rates of the relevant nuclear reactions for 26 Al nucleosynthesis, i.e., 26 Al(n, p) 26 Mg, 26 Al(n, α) 23 Na, 26 Al(p, γ) 27 Si and 25 Mg(p, γ) 26 Al.

We found a substantial decrease in the ejected amount of 26 Al in the JU-LA-BA and LA-BA cases, between a factor of two and three, compared to the STANDARD case. This is consistent with the impact of the newest 26 Al(n, α) 23 Na and 26 Al(n, p) 26 Mg reaction rates found by [21].

We then compared the ejected yields of our models for 14 SLRs (36 Cl, 41 Ca, 53 Mn, 60 Fe, 92 Nb, 97 Tc, 98 Tc, 107 Pd, 126 Sn, 129 I, 36 Cs, 146 Sm, 182 Hf, 205 Pb) with their abundances in the ESS, in order to check if a core-collapse supernova could represent a realistic scenario for the circumstances and the environment of the birth of the Sun. Only 5 out of the 14 SLRs are consistent with their observed ESS abundances. At least two potential solutions should be considered: (1) A different astrophysical scenario that is able to perform better against observations. One possibility may be represented by rotating Wolf–Rayet stars, where the rotation-enhanced mass loss may limit the amount of hydrogen to be converted into 14 N during the core H-burning phase and hence the amount of neutrons released by the 22 Ne(α , n) 25 Mg during the He-burning phase (since 22 Ne is produced by a sequence of α -captures on 14 N). This may therefore limit the production of n-capture SLRs like 60 Fe and 135 Cs. (2) An additional pollution event producing more 26 Al and less of the overproduced SLRs (such as 60 Fe) that happened close in time (within about 2.5 Myr) and space to a core-collapse supernova.

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References

1. Diehl, R.; Lugaro, M.; Heger, A.; Sieverding, A.; Tang, X.; Li, K.A.; Li, E.T.; Doherty, C.L.; Krause, M.G.H.; Wallner, A.; et al. The radioactive nuclei ²⁶Al and ⁶⁰Fe in the Cosmos and in the solar system. *Publ. Astron. Soc. Aust.* **2021**, *38*, e062. [CrossRef]

