## Article

# Synthesis of Wideband All-Frequency Absorptive Filtering Power Divider with High Selectivity and Flat Output Port Distributions 

Siran Zhang, Hongmei Liu *(D) Shuyi Chen, Zhongbao Wang (D) and Shaojun Fang<br>School of Information Science and Technology, Dalian Maritime University, Dalian 116026, China; zsr1120211310@dlmu.edu.cn (S.Z.); csy423@dlmu.edu.cn (S.C.); wangzb@dlmu.edu.cn (Z.W.); fangshj@dlmu.edu.cn (S.F.)<br>* Correspondence: lhm323@dlmu.edu.cn

Citation: Zhang, S.; Liu, H.; Chen, S.; Wang, Z.; Fang, S. Synthesis of Wideband All-Frequency Absorptive Filtering Power Divider with High Selectivity and Flat Output Port Distributions. Electronics 2023, 12, 3704. https://doi.org/10.3390/ electronics12173704

Received: 1 August 2023
Revised: 23 August 2023
Accepted: 30 August 2023
Published: 1 September 2023


Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/).


#### Abstract

In this paper, a wideband absorptive filtering power divider (AFPD) which features the characteristics of high selectivity and flat output distributions is proposed. It is composed of one unequal width three-coupled line (TCL), two coupled lines (CLs), two stepped open-circuited stubs, two kinds of isolation resistors, and two types of absorptive branches. The design equations of the proposed AFPD are derived using an even-odd decomposition method, and parametric investigations are also performed. It is found that the passband bandwidth can be adjusted by the stepped open-circuited stub which generates two transmission zeros (TZs). By combining the TCL with the CLs, the passband bandwidth is effectively enlarged. In addition, two isolated resistors are utilized for achieving good isolation and output-port matching performance. Without affecting the passband responses, the input port absorptive feature within the whole frequency band can be obtained by loading the absorptive branches both on the input and output ports. For validation, an example operating at the center frequency of 2 GHz was modeled and tested. Results exhibit that the passband FBW reaches $72 \%$ under 1 dB criterion, which illustrates flat output port distributions. In addition, for 10 dB return loss, the input and output impedance matching bandwidths are $250 \%$ and $78 \%$, respectively. The features of good filtering responses are demonstrated by realizing the rectangle coefficient of 1.24 and the out-of-band suppression of more than 20 dB .


Keywords: filtering power dividers; absorptive; wideband; three-coupled-line; high selectivity

## 1. Introduction

Filtering power dividers (FPDs), which integrate the functions of frequency selectivity and power division, have been a hot topic in recent years. Compared with the cascading configuration of power dividers and filters, the FPDs [1-10] have the merits of smaller size, better performance, and lower insertion loss. The research on FPDs has involved the wideband [1-8], dual-band [3-5], multi-way [6-9], reconfigurable [10], and so on. However, the FPDs introduced above are all reflective-type bandpass filters (BPFs), which means that the un-transmitted RF-input signal in the stopband regions will be reflected back to the source and affect the performance of adjacent active stages, such as the power amplifiers [11], the multiplexer [12], and so on. Inspired from the absorptive filters [13-17], the FPDs with input-absorptive behavior can be a good solution to deal with the above problem.

Until now, only several studies have reported on absorptive FPDs (AFPDs). In [18], the absorptive natures at the input/output ports are achieved by loading resistively terminated bandstop filtering branches. The passband 3 dB fractional bandwidth (FBW) is $13.6 \%$ and the 10 dB absorptive FBW is $75.5 \%$. In [19], a frequency reconfigurable input-absorptive FPD is designed by replacing the $\lambda / 4$ segments in PD arms with tunable BPFs and connecting the tunable bandstop filtering branch to the input port as the complementation. During the $28.1 \%$ frequency tuning range, the 3 dB FBW at each tuning state is $11.6 \%$, and the 10 dB
absorptive FBW reaches $87 \%$. However, the above reports both have the drawbacks of narrow bandwidth, poor selectivity, and large dimensions.

To widen the operating bandwidth and improve the selectivity, two cascaded coupled lines (CLs) loaded with $\lambda / 2$ open-circuited stubs are applied in designing the FPD in [20]. In addition, all-frequency input-absorption is realized by using three $\lambda / 4$ short-circuited stubs series with resistors. Measurement results indicate that the in-band FBW is $62.3 \%$ for 10 dB return loss, and the stopband suppression reaches more than 20 dB . In addition, the absorptive bandwidth under 10 dB return loss reaches $200 \%$. However, the passband 3 dB FBW is only $46 \%$. When using 1 dB FBW as the criterion, the FBW is reduced to $25.9 \%$, which indicates poor flatness. In [21], a compact wideband absorptive FPD is proposed. It exhibits the wideband filtering and power division functions by using the three-coupled lines (TCLs). In addition, the wideband input-absorptive feature is achieved by combining the T-shaped network with the absorptive stub. The 1 dB FBW is $52.8 \%$, and the 10 dB input-absorptive band reaches $200 \%$. The only drawback is the poor output matching bandwidth, which is narrower than the 1 dB FBW.

In the paper, an AFPD is presented with the advantages of wide passband bandwidth, wide input absorptive bandwidth, wide output impedance matching bandwidth, high selectivity, and flat output distributions. The main innovation of the proposed AFPD is the loading of two absorptive branches and the combination with suitable filtering sections, including the TCL, the CLs, and the stepped open-circuited stubs, to achieve a wideband absorptive bandwidth and at the same time keep good filtering responses, good output port impedance matching, and flat output distributions. A prototype was fabricated for validation. During the measurement, the FBWs for 1 dB and 3 dB passband criterions are $72 \%$ and $85 \%$, respectively, with more than a 20 dB out-of-band suppression level. Using 10 dB return loss as the criterion, the input and output port impedance matching bandwidths are $250 \%$ and $78 \%$, respectively. In addition, the rectangle coefficient (RC) reaches 1.24, which indicates high selectivity. In Section 2, the proposed AFPD is analyzed and parametric investigations are carried out. The implementation and measurements of the designed AFPD are shown in Section 3. Finally, Section 4 concludes the paper.

## 2. Theoretical Analysis and Design Procedure

### 2.1. Schematic of the AFPD

The topology of the proposed AFPD is illustrated in Figure 1. It consists of one unequal width TCL, two CLs, two stepped open-circuited stubs, two kinds of isolation resistors ( $R_{1}$ and $R_{2}$ ), and two types of absorptive branches. One of the absorptive branches is loaded on the input port of the AFPD and consists of two L-shaped microstrip structures connected by a loss resistor $\left(R_{3}\right)$. The other absorptive branch, which is composed of a $\lambda / 4$ short-circuited stub and a lossy resistor $\left(R_{4}\right)$, is shunted on the middle of the two isolation resistors, $R_{2}$. By using the TCL combined with the two CLs, a wide passband 3 dB FBW can be achieved. In addition, two transmission zeros (TZs) appear by shunting the stepped opencircuited stubs, and the frequency selectivity is simultaneously improved. The loading of absorptive branches enables the behavior of input-absorption and increases the out-of-band suppression. Good isolation and output port matching can also be achieved by inserting resistors $R_{1}$ and $R_{2}$.

In the following, the circuit parameters of the proposed AFPD are introduced in detail. Firstly, the electrical lengths of the lines in Figure 1 are all defined as $\theta$ and correspond to $90^{\circ}$ at the center frequency. Let $Z_{e}$ be the even-mode impedance of the CL, and let $Z_{o}$ be the odd-mode impedances of the CL. Since the TCL is composed of CLs with unequal widths, asymmetric CLs are utilized for the analysis of the TCL. Here, four parameters $\left(Z_{e a}, Z_{o a}, Z_{e b}\right.$ and $\left.Z_{o b}\right)$ are applied for the expression of the couplings between the edge and center lines. In detail, $Z_{e a}$ and $Z_{o a}$ are the impedances of the edge line under evenand odd-mode excitations, respectively, while $Z_{e b}$ and $Z_{o b}$ denote the impedances of the center line under even- and odd-mode cases, separately. The stepped open-circuited stub consists of two kinds of transmission lines (TLs) with the characteristic impedances of $Z_{1}$
and $Z_{2}$. The isolation resistor named as $R_{1}$ is shunted between the nonadjacent lines of the TCL. Two isolation resistors, $R_{2}$, are in series between the terminals of the two CLs. In the absorptive branch, the first L-shaped structure includes a TL $\left(Z_{3}\right)$ and an open-circuited stub $\left(Z_{4}\right)$, while the other L-shaped structure is composed of an open-circuited stub $\left(Z_{5}\right)$ and a short-circuited stub $\left(Z_{6}\right)$. For the other absorptive branch, the characteristic impedance of the short-circuited stub is defined as $Z_{7}$.

absorptive branch 1
Figure 1. Circuit topology of the proposed AFPD.

