



Article Stability and Thermophysical Properties of GNP-Fe₂O₃ Hybrid Nanofluid: Effect of Volume Fraction and Temperature

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Abstract: The study focused on the impact of concentration and temperature on the electrical conductivity, viscosity, and thermal conductivity of GNP/Fe_2O_3 hybrid nanofluids. The study found that nanofluids have better electrical conductivity, viscosity, and thermal conductivity than water. The electrical conductivity and thermal conductivity increase linearly with concentration for a constant temperature. However, the nanofluid's viscosity increases with the addition of the hybrid nanoparticles and decreases as the temperature increases. Furthermore, the study shows that the thermal conductivity of the nanofluid is enhanced with increased addition of hybrid nanoparticles in the base fluid and that the thermal conductivity ratio increases with increased addition of nanoparticles. Overall, the results suggest that GNP/Fe_2O_3 hybrid nanofluids could be used in various industrial applications to improve the heat transfer and energy efficiency of systems.

Keywords: hybrid nanofluids; graphene nanoplatelets; iron oxide; thermal conductivity; viscosity; heat transfer efficacy

1. Introduction

Modern machinery and many industrial applications employ traditional cooling fluids such as water, engine oil and glycols for heat transfer applications. The creation of incredibly effective heat transfer devices is greatly influenced by the thermophysical properties of these fluids. However, these fluids exhibit low to modest thermal conductivity (λ), which led to the development of nano-solid-liquid suspensions aimed at improving the λ of common heat transfer fluids. This nano-suspension was first created by Choi et al. in 1995 by adding copper nanoparticles into water [1]. Due to the extraordinary thermal and flow characteristics that the nanofluid exhibits in comparison to those of traditional thermal transportation medium [2–4], this unique fluid is the focus of considerable global research. It is projected that nanofluids will be widely used in the future to improve a variety of industrial applications.

Graphene, which is a carbonaceous nanomaterial, is one of the most promising materials for the preparation of nanofluids. This is due to its exceptional thermophysical characteristics, including its great mechanical strength and impressive λ [2,5,6]. A wide variety of other studies [7–9] on the thermophysical properties of graphene and other nanomaterials have been conducted. However, in recent years, a new form of nanofluid which comprises two or more different nanomaterials was created in a bid to improve the thermophysical properties and save costs [10,11]. These nanofluids are known as hybrid nanofluids.



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Borode et al. [12] studied the thermophysical properties of hybrid GNP/Al_2O_3 nanofluid of different particle size ratio in comparison to single GNP nanofluid. The single GNP nanofluid was reported to exhibit a higher λ than the hybrid nanofluids. Notwithstanding, hybridization of the nanofluid was found to reduce the μ of the single GNP nanofluid, which subsequently caused an improvement in the natural convective performance of the nanofluids. The λ and μ of Al₂O₃-Cu hybrid nanofluids with different volume contents at room temperature were investigated by Suresh et al [13]. When compared to water, they reported an increase of up to 12.11% and 115% in λ and μ , respectively. Wole-Osho et al. [14] assessed the thermophysical properties of an alumina-ZnO hybrid nanofluid with various mixture ratios for application in a photovoltaic thermal collector. They noticed an increment in the λ and μ with all the addition of the hybrid nanomaterials and with an increase in their nanomaterial loading. Giwa et al. [15] studied the μ and σ of a MWCNT-Fe₂O₃ hybrid nanofluid. They observed an enhancement in the properties with an increase in the nanomaterial loading. Adun et al. [16] investigated the effects of temperature, volume concentration, and mixing ratios of alumina-ZnO-Fe3O4 ternary hybrid nanofluids (THNF) on their λ and μ . Three THNF mixture ratios (1:1:1, 1:2:1, and 1:1:2) were synthesized at volume concentrations of 0.5%, 0.75%, 1%, and 1.25%, and all experiments were conducted at temperatures between 25 °C and 65 °C. The results showed that temperature and volume concentration significantly affected the thermophysical properties of the fluid, and the 1:1:1 mixture ratio had the highest λ enhancement of 36.018%. Additionally, the 1:1:1 mixture ratio had the lowest viscosity, while the 2:1:1 THNF mixture ratio had the highest viscosity.

The literature and a host of other studies [17–20] provide evidence that the thermophysical properties of base fluids will improve with the application of hybrid nanoparticles. Thus, the thermophysical properties of graphene-based nanofluids can be further enhanced through hybridization. However, as far as the authors are aware, little to no study has been completed on the graphene-based ferrofluid.

