



# Article Bidding Evaluation and Contractor Selection Using Balance Index Model and Comprehensive Input Efficiency Based on Data Envelopment Analysis

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Abstract: In order to ensure a smooth construction project, it is necessary to select an appropriate contractor. However, traditional bid evaluation methods are highly subjective in determining weights. Data envelopment analysis (DEA), a comprehensive bid evaluation method that considers multiple factors, was introduced to reduce subjectivity and provide a simple yet comprehensive method for evaluating bids. Based on the existing cross-evaluation and balance index models, this research proposed a new DEA ranking model-the comprehensive input efficiency model, as well as its specific application steps. Additionally, a case study on selecting contractors for a water engineering project was presented to demonstrate the effectiveness of this model. The results indicated that the comprehensive input efficiency model could achieve the same ranking function as the balance index and was suitable for assessing bidders' relative efficiency. Moreover, the comprehensive input efficiency model proposed in this research is more simplified. Thus, this research compensates for the drawbacks of the existing comprehensive evaluation models in that the bid evaluation process is cumbersome, thereby extending the research on DEA methods in bid evaluation. Additionally, the model provides tenderers with a more efficient and effective bid evaluation method to select the most appropriate contractor. In the future, research may be conducted to apply DEA to other types of projects, including service projects, real estate, and consulting services.

**Keywords:** data envelopment analysis (DEA); construction management; comprehensive bid evaluation; balance index model; comprehensive bid efficiency

# 1. Introduction

The construction industry is characterized by complex environments, adversity, intense competition, heavy construction tasks, and the high number of fixed assets required. Given these factors, it has become increasingly challenging to select reputable construction contractors who are capable of providing quality, streamlining the construction process, and reducing project costs [1–4]. Generally, tending and bidding remain the most common methods for hiring qualified contractors. Therefore, to ensure that selected contractors can deliver the project smoothly following the contract requirements, careful evaluation is exceptionally essential during the bidding process [5].

The lowest bid price is traditionally used to select contractors for construction projects [6,7]. The emphasis on price as the sole criterion for selection may result in many drawbacks, such as poor quality, delays, and additional costs resulting from rework, claims, and disputes [8–11]. Thus, contractors should be evaluated comprehensively using quantitative and qualitative criteria [12], called comprehensive bid evaluation, which considers the weights of multiple factors. For instance, weights should be determined by considering not only the project's characteristics but also the tenderer's requirements in selecting the contractor [13–15]. However, in the practice of comprehensive bid evaluation, it has been



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**Copyright:** © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). noted that the weight of the evaluation index is clearly subjective, and most quantitative methods cannot alter this element.

DEA, an effective non-parametric method to evaluate the relative effectiveness of DMUs with the same structure [16], has been introduced into the construction industry as a comprehensive evaluation method. In some research, DEA methods have been applied to assess the safety performance of contractors. For example, Nahangi, et al. [17] used DEA to conduct a safety-based efficiency evaluation of construction sites. DEA was used by El-Mashaleh, et al. [18] to benchmark construction contractors' safety performance. Additionally, some research has combined DEA with other methods to assess and select bidders. In particular, Cheaitou, Larbi and Al Housani [8] combined DEA, fuzzy logic, and mixed integer linear programming to assist public organizations in selecting the most appropriate construction contractor(s). Other methodologies are also discussed, such as the analytical hierarchy process (AHP) [19–21], the analytic network process (ANP) [22,23], partial least squares [14], fuzzy set theory [24,25], and fuzzy analytic hierarchy process [26,27]. However, these methods and model operations, coupled with modern mathematical theories, are complex and poorly defined in terms of their application. Specifically, they cannot systematically deal with uncertainty and certainty in objective things and subjective consciousness during the bid evaluation process. Therefore, they are rarely used in practical evaluating bids [26]. Furthermore, most existing research combines DEA with other methods to develop improved models instead of using the basic DEA model.

As a result, in order to fill this gap, this research introduced the DEA method into comprehensive bid evaluation and discussed its basic model first. Considering the DEA cross-evaluation model requires multiple cross-evaluations to achieve a complete ranking, the balance index model was then analyzed. Based on this, this research proposed an improved DEA ranking model—comprehensive input efficiency. Additionally, through analysis and comparison, it is demonstrated that the balance index and comprehensive input efficiency models can provide reasonable evaluation results and are more effective in ranking DMUs. Finally, a case study of selecting contractors for a water construction project in China is presented to illustrate the effectiveness of the model proposed. Through sorting out the bid evaluation indexes and methods, this research established a comprehensive, objective, understandable, and impartial comprehensive input efficiency model. Besides overcoming the shortcomings of the traditional comprehensive bid evaluation method, this model is more practical and simplified as well. Furthermore, this model enhances bid evaluation efficiency, is suitable for sectoral application and grassroots promotion, and ultimately provides a relatively objective evaluation basis for tenderers. Accordingly, the comprehensive input efficiency model contributes to the comprehensive evaluation of bidders in both theory and practice.

