

Article

# Finite Element Modelling on the Mechanical Behaviour of Marine Bonded Composite Hose (MBCH) under Burst and Collapse

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**Abstract:** Currently, the properties of composites have been harnessed on pipelines in the marine offshore industry. In this study, marine bonded composite hose (MBCH) is presented. It is aimed at understanding the stress/strain distribution on marine bonded hoses using local design pressure under burst and collapse cases. This study also investigates composite material modelling, hose modelling, liner wrinkling, helical spring deformation, and two MBCH models—with and without ovalisation. The ovalized model is considered the simplified model in this research. A mesh study was carried out on meshing the hose layers. In this study, local design pressure was considered and not operational pressure. This finite element model was adopted to predict the deformation and mechanical response behaviour of MBCH. From this study, composites could be considered to improve conventional marine hoses. The study findings include identification of buckled sections on the hose and stressed zones on the helix reinforcement. Highly reinforced hose ends are recommended in ends of the MBCH as they had maximum stress and strain values.

**Keywords:** marine bonded composite hose; finite element model; composite riser; layered marine structures; helix spring; liner wrinkling; numerical model; stress analysis; bonded model



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## 1. Introduction

The oil and gas industry has implemented a variety of technologies and hardware options to extract raw fossil fuels [1–6]. These petrochemical raw materials include crude oil and natural gas. These raw materials are refined into useable products produced using conduit hoses and marine risers [7–11]. Typical methods for the mass exploitation of natural fossil fuel reserves include permanent setups, mobile setups of dry platforms, and moored offloading/loading systems [12–15]. These installations have a complex network of marine risers and hoses connected to the platforms. [16–19]. Conversely, other components are installed directly upon oil reserve wells to extract oil. Hence, there are many techniques for deploying marine hoses and marine risers, from shallow to deep water environments. These techniques involve multiple options of hose-riser configurations, structural hose-riser designs, material selection, hose-riser manufacture, buoy design, corrosion resistance, and hose deployment [20,21]. Figure 1 shows an image of marine hoses on a rack. Typical ocean engineering applications include deployment of marine hoses on reel-mounted

FPSO (floating production, storage, and offloading) vessel/unit for (a) reel-laying and (b) ship-to-ship catenary connections.



**Figure 1.** Image of marine hoses on a rack. (Courtesy: Trelleborg; adapted with permission.).

Generally, floating offshore structures (FOS) support conduits like marine hoses. In recent years, the oil and gas industry has been harnessing composites and elastomeric material properties to manufacture marine hoses. These multi-layered marine tubular structures experience different structural issues such as buckling, liner failure, delamination, and matrix cracking of the layers of the structures. Similar mechanical behaviour has been reported on composite tubes and hoses [22–27]. This study presents a solution called marine bonded composite hose (MBCH) to solve a current problem facing the oil and gas industry on reeling hoses. Previous investigations have been conducted on the dynamic response of the marine hoses when attached to the Catenary Anchor Leg Mooring (CALM) buoy [28–31]. However, recent developments portray various hose patents by the hose manufacturers such as Dunlop Continental Oil & Gas, Yokohama, Trelleborg, etc. [32–36]. Currently, the industry has accepted, to some degree, the implementation of different composite materials in the design and manufacture of marine risers called composite risers [37–40]. These developments exist in recent academic reports and current industrial products from Airborne Oil & Gas, Magma Global, Technip, etc. [41–44], such as Magma’s M-Pipe [45]. However, there is a challenge in applying new dynamic methods for deploying these risers while maintaining a high service life in deep water environments, such as further increasing fossil fuel extraction from harder-to-reach reserves. Secondly, these multi-layered risers have similar behaviour to marine hoses in mechanical performance. They both exhibit some mechanical-related behaviours in terms of delamination, contacts, liner collapse, and fatigue [46–51]. In principle, these marine hoses are designed using both global and local designs [52–55]. The global design considerations for marine hoses includes the motion behaviour and environmental conditions [56–61]. On the other hand, the local design considerations for marine hoses include the forces, the pressure loads, and deployment operations. These operations include installation, reeling, transfer, pipe-laying, and fluid

transportation [62–66]. While improving the service life in deep water environments, this research will improve the use of marine reeling hoses. This can assist with increasing fossil fuel extraction from harder-to-reach reserves using these unique technologies. Another recent problem that has been encountered in the implementation of deploying marine composite hose-riser systems for fluid transfer via the use of a reeling drum mounted upon an FPSO is the crushing load on the hoses. Recent examples of the use of marine hoses have reported unexpected structural hose failure [67,68], and structural mooring failure of the CALM buoy-hose system [69–71]. These failures are significantly quicker than estimated in the hose's design phase and cost the industry millions in replacement for these hoses, thus risking the viability of these risers as a sustainable method of fossil fuel extraction. Analytical and numerical investigations on composite tubular structures are also considered. Xia et al. [72] presented an analysis of multi-layered filament-wound composite pipes under internal pressure. They presented analytical formulations on the composite elastic theory using a cylindrical pipe section, which considered three-dimensional (3D) elastic constants that have effective properties for thick laminates developed in an earlier study by Sun and Li [73]. Ye and Soldatos [74] investigated 3D buckling analysis of laminated composite hollow cylinders and cylindrical panels and presented profiles of the buckling modes. Bakaiyan et al. [75] examined multi-layered filament-wound composite pipes under combined internal pressure and thermomechanical loading with thermal variations. Based on the mechanical behaviour of marine hoses, Gao et al. [76] investigated the structural behaviour of ring-stiffened composite marine rubberised hose under internal pressure and validated the model. Nassiraei and Rezaadost [77,78] numerically investigated the effect of the composite material in marine structures using ANSYS, by considering the static capacity and local joint flexibility (LJF) of tubular joints having fibre-reinforced polymer (FRP) reinforcements under different loads. Gonzalez et al. [79] investigated the axial characteristics of flexible bonded marine hoses and presented some hose bending profiles. In the same vein, different researchers also presented mathematical models with numerical solutions on marine hoses' static and dynamics analysis [16,57–59,80]. Lassen et al. [81] presented an investigation on the load response of a marine bonded hose and its helix reinforcement, while Tonatto et al. [82] investigated the composite rings and spirals of an offshore hose. From these aforementioned investigations, the internal pressure loads were recorded as the most critical loads since they presented the highest stresses on the layers of the structures investigated. Another challenge is the material modelling of the composite tube or helical spring reinforcement. Thus, there is an imminent need for a better understanding of the industry's problem today, at both local and global levels, to further advance the use of composite materials in hose-riser applications.

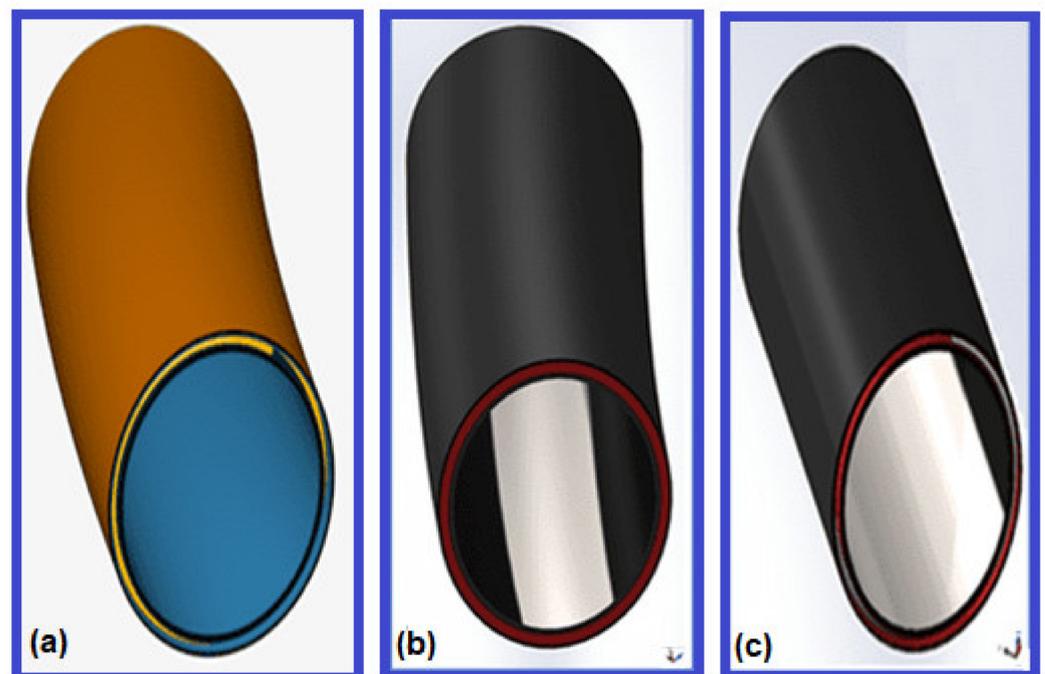
This research presents the studies conducted on the local design of marine bonded hoses under internal pressure and external pressure using the finite element modelling (FEM). Based on the local analysis, the aim was to model a reeled section of the tubular marine riser structure. Bonded contacts were utilised for the multi-layers. From the modelling in Sections 2 and 3, it was possible to simulate the stresses experienced on this section of the hose-riser to identify potential failure modes of the structure under the state as described in actual cases of hose/riser failure. The analysis of the stresses on these hose sections can be used to develop the global design model in further studies, for structural verification and postprocessing. The boundary conditions for the FEM were conducted in Section 3, while Section 4 shows FEM results of the novel MBCH structure and presents discussions on the results. The concluding remarks are provided in Section 5.