This study aims to investigate the effect of concentration and temperature on the thermophysical properties of a novel hybrid GNP/Fe_2O_3 nanofluid with a mixing ratio of 50:50. To the best of the authors' knowledge, no study has been completed using hybrid GNP/Fe₂O₃ nanomaterial. The choice of GNP/Fe₂O₃ in the formulation of a hybrid nanofluid is based on the desired properties of the resulting fluid. GNPs have high thermal conductivity and stability, making them attractive as heat transfer enhancers in nanofluids [2]. On the other hand, Fe_2O_3 nanoparticles are readily available and cost-effective compared to other types of nanoparticles such as metals or carbon nanotubes [21]. This makes them an attractive choice in the development of efficient and affordable nanofluids. Additionally, Fe_2O_3 nanoparticles are magnetic [22], allowing for easy manipulation and separation of the nanofluid using an external magnetic field. Fe₂O₃ nanoparticles are also known to produce stable water-based nanofluids, which have been extensively studied in the literature [23-25]. This suggests that incorporating Fe₂O₃ nanoparticles into a hybrid nanofluid could improve its stability and overall performance. Therefore, the combination of GNP and Fe₂O₃ in a hybrid nanofluid can potentially enhance its thermal conductivity and convective heat transfer while allowing for easy separation and reusability. The stability of the nanofluids was evaluated using a visual observation approach and TEM analysis. The study was performed for volume concentrations ranging from 0.1 vol% to 0.4 vol%. The temperature ranged between 15 °C and 40 °C for the thermal conductivity λ measurement, while it ranged between 15 $^{\circ}$ C and 55 $^{\circ}$ C for the μ and electrical conductivity (σ) measurements. Finally, a novel correlation was developed using regression analysis to estimate the measured thermophysical characteristics of the hybrid nanofluid as a function of temperature and concentration.

2. Materials and Methods

In this study, deionized water was used as the base fluid due to its higher λ_{water} and lower μ_{water} compared to other base fluids such as ethylene glycol. The hybrid nanofluid

was prepared using a mixture of GNP and nanomagnetic Fe₂O₃ with a weight ratio of 50:50. The GNP nanomaterial with thickness of 15 nm and specific surface area of 50–80 m²/g was acquired from Sigma Aldrich (DE), while the Fe₂O₃ with length of 10–30 μ m and external diameter of 10–20 nm was obtained from MKnano Company (CA). The hybrid nanofluids were stabilized using SDS surfactant obtained from Sigma Aldrich (DE) at a nanoparticle/surfactant ratio of 1:1. Equation (1) was used to compute the weight of the nanomaterials (φ).

$$\varphi = \frac{\omega_{GNP}(\frac{m}{\rho})_{GNP} + \omega_{Fe_2O_3}(\frac{m}{\rho})_{Fe_2O_3}}{\omega_{GNP}(\frac{m}{\rho})_{GNP} + \omega_{Fe_2O_3}(\frac{m}{\rho})_{Fe_2O_3} + (\frac{m}{\rho})_{water}}$$
(1)

where ω , *m*, ρ is the weight fraction, mass and density of the nanoparticle, respectively.

The hybrid nanofluids were prepared by first dispersing the nanoparticles and surfactant in deionized water using a Q-700 Qsonica ultrasonic agitator for an optimum time to ensure proper dispersion. During the agitation process, the nanofluid was placed in a water bath (LAUDA ECO) with a set temperature of 20 °C to avoid overheating and evaporation. Further, the stability of the nanofluid was monitored using visual observation technique and TEM. To achieve stable hybrid nanofluids, the sonication time needed to be optimized. The pH and σ are useful properties for determining the critical micelle concentration (CMC) of the surfactant used in nanofluid preparation [15]. The CMC is the point at which surfactant molecules form micelles that can stabilize nanoparticles in the nanofluid [26]. The CMC is identified as the inflection point in the pH and σ curve for varying sonication time. In this study, the optimum sonication time was determined by monitoring the pH and σ of the hybrid nanofluid for different sonication times at an ambient temperature as shown in Figure 1. A point of inflection was observed for the two properties at 45 min to indicate the optimum sonication time used to prepare all the hybrid nanofluid used in this study.



Figure 1. pH and electrical conductivity as a function of ultrasonication time.

The hybrid nanofluids were characterized by measuring their μ , λ and σ using a Vibroviscometer (SV-10), KD-2 Pro meter, and EUTECH electrical conductivity meter (CON700),

respectively. The μ and σ were measured for a temperature range between 15 °C and 55 °C, and a water bath (LAUDA ECO) was used to regulate the temperature. Additionally, the λ was measured at a temperature range between 15 °C and 40 °C.