## 2. Literature Review

## 2.1. Application Research of DEA in Bid Evaluation

DEA is an effective non-parametric method to evaluate the relative effectiveness of DMUs with the same structure [16]. The input–output efficiency analysis is the original type of DEA analysis. However, as a system analysis method, unlike other system methods dealing with complex systems with multiple inputs and multiple outputs, the DEA method does not require providing functional relationships between inputs and outputs, nor weightings between input indicators and output indicators. Only input and output observations are required to evaluate the relative efficiency of different DMUs. For instance, according to Guo and Wu [28], cost indicators are regarded as the input index, and efficiency indicators are regarded as the output index of the DMU, which has been transformed into the input–output evaluation and assessed by the DEA method. Further, the principles of the DEA method are the same regardless of whether it is applied to input–output analysis or the evaluation of comprehensive indicators. Inti and Tandon [29] calculated the index value through AHP to obtain the index value of the evaluation object and processed the second relative evaluation using the DEA method.

The traditional DEA methods consist of a self-evaluation of DMUs, which can only be used for determining whether they are relatively efficient but not for ranking them. In various fields, improved DEA evaluation ranking models have been developed [30–32]. Talluri [33] first introduced the DEA model based on a game model of buyers and sellers in auctions and established an auction evaluation model. Chetan, et al. [34] present an iterative multi-attribute reverse auction mechanism based on integrated data envelopment analysis (DEA) and the best-worst method (BWM). As well, DEA methods have been used to evaluate all bidders fairly and comprehensively. Zhao, et al. [35] present a novel model integrating an analytical hierarchy process and data envelopment analysis (AHP/DEA) to evaluate bids for major construction projects. Yang, et al. [36] used DEA to support best-value contractor selection. Thus, it has been demonstrated that DEA is an effective tool for objectively generating a list of bidders with comprehensive expertise. However, existing DEA evaluation models mainly combined DEA with other methods. Few research studies have proposed an improved comprehensive bid evaluation model that is directly based on the DEA basic model. Moreover, most existing models, in conjunction with modern mathematical theories, have a complex application in practice. Consequently, tenderers do not have the capacity to apply these models systematically to evaluate bidders, resulting in their rare use in practice.

By considering the comprehensive evaluation mechanism as a mixed linear multicriteria optimization problem, this research proposed a comprehensive input efficiency model and intended to solve it using an optimization algorithm. It is believed that the comprehensive input efficiency model could simplify the bid evaluation process, extending research on DEA models in evaluating construction bids. Furthermore, this model has the potential to increase the operability of existing DEA bidding models, enhance the bidding efficiency, and provide tenderers with a fairly objective evaluation basis.

#### 2.2. Contractor Selection Criteria

Choosing responsive and responsible contractors can ensure smooth project delivery and a reduction in costs. Thus, the selection criteria are essential research subjects [37]. For construction projects, contractors are typically selected based on their lowest bid price [7,38]. It is possible, however, that this may result in eliminating qualified contractors and accepting others who cannot complete the project successfully. In view of this, using price as the sole selection criterion is not advisable [12]. Rather, both quantitative and qualitative criteria should be used to make a comprehensive selection of contractors. During the comprehensive tender evaluation process, the owner must evaluate the most suitable overall bidder based on a combination of factors (price, quality, duration, etc.) to maximize the overall benefit to the bidder (minimizing costs). Over the past few years, a growing body of literature has been developed for evaluating contractors [39,40]. For instance, to address the issue that the bid evaluation process is imprecise and uncertain regarding alternative-criterion decision appraisals, Chen, et al. [41] developed a novel ELECTRE IIIbased MCGDM approach for bid evaluation, in which generalized comparative linguistic expressions (GCLEs) are used to evaluate bidder performance. Based on the logic pattern of the human cognition process and the compensatory relation among attributes, Chen, et al. [42] established a two-stage logic scoring of preference—an ELECTRE III-based approach for managing and manipulating bidder selection. Given that CO<sub>2</sub> emissions need to be prioritized in traditional bid evaluation, Liu, Yang, Huo, Shen and Wang [15] developed a conceptual, computational model for  $CO_2$  emissions, as well as a linguistic group decision-making framework for evaluating bids in mega projects that aim to reduce  $CO_2$  emissions. Thus, the establishment of standards may depend on the type of project and local norms (e.g., the local legal and industrial ecosystem). Additionally, the indicator system may be established based on the owner's requirements for the project objectives, the project conditions, and the construction conditions. However, few research studies provide a comprehensive analysis and systematic summary of evaluation indicators. Therefore, by

Category	Criteria	Sub-Criteria	Sources
The indicator system for comprehensive bid evaluation	Tendered price	Bid price The balance of the quotation	[13–15,22,37,43–49] [13–15,43,46–48]
	The intensity of project investment	Labor use plan Equipment usage plan	[13–15,45,50–53] [12–15,45,50–54]
	Enterprise comprehensive	Qualification level of the enterprise Qualification of project manager Social reputation Construction experience and	[43,53–55] [3,14,37,40,43,45] [13–15,26,43,45,48,51,52,56]
	strength	achievements Technical equipment and technical force	[13–15,26,38,43,45,51,56–58] [13–15,26,50,51,53]
	Credit level of bidder	Quality of enterprise Quality of assets Economic benefit Credit standing	[43,50,53,55] [3,12,52,53,55,56,59] [3,13–15,26,50,53,56,59] [3,13–15,26,37,45,50,51,53,56]
	Construction	Construction scheme Quality assurance system and measure Construction schedule and	[13–15,37,43,45,53,58–60] [3,12–15,26,37,43,45,50–54,58,60]
	organization design	guarantee measures Safety precautions	[3,12–15,26,37,43,45,51–54,58,60] [3,12–15,26,38,45,50–54,56,58–60]

reviewing existing research, the indicator system for the comprehensive evaluation of bids summarized in this study is shown in Table 1.

