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# A Mathematical and Numerical Framework for Traffic-Induced Air Pollution Simulation in Bamako

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**Abstract:** We present a mathematical and numerical framework for the simulation of traffic-induced air pollution in Bamako. We consider a deterministic modeling approach where the spatio-temporal dynamics of the concentrations of air pollutants are governed by a so-called chemical transport model. The time integration and spatial discretization of the model are achieved using the forward Euler algorithm and the finite-element method, respectively. The traffic emissions are estimated using a road traffic simulation package called SUMO. The numerical results for two road traffic-induced air pollutants, namely the carbon monoxide (CO) and the fine particulate matter (PM<sub>2.5</sub>), support that the proposed framework is suited for reproducing the dynamics of the pollutants specified.

Keywords: differential equations; mathematical modeling; numerical simulation; air quality



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#### 1. Introduction

Air pollution is nowadays a major risk factor for human health and a global environmental concern. It is even more worrying in urban areas because of a high concentration of population and a sustained increase in the road transport fleet [1]. There are two principal types of air pollutants: primary pollutants and secondary pollutants. The primary pollutants are directly emitted into the atmosphere from natural sources, including wildfires and volcanic eruptions, or anthropogenic sources, including industries and road traffic. As for secondary pollutants, they are formed within the atmosphere as the result of chemical reactions of primary pollutants. The most common acute and chronic illnesses associated with air pollution include lung cancer, nose and throat (ENT) disorders, chronic obstructive pulmonary disease (COPD), and cardiovascular diseases. The World Health Organization (WHO) reports that the ambient air pollution is responsible for 4.2 million premature deaths worldwide every year [2]. The outdoor air pollution has been classified as carcinogenic to humans [3] by the International Agency for Research on Cancer (IARC), the specialized cancer agency of the WHO. Faced with this serious public health and environmental issues, policies have been implemented at local and international scales for regulating and monitoring air pollution. A strategy commonly adopted, mainly in advanced countries, consists of monitoring the concentrations of the pollutants of interest on a network of fixed monitoring stations using air quality sensors. This approach is not always viable since these monitors are often expensive, especially for developing countries.

Thanks to the fast acceleration in computational power and continuous progress in robust numerical algorithms, the modeling and simulation of air pollution are alternatives that work well [4]. Air pollution modeling is a complex scientific problem that involves the transport and dispersion of the air pollutants [5] as well as the processes related to the deposition and chemical reactions.

In the literature [6], there are two main types of mathematical methods that express air pollution processes: statistical models and deterministic models. The statistical models are based on the semi-empirical statistical relationships between various data and available

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measurement. As for deterministic models, they focused on the mathematical description of the physical and chemical processes in the atmosphere. The deterministic models are most suitable for practical applications and are, in general, more accurate and flexible. There are currently two fundamental methods [7] that address the turbulent diffusion: the Eulerian scheme and the Lagrangian approach. The main idea in the Eulerian models is to numerically solve the atmospheric transport equation in a fixed coordinate frame, while the Lagrangian models calculate the trajectories of air pollutants driven by deterministic and stochastic effects.

The City of Bamako, which is the political and economic capital of Mali, is located at latitude 12°38′21″ N and longitude 8°0′10″ W and straddles the Niger River in the southwestern part of Mali, see Figure 1. It represents only about 0.02% of the total area of the country but is home to nearly 12.46% of the Malian population. The population density in this city is estimated to 9062 people per km² [8]. Bamako represents the most important commercial crossroads of Mali since it concentrates about 70% of the economic activities of the country. These robust economic activities, coupled with a fast population increase, are factors that amplify the effects of pollution in Bamako. Despite recent advances in engine technology, the traffic flow continues to be the principal source of air pollution in urban areas [9], especially in Bamako, where the obsolescence of the transport infrastructure, see Figure 2, and the aging of the transport fleet make the pollution worse.