### 2.2. Analysis of the FPD

### 2.2.1. Design Equations

Firstly, the AFPD without the absorptive branches (named as FPD) is analyzed. Figure 2 shows its sub-circuits under even-odd mode analysis. From the variables exhibited in Figure 2, the port impedances of the FPD under the odd- and even-mode cases ( $Z_{\text {TRino }}, Z_{\text {TLine }}$, and $Z_{\text {TRine }}$ ) can be derived as (1).

$$
\begin{gather*}
Z_{\text {TRino }}=\frac{Z_{\text {TRo3 }} Z_{Y}}{Z_{\text {TRo3 }}+Z_{Y}}  \tag{1a}\\
Z_{\text {TLine }}=Z_{S 2}-\frac{2 Z_{S 6}^{2}}{Z_{S 1}+Z_{S 7}+Z_{\text {TLe } 1}}  \tag{1b}\\
Z_{\text {TRine }}=\frac{Z_{Y}\left(Z_{33} Z_{11}+Z_{33} Z_{\text {TRe } 1}-Z_{13} Z_{31}\right)}{Z_{Y}\left(Z_{11}+Z_{\text {TRe } 1}\right)+\left(Z_{33} Z_{11}+Z_{33} Z_{\text {TRe } 1}-Z_{13} Z_{31}\right)} \tag{1c}
\end{gather*}
$$



Figure 2. The (a) even- and (b) odd-mode sub-circuits of the FPD.

Here, the $Z_{\text {TRino }}$ is the impedance viewed from port 2 under odd-mode case, and $Z_{\text {Trine }}$ is the impedance viewed from port 2 under even-mode case. $Z_{\text {TLine }}$ represents the impedance viewed from port 1 under even-mode case. In addition, $Z_{Y}$ is the input impedance of the stepped open-circuited stub, $Z_{T R o 3}$ is the input impedance looking in from the right end of the $C L$ in the odd-mode excitation. $Z_{T L e 1}$ and $Z_{T R e 1}$ are the input impedances looking in from the left end of the CL and the right end of the TCL, respectively, in the even-mode case. The expressions of $Z_{Y}, Z_{T R o 3}, Z_{T L e 1}$, and $Z_{T R e 1}$ are shown in (2).

$$
\begin{gather*}
Z_{Y}=j Z_{2} \frac{Z_{2} \tan \theta-Z_{1} \cot \theta}{Z_{1}+Z_{2}}  \tag{2a}\\
Z_{T R o 3}=Z_{33}-\frac{Z_{34} Z_{43}}{Z_{44}+R_{2}}-\frac{\left(Z_{13} Z_{44}+Z_{13} R_{2}-Z_{34} Z_{14}\right)^{2}}{\left(Z_{T R o 2}+Z_{11}\right)\left(Z_{44}+R_{2}\right)^{2}-Z_{14} Z_{41}\left(Z_{44}+R_{2}\right)}  \tag{2b}\\
Z_{\text {TLe1 }}=Z_{11}-\frac{Z_{13} Z_{31}\left(Z_{Y}+Z_{0}\right)}{Z_{Y} Z_{0}+Z_{33}\left(Z_{Y}+Z_{0}\right)}  \tag{2c}\\
Z_{T R e 1}=Z_{S 1}+Z_{S 7}+\frac{2 Z_{S 6}^{2}}{Z_{S 2}+Z_{0}} \tag{2d}
\end{gather*}
$$

The intermediate variable $Z_{T R o 3}$ in (2b) can be expressed in (3), which denotes the input impedance looking in from the connection node of the right end of the TCL and the resistor $R_{1}$.

$$
\begin{equation*}
Z_{T R o 2}=\frac{\left(Z_{S 1} Z_{S 2}+Z_{S 2} Z_{S 7}-Z_{S 6}^{2}\right) R_{1}}{2\left(Z_{S 1} Z_{S 2}+Z_{S 2} Z_{S 7}-Z_{S 6}^{2}\right)+Z_{S 2} R_{1}} \tag{3}
\end{equation*}
$$

Except for the mentioned variables, the variables $Z_{11}, Z_{13}, Z_{14}, Z_{31}, Z_{33}, Z_{34}, Z_{41}$, and $Z_{44}$ are the self-impedances of the $C L$ [22], while the variables $Z_{S 1}, Z_{S 2}, Z_{S 6}$, and $Z_{S 7}$ are the self-impedances of the TCL [23]. The expressions of the self-impedances are shown in (4). Here, the $Z_{e}$ and $Z_{o}$ in (4a) are defined as the even- and odd-mode characteristic impedances of the CL. In (4b) and (4c), the $Z_{e a}$ and $Z_{o a}$ are the impedances of the edge line under even- and odd-mode cases, respectively. $Z_{e b}$ and $Z_{o b}$ denote the impedances of the center line for even- and odd-mode cases, separately.

$$
\begin{gather*}
\left\{\begin{array}{l}
Z_{11}=Z_{33}=Z_{44}=\mathrm{j} \frac{Z_{e}+Z_{o}}{2} \cot \theta \\
Z_{13}=Z_{31}=\mathrm{j} \frac{Z_{e}-Z_{o}}{2} \csc \theta \\
Z_{14}=Z_{41}=\mathrm{j} Z_{e}+Z_{o} \\
Z_{34}=Z_{43}=\mathrm{j} \frac{Z_{e}-Z_{o}}{2} \csc \theta \\
\cot \theta
\end{array}\right.  \tag{4a}\\
\left\{\begin{array}{l}
Z_{S 1}=-\mathrm{j} \frac{Z_{e a}+Z_{o a}}{} \cot \theta \\
Z_{S 2}=-\mathrm{j} \frac{Z_{e b}+Z_{o b}}{2} \cot \theta \\
Z_{S 6}=-\mathrm{j} \frac{Z_{e a}-Z_{o a}}{} \csc \theta \\
Z_{S 7}=-\mathrm{j} \frac{K\left(Z_{e a}-Z_{o a}\right)}{2} \cot \theta \\
Z_{e a}-Z_{o a}=Z_{e b}-Z_{o b}
\end{array}\right. \tag{4b}
\end{gather*}
$$

Here, note that in order to obtain a wideband response, the value of $K$ is often chosen within $0.3-0.7$, and it is set to 0.5 as the average value in the design as [24]. Then, the input impedance matching and transmission performance ( $S_{11 \_ \text {FPD }}$ and $S_{21 \_ \text {FPD }}$ ) of the FPD can be obtained as (5) [20].

$$
\begin{gather*}
S_{11 \_\mathrm{FPD}}=\Gamma_{\text {ine }}=\frac{Z_{\text {TLine }}-Z_{0}}{Z_{\text {TLine }}+Z_{0}}  \tag{5a}\\
S_{21 \_\mathrm{FPD}}=S_{31 \_\mathrm{FPD}}=\frac{1}{\sqrt{2}} S_{21}^{e} \tag{5b}
\end{gather*}
$$

$$
\begin{align*}
& S_{22 \_\mathrm{FPD}}=\frac{\Gamma_{\text {oute }}+\Gamma_{\text {outo }}}{2}=\frac{Z_{\text {TRine }} Z_{\text {TRino }}-Z_{0}^{2}}{\left(Z_{\text {TRine }}+Z_{0}\right)\left(Z_{\text {TRino }}+Z_{0}\right)}  \tag{5c}\\
& S_{23 \text { _FPD }}=\frac{\Gamma_{\text {oute }}-\Gamma_{\text {outo }}}{2}=\frac{Z_{0} Z_{\text {TRine }}-Z_{0} Z_{\text {TRino }}}{\left(Z_{\text {TRine }}+Z_{0}\right)\left(Z_{\text {TRino }}+Z_{0}\right)} \tag{5d}
\end{align*}
$$

Here, $Z_{0}$ is reference impedance which is equal to $50 \Omega$ in general. $\Gamma_{\text {ine }}$ represents the reflection performance of the input port for even-mode case. $\Gamma_{\text {oute }}$ and $\Gamma_{\text {outo }}$ are the reflection coefficients of the output ports (port 2 or 3 ) under even- and odd-mode excitation, respectively.