## Table 1. The indicator system for comprehensive bid evaluation.

# 3. Methodology

3.1. Basic Model of DEA

The DEA method requires finding an optimal set of input–output weights. The basic model of the DEA method is as follows:

$$\begin{cases} \sum_{s=1}^{v} a_{r}y_{rp} \\ Max \frac{r=1}{\sum_{s=1}^{u} a_{s}x_{sp}} \\ s.t. \\ \sum_{r=1}^{v} a_{r}y_{ri} \\ \frac{r=1}{\sum_{s=1}^{u} b_{s}x_{si}} \leq 1, \forall i \\ \sum_{s=1}^{s=1} b_{s}x_{si} \\ ar, bs \geq 0, \forall r, s \end{cases}$$
(1)

 $a_r$  and  $b_s$  represent unknown output and input weights; p represents a specific bidder in n bidders i ( $i = 1, \dots, n$ ); and each bidder i has u input metrics  $x_{si}$  ( $i = 1, \dots, u$ ) and v output indicators  $y_{ri}$  ( $r = 1, \dots, v$ ).

The DEA method aims to determine the optimal output and input weights for the owner to achieve the desired target. This target represents the optimal benefit between each input and each output of all bidders (for example, the smallest input gets the largest output). This problem can be converted into a linear programming problem:

$$\begin{array}{l}
Max \sum_{r=1}^{v} a_{r}y_{rp} \\
s.t. \\
\sum_{s=1}^{v} a_{r}y_{ri} \leq \sum_{s=1}^{u} b_{s}x_{si}, \forall i \\
\sum_{s=1}^{u} b_{s}x_{si} = 1 \\
a_{r}, b_{s} \geq 0, \forall r, s
\end{array}$$
(2)

Through solving the above linear programming problem, the optimal solution of  $a_r$  and  $b_s$  (call it  $a_r^{ideal(1)}$  and  $b_s^{ideal(1)}$ ) can be obtained. Therefore, the efficiency value of each bidder, named self-evaluation value, can be calculated as follows:

$$u_i = \sum_{r=1}^{v} a_r^{ideal(1)} y_{ri} \tag{3}$$

Using (3), the efficiency value  $u_i$  of each bidder can be calculated; (1)  $u_i = 1$  indicates the bidder is valid, and (2)  $u_i < 1$  indicates the bidder is invalid. Under normal conditions, multiple bidders exist whose  $u_i$  reaches 1. Therefore, constraints must be added to further evaluate the *n* bidders.

This research will further analyze several methods which improve the relative optimal efficiency DEA evaluation model, including cross-evaluation mechanism, balance index, and comprehensive input efficiency.

# 3.2. Cross-Evaluation Mechanism

The basic idea of cross-evaluation mechanism is as follows: the optimal solutions  $a_r^{ideal(1)}$  and  $b_s^{ideal(1)}$  of each bidder are used to calculate the efficiency value of other bidders, obtaining cross-evaluation values:

$$u_t = \sum_{r=1}^{v} a_r^{ideal(1)} y_{rp}(t \in [1, \cdots, n])$$
(4)

For the above issues, the higher the cross-evaluation value  $u_t$ , the more favorable it is for bidder t, and the more unfavorable for bidder i. The above questions can be converted into

$$\begin{cases} \operatorname{Min} \sum_{r=1}^{v} a_{r} y_{rt} \\ \text{s.t.} \\ \sum_{r=1}^{v} a_{r} y_{ri} \leq \sum_{s=1}^{u} b_{s} x_{si}, \forall i \\ \sum_{s=1}^{u} b_{s} x_{st} = 1, \\ \sum_{s=1}^{v} a_{r} y_{rt} = E_{i} b_{s} x_{si}, \forall i \\ a_{r}, b_{s} \geq 0, \forall r, s \end{cases}$$

$$(5)$$

Through solving the above linear programming problem, a new set of optimal solutions for  $a_r$  and  $b_s$  (call them  $a_r^{ideal(2)}$  and  $b_s^{ideal(2)}$ ) can be obtained. The cross-evaluation value and cross-evaluation matrix are obtained by using the optimal solution:

$$u_t = \sum_{r=1}^v a_r^{ideal(2)} y_{rt} \tag{6}$$

$$u_{it} = \begin{bmatrix} u_{11} & \cdots & u_{1n} \\ \vdots & \vdots & \vdots \\ u_{n1} & \cdots & u_{nn} \end{bmatrix}$$
(7)