We focus on two primary pollutants widely used in the study and in the forecast of air pollution, namely the inhalable particulate matter less than  $10\,\mu m$  in aerodynamic diameter called  $PM_{10}$  and the fine particulate matter less than  $2.5\,\mu m$  in aerodynamic diameter called  $PM_{2.5}$ . In Bamako, the daily averaged  $PM_{10}$  concentration can reach a peak of  $600\,\mu g/m^3$  [10] while the daily maximum limit recommended by the WHO guideline is  $45\,\mu g/m^3$ . On the other hand, the daily and monthly mean  $PM_{2.5}$  concentrations over the month of October 2020 are reported in the Figures 3 and 4, respectively. As shown in Figure 3, the daily  $PM_{2.5}$  concentrations reach a peak of  $165\,\mu g/m^3$  while the daily maximum limit recommended by the WHO is fixed  $15\,\mu g/m^3$  [11].

These factors mentioned above support that the air pollution level in Bamako is very worrying. It is therefore essential to implement control and monitoring mechanisms for reducing the health and environmental impacts of the air pollution. For this purpose, we introduced in this paper a non-trivial application of the modeling and simulation of air pollution in Bamako in order to contribute to a better understanding of the dispersion pattern of road traffic-related air pollutants and to help in the decision-making process for a better regulation of the traffic emissions. It will thus make it possible to more precisely assess a possible correlation between the level of air pollution in Bamako and the frequency of diagnosis of certain diseases whose causes are still not identified. In terms of specific contribution to the current literature, this paper provides the scientific community interested in air pollution issues with a practical application based on new robust advanced numerical tools. To this end, it could serve as kernel for the implementation of eventual pollution models in other large African cities highly impacted by the effects of air pollution.

As the statistical models are in general not accurate enough for long term air pollution simulations, we consider in this framework a deterministic and Eulerian-based modeling approach. Although mathematical modeling and simulation are key tools for urban air pollution assessment, they are often challenging to implement and require high computational costs. In this work, the numerical simulations were performed using a scalable parallel computational framework proposed in [12]. The traffic emissions data required for running air pollution simulations were estimated using a useful road traffic simulation package called SUMO.

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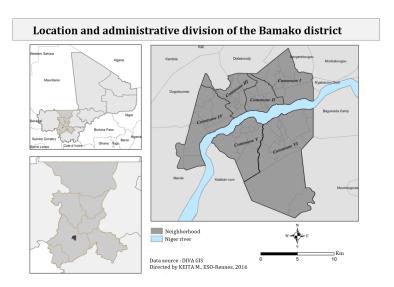


Figure 1. Geographical location and politico-administrative division of Bamako. Source: [13].

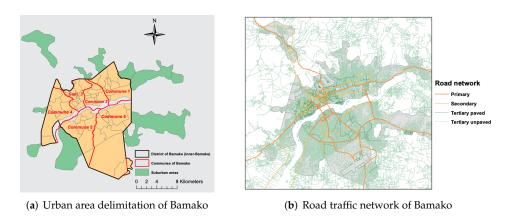
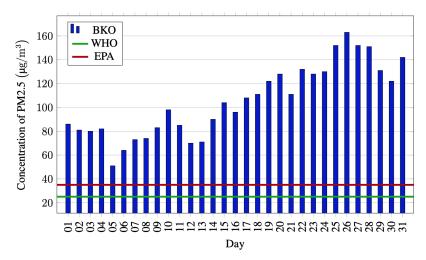
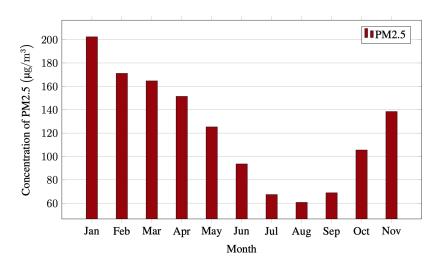


Figure 2. Urban area delimitation and road traffic network of Bamako. Source: [14].



**Figure 3.** Daily mean  $PM_{2.5}$  concentration in Bamako over October 2020. Data source: World Air Quality Index (WAQI) Project database 2020—U.S. Environmental Protection Agency.

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**Figure 4.** Monthly mean PM<sub>2.5</sub> concentration in Bamako over the period from January to November 2020. Data source: World Air Quality Index (WAQI) Project database 2020—U.S. Environmental Protection Agency.

The paper is organized as follows. Section 2 describes the mathematical model and the initial and boundary conditions. In Section 3, we present the computational mesh generation processes. Section 4 details the traffic simulation modeling and emissions. In Section 5, we present the numerical results and discuss their interpretations. Section 6 focuses on the validation of the numerical results using observational data. The main conclusions are recapped in Section 7.