### 2.2.2. Parametric Analysis

Since stepped open-circuited stubs are connected in parallel at the output ports, two $\mathrm{TZs}\left(f_{t z 1}\right.$ and $\left.f_{t z 2}\right)$ related to $f_{0}$ can be obtained when the input impedance $Z_{Y}$ is equals 0 (corresponds to $S_{21 \_ \text {FPD }}=0$ ), as shown in (6).

$$
\begin{equation*}
f_{\mathrm{tz} 1}=\frac{2 f_{0}}{\pi} \cdot \arctan \sqrt{\frac{Z_{1}}{Z_{2}}} \quad f_{\mathrm{tz} 2}=2 f_{0}-f_{\mathrm{tz} 1} \tag{6}
\end{equation*}
$$

From Equation (6), the TZs of the FPD are controlled by the impedance ratio (IR) of the stepped open-circuited stub $\left(Z_{1} / Z_{2}\right)$. Figure 3a gives the variation of the TZs and 3 dB bandwidth under different values of IR. It is observed that when IR increases, the two TZs become closer. In addition, the 3 dB FBW is reduced accordingly. For clear illustration, the $\left|S_{21 \_ \text {FPD }}\right|$ of the FPD is shown in Figure 3 b. It is revealed that when the IR changes from 0.6 to 1.45 , the TZs shift from $0.465 / 1.535 f_{0}$ to $0.56 / 2.44 f_{0}$, while the corresponding 3 dB FBW narrows from $80 \%$ to $70 \%$. In the design, on the basis of achieving the target bandwidth of $80 \%$, the IR of 0.6 is chosen, which corresponds to two TZs located at 0.84 GHz and 3.16 GHz , respectively. Therefore, when $Z_{2}$ is chosen to be $70 \Omega$, the value of $Z_{1}$ can be calculated to be $42 \Omega$.


Figure 3. Calculated performances of the FPD with different IRs. (a) TZs and 3 dB FBW. (b) $\left|S_{21 \_ \text {FPD }}\right|$.
When set $S_{11 \_ \text {FPD }}=0$, according to the method in [25], four transmission poles (TPs) $\left(f_{t p 1}, f_{t p 2}, f_{t p 3}, f_{t p 4}\right)$ within the passband can be acquired in the frequency range $0-2 f_{0}$. Here, the equation of $S_{11 \_ \text {FPD }}=0$ is a quartic equation. According to the general solutions of the quartic equation, which can be referred to ref. [25], the expression in (7) is derived. It is noted that since the expressions of the TPs are complex, two groups of intermediate variables ( $o_{1}, o_{2}, o_{3}, o_{4}, x_{0}, x_{2}, x_{4}$ ) are utilized for simplification, as shown in (8) and (9).

$$
\begin{equation*}
f_{t p 1}=\frac{2 f_{0}}{\pi} \operatorname{arccot}\left(\frac{1}{2} \sqrt{o_{1}}-\frac{1}{2} \sqrt{o_{2}}\right) \tag{7a}
\end{equation*}
$$

$$
\begin{gather*}
f_{t p 2}=\frac{2 f_{0}}{\pi} \operatorname{arccot}\left(\frac{1}{2} \sqrt{o_{1}}+\frac{1}{2} \sqrt{o_{2}}\right)  \tag{7b}\\
f_{t p 3}=2 f_{0}-f_{t p 2}  \tag{7c}\\
f_{t p 4}=2 f_{0}-f_{t p 1} \tag{7d}
\end{gather*}
$$

where

$$
\begin{gather*}
o_{1}=\frac{2 x_{2}}{3 x_{4}}+o_{3}+\frac{x_{2}^{2}+12 x_{0} x_{4}}{9 x_{4}^{2} o_{3}}  \tag{8a}\\
o_{2}=\frac{4 x_{2}}{3 x_{4}}-o_{3}-\frac{x_{2}^{2}+12 x_{0} x_{4}}{9 x_{4}^{2} o_{3}}  \tag{8b}\\
o_{3}=\frac{\sqrt[3]{2}\left(x_{2}^{2}+12 x_{0} x_{4}\right)}{3 x_{4}\left(o_{4}+\sqrt{-4\left(x_{2}^{2}+12 x_{0} x_{4}\right)^{3}+o_{4}^{2}}\right)^{\frac{1}{3}}}  \tag{8c}\\
o_{4}=2 x_{2}^{3}-72 x_{0} x_{2} x_{4} \tag{8d}
\end{gather*}
$$

and

$$
\begin{equation*}
x_{0}=\frac{Z_{2}^{2} B^{2} A_{b}}{8} \tag{9a}
\end{equation*}
$$

$x_{2}=\frac{\left(Z_{1} Z_{2} B^{2} A_{b}-Z_{2}^{2} K A_{b} B_{a}-2 Z_{1} Z_{2} B_{a} A-Z_{2}^{2} A A_{a} A_{b}+Z_{2}^{2} B^{2} A_{b}+2 Z_{2}^{2} A B_{a}^{2}-Z_{2}^{2} A^{2} A_{b}\right)}{8}$
$x_{4}=\frac{\left(Z_{1} Z_{2} A A_{a} A_{b}+K Z_{1} Z_{2} A B_{a} A_{b}+Z_{1} Z_{2} A^{2} A_{b}-Z_{1} Z_{2} B^{2} A_{b}-2 Z_{1} Z_{2} A B_{a}\right)}{8}$

$$
\begin{equation*}
A=Z_{e}+Z_{o} B=Z_{e}-Z_{o} \tag{9d}
\end{equation*}
$$

$$
\begin{equation*}
A_{a}=Z_{e a}+Z_{o a} B_{a}=Z_{e a}-Z_{o a} \tag{9e}
\end{equation*}
$$

$$
\begin{equation*}
A_{b}=Z_{e b}+Z_{o b} B_{b}=Z_{e b}-Z_{o b} \tag{9f}
\end{equation*}
$$

According to (7)-(9), the TPs varies along with different circuit parameters and are investigated when the IR is set as 0.6 . Figure 4a shows the variations with the coupling $C$ of the CL, where $C=\left(Z_{e}-Z_{o}\right) /\left(Z_{e}+Z_{o}\right)$. It is seen that there are four TPs between the two TZs when $C$ is within 4.708-6.2 dB. Out of the range, the TPs are reduced to two. Figure 4 b gives the detailed $\left|S_{11 \_F P D}\right|$ performance of the FPD. Wider bandwidth under 10 dB return loss can be obtained for $C=5-5.5 \mathrm{~dB}$. Further, it is found that good impedance matching and equally distributed TPs are obtained simultaneously when the coupling is 5.2 dB . Thus, when the value of $Z_{o}$ is chosen as the $50 \Omega$, the corresponding value of $Z_{e}$ can be obtained as $172 \Omega$.

Meanwhile, Figure 5a shows the TPs varied with the coupling $C_{T}$ of $a$-line in the TCL, where $C_{T}=\left(Z_{e a}-Z_{o a}\right) /\left(Z_{e a}+Z_{o a}\right)[24]$. It is seen that the in-band TPs change from four to three when the $C_{T}$ exceeds 6.925 dB . As illustrated in Figure 5b, wider bandwidth can be obtained with 10 dB return loss for $C_{T}=5.5-6.5 \mathrm{~dB}$. Wider impedance matching bandwidth with suitable TPs intervals is obtained when $C_{T}$ equals with 6 dB . Thus, $Z_{\text {ea }}$ can be calculated as $150.3 \Omega$ when $Z_{o a}$ is assigned as $50 \Omega$. Figure 6 shows the variations of TPs and $\left|S_{11 \_ \text {FPD }}\right|$ along with the odd-mode impedance of $b$-line $\left(Z_{o b}\right)$. Four TPs can be generated when $Z_{o b}$ is larger than $35 \Omega$. But the $\left|S_{11 \_ \text {FPD }}\right|$ bandwidth is less influenced by the $Z_{o b}$. Since the even-odd mode impedances of the edge and center lines in the TCL
satisfy the relation in (4c), the even-mode impedance $Z_{o b}$ of the $b$-line is calculated to be $156 \Omega$ when $Z_{o b}$ is selected as $60 \Omega$.