## 2. Materials and Methods

### 2.1. Model Description

For the local design of the reeling hose, ANSYS Structural version R2 2020 [83,84] and Simscale OpenFEA [47,85] were utilised. Both platforms were used to ascertain the different physics investigated on the loading conditions of the marine reeling hose to present results from both statics and dynamic behaviour of the hose. The sections of the

reeled and the unreeled hose are shown in Figure 2. The geometric parameters and the material properties of the hose are presented in Sections 2.3 and 2.4. In the present study, the ANSYS benchmark is used rather than ANSYS APDL due to the need for modelling demand to use a different package in modelling this marine hose. It is noteworthy that this is a highly multi-layered marine structure, with various contacts and layers. As such, under higher licenses, the ANSYS platform was limited to its performance in running the ANSYS model under higher element numbers while producing the results in faster time. Thirdly, there was another limitation of running the Finite Element Analysis (FEA) in high-performance computers (HPC) for this model. Hence, an Open-Source Aster Code embedded within Simscale Open FEA was considered, as it is faster, reliable, verified, and could produce more case studies for our model. Lastly, in this model, symmetry was considered but applied not in the present study but in another study that is not included in this present paper. In the present study, symmetry was not very representative due to the spiral arrangement of the spring. However, it would have reduced computational cost, as we found in the second model used in a separate study but not in the present study.

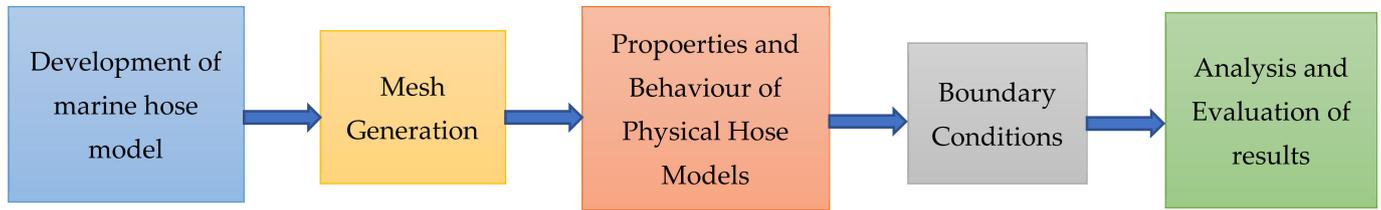


**Figure 2.** Reeling hose model showing (a) reeled section in Simscale OpenFEA, (b) reeled section in Solidworks, and (c) unreeled sections in Solidworks.

## 2.2. Methodology

In the local design, the hose geometry was generated in a CAD using Solidworks 2020. It was then modelled in ANSYS Structural version R2 2020 and ANSYS ACP Composites modules, as it had composites layers. Due to computational modelling challenges, the finite element model (FEM) was also run using Simscale OpenFEA online platform. The FEM results of the hose obtained from the local design were analysed to predict its mechanical behaviour. These analyses were performed by applying certain considerations to achieve the best results on the model. The first consideration was to simplify the model, while the second was to homogenize the model. The initial simplified model and the separate helix spring are shown in Figure 2a. The application of the FEM of the marine bonded hose involved the development of the marine hose model, the mesh generation, introduction of the properties and behaviour of the physical hose models, the introduction of the boundary conditions, the loadings (internal pressure, external pressure, and load cases), and the analysis and evaluation of results, as shown in Figure 3. The finite element analysis (FEA)

involved internal pressure, external pressure, and load case. Next, a tensile crush load on the spring reinforcement was also carried out, as stated in Sections 3.6 and 3.7.



**Figure 3.** Methodology for the finite element model of the marine bonded composite hose model.

2.3. Material Properties

The material properties considered in this model for steel and composites are presented in Table 1. These material properties were chosen based on their high potential for application in flexible bonded pipelines. They demonstrate high potential based upon their complimentary properties, such as high strength, natural corrosion resistance, lightweight, and flexibility. The physics of the contacts considered were the bonded contacts perfectly held, without any slippage and no separation. For the composite layers, the hoop layers direction was defined as 0° for the composite materials. Table 2 presents the layers and the material selections considered in this model.

**Table 1.** Material properties for steel and composites.

| Material         | Density (kg/m <sup>3</sup> ) | Young’s Modulus (Pa)   | Bulk Modulus (Pa)         | Shear Modulus (Pa)        | Compressive Yield Strength (Pa) | Tensile Yield Strength (Pa) | Tensile Ultimate Strength (Pa) | Poisons Ratio, <i>v</i> |
|------------------|------------------------------|------------------------|---------------------------|---------------------------|---------------------------------|-----------------------------|--------------------------------|-------------------------|
| Structural Steel | 7850                         | 2 × 10 <sup>11</sup>   | 1.6667 × 10 <sup>11</sup> | 7.6923 × 10 <sup>10</sup> | 2.5 × 10 <sup>8</sup>           | 2.5 × 10 <sup>8</sup>       | 4.6 × 10 <sup>8</sup>          | 0.3                     |
| Nylon PA6/6      | 1140                         | 1.06 × 10 <sup>9</sup> | 1.1778 × 10 <sup>9</sup>  | 3.9259 × 10 <sup>8</sup>  | 2.32 × 10 <sup>9</sup>          | 4.31 × 10 <sup>7</sup>      | 4.97 × 10 <sup>7</sup>         | 0.35                    |
| Nylon PA66-GF *  | 1360                         | 6.82 × 10 <sup>9</sup> | 7.5778 × 10 <sup>9</sup>  | 2.5259 × 10 <sup>9</sup>  | 3.45 × 10 <sup>7</sup>          | 1.39 × 10 <sup>8</sup>      | 1.49 × 10 <sup>8</sup>         | 0.35                    |
| CF (290GPa) **   | 1810                         | 2.9 × 10 <sup>11</sup> | 2.45 × 10 <sup>11</sup>   | 9 × 10 <sup>9</sup>       | 5.7 × 10 <sup>8</sup>           | 4.2 × 10 <sup>9</sup>       | 6 × 10 <sup>8</sup>            | 0.3                     |
| Resin Polyester  | 1200                         | 3 × 10 <sup>9</sup>    | 2.7174 × 10 <sup>9</sup>  | 1.1398 × 10 <sup>9</sup>  | 1.41 × 10 <sup>8</sup>          | 1.28 × 10 <sup>8</sup>      | 5.18 × 10 <sup>7</sup>         | 0.316                   |

Details on the anisotropic material properties for the composites are from MatWeb, Granta, and Ref. [9]. \* GF means glass-fibre-reinforced. \*\* CF means carbon fibre.

**Table 2.** Material consideration for reeled hose layers.

| Layer    | Liner            | Main Plies                                 | Filler        | Helix            | Holding Plies   | Sub Cover              | Breakers        | Cover                  |
|----------|------------------|--------------------------------------------|---------------|------------------|-----------------|------------------------|-----------------|------------------------|
| Material | Structural Steel | Nylon 6/6 glass fibre reinforced (PA66-GF) | Nylon 6 (PA6) | Structural Steel | Resin polyester | Carbon fibre (290 GPa) | Resin polyester | Carbon fibre (290 GPa) |

2.4. Marine Hose Layers

The marine hose structure is detailed within this model in order to make the simulation as realistic as possible. It is important to note that marine hose designs have more layers in reality. On the other hand, simplification was normally required without loss of generality (i.e., form) to achieve a successful numerical simulation. In this paper, it was a priority to investigate the use of the new composite materials implemented in these designs. Therefore, different composite plies were utilised in the model for the main and holding plies. The sub-cover and cover were to be made of structurally strong composites to add solidity to the structure. However, a key component to the design of this hose tubular is the steel structural helix embedded within the filler layers. This differentiates it from conventional marine

risers, pipe-in-pipe tubes, and reeled steel pipelines. The steel helix, as depicted in Figure 4, acts as a vital longitudinal reinforcement to the pipeline and is a critical component in the investigation of structural deformation behaviour, as a common fault in these hose-riser structures is helix rupture or delamination from its filling layer [86–89]. The helix also experiences deformation due to crush load of the spring against the reeling drum. Therefore, independent analysis of this layer is essential. The geometrical data of the layers for the marine hose models are presented in Tables 2 and 3.

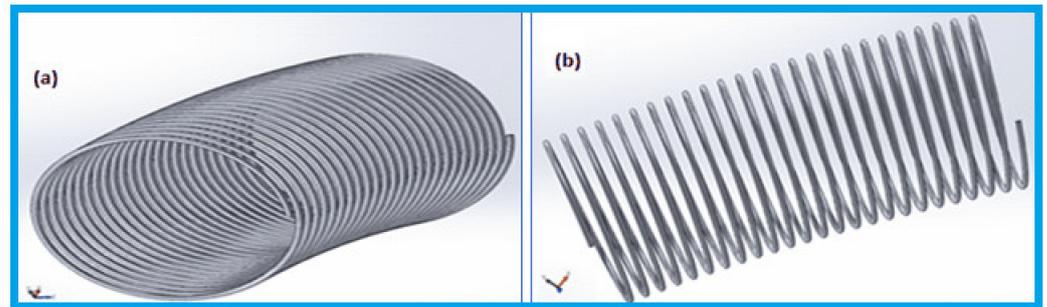


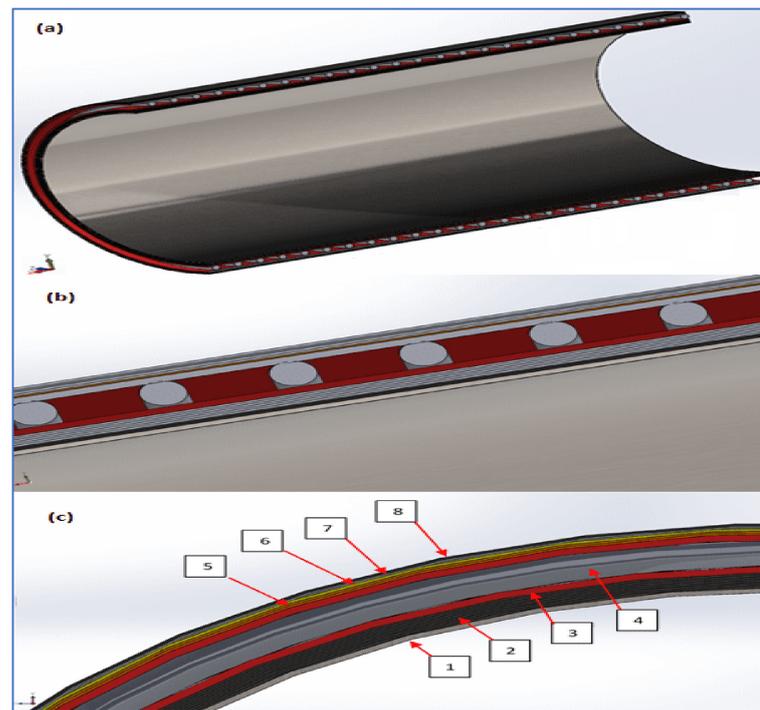
Figure 4. Helix reinforcement of the marine hose, showing (a) isotropic, and (b) side views.