The relative efficiency value  $u_i$  of the bidder obtained above is the value on the diagonal in the cross-evaluation matrix  $u_i$ , which serves as the first evaluation index. The second evaluation index is divided into two kinds. Many researchers use the average value  $u_i^*$  of off-diagonal elements in line *i* as the second index of evaluation. Additionally, the smaller the  $u_i^*$ , the better. Additionally, much research uses the average value  $u_i^*$  of the element in column *t* as the second index of evaluation. Additionally, the bigger the  $u_i^*$ , the better. In the evaluation process of DEA, the first evaluation index  $u_i$  is compared first. If  $u_i$  is the same, then the second evaluation index  $u_i^*$  is compared. This research takes the

average value  $u_t^*$  of non-diagonal elements in column *t* as the second index of evaluation. The calculation formula of  $u_t^*$  and  $u_i^*$  are as follows:

$$u_t^* = \frac{1}{n - 1} \sum_{t \neq i} u_{it}$$
(8)

$$u_i^* = \frac{1}{n-1} \sum_{i \neq t} u_{it} \tag{9}$$

In the process of bid evaluation, the efficiency  $u_i$  of bidders is compared first. Additionally, bigger  $u_i$  is prioritized. If  $u_i$  is identical,  $u_t^*$  or  $u_i^*$  is compared, with bigger  $u_t^*$  or smaller  $u_i^*$  being given priority. For the second evaluation index  $u_i^*$ , it takes the average value of off-diagonal elements in line *i* as the evaluation index. However, in the calculation process of DEA evaluation method, all calculations are carried out for each column of data, aiming to find the optimal weight distribution between input and output of each column. If  $u_i^*$  is used as the second evaluation index, reasonable results cannot be obtained in most cases. Thus, it is not suitable to use  $u_i^*$  as the second evaluation index. Thus,  $u_t^*$ , which takes the average value of non-diagonal elements in column, should be the second evaluation index.

When  $u_t^*$  is the evaluation index, in most cases, relatively complete evaluation results can be obtained. However, in special situations, the same value of  $u_t^*$  may also occur, which cannot offer complete evaluation results. As a result,  $u_t^*$  should be chosen as the second evaluation index. In view of the possibility that  $u_t^*$  may have the same value, another cross-evaluation should be conducted. The new optimal solutions  $a_r^{ideal(2)}$  and  $b_s^{ideal(2)}$ should be used to calculate the efficiency value of other bidding units to obtain a new cross-evaluation matrix. The second cross-evaluation is referred that the average value of non-diagonal elements in column *t* is used as the evaluation index (the evaluation index of the second cross-evaluation is expressed by  $u_t^*(2)$ ). The calculation process of DEA model with cross-evaluation mechanism is shown in Figure 1.

The complete evaluation can be completed after a cross-evaluation process or after a second cross-evaluation process if the number of bidders *i* is relatively small. However, if there are a large number of bidders, a second cross-evaluation process may not be able to provide a complete judgment. Therefore, to obtain a comprehensive evaluation report, multiple cross-evaluation methods must be employed.

Based on the above analysis, it appears that the cross-evaluation mechanism can assist in evaluating and ranking bidders (DMUs) more accurately. It is important to note, however, that for large numbers of bidders, DEA evaluation with the cross-evaluation mechanism may require multiple cross-evaluations to produce reasonable results.

#### 3.3. Balance Index Model

For the above DEA bid evaluation model, it can be known that  $\sum_{r=1}^{v} a_r y_{ri}$  is the total output of the *ith* bidder and  $\sum_{s=1}^{u} b_s x_{si}$  is the total input of the *ith* bidder. Then, the interest constraint conditions of the *ith* bidder are as follows.

$$\sum_{r=1}^{v} a_r y_{ri} - \sum_{s=1}^{u} b_s x_{si} \le 0, \ i = 1, \cdots, n$$
(10)

Assuming that F(x, y) = 0 is an efficiency function, then

$$\sum_{j} \frac{\partial F}{\partial y_{j}} y_{j} - \sum_{i} \frac{\partial F}{\partial x_{i}} x_{i} = 0$$
(11)

In addition, under the condition of maximizing competitive interests, the input of the *ith* bidder is proportional to  $\frac{\partial F}{\partial x_i}$ , and the output of the *jth* bidder is proportional to  $\frac{\partial F}{\partial y_j}$ . That the input of the *ith* bidder is zero is called the ideal optimum.



Figure 1. Calculation process of DEA model with cross-evaluation.

In the process of bid evaluation, when the interest constraint condition of the *ith* bidder is zero, it is said to be valid; otherwise, it is said to be invalid. If the interest constraints of other bidders are not equal to zero, then the *ith* bidder wins. If the interest constraints of several bidders are equal to zero, it is necessary to introduce "balance index" [61] for further evaluation and analysis. Balance index of each bidder refers to the sum of all other bidders' interest constraints. In the process of bid evaluation, the smaller the balance index is, the better. The balance index is expressed by  $B_i$ :

$$B_i = nu_i - \sum_{p=1}^n \sum_{s=1}^u x_{sp} b_s^{ideal(1)}(i)$$
(12)

where  $b_s^{ideal(1)}(i)$  is the optimal input weight of the *ith* bidder;  $x_{sp}$  is the input of bidder *p*. The indicators for the other parameters are as described previously.

In DEA evaluation model, which introduces balance index, the efficiency value  $u_i$  of each bidder is compared first. Additionally, the higher the  $u_i$ , the higher the priority. If  $u_i$  is

identical, then the balance index  $B_i$  is compared. Additionally, the smaller  $B_i$  is, the higher priority will be given. In this method, complete evaluation results can be well given even if the number of bidders *i* is relatively large. The advantage of this method is that it is only necessary to calculate the balance index  $B_i$  of the bidder (DMU) once to obtain a reasonable evaluation result.