Figure 4. Calculated (a) TPs and (b) $\left|S_{11 \_ \text {FPD }}\right|$ of the FPD under different $C$ when $Z_{o}$ is chosen as $50 \Omega$. $\left(Z_{1}=42 \Omega, Z_{2}=70 \Omega\right)$.


Figure 5. Calculated (a) TPs and (b) $\left|S_{11 \_ \text {FPD }}\right|$ of the FPD with different $C_{T}$ when $Z_{o a}$ is chosen as $50 \Omega$. $\left(Z_{1}=42 \Omega, Z_{2}=70 \Omega, Z_{e}=172 \Omega, Z_{o}=50 \Omega\right)$.


Figure 6. Calculated (a) TPs and (b) $\left|S_{11 \_ \text {FPD }}\right|$ of the FPD with different $Z_{o b}$. $\left(Z_{1}=42 \Omega, Z_{2}=70 \Omega\right.$, $Z_{e}=172 \Omega, Z_{o}=50 \Omega, Z_{e a}=150 \Omega, Z_{o a}=50 \Omega$ ).

The remaining parameters are the isolated resistors $R_{1}$ and $R_{2}$, which contribute to the output ports matching and isolation. On the basis of the parameters obtained above, the relationship between $R_{1}$ and $R_{2}$ can be expressed by using the condition of $S_{22 \text { _FPD }}=S_{23 \text { _FPD }}=0$, as shown in (10). Figure 7 shows the calculated $\left|S_{22_{-} \text {FPD }}\right|$ and
$\left|S_{23 \_ \text {FPD }}\right|$ of the FPD as a different $R_{2}$. It can be observed that as $R_{2}$ increases, the $\left|S_{22 \_ \text {FPD }}\right|$ and $\left|S_{23 \_ \text {FPD }}\right|$ values around the center frequency are decreasing, while both of the values deteriorate near the side frequencies. Finally, under the criterion of $\left|S_{22 \_ \text {FPD }}\right|$ and $\left|S_{23 \_ \text {FPD }}\right|$ less than $-20 \mathrm{~dB}, R_{2}$ is selected as $150 \Omega$. According to (10a), the value of $R_{1}$ is calculated as $15 \Omega$.

$$
\begin{gather*}
R_{1}=\frac{2 B_{R}\left(Z_{S 1} Z_{S 2}+Z_{S 2} Z_{S 7}-2 Z_{S 6}^{2}\right)}{A_{R}\left(Z_{S 1} Z_{S 2}+Z_{S 2} Z_{S 7}-2 Z_{S 6}^{2}\right)-B_{R} Z_{S 2}}  \tag{10a}\\
A_{R}=\left(Z_{11}-\frac{Z_{Y} Z_{0}}{Z_{Y}-Z_{0}}\right)\left(Z_{11}+R_{2}\right)^{2}-Z_{S 4}^{2}\left(Z_{11}+R_{2}\right) \tag{10b}
\end{gather*}
$$

$B_{R}=\left(Z_{11}^{2}-Z_{13}^{2}-\frac{Z_{Y} Z_{0} Z_{11}}{Z_{Y}-Z_{0}}\right)\left(Z_{11}+R_{2}\right)^{2}-\left(Z_{11} Z_{14}^{2}+Z_{11} Z_{34}^{2}+2 Z_{13} Z_{14} Z_{34}-\frac{Z_{Y} Z_{0} Z_{14}^{2}}{Z_{Y}-Z_{0}}\right)\left(Z_{11}+R_{2}\right)$


Figure 7. Calculated (a) $\left|S_{22_{2} \text { FPD }}\right|$ and (b) $\left|S_{23_{-} \text {FPD }}\right|$ of the FPD with different $R_{2}$. ( $Z_{1}=42 \Omega$, $\left.Z_{2}=70 \Omega, Z_{e}=172 \Omega, Z_{o}=50 \Omega, Z_{e a}=150 \Omega, Z_{o a}=50 \Omega, Z_{e b}=156 \Omega, Z_{o b}=60 \Omega\right)$.

### 2.3. Analysis of the AFPD

### 2.3.1. Design Equations and Parametric Analysis

In order to realize the input absorptive characteristic, two absorptive branches are loaded, where the sub-circuits under even-odd mode decomposition method are shown in Figure 8. Then, the overall $S$-parameters of the AFPD can be denoted as (11).


Figure 8. Equivalent (a) even- and (b) odd-mode sub-circuits of the AFPD.

$$
\begin{gather*}
S_{11 \_ \text {AFPD }}=\frac{A_{e_{-} \text {in }} Z_{0}+B_{e_{\_} \text {in }}-C_{e_{-} \text {in }} Z_{0}^{2}-D_{e_{-} \text {in }} Z_{0}}{A_{e_{-} \text {in }} Z_{0}+B_{e_{-} \text {in }}+C_{e_{-} \text {in }} Z_{0}^{2}+D_{e_{-} \text {in }} Z_{0}}  \tag{11a}\\
S_{21_{-} \text {AFPD }}=S_{31 \_ \text {AFPD }}=\frac{2 Z_{0}}{A_{e_{-} \text {in }} Z_{0}+B_{e_{-} \text {in }}+C_{e_{-} \text {in }} Z_{0}^{2}+D_{e_{-} \text {in }} Z_{0}}  \tag{11b}\\
S_{22_{\_} \text {AFPD }}=\frac{\Gamma_{\text {oute }}+\Gamma_{\text {outo }}}{2}  \tag{11c}\\
S_{23 \text { _AFPD }}=\frac{\Gamma_{\text {oute }}-\Gamma_{\text {outo }}}{2} \tag{11d}
\end{gather*}
$$

where

$$
\begin{equation*}
\Gamma_{\text {oute }(o)}=\frac{A_{e(o) \_ \text {out }} Z_{0}+B_{e(o) \_ \text {out }}-C_{e(o) \_ \text {out }} Z_{0}^{2}-D_{e(o) \_ \text {out }} Z_{0}}{A_{e(o) \_ \text {out }} Z_{0}+B_{e(o) \_ \text {out }}+C_{e(o) \_ \text {out }} Z_{0}^{2}+D_{e(o) \_ \text {out }} Z_{0}} \tag{12}
\end{equation*}
$$

Here, the derivations of $A_{e_{-} i n}, B_{e_{-} i n}, C_{e_{-} i n}, D_{e_{-} i n}$, and $A_{e(o) \_ \text {out }}, B_{e(o) \_ \text {out }}, C_{e(o) \_ \text {out }}, D_{e(o) \_ \text {out }}$ in (11) and (12) are shown in Appendix A. According to (11a), the parameters of the absorptive branches can be derived when assigning the absorptive criterion (for example, $\left.\left|S_{11 \_ \text {AFPD }}\right|<-10 \mathrm{~dB}\right)$. Since there are seven unknowns $\left(Z_{3}, Z_{4}, Z_{5}, Z_{6}, Z_{7}, R_{3}, R_{4}\right)$ in the absorptive branches, the particle swarm optimization algorithm (PSO) is used for fast computation. Equation (13) lists the defined objective function $F$. Here, $N_{1}$ and $N_{2}$ are the sampling points numbers in the absorptive and filtering bands, respectively. $f_{i}$ is the sample frequency, where the sample interval is $f_{0} / D$. It is noted that in the function $F$, $g_{1}$ is denoted as more than 10 dB at the input absorptive band, which corresponds to $L_{1}=10 \mathrm{~dB}$. In addition, to guarantee non-deterioration on other performances (output port impedance matching and isolation), the criteria $g_{2}$ and $g_{3}$ are added. In (13c) and (13d), the $L_{2}$ represents the limiting conditions of output port impedance matching and isolation, which equals 20 dB .

