

*Supplementary Materials*

# Bayesian Data Assimilation of Temperature Dependence of Solid–Liquid Interfacial Properties of Nickel

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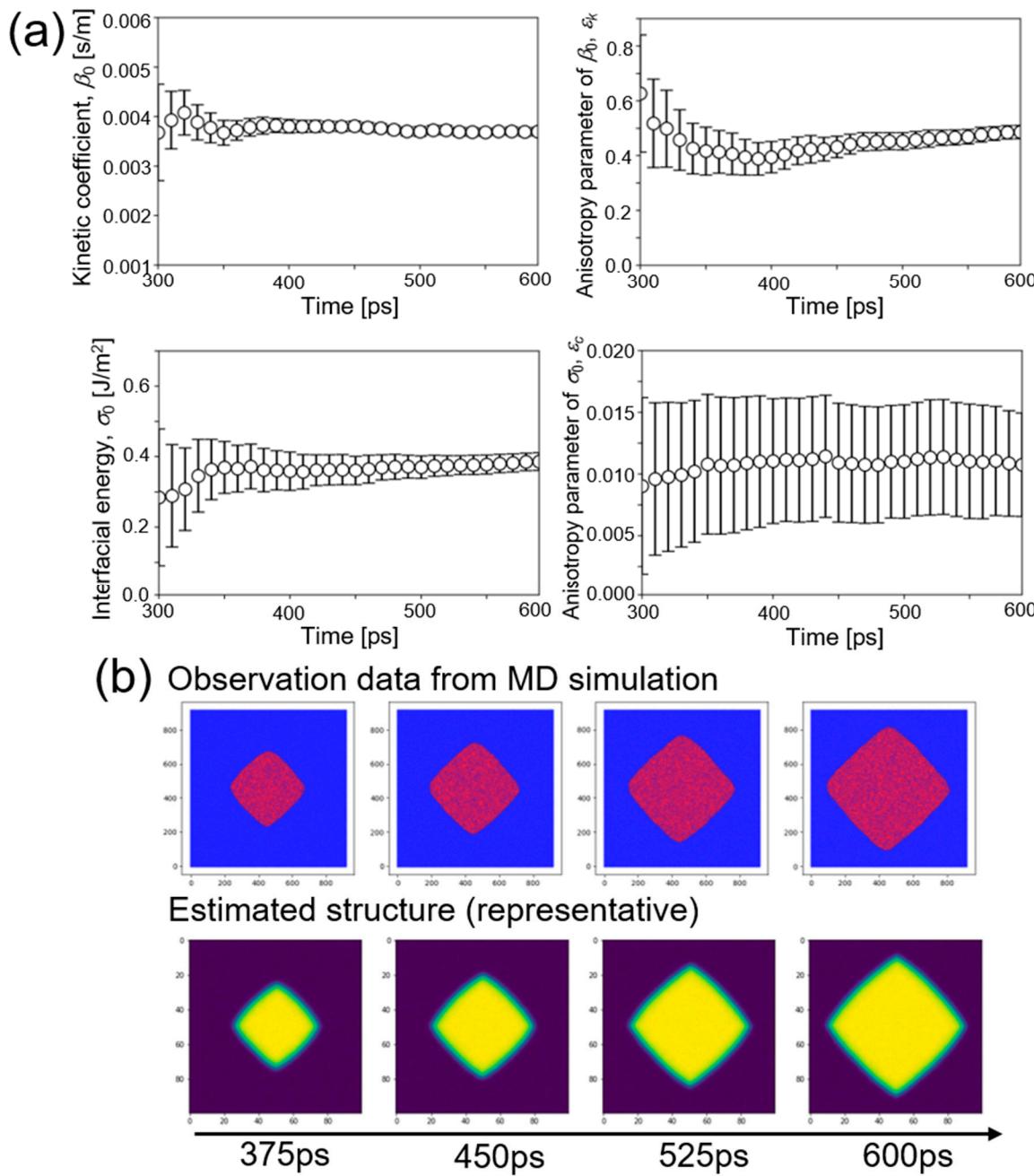
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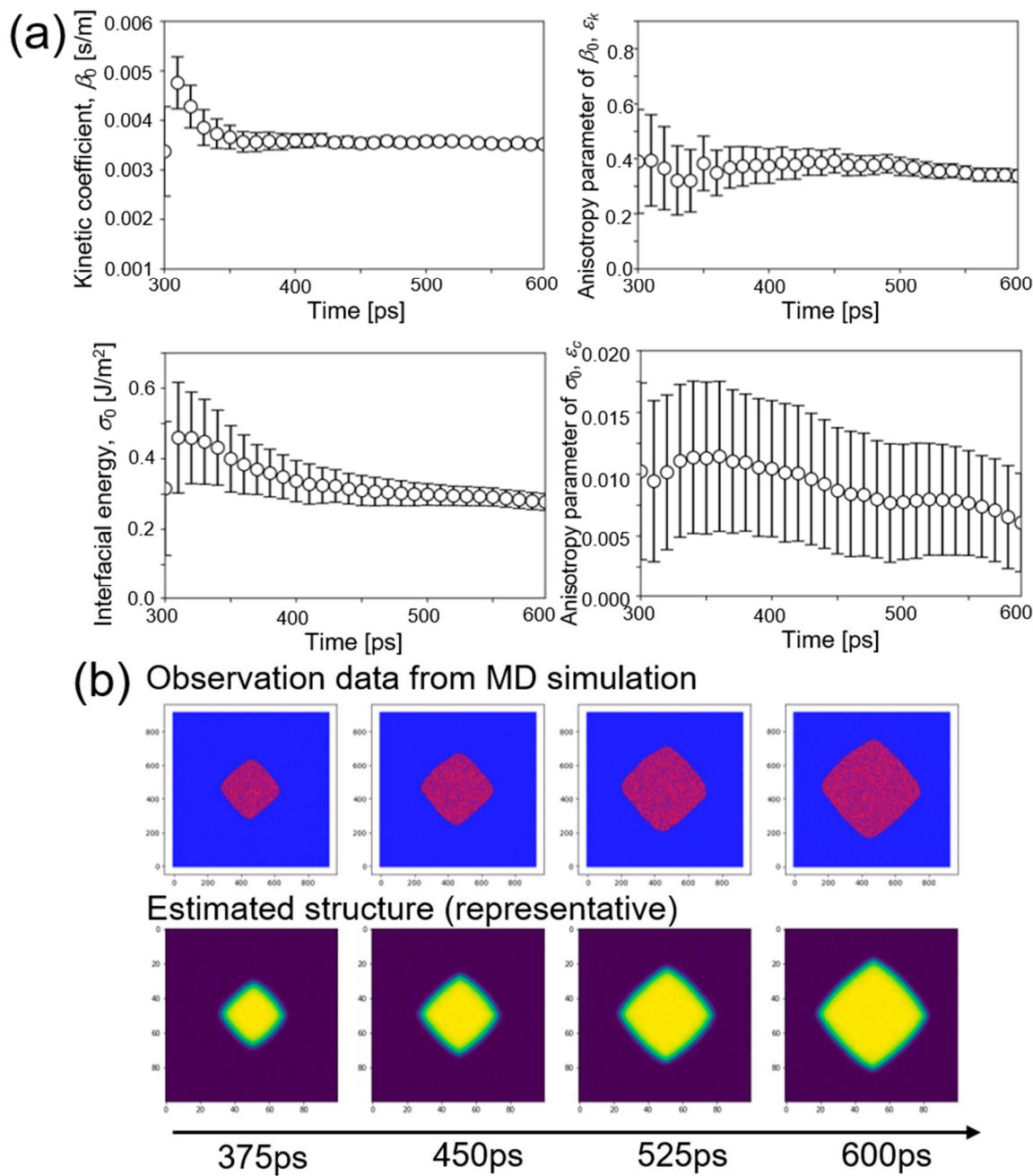
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**Table S1.** Representative properties of the EAM potential for Ni employed in this study [1,2].