Table 3. Marine hose model dimensions.

| Layer         | Inner Diameter (mm) | Outer Diameter (mm) | Thickness (mm) |
|---------------|---------------------|---------------------|----------------|
| Liner         | 488.95              | 493.95              | 5              |
| Main ply 1    | 493.95              | 496                 | 2.05           |
| Main ply 2    | 496                 | 498.05              | 2.05           |
| Main ply 3    | 498.05              | 500.1               | 2.05           |
| Main ply 4    | 500.1               | 502.15              | 2.05           |
| Main ply 5    | 502.15              | 504.4               | 2.25           |
| Main ply 6    | 504.4               | 506.25              | 1.85           |
| Main ply 7    | 506.25              | 508.3               | 2.05           |
| Main ply 8    | 508.3               | 510.35              | 2.05           |
| Filler 1      | 510.35              | 517.35              | 7              |
| Steel helix   | 517.35              | 545.79              | 14.22 **       |
| Filler 2      | 545.79              | 552.79              | 7              |
| Holding ply 1 | 552.79              | 554.84              | 2.05           |
| Holding ply 2 | 554.84              | 556.89              | 2.05           |
| Sub cover     | 556.89              | 559.39              | 2.5            |
| Breaker 1     | 559.39              | 560.59              | 1.2            |
| Breaker 2     | 560.59              | 561.79              | 1.2            |
| Cover         | 561.79              | 564.29              | 2.5            |

Note: Radius of curvature of marine hose layer = 6.25 m; \*\* Pitch of helix’s coil = 40 mm.

Dimensions were set for each layer, as illustrated in Figure 5. This setup was designed according to industry examples to represent the asset accurately. In practice, the composite ‘main plies’ are of varying angles, while the helix reinforcement layer is fully encased in a single filling layer. However, the present study’s scope did not include details on the reinforcement angles. For this design, simplicity increased the ability to vary the simulations under different loading conditions. The material choices of the model demonstrate high variation of both metallic materials and composites. In a practical design, a bonded flexible pipeline utilises a mixture of both material categories for enhanced structural properties of the asset. There are various materials chosen for different layers of the model regarding the composite material choices. Steel was chosen as the metallic component of the model for the inner liner and reinforcement helix. Composite material choices included resin polyester, carbon fibre (290 GPa), nylon 6 (PA6) and nylon 6/6 glass-fibre-reinforced (PA66-GF). These materials have been validated in modelling composite risers and thermoplastic composite (TCP) pipes in previous studies [1,9,81].



**Figure 5.** Cross-section through hose showing layers with the helix reinforcement in (a) open view, (b) closed view, and (c) labelled section of layers for the liner (1), main plies (2), filler (3), steel helix (4), holding plies (5), subcover (6), filler (7) and main plies (8).

The length of the hose in this model was 1 m long. It was modelled with filler layers whereby the helix was placed in-between fillers to sandwich the helix, rather than modelled within one filler layer. This was done for the simplicity of the model design when at the CAD stage to make construction easier while still providing satisfactory results in simulation. Both reeled and unreeled models were created with the same layering system to simulate a localised region of the pipeline, experiencing crush load from the reel drum. The reeled riser model was made with a radius of curvature of 6.25 m in order to correctly simulate the pipe being laid across the reel drum of diameter 12 m. Detailed below is the initial simulation material selection for the different layers. It is important to note that different ply angles were not applied at this stage, as the main aim was to obtain a working simulation to begin with. Therefore, the ply angles were all be considered to be unidirectional in the hoop direction.

### 3. Finite Element Model

The details on the finite element model for the MBCH are provided in this section.

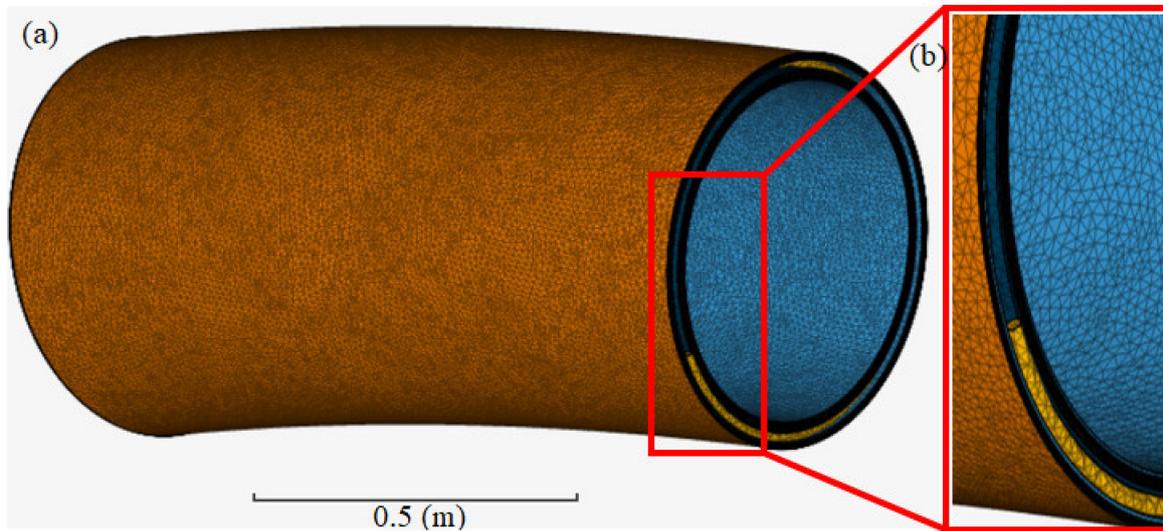
#### 3.1. Local Design

The finite element model was developed in ANSYS Workbench R2 2020. The details of the local design are presented in Section 2 and the other aspects, including the mesh details, boundary conditions, and design loads, are all in Sections 3.2–3.6. In this model, the failure criterion considered was the maximum stress criterion. The local design for the marine hose was based on beam theory [90–93].

#### 3.2. Mesh Details

The meshing details for the first case of the reeled hose model recorded a total of 2.7 million cells comprising of 12,538 edges, 1,841,382 faces, and 923,798 nodes. The mesh selection was conducted using a fine mesh with 6.8 points in Simscale and 2nd-order elements. This gave good convergence results in this study. The mesh was developed using a global gradation rate of 1.22, and a small feature suppression of  $1 \times 10^{-5}$  m. The mesh

was simplified using this mesh case, as represented in Figure 6. Some comparisons were made using a hose model without helical spring. This model was also further simplified by collectively grouping the similar layers into one layer, i.e., main plies 1–8. The spring was also modelled separately, and not homogenised with the other hose layers.



**Figure 6.** Mesh model for the marine hose in Simscale Platform showing (a) the full mesh model and (b) the magnified mesh detail.

### 3.3. Boundary Conditions

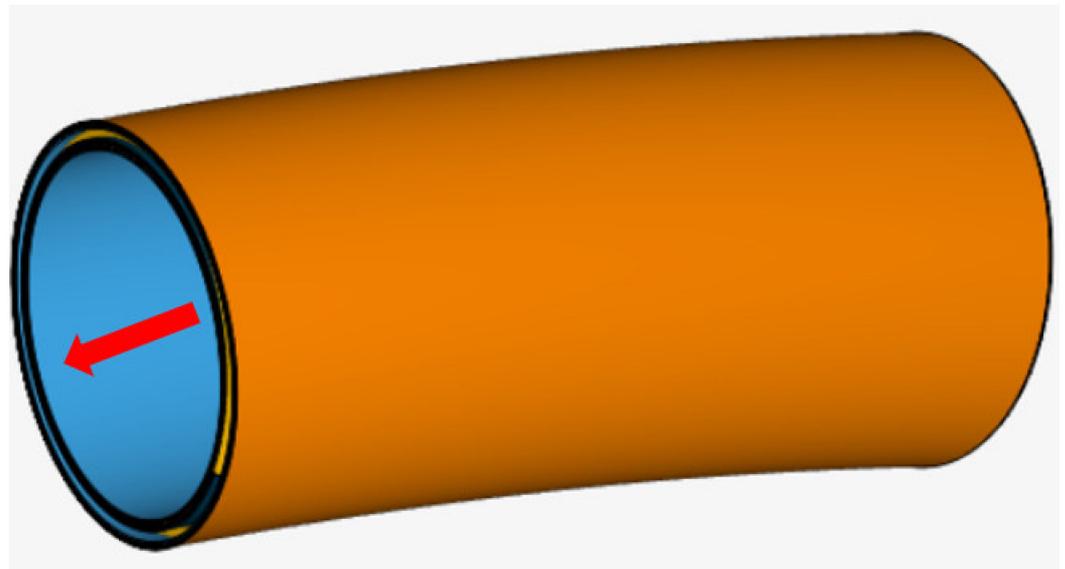
Different boundary conditions were considered based on the operation. For the pressure loading cases, fixed ends were considered, but when the torsional motions were induced, the loads were induced at one end that was set free. Fixed supports were applied to all faces at the fixed ends of the pipeline such that it was locked in place. The reinforcement helix was fixed at the end of the spring.