$$
\begin{gather*}
F\left(Z_{3}, Z_{4}, Z_{5}, Z_{6}, Z_{7}, R_{3}, R_{4}\right)=g_{1}+g_{2}+g_{3}  \tag{13a}\\
\left.g_{1}=\left.\frac{1}{N_{1}} \sum_{i=1}^{N_{1}}| | S_{11}\left(f_{i}\right)\right|^{2}-10^{-\frac{L_{1}}{10}} \right\rvert\,  \tag{13b}\\
\left.g_{2}=\left.\frac{1}{N_{2}} \sum_{i=1}^{N_{2}}| | S_{22}\left(f_{i}\right)\right|^{2}-10^{-\frac{L_{2}}{10}} \right\rvert\,  \tag{13c}\\
\left.g_{3}=\left.\frac{1}{N_{2}} \sum_{i=1}^{N_{2}}| | S_{23}\left(f_{i}\right)\right|^{2}-10^{-\frac{L_{2}}{10}} \right\rvert\, \tag{13d}
\end{gather*}
$$

Figure 9 gives the detailed optimization flow chart. In the design, the sampling interval $f_{0} / D$ is chosen as 0.1 GHz , and the number of sampling points $N_{1}$ and $N_{2}$ were selected as 21 and 13 , respectively, to cover the absorptive and filtering bands. The impedance range is limited to $40-120 \Omega$ for practical considerations and for quick calculations. Then, the parameters of the absorptive branches can be obtained.

Figure 10 shows the effects of the resistors $R_{3}$ and $R_{4}$ on $\left|S_{11}\right|$ of the AFPD. It is seen that the out-of-band absorptive feature is mainly influenced by $R_{3}$. As $R_{3}$ increases within $20-60 \Omega$, the out-of-band return loss is increased. When $R_{3}$ continues to increase from $60 \Omega$ to $100 \Omega$, the 10 dB absorptive bandwidth is nearly unchanged, only the matching degree is influenced. As can be seen in Figure 10b, the changing of $R_{4}$ will affect the matching degree of the input port, but the 10 dB absorptive bandwidth is nearly unchanged.


Figure 9. The optimization flowchart.


Figure 10. Effects of (a) $R_{3}$ and (b) $R_{4}$ on $\left|S_{11}\right|$ of the AFPD.

### 2.3.2. Theory Results and Design Procedures

Table 1 displays the calculated circuit parameters of the AFPD. Based on Table 1, the performance of the AFPD is obtained and listed in Figure 11. For convenience, the S-parameters of FPD and AFPD are compared directly. It is observed from Figure 11a that by inserting the absorptive branches, the bandwidth for 15 dB return loss at the input port is increased from $79 \%\left(0.61 f_{0}-1.40 f_{0}\right)$ to $200 \%\left(0-2 f_{0}\right)$. In addition, the out-ofband suppression has been enhanced to over 30 dB . Under the criterion of $\left|S_{21}\right|=-6 \mathrm{~dB}$, the calculated bandpass bandwidth is $85 \%$, and the $\mathrm{RC}\left(\left|\mathrm{BW}_{20 \mathrm{~dB}} / \mathrm{BW}_{3 \mathrm{~dB}}\right|\right)$ reaches 1.17. Figure 11b indicates that the output port impedance matching is less affected by the absorptive branches. But the isolation between output ports is enhanced in the filtering band. After inserting the absorptive branches, the calculated $\left|S_{23}\right|$ is less than 21 dB from $0-2 f_{0}$, while the $\left|S_{22}\right|$ is less than -15 dB from $0.61 f_{0}$ to $1.39 f_{0}$, yielding a bandwidth of $78 \%$.

Table 1. Calculated values of the AFPD.

| $Z_{\mathbf{1}}(\Omega)$ | $Z_{\mathbf{2}}(\Omega)$ | $Z_{\mathbf{3}}(\Omega)$ | $Z_{4}(\Omega)$ | $Z_{\mathbf{5}}(\Omega)$ | $Z_{\mathbf{6}}(\Omega)$ | $Z_{7}(\Omega)$ | $Z_{e}(\Omega)$ | $\theta\left({ }^{\circ}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 42 | 70 | 102 | 52.9 | 120 | 40 | 120 | 172 | 90 |
| $Z_{o}(\Omega)$ | $Z_{e a}(\Omega)$ | $Z_{o a}(\Omega)$ | $Z_{e b}(\Omega)$ | $Z_{\text {ob }}(\Omega)$ | $R_{\mathbf{1}}(\Omega)$ | $R_{\mathbf{2}}(\Omega)$ | $R_{3}(\Omega)$ | $R_{4}(\Omega)$ |
| 50 | 150.3 | 50 | 156 | 60 | 15 | 150 | 62 | 11 |



Figure 11. Theory results of the AFPD and FPD. (a) $\left|S_{11}\right|$ and $\left|S_{21}\right|$, (b) $\left|S_{22}\right|$ and $\left|S_{23}\right|$.
The design processes of the proposed APFD are concluded as follows for guidance.
(1) According to the target 3 dB FBW, determine the IR of the stepped open-circuited stub. Then, the value of $Z_{1}$ can be calculated according to the preassigned $Z_{2}$ value.
(2) According to (7)-(9), the appropriate even- and odd-mode impedances of the CLs ( $Z_{e}$ and $\left.Z_{o}\right)$ and TCLs $\left(Z_{e a}, Z_{o a}, Z_{e b}\right.$, and $\left.Z_{o b}\right)$ can be selected according to the performance of the TPs and $\left|S_{11 \_ \text {FPD }}\right|$.
(3) Based on the relationship between $R_{1}$ and $R_{2}$, as shown in (10), the values of $R_{1}$ and $R_{2}$ are obtained by considering the $\left|S_{22 \_ \text {FPD }}\right|$ and $\left|S_{23 \_ \text {FPD }}\right|$ performance.
(4) Finally, based on Figure 9, the absorptive branches ( $Z_{3}, Z_{4}, Z_{5}, Z_{6}, Z_{7}, R_{3}$, and $\left.R_{4}\right)$ can be optimized under the assigned criteria.

## 3. Implementation and Measurement

For demonstration, an example is designed at the center frequency of 2 GHz and fabricated on an F4B substrate ( $\varepsilon_{r}=3.5, \tan \delta=0.003$, and $h=1.5 \mathrm{~mm}$ ). Figure 12 shows the layout and photograph of the fabricated AFPD. The overall dimension of the fabricated prototype is $66 \mathrm{~mm} \times 79 \mathrm{~mm}$, yielding $0.44 \lambda_{\mathrm{g}} \times 0.53 \lambda_{\mathrm{g}}$ ( $\lambda_{\mathrm{g}}$ is the guide wavelength at the center frequency). Table 2 illustrates the final dimensions of the designed AFPD optimized by using the software Ansoft HFSS 13.0. In the process of modeling in the HFSS, the Perfect E boundary is assigned to represent the copper foil in realization. The resistors are represented by the Lumped RLC boundary. In addition, lumped port excitation is applied in the modeling. And the auto mesh method is applied in the simulation, which satisfies high resolution to guarantee accurate results.


Figure 12. Layout and photograph of the fabricated AFPD.