# 3.4. Comprehensive Input Efficiency Model

By referring to the principle of cross-evaluation mechanism, the optimal input weight  $b_s^{ideal(1)}$  of each bidder is used to calculate the cross-evaluation value and cross-evaluation matrix of input efficiency of other bidders:

$$u_{k} = \sum_{k=1}^{u} b_{s}^{ideal(1)} x_{si}, i, k \in [1, \cdots, n]$$
(13)

$$u_{ik} = \begin{bmatrix} u_{11} & \cdots & u_{1n} \\ \vdots & \vdots & \vdots \\ u_{n1} & \cdots & u_{nn} \end{bmatrix}$$
(14)

The efficiency value  $u_i$  of the bidder was obtained previously. In Equation (13), all the diagonal elements in the cross-evaluation matrix  $u_{ik}$  are 1. The efficiency value of each bidder is the minimum value of all elements in column k, denoted by  $u_k$ , which is equal to the efficiency value calculated above:

$$k \in [1, \cdots, n] \tag{15}$$

If only self-evaluation value  $u_k$  is used for evaluation, the same situation may occur in  $u_k$ , which will lead to failure to evaluate all bidders completely. Thus, this study presents the concept of comprehensive input efficiency, which is expressed by  $u_k^*$ :

$$u_k^* = \frac{1}{n} \sum_{i=1}^n u_{ik}$$
(16)

Through the DEA evaluation model, which introduces comprehensive input efficiency, in most cases, the bidder can be completely evaluated. The priority order of each bidder can be obtained by comparing the size of  $u_k^*$  directly. However, in special cases,  $u_i$  and  $u_k^*$  can be combined to evaluate bidders. First,  $u_i$  is compared. If  $u_i$  has the same value, then  $u_k^*$  is compared. Additionally, the bigger  $u_k^*$ , the more priority it has. Comprehensive input efficiency requires only one linear programming calculation to rank the efficacy of all bidders. Multiple cross-evaluations are not required. Moreover, this model is more efficient in its evaluation and will not be affected by the number of bidders *i*.

The calculation process of DEA model that introduces difference index or comprehensive input efficiency is shown in Figure 2.

In this section, the DEA basic model is introduced first. Then, cross-evaluation model and balance index model were analyzed. Finally, based on the above analysis, a new DEA ranking model, the comprehensive input efficiency model, is proposed. As a result of the analysis, it is evident that in the cross-evaluation model, multiple evaluation processes are required to achieve a complete ranking. However, the balance index model and the comprehensive input efficiency model only need to calculate one linear programming equation and the second evaluation index  $B_i$  or  $u_k^*$  to obtain more complete ranking results. Thus, the bid evaluation efficiency of the latter two models is higher.



Figure 2. Calculation process of DEA model with balance index or comprehensive input efficiency.

# 4. Case Study

# 4.1. General Information of the Bidding Project

In the first phase of the eastern route of the south-to-north water diversion project, the civil and construction engineering of the Huai'an pumping station was considered as an example. This project is located in Sanbao township, Chuzhou District, Huai'an City, Jiangsu Province, at the intersection of an irrigation canal and a canal, with a design flow of 100 m<sup>3</sup>/s. In conjunction with the completed stations, it was the second step of the first phase of the south-to-north water diversion project. The overall design flow for this step is  $300 \text{ m}^3$ /s, and the total installed capacity, including standby machines, is  $340 \text{ m}^3$ /s. This station is expected to be built on the west side of Huai'an II Station. A distance of 340 m separates the center line of the diversion river from the diversion river of Huai'an II Station, and a distance of 300 m separates the center line of the Station.

The scope of the bidding includes excavation of the upper and lower river diversion, civil construction of the bridge under the station, procurement, and installation of the metal structure of the pump station, hydraulic hoist, and bridge crane. The main works include 650,000 m<sup>3</sup> of earth excavation and filling; 16,500 m<sup>3</sup> of concrete and reinforced concrete; 19,000 m<sup>3</sup> of masonry; 298 t of fabrication and installation of metal structures; four sets of main pump and corresponding equipment installation; eight sets of hydraulic hoist

procurement and installation; and one bridge crane procurement and installation. It will take approximately 24 months to complete the construction.

The bidding process for the pump station project is more complicated than that for the river project, based on the general situation of the project. Therefore, there are relatively high requirements for bidders in the bidding process. In general, the requirements are as follows. It is necessary for the bidder to possess a certificate of qualification of grade I or higher of general contracting for water conservancy and hydropower projects, and for the enterprise legal representative to possess at least five years of construction experience in the field of water conservancy and hydropower projects.

## 4.2. Implementation of Comprehensive Bid Evaluation Mechanism

Since the pump station project is a complex water conservation project, it involves multiple construction management interfaces, which include the installation and debugging of pump station equipment, instruments, and an uncertain construction environment. All of these factors may contribute to an increase in transaction costs. As a result, it is imperative to evaluate the bidders from a variety of perspectives in order to select an excellent winning bidder.

(1) Comprehensive evaluation index system

In addition to the tender offer, the bidder's construction organization design, ability, performance, and credit should also be evaluated. Specific evaluation indicators are shown in Table 2.