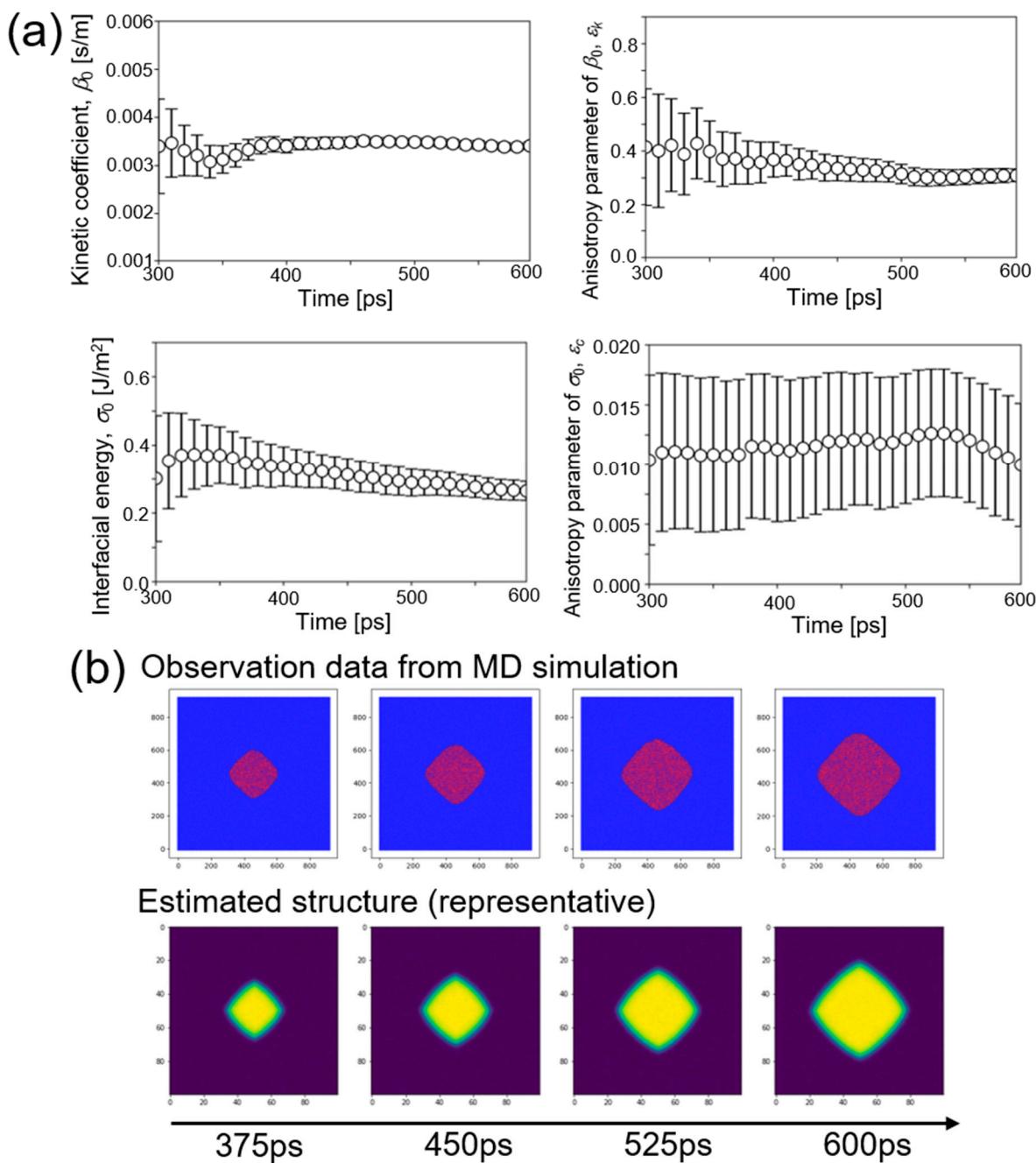
Property	Experiment	EAM
<i>Lattice constant, <math>a_0</math> (nm)</i>	0.352	0.352
<i>Cohesive energy, <math>e_0</math> (eV)</i>	-4.45	-4.45
<i>Elastic constants (GPa)</i>		
$B$	181.0	181.0
$c_{11}$	246.5	241.3
$c_{12}$	147.3	150.8
$c_{44}$	124.7	127.3
<i>Vacancy formation energy, <math>E_v^f</math> (eV)</i>	1.60	1.57
<i>Intrinsic stacking fault energy, <math>\gamma_S</math> (mJ/m<sup>2</sup>)</i>	125	134
<i>Symmetrical twin boundary energy, <math>\gamma_T</math> (mJ/m<sup>2</sup>)</i>	43	68
<i>Surface energies (mJ/m<sup>2</sup>)</i>		
(110)	2280* (average)	2087
(100)	2280* (average)	1936
(111)	2280* (average)	1759