## 2. Model Description

Let  $\Omega$  be a bounded domain of  $\mathbb{R}^3$ , see Figure 5. Let  $\partial\Omega$  the boundary of  $\Omega$ . We denote by c the vector field of concentrations, where the ith component  $c_i$  represents the scalar concentration field of the air pollutant labeled i. The spatial and temporal dynamics of the concentration  $c_i$  in the computational domain  $\Omega$  over the time interval (0,T) are governed by the following atmospheric chemical transport model:

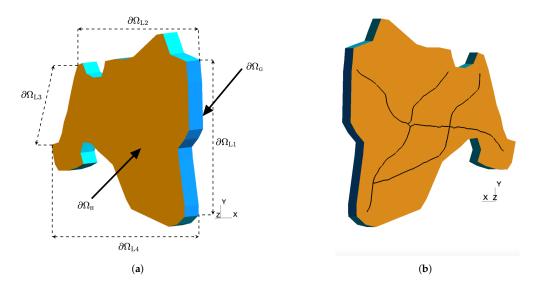
Fried by the following atmospheric chemical transport model: 
$$\begin{cases} \frac{\partial c_i}{\partial t} + \nabla \cdot (\mathbf{u}c_i) - \nabla \cdot (\mu \nabla c_i) - \chi_i(c) + \Lambda_i(\mathbf{x}, t)c_i &= S_i(\mathbf{x}, t) & \text{in} \quad \Omega \times (0, T) \\ + \text{Initial conditions} \\ + \text{Boundary conditions} \end{cases} \tag{1}$$

where

- (i)  $c_i = c_i(\mathbf{x}, t)$ : concentration of pollutant labeled i;
- (ii)  $\mu(\mathbf{x}, t)$ : diffusion coefficient;
- (iii)  $\mathbf{u} = \mathbf{u}(\mathbf{x}, t)$ : wind flow speed;
- (iv)  $\chi_i = \chi_i(\mathbf{x}, t)$ : sources of chemical reactions;
- (v)  $\Lambda_i(\mathbf{x}, t)$ : scavenging coefficient;
- (vi)  $S_i = S_i(\mathbf{x}, t)$ : source terms;
- (vii)  $\mathbf{x} = (x, y, z)$ : spatial variables, where z represents the altitude;
- (viii) *t*: model time.

Table 1 summarizes the parameters and physical fields presented above and their units.

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**Figure 5.** Three-dimensional computational domain of Bamako and traffic roads. (a) Three-dimensional domain of Bamako. View on upper limit and lateral boundaries. (b) Three-dimensional domain of Bamako. View on the ground boundary with roads. Source: [12].

Symbol	Name	Unit
С	concentration	${ m kg}~{ m m}^{-3}$
u	wind velocity	$\mathrm{m}\mathrm{s}^{-1}$
μ	diffusion coefficient	$\mathrm{m^2s^{-1}}$
$v^{dep}$	deposition velocity	${ m m\ s^{-1}}$
Λ	scavenging coefficient	$\mathrm{s}^{-1}$
χ	chemical sources	${\rm kg}~{\rm m}^{-3}~{\rm s}^{-1}$
S	volume emissions	$kg m^{-3} s^{-1}$
Ε	surface emissions	$ m kg \ m^{-3} \ s^{-1} \ kg \ m^{-3} \ s^{-1} \ kg \ m^{-2} \ s^{-1}$
H	maximum altitude	m
τ	characteristic time	S

**Table 1.** Fields and physical parameters of the model (1) introduced in [12].

In model (1), we neglect the feedback between the pollutants and the flow fields. The flow is supposed to be incompressible and the urban terrain is assumed to be homogeneous. The wind velocity  $\mathbf{u}$  is traditionally provided by meteorological models [15]. We focus on a maximum altitude H included in the atmospheric boundary layer [16].