Category	Specific Evaluation Index
Torn dow offer $\Lambda$ (47 moints)	Quotation A <sub>11</sub> (45 points)
Tender offer $A_1$ (47 points)	Balance and rationality of quotation $A_{12}$ (2 points)
Construction plan A <sub>2</sub> (48 points)	Construction layout $A_{21}$ (2 points) Construction cofferdam and drainage $A_{22}$ (3 points) Construction progress $A_{23}$ (3 points) Construction equipment and labor allocation $A_{24}$ (3 points) Construction personnel $A_{25}$ (4 points) Quality assurance measures $A_{26}$ (2 points) Concrete works A27 (2 points) Earthworks $A_{28}$ (2 points) Foundation works $A_{29}$ (2 points) Masonry and bedding $A_{210}$ (1 point) Material $A_{211}$ (2 points) Metal structure $A_{212}$ (2 points) Hoist $A_{213}$ (2 points) Procurement and installation of auxiliary equipment of pump station $A_{214}$ (2 points) Electrical equipment $A_{215}$ (3 points) Main engine pump installation and combined trial run $A_{216}$ (5 points) Procurement, installation, and commissioning of crane $A_{217}$ (1 point) Building engineering $A_{218}$ (1.5 points) Civilized construction site $A_{219}$ (1 point) Safety production $A_{220}$ (1 point) Integrity commitment $A_{221}$ (0.5 points)
Performance and credit A <sub>3</sub> (5 points)	Similar engineering experience A <sub>31</sub> (3 points) Enterprise credit A <sub>32</sub> (2 points)

Table 2. Evaluation index of bidders.

(2) Comprehensive scoring mechanism and evaluation results

In total, nine bidders participated in the bidding process. All of their bid documents met the requirements of the bidding documents and passed the prequalification phase, entering into the second phase of the review process.

The bid evaluation committee is composed of nine experts, who respectively score the bidders' evaluation indexes and take the average value as the final score. The total price of the pre-tender estimate is RMB 4,602,000.00, and the composite pre-tender estimate is RMB 46,398,032.17. The owner's pre-tender estimate has a weight coefficient of 0.60. Expert ratings are shown in Table 3.

Table 3. Experts' scores.

Index	Α	В	С	D	Ε	F	G	Н	I
A11	42.2	45	43.4	31.8	27.2	26.4	42.3	43.8	28.00
A12	1.00	1.00	1.00	0.50	1.50	1.00	1.50	0.83	0.00
A21	1.11	2.00	1.51	1.00	1.00	1.50	1.03	2.00	150
A22	1.56	2.50	2.03	2.50	0.56	2.50	2.09	1.06	3.00
A23	3.00	3.00	2.56	2.56	2.06	3.00	3.00	2.56	3.00
A24	3.00	2.50	1.50	1.50	1.50	3.00	2.53	2.92	2.99
A25	3.98	3.98	3.51	3.02	3.98	3.97	3.98	3.51	2.56
A26	2.00	1.53	2.00	1.00	2.00	1.53	1.99	1.99	2.00
A27	1.06	1.99	1.03	1.53	1.06	1.56	1.50	1.56	1.11
A28	1.56	2.00	1.06	1.11	1.06	1.56	1.94	1.50	1.06
A29	4.00	4.94	4.44	4.28	3.67	4.06	4.50	4.44	4.44
A210	1.00	1.00	0.50	1.00	0.50	1.00	1.00	1.00	1.00
A211	2.00	2.00	2.00	1.50	1.00	2.00	2.00	2.00	1.50
A212	2.00	2.00	1.77	1.68	1.50	1.82	1.82	1.91	1.91
A213	1.82	1.82	1.82	1.82	1.82	1.50	1.82	1.91	1.91
A214	2.00	1.50	2.00	2.00	1.00	1.50	2.00	2.00	1.11
A215	1.50	3.00	3.00	2.50	2.00	2.50	3.00	3.00	3.06
A216	3.17	4.50	4.00	4.00	3.56	4.39	3.14	4.50	3.50
A217	0.50	1.00	1.00	1.00	0.28	1.00	1.00	0.42	0.21
A218	1.00	1.50	1.50	1.50	1.00	1.50	1.50	1.00	1.00
A219	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
A220	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
A221	0.50	0.50	0.00	0.50	0.50	0.50	0.00	0.00	0.00
A31	3.00	3.00	3.00	3.00	3.00	1.50	3.00	1.50	3.00
A32	2.00	2.00	2.00	2.00	2.00	2.00	2.00	1.50	2.00
Total points	86.94	96.27	88.63	75.30	65.61	73.39	90.68	88.80	71.51

# (3) Comprehensive score result

According to the bid evaluation method, bidder B is selected as the first winning candidate and G as the second winning candidate. Comprehensive scoring results of nine bidders are shown in the Table 4.

 Table 4. Comprehensive scoring results.

Bidder	Tender Offer (Yuan)	Total Points	Bid Ranking
Α	42,482,107.00	86.9	5
В	44,580,000.00	96.3	1
С	43,019,720.00	88.6	4
D	49,704,915.00	75.3	6
Е	50,760,636.00	65.6	9
F	50,936,817.00	73.4	7
G	46,718,760.00	90.7	2
Н	43,401,777.00	88.8	3
Ι	50,569,755.00	71.8	8

# 4.3. Improvement of Comprehensive Bid Evaluation Mechanism

In this tender, scoring quotations based on the base bid was an unreasonable aspect of comprehensive scoring. Moreover, the bid evaluation results obtained by setting weights are not necessarily appropriate for the comprehensive scoring of the project bid. Therefore, this construction example is analyzed below using an improved DEA evaluation method.