The electrical conductivity meter was calibrated using the calibration fluid provided by the manufacturer, and the standard fluid was measured three times at room temperature to obtain an average value of 1414 μ S/m, which was found to be close to the manufacturer's specified value of 1413 μ S/m. The reliability of both the viscometer and KD2Pro Meter was assessed by measuring their μ and λ and comparing them to the established standard values for water found the literature.

To ensure accurate measurement of the thermophysical properties (P), potential sources of error were identified, including the measurement of the weight of nanomaterials and surfactants (W), volume of water (V), and temperature (T). These errors were accounted for by using Equation (2) to estimate the uncertainty (e) associated with the properties.

$$e(\%) = \pm \sqrt{\left(\frac{\partial P}{P}\right)^2 + \left(\frac{\partial W}{W}\right)^2 + \left(\frac{\partial V}{V}\right)^2 + \left(\frac{\partial T}{T}\right)^2}$$
(2)

The degree of uncertainty associated with the measurement of σ is $\pm 2.06\%$, while for λ and μ , it is $\pm 2.12\%$ and $\pm 2.07\%$, respectively.

3. Results and Discussion

3.1. Nanofluid Stability

Figure 2 displays the TEM micrograph of the GNP/Fe₂O₃ hybrid nanofluid. The homogenous dispersion of the GNP and Fe₂O₃ nanomaterials is clearly evident in the micrograph. To demonstrate the nanofluids' improved stability, other stability evaluation techniques, including visual and μ measurement techniques, were employed. The photographic image of the nanofluids after 4 days is presented in Figure 3. To validate the stability, the μ_{HNF} was also monitored for 24 h, as illustrated in Figure 4. It is evident that the nanofluid with 0.1 vol% and 0.3 vol% maintains average stability over a period of 24 h due to the negligible changes in the μ_{HNF} over the examined duration.



Figure 2. TEM Images of the GNP/Fe₂O₃ hybrid nanofluid.



Figure 3. Photographs of the hybrid nanofluids 4 days after preparation.



Figure 4. Viscosity-based stability measurement for 0.1 vol% and 0.3 vol% hybrid nanofluids.

3.2. Viscosity

A fluid's dynamic viscosity is the key component that determines how it behaves and travels in close proximity to solid boundaries. Additionally, it demonstrates a considerable influence on the pressure drop and pumping efficiency in any industrial system. Figure 5 shows the results of a measurement of the viscosity (μ_{HNF}) of a GNP/Fe₂O₃ hybrid nanofluid at volume concentration of 0.1–0.4% and temperatures of 15–40 °C. Considering the changes in μ_{HNF} at various volume concentrations, it can be seen that adding GNP/Fe₂O₃ nanoparticles at a steady temperature increases the μ_{HNF} .

Whilst also analyzing the changes in μ_{HNF} at various temperatures as shown in Figure 6, it is easy to see that, for a given volume fraction, the μ_{HNF} declines as temperature rises. The increase in temperature accelerates the Brownian motion of fluid molecules, which is what causes the μ_{HNF} to lower. By increasing the frequency of molecular collisions

as the velocity increases and decreasing the intermolecular interactions, μ_{HNF} lowers. Because temperature enhances the Brownian motion, there is an inverse relationship between temperature and μ_{HNF} .



Figure 5. Influence of concentration on the viscosity of the hybrid nanofluids at various temperatures.



Figure 6. Influence of temperature on the viscosity of the hybrid nanofluids at various concentrations.

The μ_{HNF} is decreased as a result of the lessening of intermolecular forces. In other words, μ_{HNF} decreases as temperature increases. Another explanation is that when the temperature rises, the distance between molecules in the base fluid and the nanoparticles shortens, thus, reducing μ_{HNF} and flow resistance. This study outcome is well-supported and validated by the existing literature [12,27,28].

The relative dynamic viscosity ($\mu_{relative}$) is presented in Figures 7 and 8 as a function of concentration and temperature, respectively. Figure 7 shows that there is an augmentation in the $\mu_{relative}$ with an increased addition of hybrid nanoparticles in the nanofluids. This observation is well-supported by the existing literature [15,16,21]. This increase in $\mu_{relative}$

could be attributed to the build-up of some agglomerates with a rising concentration within the nanofluid. Figure 8 shows a slight diminution in $\mu_{relative}$ with an increase in temperature from 15 °C to 20 °C. However, an increase in temperature above 20 °C results in an increase in the $\mu_{relative}$. According to this study, a μ increment of 3.22–8.77%, 4.30–10.53%, 6.45–12.28% and 8.60–15.79% was observed for the hybrid nanofluid with GNP/Fe₂O₃ loading of 0.10, 0.20, 0.30 and 0.40 vol% respectively at 15–40 °C.