- 2. Laird, A.M.; Lugaro, M.; Kankainen, A.; Adsley, P.; Bardayan, D.W.; Brinkman, H.E.; Côté, B.; Deibel, C.M.; Diehl, R.; Hammache, F.; et al. Progress on nuclear reaction rates affecting the stellar production of ²⁶ Al. *J. Phys. Nucl. Phys.* **2023**, *50*, 033002. [CrossRef]
- 3. Diehl, R.; Halloin, H.; Kretschmer, K.; Lichti, G.G.; Schönfelder, V.; Strong, A.W.; von Kienlin, A.; Wang, W.; Jean, P.; Knödlseder, J.; et al. COMPTEL observations of galactic ²⁶Al emission. *Nature* **2006**, 439, 45. [CrossRef] [PubMed]
- 4. Lugaro, M.; Ott, U.; Kereszturi, Á. Radioactive nuclei from cosmochronology to habitability. *Prog. Part. Nucl. Phys.* **2018**, 102, 1–47. [CrossRef]
- 5. Diehl, R.; Steinle, H.; Strong, A.; Schoenfelder, V.; Varendorff, M.; Bennett, K.; Lichti, G.G.; Blömen, H.; Dupraz, C.; Hermsen, W.; et al. COMPTEL observations of Galactic ²⁶Al emission. *Astron. Astrophys.* **1995**, 298, 445.
- 6. Georgy, C.; Ekström, S.; Meynet, G.; Lichti, G.G.; Schönfelder, V.; Strong, A.W.; von Kienlin, A.; Wang, W.; Jean, P.; Knödlseder, J.; et al. Radioactive ²⁶Al from massive stars in the Galaxy. *Nature* **2012**, *542*, A29. [CrossRef]
- 7. Brinkman, H.E.; Doherty, C.L.; Pols, O.R.; Li, E.T.; Côté, B.; Lugaro, M. Aluminium-26 from Massive Binary Stars. I. Nonrotating Models. *Astrophys. J.* **2019**, *884*, 38. [CrossRef]
- 8. Prantzos, N.; Doom, C.; de Loore, C.; Arnould, M. Nucleosynthesis and evolution of massive stars with mass loss and overshooting. *Astrophys. J.* **1986**, *304*, 695. [CrossRef]
- 9. Palacios, A.; Meynet, G.; Vuissoz, C.; Knödlseder, J.; Schaerer, D.; Cerviño, M.; Mowlavi, N. New estimates of the contribution of Wolf-Rayet stellar winds to the Galactic ²⁶Al. *Anesth. Analg.* **2005**, 429, 613.:20041757. [CrossRef]
- 10. Vasini, A.; Matteucci, F.; Spitoni, E. Chemical evolution of ²⁶Al and 60Fe in the Milky Way. *Mon. Not. R. Astron. Soc.* **2022**, 517, 4256–4264. [CrossRef]
- 11. Limongi, M.; Chieffi, A. The Nucleosynthesis of ²⁶Al and60Fe in Solar Metallicity Stars Extending in Mass from 11 to 120M_☉: The Hydrostatic and Explosive Contributions. *Astrophys. J.* **2006**, *647*, 483. [CrossRef]
- 12. Lawson, T.V.; Pignatari, M.; Stancliffe, R.J.; Hartogh, J.D.; Jones, S.; Fryer, C.L.; Gibson, B.K.; Lugaro, M. Radioactive nuclei in the early Solar system: Analysis of the 15 isotopes produced by core-collapse supernovae. *Mon. Not. R. Astron. Soc.* **2022**, *511*, 886. [CrossRef]
- 13. José, J.; Hernanz, M.; Coc, A. New Results on ²⁶Al Production in Classical Novae. Astrophys. J. 1997, 479, L55. [CrossRef]
- 14. Guélin, M.; Forestini, M.; Valiron, P.; Ziurys, L.M.; Anderson, M.A.; Cernicharo, J.; Kahane, C. Nucleosynthesis in AGB stars: Observation of ²⁵Mg and ²⁶Mg in IRC+10216 and possible detection of ²⁶Al. A*Stronomy Astrophys.* **1995**, 297, 183–196.