# 2.1. Initial and Boundary Conditions

Equation (1) is supplemented by initial and boundary conditions. We suppose that the region of interest, i.e., the computational domain, is free of pollution at the beginning of the emission, i.e.,  $c_i(\mathbf{x},0) = 0 \ \forall \mathbf{x} \in \Omega$ . The boundary of  $\Omega$  shown in Figure 5a is decomposed as:

$$\partial\Omega = \partial\Omega_{G} \cup \partial\Omega_{H} \cup \partial\Omega_{L1} \cup \partial\Omega_{L2} \cup \partial\Omega_{L3} \cup \partial\Omega_{L4} \tag{2}$$

where  $\partial\Omega_G$  (z=0) denotes the ground boundary of  $\Omega$  and  $\partial\Omega_H$  (z=H) is the upper limit of  $\Omega$ . The subsets  $\partial\Omega_{L1}$ ,  $\partial\Omega_{L2}$ ,  $\partial\Omega_{L3}$  and  $\partial\Omega_{L4}$  are lateral boundaries. The boundary conditions on the ground surface  $\partial\Omega_G$  are given by a contribution of deposits and emissions. They are the following form:

$$-\mu\nabla c_i\cdot\mathbf{n}=E_i-v_i^{dep}c_i\tag{3}$$

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where  $E_i$  is the surface emissions of the species labeled i emitted from road traffic,  $\mathbf{n}$  denotes the unit outward vector normal to the boundary  $\partial\Omega$ . The field  $v_i^{dep}$  refers to the dry deposition velocity [6], see Section 2.2 for more details. On the upper limit boundary  $\partial\Omega_{\rm H}$  (z=H), the boundary conditions are given by a zero diffusive pollution flow:

$$\mu \nabla c_i \cdot \mathbf{n} = 0. \tag{4}$$

On the lateral boundaries, no pollution sources outside the domain  $\Omega$  are considered, i.e., the advective pollution flow is assumed to be zero:

$$c_i \mathbf{u} \cdot \mathbf{n} = 0. \tag{5}$$

# 2.2. Dry Deposition and Scavenging Processes

The dry deposition refers to the direct transfer of species to the ground without the aid of precipitation [17]. It constitutes a loss term and its intensity depends on the pollutants, meteorological conditions and season. The dry deposition flux [18] related to the species labeled i is computed as follows:

$$Df = -v_i^{dep} c_i (6)$$

The dry deposition velocity  $v_i^{dep}$  is parameterized by chemical species. It is a function of the meteorological conditions in the surface boundary layer and the type of soil characterized by the land use coverage (LUC) and the specific roughness parameter  $z_0$  ([15], [Table 3.5]). Some typical values of  $v_i^{dep}$  as a function of LUC are reported in ([19], [Table 3]). An illustration of the evolution of  $v_i^{dep}$  as a function of the size of particles for some specific values of the wind velocity is presented in ([15], [Figure 3.24]).

The loss due to the mass transfers with the aqueous phase (clouds or rain) is called wet deposition or wet scavenging. The soluble pollutants can penetrate raindrops when they fall; thus, they are precipitated on the ground. This type of deposit is known as below-cloud scavenging (BCS). Another form of wet scavenging takes place in the clouds where the soluble pollutants interacts (mass transfers) with the drops of water. This type of deposit is known as in-cloud scavenging (ICS). The wet scavenging plays a major role for gas-phase soluble species and aerosols since it governs their residence time in the atmosphere. Although the rainfall are a key process in pollution models, they generally focus on BCS wet scavenging since there is insufficient data on ICS wet deposition [20]. The scavenged concentrations satisfy the following time evolution:

$$\frac{dc}{dt} = -\Lambda c \tag{7}$$

The coefficient  $\Lambda$ , called scavenging coefficient, is the parametrization of all processes that result in scavenging. It is a function depending on the rain properties and the scavenged matter. Through numerous observational data, it follows that the scavenging coefficient for the aerosols can be configured as follows ([15], [Chapter 5, Section 5.3.2]):

$$\Lambda = \alpha p_0^{\beta} \tag{8}$$

where  $p_0$  (in mm h<sup>-1</sup>) is the rainfall intensity. The coefficients  $\alpha$  and  $\beta$  are specific constants that depend on aerosols. For the coarse fraction of aerosols distribution (diameters greater than 1 µm), typical values of  $\alpha$  and  $\beta$  are:  $\alpha \in [10^{-5}, 10^{-3}]$  and  $\beta \approx 0.8$ . For the submicronic fraction of aerosols distribution (diameters less than 1 µm), we have:  $\alpha \in [10^{-8}, 10^{-6}]$  and  $\beta \approx 0.6$ .