### 3.4. Design Load Conditions

This marine hose model’s local design followed the design standards for bonded pipes in industry specifications [94–97]. The following loading conditions were applied to simulate burst, collapse, tension, and crushing, as given in Table 4. The results of total deformation, shear stress, equivalent stress, and elastic strain were obtained using the simplified model. The hose structure was subjected to both internal and external pressures during the operation conditions. External pressures occurred due to the dynamics of the wave motion surrounding the hose accompanied by varying hydrostatic forces, varying with depth. However, the hose also had to operate under significant internal pressure to transport the targeted fluid while the production/drilling asset was extracting or transferring fluid. These internal fluids may be gaseous or liquid, with varying levels of viscosity. With an increase in viscosity, an increase in operational internal pressure was required to move the object fluid inside the hose. An internal pressure of a magnitude of 9 bar, as depicted in Figure 7, was applied to the liner inner face as a realistic starting operating pressure. Additionally, the standard gravitational force was applied to the pipeline to represent the self-weight of the marine hose.

**Table 4.** Design load conditions.

| Design Load                  | Loading Description                                                                                    |
|------------------------------|--------------------------------------------------------------------------------------------------------|
| Burst (Internal Pressure)    | Burst test at 2.0 MPa, 3.5 MPa and 5 MPa                                                               |
| Collapse (External Pressure) | Collapse test at $4.5 \times 10^5$ Pa, $7 \times 10^5$ Pa, $9.5 \times 10^5$ Pa, $1.26 \times 10^6$ Pa |
| Crushing Load                | The crush load was an external pressure of $2.1 \times 10^5$ Pa                                        |



**Figure 7.** Internal pressure load applied on the offshore hose in Simscale Platform.

### 3.5. Helix Compression/Tension

This model was created with similar dimensions to industrial designs. The helix was of a short pitch, 40 mm, and the diameter of about 14.22 mm. The material chosen for this simulation was steel, as stated previously. The model used for this simulation is depicted in Figure 8. An external pressure of 2000 Pa was applied perpendicularly at each end of the helix to the faces of the ends of the helix. This was done purely to observe the general mechanical behaviours when the entire helix is subject to uniform compressive force at each end. Lower pressure was applied upon the model to observe the trend on this hose's helix being investigated. The hose section was loaded from both ends. This was to observe its response from its own weight or other connecting sections pushing against the hose section. It should be noted that the spring could have been modelled by selecting an equivalent elastic support condition or even a virtual spring in ANSYS, making the model substantially more efficient. These spring loads may be considered in both tensile and compressive directions. However, the spring was fully modelled because the study aim was to investigate the spring behaviour so that spring load and the number of spring layers (one or two helix springs) could be factored into the conceptualisation of the model.

### 3.6. Crush Load on Helix Spring

During operation, the marine hose structure experiences compressive loading from other surrounding spooled sections, the reel drum itself or a combination of both. These crush loads will be consistently applied throughout the hose's life span. With continually repetitive loading of this nature, this could lead to potential fatigue cracking of the helix structure. As the helix is compressed, the shape begins to ovalise and offer a high potential for cracking. As a result, it was deemed imperative that this loading case be analysed via simulation to better understand the resulting mechanical behaviours of the helix due to crush loading. The crush load, as depicted in Figure 9a, is necessary as the helix can induce either layer delamination or reinforcement helix rupture. However, details on the delamination are not included in the scope of the present study. The OCIMF industry guidelines [98,99] do not specify crush load for helix spring specification. However, the GMPHOM OCIMF 2009 [99] determines guidelines for a marine hose section, without specifics for the helix reinforcement. It defines a shorter hose section as the test profile with a nominal length of 500 mm placed on a flat surface with supports. The test criteria further prescribed for the hose crush load apply a crushing load by utilising a flat beam profile of 500 mm lengthwise and 400 mm widthwise. This study proposes a longer profile for the helix, as shown in Figure 9a,b. Table 5 presents the parameters considered in developing the

helix geometry considered in the crushing test. The helix models have the same dimensions and materials as used in both ANSYS and Simscale simulations. In this model, the helix was not modelled in a reeled state, as it was formerly, but in a straight and unreeled layout. This helix was then modelled between two steel plates of the same dimension. These metal plates were then bonded to the helix structure, and external pressure was applied to each plate directed in opposite directions as each other in order to replicate a crushing load, with respect to (w.r.t) X-X and Y-Y planes, as depicted in Figure 9a. The simulation setup is depicted in Figure 9b.

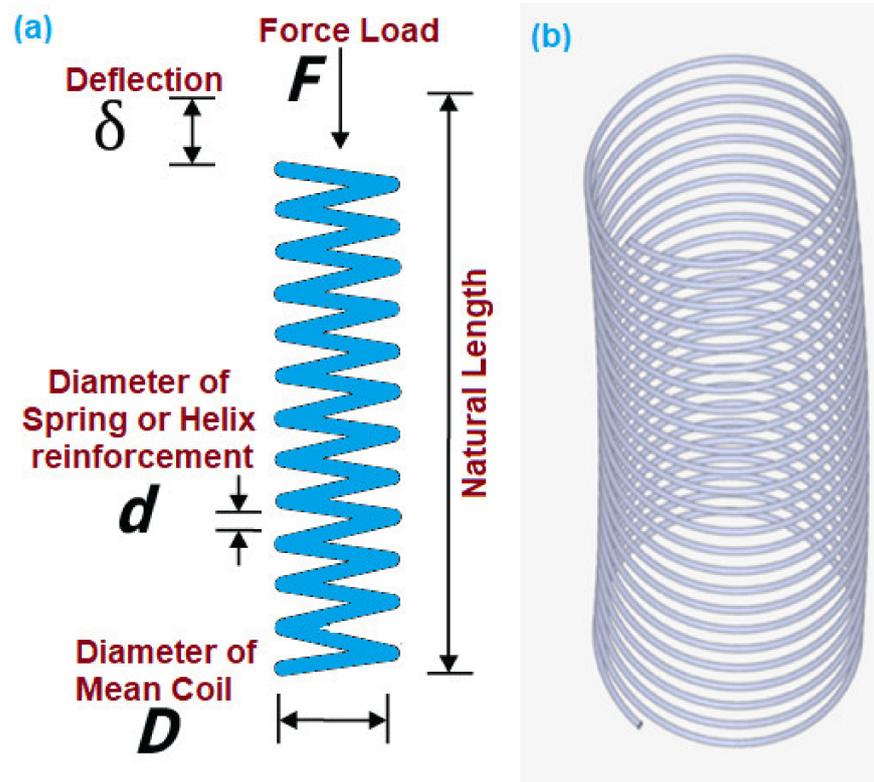


Figure 8. Schematic, showing (a) notation for helix spring, and (b) the reinforcement helix model.

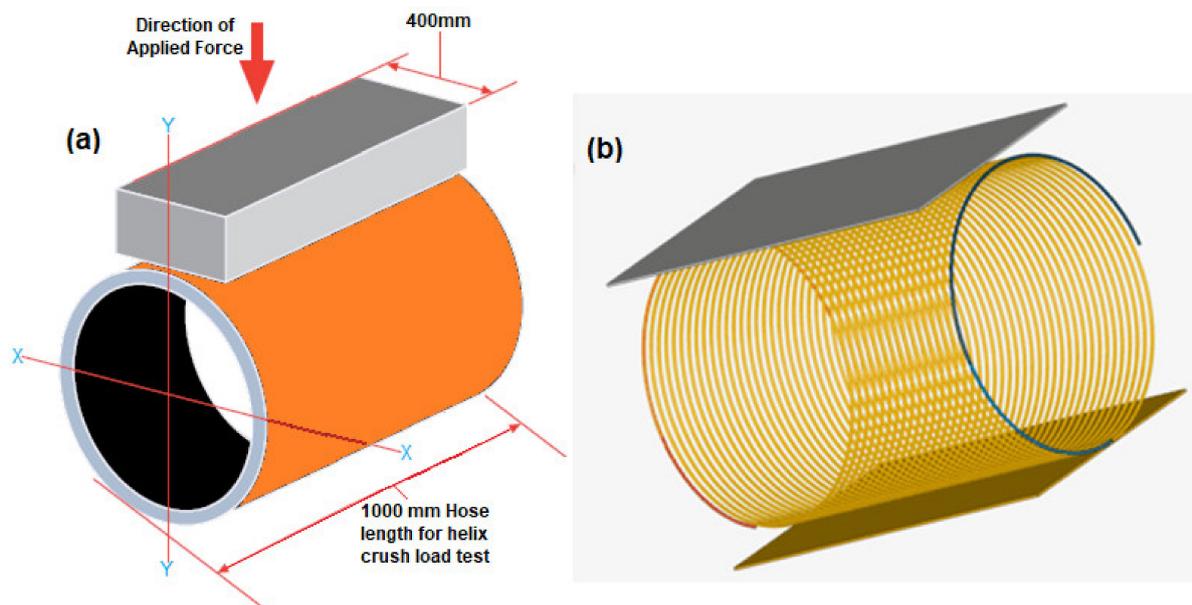


Figure 9. Reinforcement helix model compression, showing (a) hose crush load and (b) FEM of spring.