Figure 7. Influence of concentration on the relative viscosity of the hybrid nanofluids at various temperatures.



Figure 8. Influence of temperature on the relative viscosity of the hybrid nanofluids at various concentrations.

3.3. Thermal Conductivity

The thermal conductivity (λ_{HNF}) of a hybrid GNP/Fe₂O₃ nanofluid at volume fractions of 0.1–0.4% was assessed at temperature of 15–40 °C. The outcomes are shown in Figures 9–12. Figure 9 shows that at steady temperature the λ_{HNF} is increased in com-

parison to the base fluid by the addition of the hybrid nanoparticles in the base fluid. Additionally, as the volume percentage of nanoparticles grows, the surface-to-volume ratio rises. This process ultimately causes the λ_{HNF} coefficient to rise significantly.



Figure 9. Influence of concentration on the thermal conductivity of the hybrid nanofluids at various temperatures.



Figure 10. Influence of temperature on the thermal conductivity of the hybrid nanofluids at various concentrations.



Figure 11. Influence of concentration on the thermal conductivity ratio of the hybrid nanofluids at various temperatures.



Figure 12. Influence of temperature on the thermal conductivity ratio of the hybrid nanofluids at various concentrations.

Additionally, when the volume fraction grows, there are more intermolecular collisions between molecules, which increases the amount of temperature effects on the λ_{HNF} coefficient. The effect of temperature is further illustrated in Figure 10, as the λ_{HNF} is augmented at a higher temperature. The primary causes of the increase in fluid λ_{HNF}

with temperature are Brownian motion and collisions between nanoparticles [29]. This augmentation can also be attributed to improved heat transfer at particle-fluid interface.

The thermal conductivity ratio (λ_{ratio}) is presented in Figures 11 and 12 as a function of concentration and temperature, respectively. Figure 11 shows that there is an augmentation in the λ_{ratio} with an increased addition of hybrid nanoparticles in the nanofluids. This increase could be attributed to the build-up of some agglomerates with a rising concentration within the nanofluid. Figure 12 shows a slight diminution in λ_{ratio} with an increase in temperature from 15 °C to 20 °C. However, an increase in temperature from 20 °C to 30 °C results in an increase in the λ_{ratio} before it declines as the temperature is increased to 40 °C. The λ_{ratio} is influenced by the intermolecular forces between the nanoparticles and the base fluid. When the temperature is raised from 15 °C to 20 °C, the intermolecular forces between the nanoparticles and the base fluid start to weaken due to thermal motion and vibrations of the particles, which causes a reduction in λ_{ratio} . However, as the temperature is further elevated from 20 °C to 25 °C, the Brownian motion of the nanoparticles becomes more significant, leading to better dispersion and contact between the nanomaterial and the base fluid. As a result, the intermolecular forces increase, leading to an increase in λ_{ratio} . At higher temperatures above 30 °C, the λ_{ratio} starts to decrease again due to the formation of agglomerates and the decrease in intermolecular forces caused by the increased thermal motion of the particles. This behavior is commonly observed in nanofluids and is attributed to the complex interplay between the thermal energy, Brownian motion, and intermolecular forces between the nanoparticles and the base fluid. It is important to note that the exact reasons for the observed trends in λ_{ratio} may depend on several factors, such as the type and size of the nanoparticles and the experimental conditions. Therefore, further research may be needed to fully understand the underlying mechanisms.

According to this study, a thermal conductivity augmentation of 6.36–10.85%, 8.29–11.45%, 8.94–13.35% and 10.30–16.83% was observed for the hybrid nanofluid with a nanoparticle loading of 0.10, 0.20, 0.30, and 0.40 vol% respectively at 15–40 °C. The λ_{HNF} results and trends of this study are well supported and validated by existing studies [12,30,31].

3.4. Electrical Conductivity

Although it has not received much attention, σ is a crucial feature for the technical application of nanofluids. Figures 13 and 14 depict the effect of concentration and temperature, respectively on the electrical conductivity of the GNP/Fe₂O₃ hybrid nanofluid (σ_{HNF}). The figures show that, when compared to water, all nanofluids have a better σ_{HNF} than water. Similar to the λ_{HNF} observation, the σ_{HNF} increases linearly with concentration for a constant temperature. The improvement in σ_{HNF} is facilitated by the formation of the electrical double layer (EDL) on the surface of the hybrid nanoparticle when dispersed in deionized water. The formation of the EDL is impacted by the polarity of water, which advances the growth of charges on the hybrid nanofluid's surface and subsequently transfers charges into the nanofluid solution.