Some tables presented in [19] report typical values of  $\alpha$  and  $\beta$ , sometimes obtained from experimental data, as a function of the size of the aerosols. An illustration of the scavenging coefficient  $\Lambda$  as a function of the size of the aerosols for different intensities  $p_0$  of the rain is presented in ([19], [Figure 3]).

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#### 2.3. Chemical Kinetics

The temporal evolution of the concentrations of pollutants due to the chemical kinetics in the reactive dispersion Equation (1) is described by the following system of ordinary differential equations:

$$\frac{dc_i}{dt} = \chi_i(c), \qquad 1 \le i \le n \tag{9}$$

where n is the number of species. This time integration of chemical kinetics is very challenging [21]. The first difficulty is related to the size of of the system (9), which can be very large  $(n \gg 1)$ . The second issue is associated with the non-linearity of the system (9) since the species are coupled together through chemical reactions. Many explicit or quasi-explicit methods devoted to the solution of this system are available in the literature [21]. Among them, the class of methods known as QSSA (quasi steady state assumption) [22] is still widely used. It is based on the so-called production-consumption form of the chemical reaction:

$$\chi_i(c) = P_i(c) - L_i(c)c_i \tag{10}$$

where  $P_i$  and  $L_i$  represents the production and loss term, respectively. If we consider the first-order chemical reaction, then  $P_i$  and  $L_i$  are constants and the concentration is expressed in the form:

$$c_i(t) = \left(c_i(0) - \frac{P_i}{L_i}\right) \exp\left(-L_i t\right) + \frac{P_i}{L_i} \tag{11}$$

with a characteristic timescale of  $1/L_i$ . By extension, the characteristic timescale of the pollutant labeled i is computed as:

$$\tau_i = \frac{1}{L_i}. (12)$$

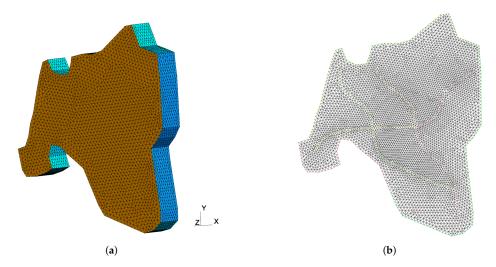
The characteristic timescale  $\tau_i$  for the species labeled i is computed from the dry deposition velocity and the maximum altitude H as follows:

$$\tau_i = \frac{H}{v_i^{dep}} \tag{13}$$

#### 3. Computational Mesh Processing

We start this step by extracting a map of Bamako from the OpenStreetMap (OSM) [23], a collaborative project for a free editable map of the world. This map contains, among others, the information on buildings, road networks and geospatial data initially expressed in the World Geodetic System 1984 (WGS 84). It has been processed and edited using an extensible editor for OSM data called JOSM [24]. For reasons of simplification, we have only considered the road networks and other useful information associated with them. Then, the map was imported into an open-source geographic information system called QGIS [25], from which, a geometry input file for the mesh generator Gmsh [26] was created using an external plugin. We exported the built geometry file according to the Universal Transverse Mercator (UTM) Coordinate System, zone 29N. Finally, a three-dimensional (3D) computational mesh over the region of interest was generated from the geometry file using Gmsh. This three-dimensional computational mesh and the ground boundary mesh extracted from it are plotted in Figure 6a,b, respectively.

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**Figure 6.** Three-dimensional computational mesh and two-dimensional mesh of the ground. (a) Three-dimensional mesh from the computational domain Figure 5a. (b) Mesh of the ground boundary extracted from three-dimensional mesh. Source: [12].

#### 4. Traffic Simulation Model

The emissions data are required for initializing a simulation of air pollution. Since experiments with traffic networks in real-life environment are often difficult, even impractical, the traffic flow simulation models [27] are common tools used to analyze traffic operations, assess traffic management strategies and report emission rates of pollutants. The traffic-induced emissions studied in this framework were estimated using SUMO [28]—Simulation of Urban MObility. SUMO is an open-source, microscopic and continuous multi-modal road traffic simulation package dedicated to handle large and complex road networks [29]. We carried out traffic simulations on the main and most frequented roads of the city of Bamako, see Figure 5b. These roads are susceptible to severe traffic congestion over peak hours, mainly from 7 a.m. to 11 a.m. on working days. The main data required for traffic simulations using SUMO were obtained from the Malian department of transport and infrastructure.