**Table 5.** Parameters for marine bonded composite hose (MBCH) and helix reinforcement models.

| Parameter                            | Value | Unit |
|--------------------------------------|-------|------|
| Hose Nominal inner radius            | 250   | m    |
| Outer radius                         | 294   | mm   |
| Length of Hose model                 | 1000  | mm   |
| Mean Radius of helix reinforcement   | 284   | mm   |
| Diameter of helix reinforcement coil | 12.7  | mm   |
| Pitch of helical reinforcement       | 36    | mm   |
| Total number of coil turns           | 41    | -    |
| Height of helix reinforcement        | 1500  | mm   |
| Width of helix reinforcement         | 1200  | mm   |

### 3.7. Validation

To understudy this model, the results of this investigation were compared using a composite riser with 18 layers of composite plies [9]. As observed in Table 6, the factor of safety (F.S) values obtained for the composite plies and the steel layer were 9.2 and 7, respectively. The FEM’s strain results from the present study were profiled by a comparative validation method using a similar hose study but on stiffened marine hoses [76]. The present model is a marine hose without stiffened layers considerable for submarine hoses and floating hoses, while the study by Gao et al. [76] is a marine hose with a steel-stiffened layer considerable for dredging hoses. Thus, this study was not comparable due to the differences between the material and the hose’s purpose. Both did not have a very close relationship in the strains because the type of marine hoses differed. However, the validation method is acceptable as it observed that the strains have similar intercepts in Figure 10. It gives a linear equation obtained using the line-fitting function on the data expressed in Equation (1). Moreover, the study showed that the axial strain is almost directly proportional to the internal pressure, as axial strain increased as burst load increased. However, note that a detailed validation is recommended in further studies, including analytical or experimental modelling of the marine hose.

$$y = 0.0007x + (6 \times 10^{-5}), R^2 = 0.9966 \tag{1}$$

for the validation of the spring model, an analytical method is considered. Using the analytical spring formula presented in [100] for the analytical relationships from Wahl’s spring equations, the stiffness of the spring can be computed. Using these formulations, the spring constant,  $k$  obtained is  $k = 3.62 \text{ N/mm}$ . This was used to validate the simulation result of the helix reinforcement in Section 4. Some theoretical formulations used are given in Equations (2)–(4), where  $d$  is the spring wire diameter,  $D_{outer}$  is the spring outside diameter,  $G$  is the material’s shear modulus,  $\nu$  is the material’s Poisson ratio,  $E$  is the material’s Young’s modulus, and  $nI_a$  is the active coils or turns on the spring.

$$D = D_{outer} - d \tag{2}$$

$$G = \frac{E}{2(1 + \nu)} \tag{3}$$

$$k = \frac{Gd^4}{8D^3n_a} \tag{4}$$

**Table 6.** Comparison on study comparing factor of safety (F.S).

| Model Particulars | F.S of Composite Plies | F.S of Steel Layer |
|-------------------|------------------------|--------------------|
| Present Study     | 9.2                    | 7                  |

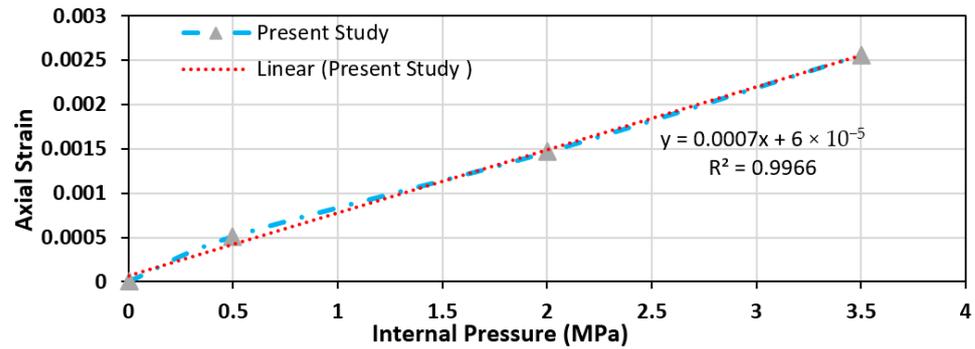


Figure 10. Validation plot for axial strains against internal pressure.

#### 4. Results and Analysis

This section provides a concise and precise description of the numerical results, their interpretation, the observations made, and discussions drawn on this study.

##### 4.1. Results of Helix Reinforcement

The FEA results on helix reinforcement presented in Section 3 are discussed here. In Figure 11, it can be observed that the spring has different tensile and compressive behaviour. Two spring helix reinforcement models were investigated, which are made of stainless steel and composite material, respectively. However, only the results of the stainless-steel model for the helix reinforcement were considered in this paper. All the models discussed in this section were set-up and run to completion, utilising the Simsacle online virtual FEA tool. The models were designed to simulate and analyse multiple loading conditions of marine reeling bonded flexible riser pipelines, utilising composite material and helical reinforcement layers. For the models demonstrated in Figure 11, an internal pressure of 2.5 MPa was applied to observe the resulting behaviours of the model. The factors to be observed were strain magnitude, von Mises stress, and displacement. As expected, with the internal pressure acting uniformly throughout the hoseline section, the force was greatest at the inner face of the pipeline liner. The areas experiencing the greatest force per unit area had higher magnitudes of profiled parameters. Moreover, the effects of this should gradually decrease throughout the model layers from the internal face of the liner.

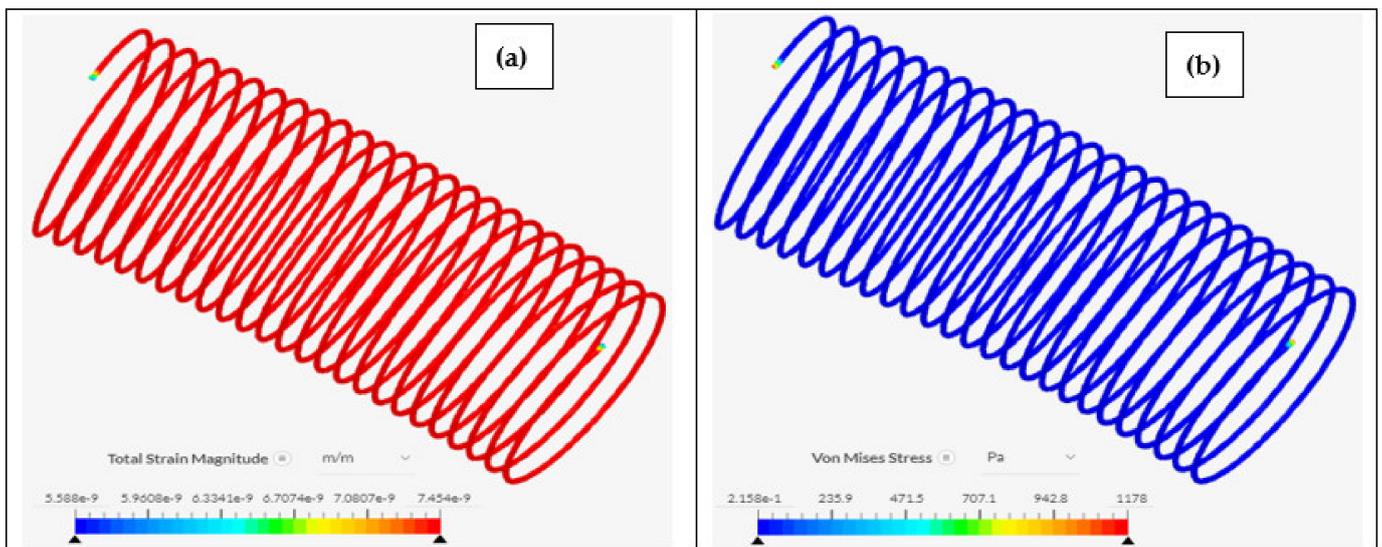
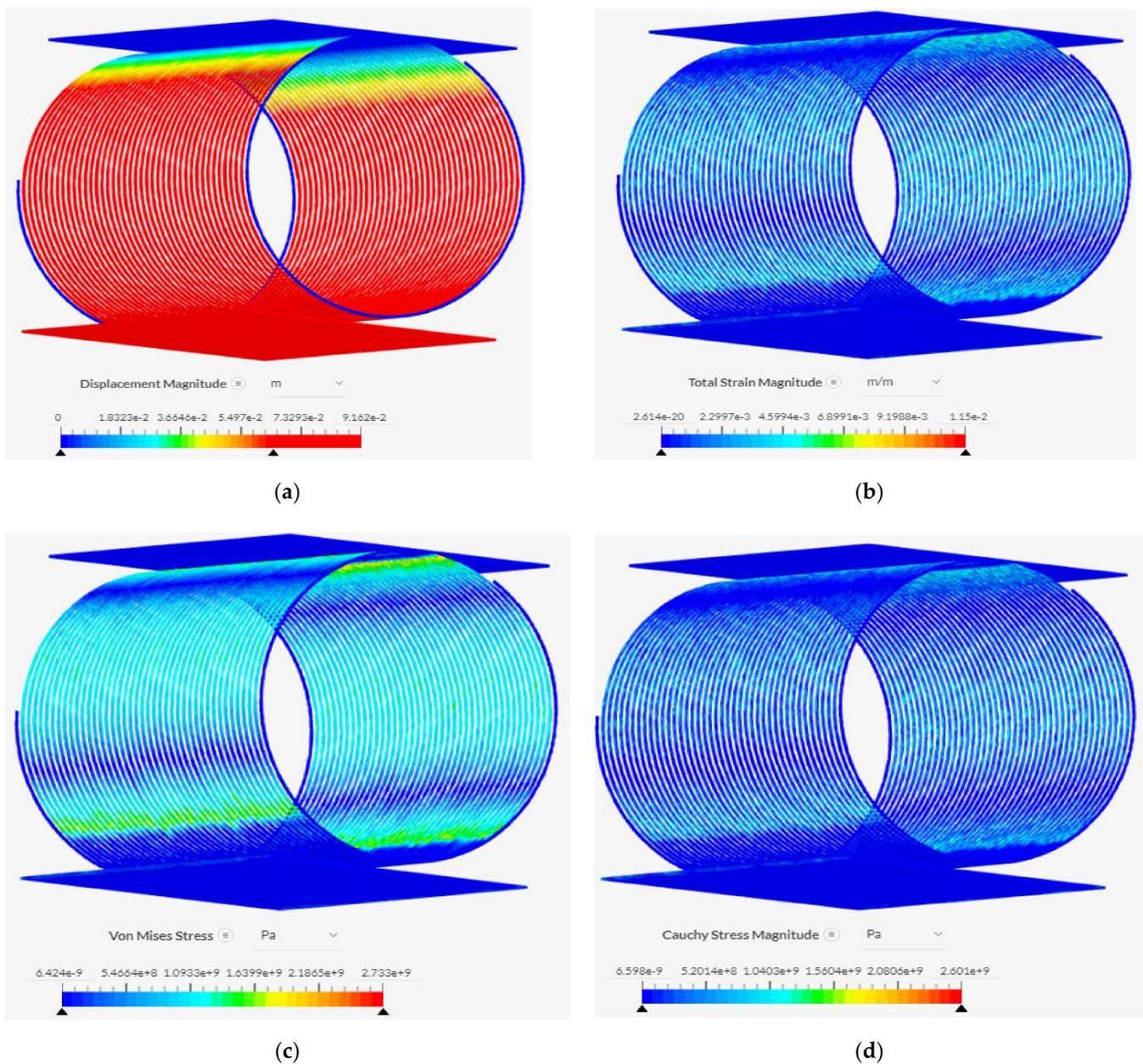


Figure 11. Reinforcement helix for the bonded flexible hose under loading, showing (a) strain magnitude, and (b) von Mises stress, as carried out in Simsacle OpenFEA.