As shown in Figure 14, the σ_{HNF} of the GNP/Fe₂O₃ hybrid nanofluid also rises with an increase in the nanoparticle loading, following a similar pattern to that of the thermal conductivity. The temperature-induced augmentation could be ascribed to the fact that an elevated temperature makes ions more mobile, subsequently augmenting the σ_{HNF} . This improved ion mobility can be attributed to the Brownian motion of the nanomaterials in the base fluid, which can enhance the contact between particles and result in more efficient electrical conduction paths. This increased Brownian motion can also disrupt the electric double layer surrounding the particles, resulting in a decrease in the electrical resistance and an increase in the σ_{HNF} . In addition, the temperature elevation results in a reduction in the μ_{HNF} , which subsequently improves the mobility of the nanoparticles and promotes their suspension stability in the fluid. This can facilitate the formation of conductive pathways between the particles, leading to an increase in σ_{HNF} . The increase in σ_{HNF} with increasing nanoparticle loading and temperature is consistent with previous studies [7,12,30] on the electrical properties of nanofluids.



Figure 13. Influence of temperature on the electrical conductivity of the hybrid nanofluids at various concentrations.



Figure 14. Influence of concentration on the electrical conductivity of the hybrid nanofluids at various temperatures.

The σ_{ratio} is presented in Figures 15 and 16 as a function of concentration and temperature, respectively. It can be observed that there is a linear increase in σ_{ratio} with an increase in concentration and temperature. At constant temperature of 15 °C, the σ_{water} is augmented by 108.97% with the addition of 0.1 vol% GNP/Fe₂O₃ nanoparticle up to

300.38% for 0.4 vol%. Moreover, with a nanomaterial loading of 0.1 vol%, the σ_{HNF} is increased from enhancement of 108.97% at 15 °C up to 119.86% at 55 °C. The maximum enhancement was observed to be 351.26% for 0.4 vol% hybrid nanofluid at 55 °C.



Figure 15. Influence of concentration on the electrical conductivity ratio of the hybrid nanofluids at various temperatures.



Figure 16. Influence of temperature on the electrical conductivity ratio of the hybrid nanofluids at various concentrations.

3.5. Heat Transfer Efficacy

To evaluate the cooling effectiveness or heat transfer efficacy of the hybrid nanofluid, the idea of properties enhancement ratio (PER) is utilized [32]. The *PER* of nanofluids is typically calculated based on the λ_{HNF} and μ_{HNF} , which are key parameters governing the heat transfer performance of the fluid. The PER can be calculated using Equation (1) [33].

$$PER = \frac{(\mu_{relative} - 1)}{(\lambda_{ratio} - 1)}$$
(3)

It is important to note that hybrid nanofluids have high potential for heat transfer when the *PER* value is below 5, while a nanofluid with a *PER* value higher than 5 demonstrates poor thermal performance [32]. Thus, a lower *PER* value indicates better heat transfer performance for nanofluids as a cooling medium.

In Figure 17, the *PER* of the hybrid nanofluids is illustrated as a function of volume fraction and temperature. The results indicate that all the prepared hybrid nanofluids are suitable as coolants, as their *PER* values are much lower than 5, with the highest value of 1.31 obtained for a GNP/Fe₂O₃ loading of 0.4 at 20 °C. This shows that an increase in the concentration of nanoparticles raises the *PER* value. However, there is a reduction in the *PER* value when the temperature is elevated. This could be attributed to the temperature-induced reduction in μ_{HNF} and augmentation in λ_{HNF} due to Brownian motion. The low *PER* values observed in this study indicate that GNP/Fe₂O₃ hybrid nanofluids are favrable for high temperature applications.



Figure 17. PER values of the hybrid nanofluid in relation to temperature and concentration.

3.6. Correlation

Various models have been used to predict the thermophysical properties of nanofluids, but classical models may not be suitable for predicting the properties of advanced nanofluids such as hybrid nanofluids [15,34–36]. Thus, new models are needed to accurately predict the properties of these advanced nanofluids. In this study, the authors used experimental data to develop prediction models for the thermophysical properties of the hybrid nanofluids. Regression analysis was used to create correlations between volume fraction, temperature, and the experimental data (λ_{ratio} , $\mu_{relative}$ and σ_{ratio}) of the nanofluids, allowing for predictions of these properties.