#### Index system conversion and data process

Due to the large number of evaluation indicators in this engineering example, they are grouped together here as follows:  $A_{21} - A_{26}$  are combined into  $I_1$ ;  $A_{27} - A_{217}$  are combined into  $I_2$ ;  $A_{218} - A_{221}$  are combined into  $I_3$ ;  $A_{31} - A_{32}$  are combined into  $I_4$ ;  $I_1$ ,  $I_2$ ,  $I_3$ , and  $I_4$  are taken as input indices; and  $A_{11}$  and  $A_{12}$  are taken as the output indicators  $O_1$  and  $O_2$ .

For data processing, the largest output with the smallest input is obtained; therefore, the above input indicators should be converted into a minimal indicator, while the output index is converted into a maximal index.

If it is determined by the expert scoring system, most input indexes are qualitative. Suppose there are *n* bidders, and *m* experts scored each indicator of the *n* bidders. Each index can be represented by an  $n \times m$  scoring matrix *P*:

$$P = \begin{bmatrix} p_{11} & \cdots & p_{1m} \\ \vdots & \vdots & \vdots \\ p_{n1} & \cdots & p_{nm} \end{bmatrix}$$
(17)

$$\overline{P} = \begin{bmatrix} \overline{P}_1 \\ \vdots \\ \overline{P}_n \end{bmatrix}$$
(18)

where  $p_{nm}$  is the *m* expert's score for the *n* bidder;  $\overline{P_i} = \sum_{j=1}^{m} p_{ij}$  means that the score of *m* experts on the *i*th bidder is averaged. According to the previous analysis, input indicators are processed as minimal indicator data:

$$\overline{P'_i} = \frac{P_{\max} - P_{\min}}{\overline{P_i} - P_{\min}}$$
(19)

 $P'_i$  is the processed data;  $P_{max}$  and  $P_{min}$  are the maximum and minimum values in the expert rating matrix; and  $\overline{P_i}$  is the average of the original expert scores.

The rationality of the quotation in the output index  $O_2$  is a qualitative indicator, which is determined by the expert rating system. According to the previous analysis, the more reasonable the quotation, the higher the score. Thus, it is a maximal index. Suppose there are *m* experts to evaluate this index of these *n* bidders; the expert scoring matrix and mean scoring matrix are shown in Equations (17) and (18):

$$\overline{P'_i} = \frac{\overline{P_i}}{\overline{P_{i\max}}}$$
(20)

where  $\overline{P'_i}$  is the processed data;  $\overline{P_i}$  is the average of the original expert scores; and  $\overline{P_{imax}}$  is the maximum value in the expert average score matrix  $\overline{P}$ .

The bid price indicator in the output indicator no longer uses the method that tender evaluation experts score quotations in engineering tenders based on the base bid. Rather, it evaluates whether a bidder's price is lower than its individual costs based on the level of individual costs determined by the evaluation experts. If less, the bid is rejected. For the bidder whose quotation is judged to be reasonable, the transformation of its quotation index should reflect the principle of market competition, that is, the idea of the lowest-bid mechanism. Additionally, the lower the quotation, the higher the index value. Quotation (bidding period) sequence  $y_i$  ( $i = 1, \dots n$ ), the processing method is as follows:

$$y'_i = 1 + \frac{y_{\min}}{y_{\max}} - \frac{y_i}{y_{\max}}$$
(21)

where  $y'_i$  is the processed value;  $y_{max}$  and  $y_{min}$  are the maximum and minimum values in the bidding sequence; and  $y_i$  is the original bidding sequence, converted to maximal indicators. Evaluation index and data disposed of bidders are shown in Table 5.

Index Data	Α	В	С	D	Ε	F	G	Н	Ι
I <sub>1</sub>	0.7461	0.6509	0.8562	0.8941	1.0000	0.6516	0.7475	0.7890	0.7175
I <sub>2</sub>	0.8842	0.7130	0.8105	0.8545	1.0000	0.8178	0.7705	0.7515	0.8768
$I_3$	0.8750	0.7500	0.8750	0.7500	0.8750	0.7500	0.8750	1.0000	1.0000
$I_4$	0.6000	0.6000	0.6000	0.6000	0.6000	0.9000	0.6000	1.0000	0.6000
O1	1.0000	0.9529	0.9875	0.8547	0.8369	0.8340	0.9093	0.9788	0.8401
O <sub>2</sub>	0.6667	0.6667	0.6667	0.3333	1.0000	0.6667	1.0000	0.5533	0.0000

Table 5. Evaluation index and data disposed of bidders.