#### 4.2. Results of Crush Load on Helix Spring

For the crush test displayed in Figure 12, the crush load was an external pressure of  $2.1 \times 10^5$  Pa exerted on the flat planes. The stainless-steel model was selected as it was observed that it performed better in a pre-analysis. From the crush load test, the deformation, strain, and stress results are presented. The present study investigated the crush load only on the spring reinforcement. It can be observed in Figure 12c,d that the end of the spring attracted the maximum deformations and stresses. Thus, proper attention had to be given to it during the design and manufacture of marine bonded hoses. A detailed crush load effect is recommended to investigate the effect of couplings and end-fittings of marine hoses when in contact with the FPSO body or reeling drum. Typical nonlinear analyses of spring models with similar failure mode analysis of hoses are in [48–51,82].



**Figure 12.** Compression on reinforcement helix for the bonded flexible hose, showing (a) deformation, (b) total strain magnitude, (c) von Mises stress, and (d) Cauchy stress using Simscale.

### 4.3. Results of Helix Spring Beam Model

A significant force that is involved in the reeling process is the crush load experienced by the pipeline crushing against the reel drum under tension and its own weight. Although unlikely to be crushed uniformly, a simulation of a collapsing case of the pipeline was carried out. In the reeling process, this could perhaps be experienced to a certain extent due to the possible build-up of pipeline sections stacked on top of each other, either during storage or through piled reeling on the reel drum. Two different modelling methods were considered to investigate this mechanical behaviour. The first is the beam model while the second is the hex-solid model. The effect of compression from a crushing load can be observed on both the models in Figures 13 and 14. As seen on Figure 13, there is a relationship between the force reaction per time obtained using the beam model and the hose helical spring reinforcement model. Moreover, the linear relationships in Equation (5) and the polynomial relationship in Equation (6) show that the spring beam model can have a linear and a nonlinear relationship. As such, it could have issues with damping the helical spring reinforcement even during crush load application, as shown in Figure 13.

$$y = -0.1297x + 0.1481, R^2 = 0.9725 \tag{5}$$

$$y = -0.0084x^2 - 0.0451x + 0.0057, R^2 = 0.9998 \tag{6}$$

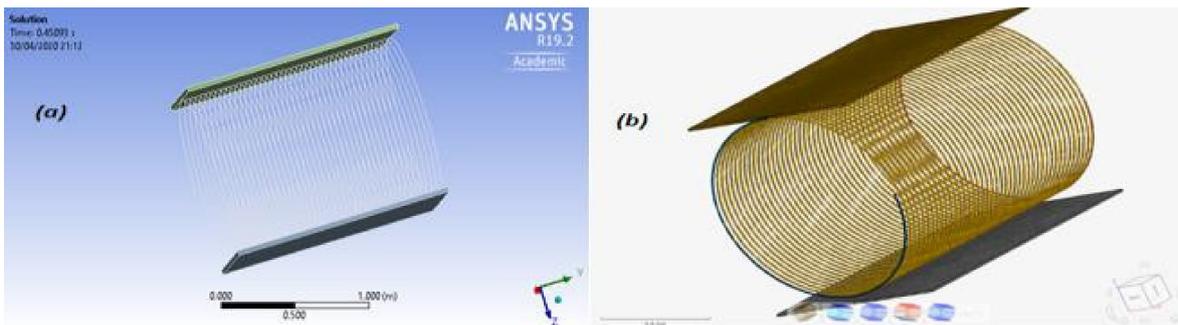


Figure 13. The offshore bonded composite hose for the (a) beam model in ANSYS Structural R19.2 and (b) hex-element model in Simscale OpenFEA.

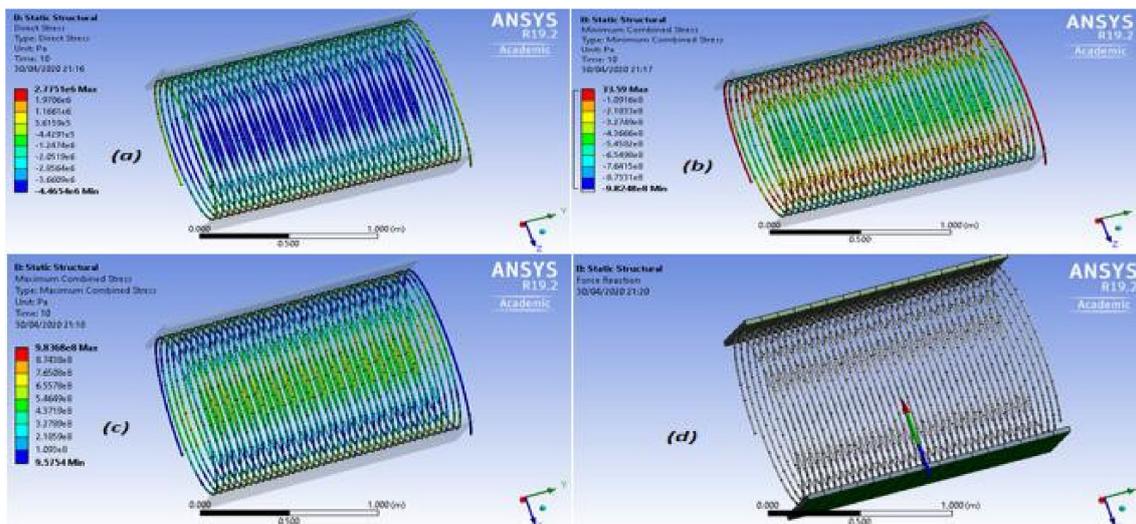


Figure 14. Helical spring beam model of the offshore bonded composite hose, showing (a) direct stress, (b) minimum combined stress, (c) maximum combined stress, and (d) force reaction.

Thus, the second model used had a much better representation of the stress behaviour of the spring in Figure 14. It shows areas of high stress magnitude which must be considered when laying the reinforcement or embedding it into the offshore bonded composite hose. Figure 15 presents the plot from the dynamic analysis of the beam model. The analysis is time-dependent, and the supporting plates were fixed. Both Equations (5) and (6) have spring meaning when compared to the spring equations presented in Appendix, as proposed earlier by Wahl [100]; however, this holds for steel materials. Further studies are recommended using sustainable spring materials such as high strength composites.

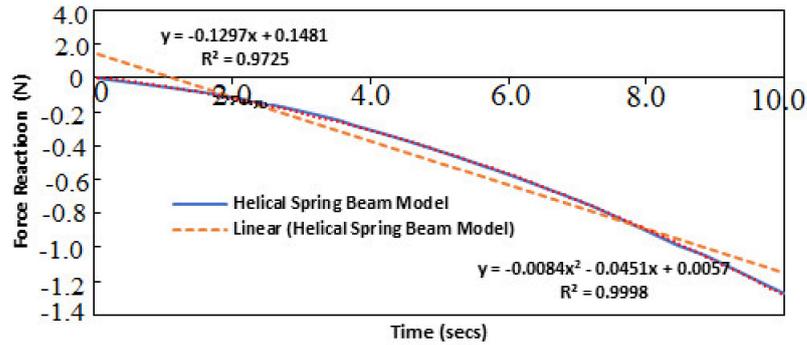
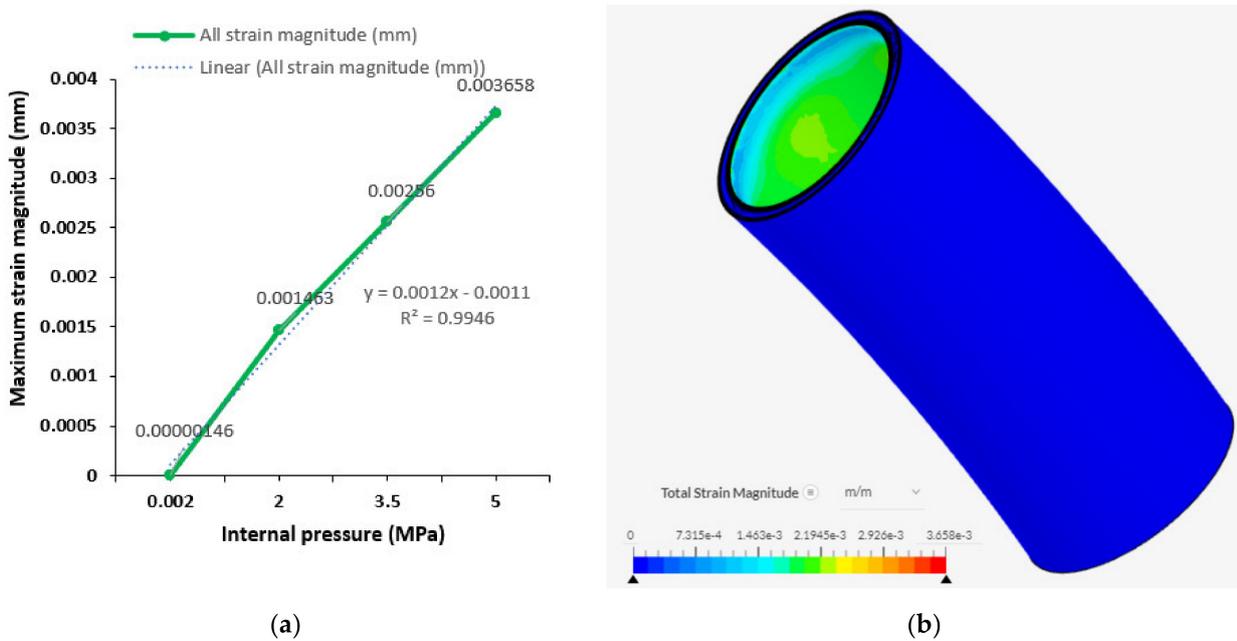