# 5. Numerical Experiments

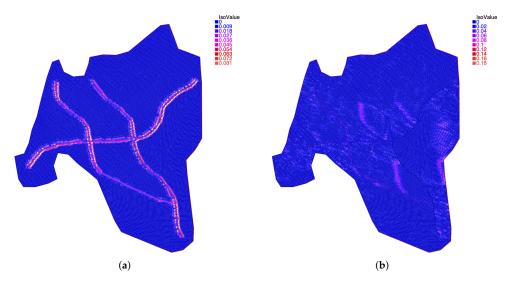
In this framework, we are interested in two traffic-induced primary pollutants, namely carbon monoxide (CO) and fine particulate matter ( $PM_{2.5}$ ). The CO is an odorless, colorless and tasteless gas emitted in the city mainly by motor vehicles, far ahead of the concentration emitted during combustion processes. The choice of this pollutant is motivated by the fact that its exposure remains one of the leading causes of unintentional poisonings worldwide [30]. Regarding the widespread air pollutant  $PM_{2.5}$ , its choice is inspired by the fact that the short-term exposures to these loads have been associated with several respiratory diseases.

We consider a first-order chemical reaction, see Section 2.3; therefore the balance of the physico-chemical transformations is written in the form  $\chi_i = -\kappa c_i$ , where  $\kappa$  denotes the rate of the reaction. The losses due to the deposit and scavenging are assumed to be negligible, which results in  $\Lambda=0$ . The physico-chemical parameters corresponding to CO are  $\mu=3.110^{-9}$  m  $^2$  s  $^{-1}$  and  $\kappa=1.6710^{-6}$  s  $^{-1}$ . The physico-chemical parameters for PM<sub>2.5</sub> are given by:  $\mu=6.3610^{-6}$  m  $^2$  s  $^{-1}$  and  $\kappa=3.1710^{-6}$  s  $^{-1}$ . We consider a maximum altitude H=10 m. The dry deposition velocity is computed as  $v_i^{dep}=H\kappa$ . The time step is set to 60 s. The three-dimensional mesh used for the simulations and the two-dimensional mesh of the ground boundary are presented in Figure 6. The wind data used for the simulations have a resolution of 10 m and were obtained from the European Centre for Medium-Range Weather Forecasts (ECMWF). The first-order finite-element approximation is used for the spatial discretization of the model.

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The simulations were carried out on the "Centre de Calcul, Modélisation et Simulation" (CCMS) of the Faculty of Sciences and Technologies (FST) of Bamako using the parallel and scalable computational framework presented in [12]. The configurations of the cluster CCMS are also described in [12].

The partial concentrations of CO and  $PM_{2.5}$  obtained from numerical simulations from 7 a.m. to 11 a.m. of 15 May 2020 are plotted in Figures 7 and 8, respectively.



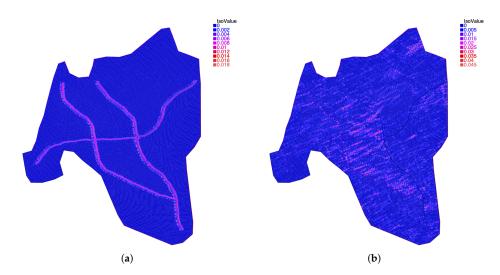
**Figure 7.** Spatial concentrations of CO in Bamako on 15 May 2020 at 7 a.m. and 11 a.m. (a) Spatial concentration of CO  $(g/m^3)$  from the road traffic on 15 May 2020 at 7 a.m. (b) Spatial concentration of CO  $(g/m^3)$  from the road traffic on 15 May 2020 at 11 a.m.

In Figures 7a and 8a, we observe that the CO and  $PM_{2.5}$  are clearly concentrated around the main traffic roads. This is due to the fact that the wind advection and diffusion are not yet sufficiently concretized since the simulation had just started. In contrast, after four hours of simulation, we observe in Figures 7b and 8b a continuous propagation of CO and  $PM_{2.5}$  in the computational domain. This is the result of a sustained wind action and a constant increase in the number of vehicles in the traffic.