Table 1 shows the correlation equation, Pearson correlation coefficient (R), the correlation of determination (R²), and the root-mean-square error (RSME) developed for the temperature-dependent λ_{ratio} , $\mu_{relative}$, and σ_{ratio} of GNP-Fe₂O₃ hybrid nanofluids at different nanomaterial loading. All the correlations demonstrated high correlation coefficients, with considerably low errors, as indicated by these variables in Table 1. The linear fitting of the experimental and predicted values of the thermophysical properties are shown in Figure 18A–C. The figures indicate that there is a strong correlation between the predicted data and the experimental data for all the properties with minimal deviations as observed in Figure 18A,B. It was noticed that the established relationship between μ_{HNF} and λ_{HNF} was able to forecast the experimental results with a margin of deviation (MOD) within a range from –2.14 to 2.99% and –2.08 to 2.07%, correspondingly. Similarly, the range of difference between the predicted and experimental values of σ_{HNF} was found to be between –5.14 and 4.35%.

Table 1. Correlation equation for the thermophysical properties of the GNP-Fe₂O₃ hybrid nanofluid.

Property	Equation	R	R ²	RSME
μ _{relative}	$\frac{\mu_{HNF}}{\mu_{Water}} = 0.96360 + 0.2852\varphi + 0.001393T$	0.91999	0.8464	0.015968
λ_{ratio}	$\frac{\lambda_{HNF}}{\lambda_{Water}} = 1.01568 + 0.1625 \varphi + 0.001811T$	0.91291	0.8334	0.010666
σ_{ratio}	$rac{\sigma_{HNE}^{r}}{\sigma_{Water}} = 1.17200 + 7.1380 arphi + 0.007740 T$	0.99596	0.9919	0.072709



Figure 18. Linear fitting of the experimental and predicted values of the thermophysical properties. **(A)** Relative viscosity; **(B)** Thermal Conductivity Ratio; **(C)** Electrical Conductivity Ratio.

4. Conclusions

This study investigated the impacts of concentration and temperature on the σ_{HNF} , μ_{HNF} , and λ_{HNF} of GNP/Fe₂O₃ hybrid nanofluids. The findings showed that the σ_{HNF} , λ_{HNF} , and μ_{HNF} were notably increased in comparison to the base fluid. The boost in electrical conductivity was due to the creation of an electrical double layer (EDL) on the surface of the hybrid nanoparticles, which was influenced by the polarity of water. The λ_{HNF} increase was ascribed to the increase in the surface-to-volume ratio and the number of intermolecular collisions between nanoparticles. Brownian motion and collisions between nanoparticles were identified as one of the primary causes of the increase in λ_{HNF} with temperature.

Furthermore, the μ_{HNF} was found to increase with the addition of nanoparticles at a steady temperature, while it decreased with an increase in temperature due to the lessening of intermolecular forces. The increase in $\mu_{relative}$ with an increase in concentration was attributed to the formation of some agglomerates within the nanofluid. In addition, the regression formula developed to establish the relationship between σ_{HNF} , λ_{HNF} , and μ_{HNF} as a function of temperature and concentration corresponds well with the experimental data.

Overall, the results suggest that GNP/Fe_2O_3 hybrid nanofluids have excellent thermal and electrical conductivity properties, which make them suitable for various industrial applications such as heat transfer fluids, lubricants, and coolants. However, the study also highlights the importance of careful consideration of the concentration and temperature effects on the properties of nanofluids, as they can significantly impact the performance of the fluid in various applications.

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References

- Eastman, J.; Choi, U.S.; Li, S.; Thompson, L.J.; Lee, S. Enhanced Thermal Conductivity Through the Development of Nanofluids. MRS Online Proc. Libr. 1996, 457, 3. [CrossRef]
- Borode, A.O.; Ahmed, N.A.; Olubambi, P.A. A review of heat transfer application of carbon-based nanofluid in heat exchangers. Nano-Struct. Nano-Objects 2019, 20, 100394. [CrossRef]
- Elsheikh, A.H.H.; Sharshir, S.W.W.; Mostafa, M.E.; Essa, F.A.A.; Ali, M.K.A. Applications of nanofluids in solar energy: A review of recent advances. *Renew. Sustain. Energy Rev.* 2018, 82, 3483–3502. [CrossRef]
- 4. Khanafer, K.; Vafai, K. A review on the applications of nanofluids in solar energy field. Renew. Energy 2018, 123, 398–406. [CrossRef]
- 5. Ahmadi, A.; Ganji, D.D.; Jafarkazemi, F. Analysis of utilizing Graphene nanoplatelets to enhance thermal performance of flat plate solar collectors. *Energy Convers. Manag.* **2016**, *126*, 1–11. [CrossRef]
- Wang, Y.; Al-Saaidi, H.A.I.; Kong, M.; Alvarado, J.L. Thermophysical performance of graphene based aqueous nanofluids. *Int. J. Heat Mass Transf.* 2018, 119, 408–417. [CrossRef]
- Borode, A.O.; Ahmed, N.A.; Olubambi, P.A.; Sharifpur, M.; Meyer, J.P. Effect of Various Surfactants on the Viscosity, Thermal and Electrical Conductivity of Graphene Nanoplatelets Nanofluid. *Int. J. Thermophys.* 2021, 42, 158. [CrossRef]
- 8. Selvam, C.; Lal, D.M.; Harish, S.; Lal, D.M.; Harish, S. Enhanced heat transfer performance of an automobile radiator with graphene based suspensions. *Appl. Therm. Eng.* **2017**, *123*, 50–60. [CrossRef]
- Osama, M.; Singh, A.; Walvekar, R.; Khalid, M.; Gupta, T.C.S.M.; Yin, W.W. Recent developments and performance review of metal working fluids. *Tribol. Int.* 2017, 114, 389–401. [CrossRef]