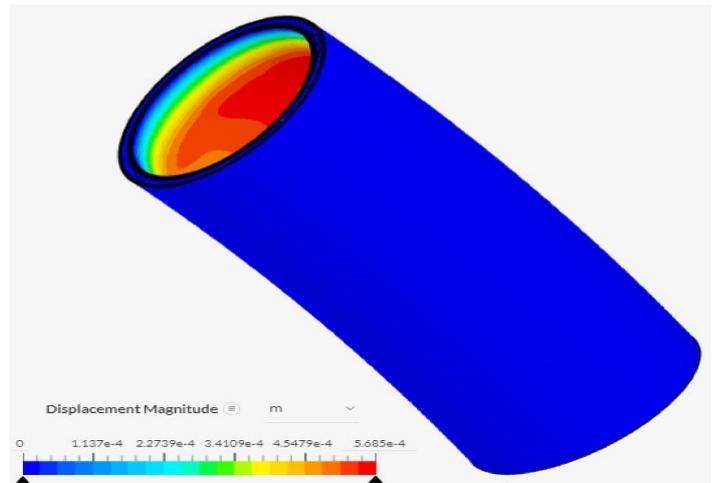
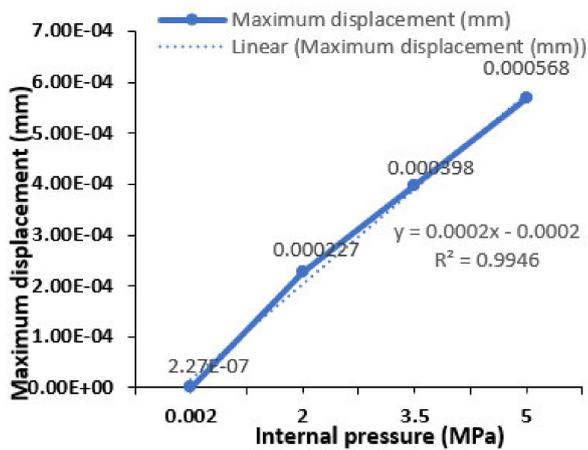
Figure 15. Helical spring beam model showing the force reaction of the marine bonded composite hose.

4.4. Results of Internal Pressure

The results obtained from the burst case on the reeling hose in the local design are presented in Figures 16–18. Three different ranges were considered based on previous predictions for the internal pressure, these are: 2.0 MPa, 3.5 MPa and 5 MPa. With the internal pressure acting directly at the innermost face of the liner of the hoseline, the results demonstrated maximum magnitudes of all monitored factors at this layer.



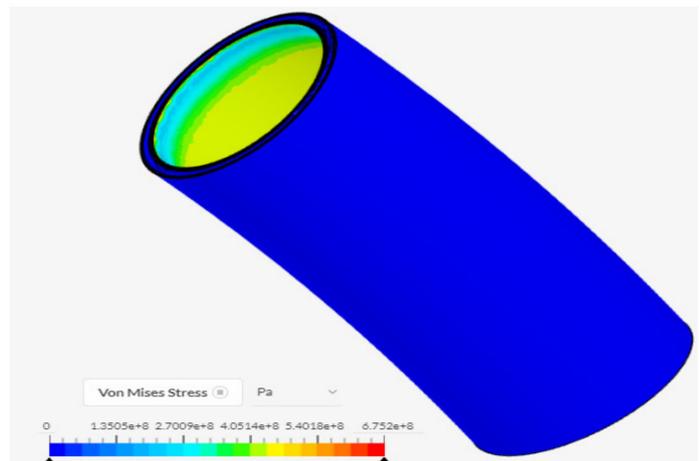
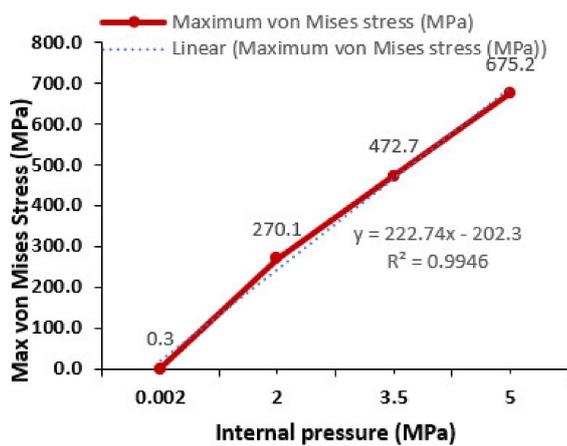
(a) (b)  
 Figure 16. Strain Profile of the bonded flexible hose under internal pressure, showing (a) the maximum strain magnitude under internal pressure at 5 MPa, and (b) Total strain magnitude of the hose.



(a)

(b)

Figure 17. Deformation Profile of the bonded flexible hose under internal pressure, showing (a) the displacement profile under internal pressure at 5 MPa, and (b) Maximum displacement of the hose.



(a)

(b)

Figure 18. Stress Profile of the bonded flexible hose under internal pressure, showing (a) the von Mises stress profile under internal pressure at 5 MPa, and (b) Maximum von Mises stress of the hose.

Displacement demonstrated the highest magnitudes at the inner liner, with some distance from the end of the section. Although the values displayed would be realistic values experienced, this also shows the behaviour of the marine bonded composite hose model under extreme and operational conditions. It should also be noted that the same boundary conditions were also applied to this burst case to obtain the results presented.

However, the results of this case are significant in identifying the pipeline behaviour mechanically to a crushing load. Generally, composite riser pipelines and offshore reeling hoses fail in service, before their theoretical lifetime, due to the mechanical fatigue experienced by the pipeline crushing against the reel drum. As given in Figures 16–18, the plots have a curve fitting of linearity given in Equations (7)–(9), showing a relative increase as the pressure increases, and thus showing an effective material model. Moreover, this study demonstrates the location of the maximum stresses and deformation occurrence when the structure is constricted. The results in Figures 16–18 show that the reinforcement layer would have certain areas likely to have earlier fatigue if the extreme loadings cause the structure to fail, or that possibly indicate the areas of deformations. It is recommended that

there be more reinforcement along the locations of these primary areas of delamination from the filler layer surrounding the reinforcement.

$$y = 0.0002x - 0.0002, R^2 = 0.9946 \tag{7}$$

$$y = 227.74x - 202.3, R^2 = 0.9946 \tag{8}$$

$$y = 0.0012x - 0.0011, R^2 = 0.9946 \tag{9}$$

Magnitudes of displacement decreased severely with radial distance from the inner liner. This results from the liner itself absorbing the highest magnitude of force per unit area, with the following composite plies experiencing less from this force with distance from the displaced liner. Following similarly are results of strain magnitude as well as both principal and von Mises stress. The highest magnitudes occur at the inner liner face and, again, they severely decrease with radial distance. However, it is noteworthy with regards to the von Mises stress that it can be demonstrated that at the very edges of the ends of the section are small areas demonstrating the highest magnitudes of stress, at around 270 MPa. These small areas demonstrate areas of high potential for potential cracking or fatigue, especially at higher operational pressures or possible uncontrolled pressure spikes. The liner at the very ends of the section should be an area of close monitoring if the asset exhibits this behaviour under internal pressure. In industry, ruptures and cracks have been witnessed at the end connections of these flexible risers, and this sort of mechanical behaviour may potentially demonstrate why this occurs. It is recommended that the reeling be done under operational pressure and not design pressure, as the study shows that design pressure could be high.

#### 4.5. Results of External Pressure

From the collapse case on the reeling hose in the local design, the results obtained are presented in Figure 19. Three different ranges were considered for the external pressure, these are:  $4.5 \times 10^5$  Pa,  $7 \times 10^5$  Pa,  $9.5 \times 10^5$  Pa, and  $1.26 \times 10^6$  Pa. Upon observation of the post simulation images and graphical results it was determined that the results were as predicted. With an increase in compressive force comes a proportional increase in all factors monitored. As given in Figure 19a–c, the plots have a polynomial curve fitting given in Equations (10)–(12), showing a relative increase as the pressure increases, and thus showing an effective material model. In addition, wrinkling was observed on the body of the offshore bonded composite hose along the arc length.