These results support that, despite the area of Bamako (about 267 km<sup>2</sup>) and the low diffusion coefficients of the air pollutants studied in this framework, it only took an average of four hours during peak-period traffic congestion for these pollutants to spread over a large part of the city depending on the meteorological conditions.

The results presented in the Figures above appear promising; however, comparison studies with the data from the observations are needed for their validation, see Section 6.

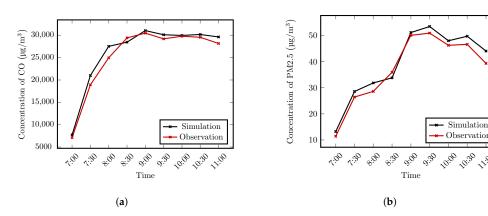
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**Figure 8.** Spatial distribution of PM<sub>2.5</sub> in Bamako on 15 May 2020 at 7 a.m. and 11 a.m. (a) Spatial distribution of PM<sub>2.5</sub> (mg/m<sup>3</sup>) from the road traffic on 15 May 2020 at 7 a.m. (b) Spatial distribution of PM<sub>2.5</sub> (mg/m<sup>3</sup>) from the road traffic on 15 May 2020 at 11 a.m.

#### 6. Numerical Validation

This section aims to evaluate the accuracy and validity of the numerical simulation results presented in Figures 7a and 8a using observational data. For this purpose, we focused on one of the most frequented traffic roundabouts of Bamako, commonly called "independence monument", during peak hours. The concentrations of the pollutants of interest were sampled and recorded every thirty minutes at this discrete point of the computational domain using a mobile air quality sensor. The concentrations of CO and  $PM_{2.5}$  from numerical simulation and observations on 15 May 2020 for the period from 7 a.m. to 11 a.m. are plotted in Figure 9a,b, respectively. Through a qualitative analysis of these figures, we can observe that, despite some simplifying assumptions in the continuous model, the simulation results are consistent with observational data since the trends of the different concentrations are similar over the period we considered.



**Figure 9.** Concentration of CO and  $PM_{2.5}$  from simulation and observation on 15 May 2020. (a) Concentration of CO from simulation and observation on 15 May 2020. (b) Concentration of  $PM_{2.5}$  from simulation and observation on 15 May 2020.

### 7. Conclusions

In this paper, we presented a mathematical and numerical framework for traffic-induced air pollution simulation in Bamako, the capital of Mali. The chemical transport model that governs the spatio-temporal dynamics of the concentrations of air pollutants has been described. The initial and boundary conditions, the deposits and the chemical kinetics of the pollutants have also been presented. The traffic simulations on the main and

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most frequented roads of the city of Bamako were carried out using a road traffic simulation package called SUMO. The numerical simulations have been focused on the carbon monoxide (CO) and the fine particulate matter ( $PM_{2.5}$ ). The numerical results presented here are being promising and consistent with the observational data as evidenced by the numerical validation study. These results support that the proposed framework is well suited for reproducing the spatio-temporal dynamics of the pollutants specified.

The numerical results presented in this framework were obtained using wind data of 10 m spatial resolution from the European Centre for Medium-Range Weather Forecasts (ECMWF). In order to improve the model accuracy and capture more spatial information, it would be important to perform numerical simulations at higher spatial resolution, i.e., 5 m or less. For that purpose, the meteorological data, especially the wind velocity fields, of similar resolution will be required. Unfortunately, we have not been able to obtain data at such a resolution from the meteorological data sources we used so far, including the ECMWF. To overcome these difficulties related to accessing high-resolution wind data, two approaches could be explored in the future. The first one involves computing the wind velocity as solution of the Reynolds-averaged Navier–Stokes (RANS) equations, which will be coupled with the reactive dispersion equation. The second approach focuses on the use of a downscaling technique to capture finer-scaled wind velocity.

The extension of this work to secondary pollutants and the processing of the chemical reactions resulting from the interactions between them in the atmosphere will be considered in the near future.

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Conflicts of Interest: The authors declare no conflict of interest.

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