- 10. Esfe, M.H.; Esfandeh, S.; Kamyab, M.H. History and introduction. In *Hybrid Nanofluids for Convection Heat Transfer*; ACM: New York, NY, USA, 2020; pp. 1–48. [CrossRef]
- Scott, T.O.; Ewim, D.R.E.; Eloka-Eboka, A.C. Hybrid nanofluids flow and heat transfer in cavities: A technological review. *Int. J. Low-Carbon Technol.* 2022, 17, 1104–1123. [CrossRef]
- Borode, A.O.; Ahmed, N.A.; Olubambi, P.A.; Sharifpur, M.; Meyer, J.P. Investigation of the Thermal Conductivity, Viscosity, and Thermal Performance of Graphene Nanoplatelet-Alumina Hybrid Nanofluid in a Differentially Heated Cavity. *Front. Energy Res.* 2021, 9, 737915. [CrossRef]
- 13. Suresh, S.; Venkitaraj, K.P.; Selvakumar, P.; Chandrasekar, M. Synthesis of Al₂O₃-Cu/water hybrid nanofluids using two step method and its thermo physical properties. *Colloids Surf. A Physicochem. Eng. Asp.* **2011**, *388*, 41–48. [CrossRef]
- 14. Wole-Osho, I.; Adun, H.; Adedeji, M.; Okonkwo, E.C.; Kavaz, D.; Dagbasi, M. Effect of hybrid nanofluids mixture ratio on the performance of a photovoltaic thermal collector. *Int. J. Energy Res.* **2020**, *44*, 9064–9081. [CrossRef]
- 15. Giwa, S.O.; Sharifpur, M.; Ahmadi, M.H.; Murshed, S.M.S.; Meyer, J.P. Experimental Investigation on Stability, Viscosity, and Electrical Conductivity of Water-Based Hybrid Nanofluid of MWCNT-Fe₂O₃. *Nanomaterials* **2021**, *11*, 136. [CrossRef] [PubMed]
- Adun, H.; Kavaz, D.; Dagbasi, M.; Umar, H.; Wole-Osho, I. An experimental investigation of thermal conductivity and dynamic viscosity of Al₂O₃-ZnO-Fe₃O₄ ternary hybrid nanofluid and development of machine learning model. *Powder Technol.* 2021, 394, 1121–1140. [CrossRef]
- 17. Esfe, M.H.; Amiri, M.K.; Alirezaie, A. Thermal conductivity of a hybrid nanofluid. J. Therm. Anal. Calorim. 2018, 134, 1113–1122. [CrossRef]
- 18. Kakavandi, A.; Akbari, M. Experimental investigation of thermal conductivity of nanofluids containing of hybrid nanoparticles suspended in binary base fluids and propose a new correlation. *Int. J. Heat Mass Transf.* **2018**, *124*, 742–751. [CrossRef]
- 19. Sajid, M.U.; Ali, H.M. Thermal conductivity of hybrid nanofluids: A critical review. Int. J. Heat Mass Transf. 2018, 126, 211–234. [CrossRef]
- Nasrin, R.; Hossain, S.; Zahan, I.; Ahmed, K.F.U.; Fayaz, H. Performance analysis of hybrid/single nanofluids on augmentation of heat transport in lid-driven undulated cavity. *Heat Transf.* 2020, 49, 4204–4225. [CrossRef]
- Colla, L.; Fedele, L.; Scattolini, M.; Bobbo, S. Water-Based Fe₂O₃ Nanofluid Characterization: Thermal Conductivity and Viscosity Measurements and Correlation. *Adv. Mech. Eng.* 2012, *4*, 674947. [CrossRef]
- Krasia-Christoforou, T.; Socoliuc, V.; Knudsen, K.D.; Tombácz, E.; Turcu, R.; Vékás, L. From Single-Core Nanoparticles in Ferrofluids to Multi-Core Magnetic Nanocomposites: Assembly Strategies, Structure, and Magnetic Behavior. *Nanomaterials* 2020, 10, 2178. [CrossRef] [PubMed]