Table 2. Final dimensions of the AFPD (Unit: mm).

| $W_{t}$ | $L_{t}$ | $W_{1}$ | $L_{1}$ | $W_{2}$ | $L_{2}$ _1 | L2_2 | $W_{3}$ | $L_{3}$ | $W_{4}$ | $L_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.3 | 14.5 | 5.1 | 22.23 | 2 | 6.24 | 19.26 | 0.65 | 28.9 | 3.04 | 21.8 |
| $W_{5}$ | $L_{5-1}$ | $L_{5 \_2}$ | $W_{6}$ | $L_{6 \_1}$ | $L_{6 \_2}$ | $W_{7}$ | $L_{7 \_1}$ | $L_{7 \_2}$ | $L_{7 \_3}$ | $L_{7 \_4}$ |
| 0.33 | 20 | 4.2 | 4.54 | 12 | 9.8 | 0.44 | 3 | 2.4 | 3.2 | 7.4 |
| $L_{7-5}$ | $L_{7-6}$ | $W_{e}$ | $L_{e}$ | $S_{e}$ | $L_{S}$ | $W_{S}$ | $W_{a}$ | $W_{b}$ | $W_{d}$ | $r$ |
| 2.4 | 3.1 | 0.51 | 21.8 | 0.2 | 23.4 | 0.24 | 0.59 | 0.49 | 1.5 | 1.5 |
| $R_{1}$ | $R_{2}$ | $R_{3}$ | $R_{4}$ |  |  |  |  |  |  |  |
| $15 \Omega$ | $150 \Omega$ | $50 \Omega$ | $13 \Omega$ |  |  |  |  |  |  |  |

The circuit is fabricated through the high-precision corrosion equipment, where the accuracy is 0.01 mm . During the optimization using the HFSS, it is verified that the changing of about 0.01 mm has less effect on the overall performances of the prototype, while the resistors and connectors are soldered by hand. The vector network analyzer (VNA) Agilent N5230A $(0.3-25.6 \mathrm{GHz})$ is used as the test equipment. Firstly, three high-frequency test cables are connected to the port of the VNA. Then, the dedicated calibrator is used to calibrate the three cables simultaneously in the frequency range of $0.3-5 \mathrm{GHz}$. Finally, connect the three cables to the three ports of the prototype separately and performing the measurement.

Figure 13 shows the simulated and measurement results of the fabricated AFPD, which exhibit great agreements. Firstly, the results between the simulated and theoretical results (Figure 11) are compared. It is found that the curves for the theoretical results are more symmetric and better. This is due to the theory results being based on the equations (obtained from formulas by using the MATLAB), and the field coupling between the structures are not considered. While using the HFSS software to construct the layout, the couplings between the structures for the real layout are taken into consideration. Since the simulated results are influenced by the field coupling between the coupled lines, the bending of the transmission lines, the corner and the connection to the output ports, the layout should be optimized to obtain the best results.


Figure 13. The simulated and measured results of the fabricated AFPD. (a) $\left|S_{11}\right|$ and $\left|S_{21}\right|$, (b) $\left|S_{22}\right|$ and $\left|S_{23}\right|$.

As seen in Figure 13a, the input port of the AFPD is absorptive in the whole measured frequency range, yielding a bandwidth of $250 \%$. In the measurement, at the frequencies of 0.89 GHz and 3.25 GHz , two TZs are observed. Under 3 dB criterion, the passband FBW reaches $82.5 \%(1.24-2.89 \mathrm{GHz})$. In addition, the insertion loss (IL) at the center frequency achieved its minimum value of 0.35 dB . It is observed that the insertion loss in simulation is 0.28 dB . This is mainly due to the loss of the substrate, while in measurement, an extra loss of 0.07 dB appears. This may due to the loss induced by the connector or the fabrication
error. Under the more strict criterion of 1 dB relative bandwidth, the measured bandwidth is from 1.33 GHz to $2.77 \mathrm{GHz}(72 \%)$, indicating good passband flatness. In addition, the measured RC is 1.24 and the out-of-band rejection is larger than 20 dB , which indicates good filtering responses. It is observed from Figure 13b that in the absorptive bandwidth, the isolation between the output ports is larger than 12 dB . Under the criterion of 10 dB return loss (RL), the bandwidth for output ports matching reaches $78 \%(1.22-2.78 \mathrm{GHz})$.

The performance comparisons between the proposed and representative AFPDs are illustrated in Table 3. In $[18,19]$, the 3 dB BPBW are both less than $20 \%$, and the IL at the center frequency is high. In addition, no output reflection FBW is provided. Compared with the AFPDs in [20,21], which both exhibit more than $50 \% 3 \mathrm{~dB}$ FBW and $200 \% 10 \mathrm{~dB}$ input reflection FBW, the proposed AFPD shows a wider 3 dB BPBW of more than $80 \%$, wider output reflection FBW of more than $70 \%$, and smaller RC of 1.24 . The out-of-band suppression of the proposed AFPD is also better than the work in [21]. In addition, in consideration of the 1 dB BPBW and 3 dB BPBF items, it is found that the designed AFPD exhibits more flat output port distributions.

Table 3. Performance Comparisons Between the Proposed and Representative AFPDs.

|  | $\begin{gathered} \text { Test Band } \\ (\mathrm{GHz}) \end{gathered}$ | $\begin{gathered} 1 \mathrm{~dB} \text { BPBW } \\ (\%) \end{gathered}$ | 3 dB BPBW <br> (\%) | 10 dB IRFBW (\%) | $\begin{gathered} 10 \mathrm{~dB} \\ \text { ORFBW } \\ (\%) \end{gathered}$ | Out-of-Band Rejection (dB) | RC | $\mathrm{IL}^{a}(\mathrm{~dB})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| [18] | 1-3 | 7.4 * | 13.6 | 75.5 * | - | >15 | 2.88* | 0.9 |
| [19] | 0.5-2 | 9.1 * | 11.6 * | 87 | - | $>23$ | 1.42 * | 2.5 |
| [20] | 0-5 | 25.9 * | 51.4 * | 285 | 62.3 | >30 | 1.56* | 0.9 |
| [21] | 0-5 | 52.8 | - | 212 | 42.4 | $>17$ | 1.45 * | 0.32 |
| This work | 0-5 | 72 | 82.5 | 250 | 78 | >20 | 1.24 | 0.35 |

BPBW: Passband bandwidth based on $\left|S_{21}\right|$. IRFBW: Input reflection FBW. ORFBW: Output reflection FBW. $\mathrm{RC}=$ rectangular coefficient $=\left|\mathrm{BW}_{20 \mathrm{~dB}} / \mathrm{BW}_{3 \mathrm{~dB}}\right| .^{a}:$ Minimum passband IL. *: Estimated from the results.

## 4. Conclusions

In this paper, an AFPD with a wide 3 dB passband bandwidth, wide input absorptive bandwidth, wide 10 dB output reflection bandwidth, high selectivity, deep out-of-band rejection, and flat passband response is proposed. In the measurement, the results indicate that more than $70 \%$ bandwidths are achieved for 1 dB passband and 10 dB output reflection. The absorptive bandwidth for the input port reaches $250 \%$. In addition, a minimum passband insertion loss of 0.35 dB is obtained. Due to its simple structure and complete design process, the proposed AFPD can be used as a replacement of the traditional reflective PD for improving the system performance, which has broad application prospects in the modern wideband communication system.

Author Contributions: Conceptualization, H.L. and S.Z.; methodology, H.L. and S.Z.; software, S.C.; validation, Z.W. and S.F.; formal analysis, H.L. and S.Z.; investigation, S.C.; resources, H.L., Z.W. and S.F.; data curation, Z.W. and S.F.; writing-original draft preparation, S.Z.; writing-review and editing, H.L.; visualization, S.C.; supervision, S.Z.; project administration, S.F.; funding acquisition, H.L. and Z.W. All authors have read and agreed to the published version of the manuscript.

Funding: This work was supported in part by the National Natural Science Foundation of China under Grant 51809030, in part by the Liaoning Revitalization Talents Program under Grant XLYC2007067, in part by the Young Elite Scientists Sponsorship Program by CAST under Grant 2022QNRC001, and in part by the Fundamental Research Funds for the Central Universities under Grant 3132023246.

Data Availability Statement: All data are included within the manuscript.
Conflicts of Interest: The authors declare no conflict of interest.