- 15. Bennett, M.B.; Wrede, C.; Chipps, K.A.; José, J.; Liddick, S.N.; Santia, M.; Bowe, A.; Chen, A.A.; Cooper, N.; Irvine, D.; et al. Classical-Nova Contribution to the Milky Way's 26 Al Abundance: Exit Channel of the Key 25 Al(p, γ) 26 Si Resonance. *Phys. Rev. Lett.* **2013**, *111*, 232503. [CrossRef]
- 16. Forestini, M.; Arnould, M.; Paulus, G. On the production of Al-26 in AGB stars. Astron. Astrophys. 1991, 252, 597-604.
- 17. Meisel, Z.; Merz, G.; Medvid, S. Influence of Nuclear Reaction Rate Uncertainties on Neutron Star Properties Extracted from X-ray Burst Model–Observation Comparisons. *Astrophys. J.* **2019**, *872*, 84. [CrossRef]
- 18. Iliadis, C.; Champagne, A.; Chieffi, A.; Limongi, M. The effects of thermonuclear reaction rate variations on ²⁶Al production in massive stars: A sensitivity study. *Astrophys. J.* **2011**, *193*, 16. [CrossRef]
- 19. Straniero, O.; Imbriani, G.; Strieder, F.; Bemmerer, D.; Broggini, C.; Caciolli, A.; Corvisiero, P.; Costantini, H.; Cristallo, S.; DiLeva, A.; et al. Impact of a revised $25mg(p,\gamma)^{26}$ Al reaction rate on the operation of the Mg-Al cycle. *Astrophys. J.* **2013**, 763, 100. [CrossRef]
- 20. Zhang, H.; Su, J.; Li, Z.H.; Li, Y.J.; Li, E.T.; Chen, C.; He, J.J.; Shen, Y.P.; Lian, G.; Guo, B.; et al. Updated reaction rate of Mg25(p,γ)Al26 and its astrophysical implication. *Phys. Rev. C* **2023**, *107*, 065801. [CrossRef]
- 21. Battino, U.; Lederer-Woods, C.; Pignatari, M.; Soós, B.; Lugaro, M.; Vescovi, D.; Cristallo, S.; Woods, P.J.; Karakas, A. Impact of newly measured ²⁶Al(n, p)26Mg and ²⁶Al(n, α)23Na reaction rates on the nucleosynthesis of ²⁶Al in stars. *Mon. Not. R. Astron. Soc.* **2023**, *520*, 2436. [CrossRef]
- 22. Borcea, C.; Cennini, P.; Dahlfors, M.; Ferrari, A.; Garcia-Muñoz, G.; Haefner, P.; Herrera-Martinez, A.; Kadi, Y.; Lacoste, V.; Radermacher, E.; et al. Results from the commissioning of the n_TOF spallation neutron source at CERN. *Nucl. Instruments Methods Phys. Res. A* 2003, 513, 524–537. [CrossRef]
- 23. Lederer-Woods, C.; Battino, U.; Ferreira, P.; Gawlik, A.; Guerrero, C.; Gunsing, F.; Heinitz, S.; Lerendegui-Marco, J.; Mengoni, A.; Reifarth, R.; et al. Measurement of 73 Ge(n, γ) cross sections and implications for stellar nucleosynthesis. *Phys. Lett. B* **2019**, 790, 458–465. [CrossRef]
- 24. Domingo-Pardo, C.; Babiano-Suarez, V.; Balibrea-Correa, J.; Caballero, L.; Ladarescu, I.; Lerendegui-Marco, J.; Tain, J.L.; Tarifeño-Saldivia, A.; Aberle, O.; Alcayne, V.; et al. Advances and new ideas for neutron-capture astrophysics experiments at CERN n_TOF. *Eur. Phys. J. A* 2023, *59*, 8. [CrossRef]
- 25. Trautvetter, H.P.; Becker, H.W.; Heinemann, U.; Buchmann, L.; Rolfs, C.; Baumann, M.; Freiesleben, H.; Geltenbort, P.; Käppeler, F.; Lütke-Stetzkamp, H.J.; et al. Destruction of ²⁶Al in explosive nucleosynthesis. *Z. Fur Phys. Hadron. Nucl.* **1986**, 323, 1–11. [CrossRef]