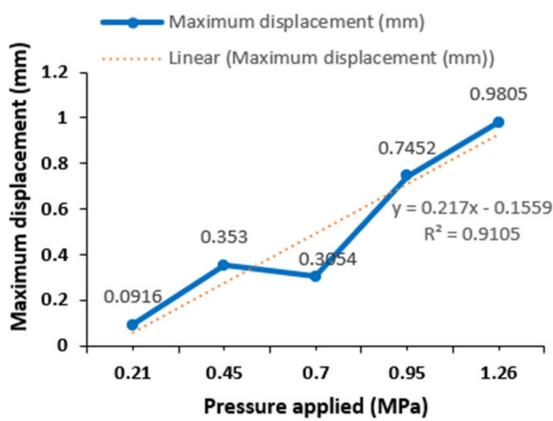
Based upon the post-simulation images, maximum deformation occurs at one half of the reinforcement coil structure, with a stark contrast in magnitude in the opposite section. Thus, this demonstrates the effect of ovalisation on the helix under crushing load, as observed in Figure 19d. Maximum stresses occur in a symmetric pattern, with the most severe distribution of stress demonstrated in three areas of the helix. This observation could suggest likely sites of the helical structure that show the highest potential for fatigue and microcracking, leading to the eventual rupture observed in real industry projects.

$$y = -0.0084x^2 - 0.0451x + 0.0057, R^2 = 0.9998 \tag{10}$$

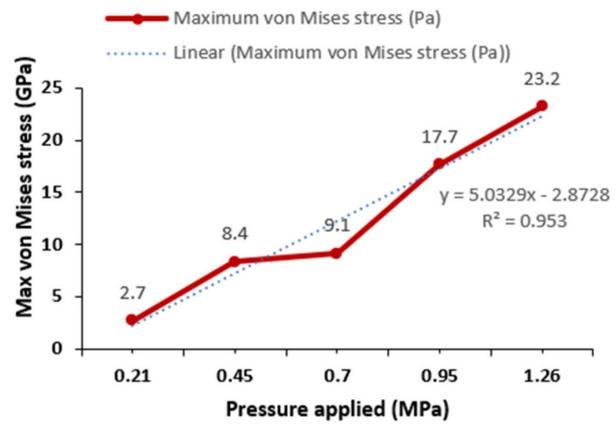
$$y = -0.0084x^2 - 0.0451x + 0.0057, R^2 = 0.9998 \tag{11}$$

$$y = -0.0084x^2 - 0.0451x + 0.0057, R^2 = 0.9998 \tag{12}$$

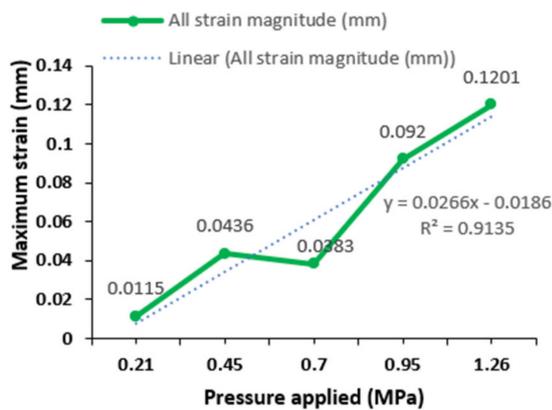
The external pressure has an impact on the walls of each layer differently for the normal stress and the equivalent von Mises stress. In view of that, such locations need to have thicker external liner material or increase the coefficient of friction in the bonding contact. It can also be observed that the ends that had been fixed have high stress profiles. As such, it is recommended that highly reinforced ends be used at such ends to offset the high collapse pressure, such as the helix profile in Figure 8.



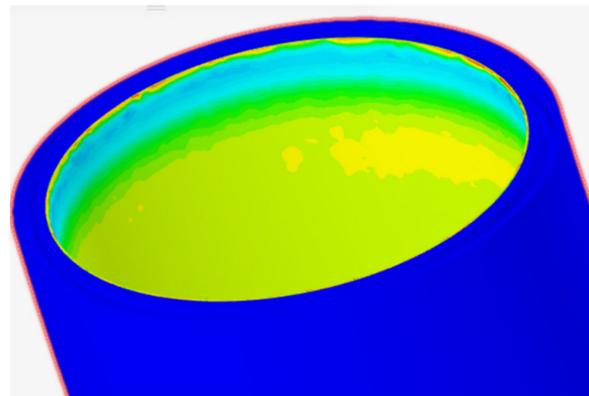
(a)



(b)



(c)



(d)

**Figure 19.** Profile distribution of Bonded flexible hose under external pressure showing (a) Deformation (b) Max von Mises stress, (c) Max strain magnitude, (d) Section of Von Mises Stress (VMS) profile.

#### 4.6. Discussion of Results

The local analysis for the multiple layers simulated yielded useful results, demonstrating key areas of the internal pipeline structure that would be subject to the highest magnitudes of stress and deformation. The bursting case simulation results demonstrated how the pipeline would act under increased internal pressure as well as operational pressure. The simulation yielded expected results that coincide with the observations made in the literature when controlled burst tests were performed on the pipeline. In these tests, it was demonstrated that the pipeline structure failed due to open mode tearing of the structure with fast fracture. The results of the simulation showed areas of maximum deformation at the points of maximum curvature of the pipeline. With the pipeline already being in a reeled state, it provides an area of maximum stress concentration at the area of maximum curvature, indicating that this region of the pipeline section is most likely to fail first. A combination of tension, hoop stress from internal pressure, and increased deformation of the pipeline in this region demonstrates the optimal conditions of fracture of the pipeline materials. It can also be seen in deformation cases of extreme pressure that the internal reinforcement helix can be seen to bulge outwards, through the covering layers on top of the helix. This could indicate that as the pipe structure expands due to pressure the helix acts as a further source contribution to the actual opening mode tear, causing the surrounding layers to be stretched further as the helix expands resulting in increased

localised stress on the materials in question. Regarding the equivalent von Mises stress and normal stress results, it can be noted that higher magnitudes of stress can be seen to occur at the ends of the pipeline section. This result could be due to the pipeline's bulging motion. Thus, the ends should be reinforced with reinforced hose end. As the layers of the pipe expand at the area of maximum curvature, there will be an increase in tension in the structure as the layers are stretched, therefore resulting in increased stress at the end joints of the section. This indicates an area with increased likelihood of failure.

The simulation of the case of collapse of the pipeline, as already mentioned, was the first step in replicating a crushing load applied to the pipe section. Crush loading is a recent suggestion for the reason behind the fact that the actual in-service lifetime of composite reeled riser pipelines is significantly less than predicted. The results, alike for the bursting case, demonstrated key areas of the structure that could be cause for concern regarding increased likelihood of failure. Areas of maximum magnitudes were identified from the deformation profiles, which are also at the points of maximum curvature. It can also be noted that significant deformation can be shown at the inner liner, with internal bulging effects being demonstrated by the external layers surrounding it. The results obtained for the equivalent von Mises stress are useful for identifying areas of high magnitude. It was demonstrated in the results that the ends of the section are areas which seem to experience a higher magnitude of stress, similar to the results for the bursting case. This seems to be a reoccurring trend for both cases, therefore indicating that the end-to-end sections of the pipeline are an area of the section which should be monitored closely for fatigue analysis. Moreover, results for normal stress show a similar pattern as was shown in the previous bursting case, which also follows similar trends of the equivalent stress. Normal stress shows maximum magnitudes at the ends of the pipe section, further highlighting the ends of the section as being areas of increased likelihood of mechanical fatigue. Additionally, the results obtained from the collapse case in Section 4.5 also demonstrate how stresses are carried on the steel reinforcement layer alone. These results can be useful in replicating crush loading of the section on the helix, which can lead to the observed results of helix delamination from its filling layer or even rupture. Deformation results follow similar trends to those obtained in the burst case, with highest magnitudes being experienced at the area of maximum curvature of the section. Normal stress shows an almost uniform application throughout the helix structure and equivalent von Mises stress experiencing uniform application on all areas, except the very ends of the section.

## 5. Concluding Remarks

A finite element model of a bonded marine hose has been presented based on local design. The novel material model was developed with the material properties presented in Section 2. It was then used to investigate different design loads on the tubular structure developed. The meshing details, the boundary conditions, and the loads applied were discussed in Section 3. The application of the local design using a small section was to ensure less computational time and resources. This study presents the novelty of the local design and material modelling of marine bonded hoses with improved modelling techniques for marine composites in the oil and gas industry. Some recommendations were made on other modelling methods to consider in further study. Moreover, some areas of the designed hose were identified for further studies and optimisation to achieve a longer in-service life span.

The model highlights include: a novelty in the material modelling for the finite element modelling of marine hoses, used in local design. This concept was applied on flexible risers and pipelay analysis. This proposed method saves computational resources, is cost-effective, and has high accuracy. Extensive local design was also carried out on the hose model for reeled and unreeled sections. The second novelty was the study of the effect of compression load on marine hoses. In reality, some loadings originate from the vessel load response and the effect of fluid content density on marine hoses. Thirdly, application of composites on the multi-layered bonded structure was considered in this study. Fourthly,

there was some novelty in the crush load analysis on helix spring reinforcement of reeling hose, and combined loading on the reeling hose. Lastly, the model presents the behaviour of the bonded tubular pipe under pressure loads using design pressures and the bending scenario by analysing the deflections under burst and collapse loads.

From this study, the following conclusions and recommendations may be drawn:

1. The internal pressure and external pressure tests are very important aspects of the design of the marine bonded hoses. It was observed that the higher the pressure, the higher the von Mises stresses, maximum strains, and maximum deformations on the reeling hose, as presented in Section 4. However, detailed study is recommended based on combined loading and the effect of the composite materials in the layers.
2. Based on the study of the reeling hose operation, some deformations were observed in the structure. However, this can be minimised by increasing the reinforcement of the marine hose, by using lighter materials with high strength–weight ratio, such as composites, or by applying the hose hydrodynamic loads. It is also recommended that the reeling be done under operational pressure and not design pressure, as the study shows that design pressure could be high. It is also recommended that an explicit code be used which runs better for simulating higher failure conditions in further studies.
3. The crush load was a significant part of the study as it showed the behaviour of the helix spring reinforcement under compression. The spring material performed well as stainless steel, however further studies should consider other spring coil materials like composites. Secondly, further study is recommended on the detailed crush load based on different materials and hose layer delamination.
4. Based on the result on the helix reinforcement, it is important to optimise the hose model and investigate further on the helix. The results of the study also showed that the strains along the hose sections are reflected from the helix reinforcement.
5. In reality, based on oil field operation, the crush load analysis of the reeling hose section will consider HEV coupling along the reeling hose string. A detailed crush load effect is recommended to investigate the effect of couplings and end-fittings of marine hoses when in contact with the FPSO body or reeling drum. In addition, further research is also recommended on the reeling process under transient mode in the FEA, as well as the global design of the marine bonded hose under marine operations like reeling.

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