## Appendix A

$$
\mathrm{M}_{e_{-} \text {in }}=\left[\begin{array}{ll}
A_{e_{-} \text {in }} & B_{e_{-} \text {in }}  \tag{A1}\\
C_{e_{-} \text {in }} & D_{e_{-} \text {in }}
\end{array}\right]=\mathrm{M}_{A} \cdot \mathrm{M}_{T C L} \cdot \mathrm{M}_{C L_{-} A} \cdot \mathrm{M}_{Y}
$$

Here, the $M_{A}, M_{T C L}, M_{C L_{-} A}$ and $M_{Y}$ represent the $A B C D$ matrices of the absorptive branch at the input port, the TCL, the CL with absorptive branch, and the stepped opencircuited stub, respectively, when input from port 1. And Equation (A2) gives the detailed $A B C D$ expressions of $M_{A}, M_{T C L}, M_{C L_{-} A}$ and $M_{Y}$.

$$
\begin{align*}
& M_{A}=\left[\begin{array}{cc}
1 & 0 \\
\frac{Z_{3}+j Z_{c} \tan \theta}{Z_{3}\left(Z_{c}+j Z_{3} \tan \theta\right)} & 1
\end{array}\right]  \tag{A2a}\\
& M_{T C L}=\left[\begin{array}{cc}
\frac{Z_{S 2}}{Z_{S 6}} & \frac{Z_{S 2}\left(Z_{S 1}+Z_{S 7}\right)}{Z_{S 6}}-2 Z_{S 6} \\
\frac{1}{Z_{S 6}} & \frac{Z_{S 1}+Z_{S 7}}{Z_{S 6}}
\end{array}\right]  \tag{A2b}\\
& M_{C L_{-} A}=\left[\begin{array}{cc}
\frac{Z_{22}\left(Z_{33}+R_{e}\right)-Z_{23} Z_{32}}{Z_{42}\left(Z_{33}+R_{e}\right)-Z_{43} Z_{32}} & \left(Z_{22}-\frac{Z_{23} Z_{32}}{Z_{33}+R_{e}}\right)\binom{Z_{44}\left(Z_{33}+R_{e}\right)-Z_{34} Z_{43}}{Z_{42}\left(Z_{33}+R_{e}\right)-Z_{33} Z_{43}}+\frac{Z_{34} Z_{23}}{Z_{33}+R_{e}}-Z_{24} \\
\frac{Z_{42}\left(R_{e}\right.}{Z_{42}\left(Z_{33}+R_{e}\right)-Z_{43} Z_{32}} & \frac{\left.Z_{43}+R_{e}\right)-Z_{34} Z_{43}}{Z_{42}\left(Z_{33}+R_{e}\right)-Z_{32} Z_{43}}
\end{array}\right]  \tag{A2c}\\
& M_{Y}=\left[\begin{array}{cc}
1 & 0 \\
j \frac{Z_{1}+Z_{2}}{Z_{2}\left(Z_{1} \cot \theta-Z_{2} \tan \theta\right)} & 1
\end{array}\right] \tag{A2d}
\end{align*}
$$

where

$$
\begin{gather*}
Z_{c}=\frac{Z_{4} Z_{5} Z_{6} \cot \theta+j R_{3}\left(Z_{4} Z_{6}-Z_{4} Z_{5} \cot ^{2} \theta\right)}{j\left(Z_{5} Z_{6}+Z_{4} Z_{6}-Z_{4} Z_{5} \cot ^{2} \theta\right)+R_{3}\left(Z_{5} \cot \theta-Z_{6} \tan \theta\right)}  \tag{A3a}\\
R_{e}=R_{2}+2 R_{4}+j 2 Z_{7} \tan \theta \tag{A3b}
\end{gather*}
$$

When input at port 2 under the even-mode excitation, the corresponding $A B C D$ matrix [ $\mathrm{M}_{\text {e_out }}$ ] is listed in (A4).

$$
\mathrm{M}_{e_{-} \text {out }}=\left[\begin{array}{ll}
A_{e^{\prime} \text { out }} & B_{e^{\prime} \text { out }}  \tag{A4}\\
C_{e^{\prime} \text { out }} & D_{e^{\prime} \text { out }}
\end{array}\right]=\mathrm{M}_{Y} \cdot \mathrm{M}_{C L \_A 1} \cdot \mathrm{M}_{T C L 1} \cdot \mathrm{M}_{A}
$$

where

$$
M_{T C L 1}=\left[\begin{array}{cc}
\frac{Z_{S 1}+Z_{S 7}}{2 Z_{S 6}} & \frac{Z_{S 2}\left(Z_{S 1}+Z_{S 7}\right)}{2 Z_{S 6}}-Z_{S 6}  \tag{A5a}\\
\frac{1}{2 Z_{S 6}} & \frac{Z_{S 2}}{2 Z_{S 6}}
\end{array}\right]
$$

$M_{C L_{-} A 1}=\left[\begin{array}{cc}\frac{Z_{44}\left(Z_{33}+R_{e}\right)-Z_{43} Z_{34}}{Z_{24}\left(Z_{33}+R_{e}\right)-Z_{23} Z_{34}} & \left(Z_{44}-\frac{Z_{43} Z_{34}}{Z_{33}+R_{e}}\right)\binom{Z_{22}\left(Z_{33}+R_{e}\right)-Z_{32} Z_{23}}{Z_{32}\left(Z_{33}+R_{e}\right)-Z_{33} Z_{23}}+\frac{Z_{33} Z_{43}}{Z_{33}+R_{e}}-Z_{42} \\ \frac{Z_{22}\left(Z_{33}+R_{e}\right)-Z_{32} Z_{23}}{\left.Z_{23}+R_{e}\right)-Z_{23} Z_{34}} & Z_{24}\left(Z_{33}+R_{e}\right)-Z_{34} Z_{23}\end{array}\right]$
Here, $M_{T C L 1}$ and $M_{C L \_A 1}$ are the $A B C D$ matrices of the TCL and the absorptive-branchloaded CL, respectively, when input from port 2. Based on Figure 8b, the $A B C D$ matrix [ $\mathrm{M}_{0 \_ \text {out }}$ ] between ports 2 and 3 under odd-mode excitation is shown in (A6). It is noted that the $M_{T C L \_S}$ is defined as the $A B C D$ matrix of the TCL with center-line shorted. Let $M_{C L \_R 1}$ and $M_{C L \_R}$ represent the $A B C D$ matrices of the absorptive-branch-loaded CL connected to port 2 and 3 , respectively. $M_{1}$ is the $A B C D$ matrix of the resistor $R_{1} / 2$.

$$
\mathrm{M}_{o_{-} \text {out }}=\left[\begin{array}{ll}
A_{o_{0} \text { out }} & B_{o_{0} \text { out }}  \tag{A6}\\
C_{\text {o_out }} & D_{o_{-} \text {out }}
\end{array}\right]=\binom{\mathrm{M}_{Y} \cdot \mathrm{M}_{C L \_R 1} \cdot \mathrm{M}_{1} \cdot \mathrm{M}_{T C L \_S}}{\cdot \mathrm{M}_{1} \cdot \mathrm{M}_{C L_{-} R} \cdot \mathrm{M}_{Y}}
$$

where

$$
\begin{align*}
& M_{C L \_R}=\left[\begin{array}{cc}
\frac{Z_{22}\left(Z_{33}+R_{2}\right)-Z_{23} Z_{32}}{Z_{42}\left(Z_{33}+R_{2}\right)-Z_{43} Z_{32}} & \left(Z_{22}-\frac{Z_{23} Z_{32}}{Z_{33}+R_{2}}\right)\binom{Z_{44}\left(Z_{33}+R_{2}\right)-Z_{34} Z_{43}}{\left.Z_{42}+R_{33}+R_{2}\right)-Z_{33} Z_{43}}+\frac{Z_{34} Z_{23}}{Z_{33}+R_{2}}-Z_{24} \\
\frac{Z_{42}\left(Z_{33}+R_{2}\right)-Z_{43} Z_{32}}{} & \frac{Z_{44}\left(Z_{33}+R_{2}\right)-Z_{34} Z_{43}}{Z_{42}\left(Z_{33}+R_{2}\right)-Z_{32} Z_{43}}
\end{array}\right]  \tag{A7a}\\
& M_{C L \_R 1}=\left[\begin{array}{cc}
\frac{Z_{44}\left(Z_{33}+R_{2}\right)-Z_{34} Z_{43}}{Z_{24}\left(Z_{33}+R_{2}\right)-Z_{34} Z_{23}} & \left(Z_{44}-\frac{Z_{43} Z_{34}}{Z_{33}+R_{2}}\right)\binom{Z_{22}\left(Z_{33}+R_{2}\right)-Z_{23} Z_{32}}{Z_{24}\left(Z_{33}+R_{2}\right)-Z_{23} Z_{34}}+\frac{Z_{34} Z_{23}}{Z_{33}+R_{2}}-Z_{24} \\
\frac{Z_{22}\left(Z_{33}+R_{2}\right)-Z_{23} Z_{32}}{\left.Z_{24}+R_{2}\right)-Z_{23} Z_{34}} & \left.Z_{33}+R_{2}\right)-Z_{23} Z_{34}
\end{array}\right]  \tag{A7b}\\
& M_{T C L \_S}=\left[\begin{array}{cc}
\frac{Z_{S 1} Z_{S 2}-Z_{S 6}^{2}}{Z_{S 2} Z_{S 7}-Z_{S 6}^{2}} & \left(Z_{S 1}-\frac{Z_{S 6}^{2}}{Z_{S 2}}\right)\left(\begin{array}{c}
\left.\frac{Z_{S 1} Z_{S 2}-Z_{S 6}^{2}}{Z_{S S} Z_{S 7}-Z_{S 6}^{2}}\right)+\frac{Z_{S 6}^{2}}{Z_{S 2}}-Z_{S 7} \\
\frac{Z_{S 2}}{Z_{S 2} Z_{S 7}-Z_{S 6}^{2}}
\end{array}\right] . \frac{Z_{S 1} Z_{S 2}-Z_{S 6}^{2}}{Z_{S 2} Z_{S 7}-Z_{S 6}^{2}}
\end{array}\right]  \tag{A7c}\\
& M_{1}=\left[\begin{array}{cc}
1 & 0 \\
\frac{2}{R_{1}} & 1
\end{array}\right] \tag{A7d}
\end{align*}
$$