(2) Comprehensive bid evaluation analysis based on DEA

Four DEA models with self-efficiency evaluation, cross-evaluation mechanism, balance index model, and comprehensive input efficiency were analyzed and compared. The calculation and ranking results of different models are shown in Table 6.

|--|

Bidder	Self-Evaluation Efficiency	Rank	Cross- Evaluation	Rank	Balance Index	Rank	Comprehensive Input Efficiency	Rank
Α	0.9445	5	0.7842	4	-1.1667	6	1.0833	8
В	1.0000	1	0.9012	2	-1.5175	1	1.1897	1
С	0.9682	4	0.8027	3	-1.1667	6	1.1458	5
D	0.7067	8	0.5368	7	-1.3146	5	1.1643	4
Ε	0.7778	7	0.4632	8	-1.1154	9	1.0955	7
F	1.0000	1	0.6599	5	-1.3333	3	1.1666	3
G	1.0000	1	0.9357	1	-1.3153	4	1.1841	2
Н	0.9234	6	0.5515	6	-1.4129	2	1.1254	6
I	0.6222	9	0.3315	9	-1.1667	6	1.0625	9

It can be seen that the top three bidders with better self-evaluation efficiency are B, F, and G (relative efficiency value reaches 1). In the cross-evaluation model and margin (balance) index models, such results were not obtained; however, they were obtained in the comprehensive input efficiency model analysis. As a result, the comprehensive input efficiency model analysis. As a result, the comprehensive input efficiency model in this research is more scientific and reasonable than the other three models.

(3) Analysis of evaluation results

The evaluation results in comprehensive scoring bidding and under different bid evaluation models are shown in Table 7.

It can be seen that the quantitative model evaluation is consistent with quantitative scoring. The results of the comprehensive input efficiency model are consistent with those of the integrated score. Additionally, the first winning bidder and the second winning bidder are the same. It indicates that the scoring weight adopted in the bidding process of this project is relatively reasonable, evaluating the outstanding winning bidder. Through this case, the rationality of the comprehensive input efficiency model is demonstrated in practice. Additionally, the results indicate that the comprehensive input efficiency model is demonstrated in the second winning bidder.

Bidder	Comprehensive Score	Balance Index Model	Comprehensive Input Efficiency Model
Α	5	6	8
В	1	1	1
С	4	6	5
D	6	5	4
Е	9	9	7
F	7	3	3
G	2	4	2
Н	3	2	6
Ι	8	6	9

a simple, operational model that project tenderers can use to evaluate bidders efficiently and accurately.

Table 7. Result under different bidding evaluation methods.

# 5. Conclusions and Discussions

By incorporating the DEA method into comprehensive bid evaluation, this research also proposed a comprehensive input efficiency model based on the existing cross-evaluation ranking mechanisms and difference index model. Additionally, through a case study, this research explores the application of the bid evaluation model systematically and further proves the scientific validity and applicability of the model.

First, this research introduces the basic DEA model. In light of the differences between the engineering bid evaluation process and the DEA method evaluation process, it is necessary to process the input and output index data before applying the DEA method to construction project evaluation. Considering this difference, this research proposed that different data processing methods should be adapted to ensure the feasibility of the DEA method based on the different characteristics of each input and output index in the bid evaluation process. As a result, a new DEA model, namely the comprehensive input efficiency model, was developed. This model extends the research on DEA bid evaluation models, which mainly use a one-input and multiple-output model to assess bidders.

Second, it is impossible to make a complete evaluation of all DMUs if only selfevaluation values were considered in the course of the DEA model calculation. Thus, this research analyzed and compared three DEA evaluation models in detail. Results showed that to obtain complete evaluation results, the cross-evaluation ranking mechanism needed to conduct further cross-evaluation. In contrast, the difference index  $B_i$  and comprehensive input efficiency  $u_k^*$  model only needed to solve linear programming equations and calculate the second evaluation index  $B_i$  or  $u_k^*$ . Thus, the latter two models were more effective, which extends the comprehensive bid evaluation model based on the DEA method theoretically. These findings address the shortcoming of how the evaluation process of the cross-evaluation mechanism is too cumbersome. Furthermore, the comprehensive input efficiency model simplifies and streamlines the evaluation process compared to previous evaluation models that incorporated DEA and other methods.

The civil and construction engineering of the Huai'an pumping station in the first phase of the eastern route of the south-to-north water diversion project was taken as an example. As a result of applying the theories and methods proposed in this research comprehensively, the results indicate that the comprehensive input efficiency model is more scientifically sound and reasonable than the other three models (self-evaluation efficiency model, cross-evaluation mechanism, and balance indicator model). It is further demonstrated that the model is scientifically valid and practical from a practical point of view.

This article can provide some insightful information for tenderers who assess bidders. First, this research summarized and proposed the bid evaluation indexes and methods which can be used to reflect the contractors' capabilities. Moreover, these indexes and methods are suitable for application and grassroots promotion. Therefore, tenderers can use this template to determine the bidder evaluation indicators for the actual projects. In addition, the traditional comprehensive bid evaluation method is highly subjective, and the application of existing bid evaluation models is complex and impractical. Therefore, this research presented a comprehensive input efficiency model based on the cross-evaluation ranking mechanism and balance index models. Through practical examples, the comprehensive input efficiency model has also been demonstrated to simplify bid evaluation, improve bid evaluation efficiency, reduce subjectivity in weight determination, and provide a more comprehensive and credible ranking of bidders.

Further research can be conducted in the following directions. First, the input values of DEA are set to 1.0 to simplify the assumption that all bidders will do their best to prepare their proposals for the competition. It would be beneficial to explore a new model to overcome this simplification. Additionally, the case studies here are limited to construction work. In the future, research may be conducted to apply DEA to other types of projects, including service projects, real estate, and consulting services.

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