26. Chieffi, A.; Limongi, M. Pre-supernova evolution of rotating solar metallicity stars in the mass range 13–120 M_{\odot} and their explosive yields. *Astrophys. J.* **2013**, 764, 21. [CrossRef]

- 27. Limongi, M.; Chieffi, A. Presupernova Evolution and Explosive Nucleosynthesis of Rotating Massive Stars in the Metallicity Range −3≤ [Fe/H]≤ 0. *Astrophys. J. Suppl. Ser.* **2018**, 237, 13. [CrossRef]
- 28. Asplund, M.; Grevesse, N.; Sauval, A.J.; Scott, P. The Chemical Composition of the Sun. *Annu. Rev. Astron. Astrophys.* **2009**, 47, 481–522. [CrossRef]
- 29. Roberti, L.; Limongi, M.; Chieffi, A. Zero and Extremely Low-metallicity Rotating Massive Stars: Evolution, Explosion, and Nucleosynthesis Up to the Heaviest Nuclei. *Astrophys. J. Suppl. Ser.* **2024**, 270, 28. [CrossRef]
- 30. Limongi, M.; Chieffi, A. Hydrodynamical Modeling of the Light Curves of Core-collapse Supernovae with HYPERION. I. The Mass Range $13-25 \text{ M}_{\odot}$, the Metallicities $-3 \le [\text{Fe/H}] \le 0$, and the Case of SN 1999em. *Astrophys. J.* **2020**, 902, 95. [CrossRef]
- 31. Colella, P.; Woodward, P.R. The Piecewise Parabolic Method (PPM) for gas-dynamical simulations. *J. Comput. Phys.* **1984**, 54, 174. [CrossRef]
- 32. Iliadis, C.; Longland, R.; Champagne, A.E.; Coc, A.; Fitzgerald, R. Charged-particle thermonuclear reaction rates: II. Tables and graphs of reaction rates and probability density functions. *Nucl. Phys. A* **2010**, *841*, 31. 04.009. [CrossRef]
- 33. Caughlan, G.R.; Fowler, W.A. Thermonuclear reaction rates V. *At. Data Nucl. Data Tables* **1988**, 40, 283. 92-640X(88)9009-5. [CrossRef]
- 34. Angulo, C.; Arnould, M.; Rayet, M.; Descouvemont, P.; Baye, D.; Leclercq-Willain, C.; Coc, A.; Barhoumi, S.; Aguer, P.; Rolfs, C.; et al. A compilation of charged-particle induced thermonuclear reaction rates. *Nucl. Phys. A* **1999**, *656*, 3. [CrossRef]
- 35. Langer, N. Evolution of massive stars in the Large Magellanic Cloud: Models with semiconvection. *Astron. Astrophys.* **1991**, 252, 669–688.
- 36. Vink, J.S.; de Koter, A.; Lamers, H.J.G.L.M. New theoretical Mass-loss rates of O and B Stars. *Anesth. Analg.* **2000**, *362*, 295. [CrossRef]
- 37. Vink, J.S.; de Koter, A.; Lamers, H.J.G.L.M. Mass-loss predictions for O and B stars as a function of metallicity. *Anesth. Analg.* **2001**, *369*, 574–588.:20010127. [CrossRef]
- 38. de Jager, C.; Nieuwenhuijzen, H.; van der Hucht, K.A. Mass loss rates in the Hertzsprung-Russell diagram. *Astron. Astrophys. Suppl. Ser.* **1988**, 72, 259–289.
- 39. van Loon, J.T.; Oliveira, J.M.; Wood, P.R.; Zijlstra, A.A.; Sloan, G.C.; Matsuura, M.; Whitelock, P.A.; Groenewegen, M.A.T.; Blommaert, J.A.D.L.; Cioni, M.R.L.; et al. ESO-VLT and Spitzer spectroscopy of IRAS 05328–6827: A massive young stellar object in the Large Magellanic Cloud. *Mon. Not. R. Astron. Soc.* 2005, 364, L71. [CrossRef]
- 40. Nugis, T.; Lamers, H.J.G.L.M. Mass-loss rates of Wolf-Rayet stars as a function of stellar parameters. *Astron. Astrophys.* **2000**, *360*, 227–244.
- 41. Woosley, S.E. SN 1987A—After the peak. *Astrophys. J.* **1988**, 330, 218–253. [CrossRef]
- 42. Rauscher, T.; Heger, A.; Hoffman, R.D.; Woosley, S.E. Nucleosynthesis in Massive Stars with Improved Nuclear and Stellar Physics. *Astrophys. J.* **2002**, *576*, 323. [CrossRef]