## References

1. Chen, M.-T.; Tang, C.-W. Design of the filtering power divider with a wide passband and stopband. IEEE Microw. Wirel. Compon. Lett. 2018, 28, 570-572. [CrossRef]
2. Yu, X.; Sun, S. A novel wideband filtering power divider with embedding three-line coupled structures. IEEE Access 2018, 6, 41280-41290. [CrossRef]
3. Wang, X.; Wang, J.; Zhang, G.; Hong, J.-S.; Wu, W. Dual-wideband filtering power divider with good isolation and high selectivity. IEEE Microw. Wirel. Compon. Lett. 2017, 27, 1071-1073. [CrossRef]
4. Zhang, G.; Wang, J.; Zhu, L.; Wu, W. Dual-band filtering power divider with high selectivity and good isolation. IEEE Microw. Wirel. Compon. Lett. 2016, 26, 774-776. [CrossRef]
5. Wang, X.; Wang, J.; Choi, W.-W.; Yang, L.; Wu, W. Dual-wideband filtering power divider based on coupled stepped-impedance resonators. IEEE Microw. Wirel. Compon. Lett. 2018, 28, 873-875. [CrossRef]
6. Zhang, G.; Qian, Z.; Yang, J.; Hong, J.-S. Wideband four-way filtering power divider with sharp selectivity and high isolation using coshared multi-mode resonators. IEEE Microw. Wirel. Compon. Lett. 2019, 29, 641-644. [CrossRef]
7. Zhu, H.; Abbosh, A.M.; Guo, L. Wideband four-way filtering power divider with sharp selectivity and wide stopband using looped coupled-line structures. IEEE Microw. Wirel. Compon. Lett. 2016, 26, 413-415. [CrossRef]
8. Zhu, C.; Zhang, J. Design of high-selectivity asymmetric three-way equal wideband filtering power divider. IEEE Access 2019, 7, 55329-55335. [CrossRef]
9. Zhao, X.; Song, K.; Zhu, Y.; Fan, Y. Wideband four-way filtering power divider with isolation performance using three parallelcoupled lines. IEEE Microw. Wirel. Compon. Lett. 2017, 27, 800-802. [CrossRef]
10. Psychogiou, D.; Gómez-García, R.; Guyette, A.C.; Peroulis, D. Reconfigurable single/multi-band filtering power divider based on quasi-bandpass sections. IEEE Microw. Wirel. Compon. Lett. 2016, 26, 684-686. [CrossRef]
11. Yahya, S.I.; Alameri, B.M.; Jamshidi, M.; Roshani, S.; Chaudhary, M.A.; Ijemaru, G.K.; Mezaal, Y.S.; Roshani, S. A New Design Method for Class-E Power Amplifiers Using Artificial Intelligence Modeling for Wireless Power Transfer Applications. Electronics 2022, 11, 3608. [CrossRef]
12. Jamshidi, M.; Yahya, S.I.; Nouri, L.; Hashemi-Dezaki, H.; Rezaei, A.; Chaudhary, M.A. A Super-Efficient GSM Triplexer for 5G-Enabled IoT in Sustainable Smart Grid Edge Computing and the Metaverse. Sensors 2023, 23, 3775. [CrossRef] [PubMed]
13. Lee, J.; Lee, B.; Nam, S.; Lee, J. Rigorous design method for symmetric reflectionless filters with arbitrary prescribed transmission response. IEEE Trans. Microw. Theory Techn. 2020, 68, 2300-2307. [CrossRef]
14. Fan, M.; Song, K.; Yang, L.; Gómez-García, R. Frequency-tunable constant-absolute-bandwidth single-/dual-passband filters and diplexers with all-port-reflectionless behavior. IEEE Trans. Microw. Theory Techn. 2021, 69, 1365-1377. [CrossRef]
15. Gómez-García, R.; Muñoz-Ferreras, J.; Psychogiou, D. Symmetrical quasi-absorptive RF bandpass filters. IEEE Trans. Microw. Theory Techn. 2019, 67, 1472-1482. [CrossRef]
16. Wu, X.; Li, Y.; Liu, X. Quasi-reflectionless microstrip bandpass filters with improved passband flatness and out-of-band rejection. IEEE Access 2020, 8, 160500-160514. [CrossRef]
17. Xu, K.-D.; Lu, S.; Guo, Y.-J.; Chen, Q. Quasi- reflectionless filters using simple coupled line and t-shaped microstrip structures. IEEE J. Radio Freq. Identif. 2020, 6, 54-63. [CrossRef]
18. Gómez-García, R.; Muñoz-Ferreras, J.-M.; Psychogiou, D. RF reflectionless filtering power dividers. IEEE Trans. Circuits Syst. II Exp. Briefs 2019, 66, 933-937. [CrossRef]
19. Fan, M.; Song, K.; Yang, L.; Gómez-Garcia, R. Frequency-reconfigurable input-reflectionless bandpass filter and filtering power divider with constant absolute bandwidth. IEEE Trans. Circuits Syst. II Exp. Briefs 2021, 68, 2424-2428. [CrossRef]
20. Zhang, Y.; Wu, Y.; Yan, J.; Wang, W. Wideband high-selectivity filtering all-frequency absorptive power divider with deep out-of-band suppression. IEEE Trans. Plasma Sci. 2021, 49, 2099-2106. [CrossRef]
21. Zhu, Y.-H.; Cai, J.; Cao, Y.; Chen, J.-X. Compact wideband absorptive filtering power divider with a reused composite T-Shape network. IEEE Trans. Circuits Syst. II Exp. Briefs 2023, 70, 899-903. [CrossRef]
22. Zysman, G.I.; Johnson, A.K. Coupled Transmission Line Networks in an Inhomogeneous Dielectric Medium. IEEE Trans. Microw. Theory Techn. 1969, 17, 753-759. [CrossRef]
23. Ozaki, H.; Ishii, J. Synthesis of a Class of Strip-Line Filters. IRE Trans. Circuit Theory 1958, 5, 104-109. [CrossRef]
24. Chen, C.P.; Kato, N.; Anada, T. Synthesis scheme for wideband filters consisting of three-coupled-lines including the cross coupling between non-adjacent lines. IET Microw. Antennas Propag. 2015, 9, 1558-1566. [CrossRef]
25. Wu, Y.; Cui, L.; Zhuang, Z.; Wang, W.; Liu, Y. A simple planar dual-band bandpass filter with multiple transmission poles and zeros. IEEE Trans. Circuits Syst. II Exp. Briefs 2018, 65, 56-60. [CrossRef]

Disclaimer/Publisher's Note: The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.