**Figure S1.** Estimation of four parameters (kinetic coefficient  $\beta_0$ , interfacial energy  $\sigma_0$ , and their anisotropy parameters  $\epsilon_k$  and  $\epsilon_c$ ) using observation data of molecular dynamics (MD) simulation at 1455 K. **(a)** Time changes of the estimated values of four parameters,  $\beta_0$ ,  $\sigma_0$ ,  $\epsilon_k$  and  $\epsilon_c$ . **(b)** Snapshots of observation data from MD simulation and representative result of estimated structure.



**Figure S2.** Estimation of four parameters (kinetic coefficient  $\beta_0$ , interfacial energy  $\sigma_0$ , and their anisotropy parameters  $\alpha$  and  $\varepsilon$ ) using observation data of molecular dynamics (MD) simulation at 1505 K. (a) Time changes of the estimated values of four parameters,  $\beta_0$ ,  $\sigma_0$ ,  $\alpha$  and  $\varepsilon$ . (b) Snapshots of observation data from MD simulation and representative result of estimated structure.



**Figure S3.** Estimation of four parameters (kinetic coefficient  $\beta_0$ , interfacial energy  $\sigma_0$ , and their anisotropy parameters  $\epsilon_k$  and  $\epsilon_c$ ) using observation data of molecular dynamics (MD) simulation at 1530 K. **(a)** Time changes of the estimated values of four parameters,  $\beta_0$ ,  $\sigma_0$ ,  $\epsilon_k$  and  $\epsilon_c$ . **(b)** Snapshots of observation data from MD simulation and representative result of estimated structure.

## References

- Purja Pun, G.P.; Mishin, Y. Development of an interatomic potential for the Ni-Al system. *Philos. Mag.* **2009**, *89*, 3245–3267.
- Mishin, Y. Atomistic modeling of the  $\gamma$  and  $\gamma'$ -phases of the Ni-Al system. *Acta Mater.* **2004**, *52*, 1451–1467.