- 23. Kumar, N.; Sonawane, S.S. Experimental study of Fe₂O₃/water and Fe₂O₃/ethylene glycol nanofluid heat transfer enhancement in a shell and tube heat exchanger. *Int. Commun. Heat Mass Transf.* **2016**, *78*, 277–284. [CrossRef]
- 24. Guo, S.Z.; Li, Y.; Jiang, J.S.; Xie, H.Q. Nanofluids Containing γ-Fe₂O₃ Nanoparticles and Their Heat Transfer Enhancements. *Nanoscale Res. Lett.* **2010**, *5*, 1222–1227. [CrossRef] [PubMed]
- 25. Syarif, D.G.; Prajitno, D.H.; Pane, J.S. Viscosity and CHF of water-γ-Fe₂O₃ nanofluids utilizing γ-Fe₂O₃ nanoparticles synthesized from local material using carbon reduction. *AIP Conf. Proc.* **2018**, *1984*, 020006. [CrossRef]
- Borode, A.O.; Ahmed, N.A.; Olubambi, P.A. Surfactant-aided dispersion of carbon nanomaterials in aqueous solution. *Phys. Fluids* 2019, *31*, 071301. [CrossRef]
- Ilyas, S.U.; Pendyala, R.; Narahari, M. Stability and thermal analysis of MWCNT-thermal oil-based nanofluids. *Colloids Surf. A Physicochem. Eng. Asp.* 2017, 527, 11–22. [CrossRef]
- Devendiran, D.K.; Amirtham, V.A. A review on preparation, characterization, properties and applications of nanofluids. *Renew. Sustain. Energy Rev.* 2016, 60, 21–40. [CrossRef]
- 29. Borode, A.; Ahmed, N.; Olubambi, P. A review of solar collectors using carbon-based nanofluids. J. Clean. Prod. 2019, 241, 118311. [CrossRef]
- 30. Giwa, S.O.; Sharifpur, M.; Meyer, J.P. Experimental investigation into heat transfer performance of water-based magnetic hybrid nanofluids in a rectangular cavity exposed to magnetic excitation. *Int. Commun. Heat Mass Transf.* 2020, *116*, 104698. [CrossRef]
- Khairul, M.A.; Shah, K.; Doroodchi, E.; Azizian, R.; Moghtaderi, B. Effects of surfactant on stability and thermo-physical properties of metal oxide nanofluids. *Int. J. Heat Mass Transf.* 2016, 98, 778–787. [CrossRef]
- Mukherjee, S.; Mishra, P.C.; Chaudhuri, P. Thermo-economic performance analysis of Al₂O₃-water nanofluids—An experimental investigation. J. Mol. Liq. 2019, 299, 112200. [CrossRef]
- Zhai, Y.; Li, L.; Wang, J.; Li, Z. Evaluation of surfactant on stability and thermal performance of Al₂O₃-ethylene glycol (EG) nanofluids. *Powder Technol.* 2018, 343, 215–224. [CrossRef]
- 34. Abdolbaqi, M.K.; Azmi, W.H.; Mamat, R.; Sharma, K.V.; Najafi, G. Experimental investigation of thermal conductivity and electrical conductivity of BioGlycol–water mixture based Al₂O₃ nanofluid. *Appl. Therm. Eng.* **2016**, *102*, 932–941. [CrossRef]
- 35. Saeedi, A.H.; Akbari, M.; Toghraie, D. An experimental study on rheological behavior of a nanofluid containing oxide nanoparticle and proposing a new correlation. *Phys. E Low-Dimens. Syst. Nanostruct.* **2018**, *99*, 285–293. [CrossRef]
- Giwa, S.O.; Sharifpur, M.; Meyer, J.P.; Wongwises, S.; Mahian, O. Experimental measurement of viscosity and electrical conductivity of water-based γ-Al₂O₃/MWCNT hybrid nanofluids with various particle mass ratios. *J. Therm. Anal. Calorim.* 2020, 143, 1037–1050. [CrossRef]

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