- 43. Limongi, M.; Chieffi, A. Evolution, Explosion, and Nucleosynthesis of Core-Collapse Supernovae. *Astrophys. J.* **2003**, 592, 404–433. [CrossRef]
- 44. Sieverding, A.; Martínez-Pinedo, G.; Huther, L.; Langanke, K.; Heger, A. The v-Process in the Light of an Improved Understanding of Supernova Neutrino Spectra. *Astrophys. J.* **2018**, *865*, 143. [CrossRef]
- 45. Ritter, C.; Andrassy, R.; Côté, B.; Herwig, F.; Woodward, P.R.; Pignatari, M.; Jones, S. Convective-reactive nucleosynthesis of K, Sc, Cl and p-process isotopes in O-C shell mergers. *Mon. Not. R. Astron. Soc.* **2018**, 474, L1–L6,
- 46. Fryer, C.L.; Belczynski, K.; Wiktorowicz, G.; Dominik, M.; Kalogera, V.; Holz, D.E. Compact remnant mass function: Dependence on the explosion mechanism and metallicity. *Astrophys. J.* **2012**, 749, 91. [CrossRef]
- 47. Umeda, H.; Nomoto, K. Nucleosynthesis of Zinc and Iron Peak Elements in Population III Type II Supernovae: Comparison with Abundances of Very Metal Poor Halo Stars. *Astrophys. J.* **2002**, *565*, 385. [CrossRef]
- 48. Umeda, H.; Nomoto, K. Variations in the Abundance Pattern of Extremely Metal-Poor Stars and Nucleosynthesis in Population III Supernovae. *Astrophys. J.* **2005**, *619*, 427–445. [CrossRef]
- 49. Woosley, S.E.; Heger, A.; Weaver, T.A. The evolution and explosion of massive stars. *Rev. Mod. Phys.* **2002**, *74*, 1015–1071. [CrossRef]
- 50. Limongi, M.; Chieffi, A. Final stages of massive stars. SN explosion and explosive nucleosynthesis. *Eas Publ. Ser.* **2008**, 32, 233–281.:0832007. [CrossRef]
- 51. Nomoto, K.; Kobayashi, C.; Tominaga, N. Nucleosynthesis in Stars and the Chemical Enrichment of Galaxies. *Annu. Rev. Astron. Astrophys.* **2013**, *51*, 457–509. [CrossRef]
- 52. Pignatari, M.; Hoppe, P.; Trappitsch, R.; Fryer, C.; Timmes, F.; Herwig, F.; Hirschi, R. The neutron capture process in the He shell in core-collapse supernovae: Presolar silicon carbide grains as a diagnostic tool for nuclear astrophysics. *Geochim. Cosmochim. Acta* 2018, 221, 37. [CrossRef]
- 53. Trueman, T.C.L.; Côté, B.; Yagüe López, A.; Hartogh, J.D.; Pignatari, M.; Soós, B.; Karakas, A.I.; Lugaro, M. Galactic Chemical Evolution of Radioactive Isotopes with an s-process Contribution. *Astrophys. J.* **2022**, 924, 10. [CrossRef]

54. Murray, N. Star formation efficiencies and lifetimes of giant molecular clouds in the milky way. *Astrophys. J.* **2011**, 729, 133. [CrossRef]

- 55. Lee, T.; Papanastassiou, D.A.; Wasserburg, G.J. Aluminum-26 in the early solar system—Fossil or fuel. *Astrophys. J.* **1977**, 211, L107. [CrossRef]
- 56. Yin, Q.Z.; Jacobsen, B.; Moynier, F.; Amelin, Y.; Krot, A.N.; Nagashima, K.; Hutcheon, I.D.; Palme, H. 26Al-26Mg and 207Pb-206Pb Systematics of Allende CAIs: Reinstated Canonical Solar Initial 26Al/27Al Ratio, Variable kappa-Values (232Th/238U) and the Age of the Galaxy. In Proceedings of the 39th Annual Lunar and Planetary Science Conference, Houston, TX, USA, 10–14 March 2008.
- 57. Luu, T.-H.; Hin, R.C.; Coath, C.D.; Elliott, T. Bulk chondrite variability in mass independent magnesium isotope compositions— Implications for initial solar system ²⁶Al/²⁷Al and the timing of terrestrial accretion. *Earth Planet. Sci. Lett.* **2019**, 522, 166. [CrossRef]

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