

Article

Performance Comparison of Traction Synchronous Motors with Ferrite Magnets for a Subway Train: Reluctance versus Homopolar Variants

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Abstract: Due to the high cost and the predicted shortage of rare earth elements in the near future, the task of developing energy-efficient electric machines without rare earth magnets is of great importance. This article presents a comparative analysis of optimized designs of a ferrite-assisted synchronous reluctance machine (FaSynRM) and a ferrite-assisted synchronous homopolar machine (FaSHM) in a 370-kW subway train drive. The objectives of optimizing these traction machines are to reduce their losses, maximum armature current, and torque ripple. The optimization considers the characteristics of the machines in the subway train moving cycle. The problem of the risk of irreversible demagnetization of ferrites in the FaSynRM and FaSHM is also considered. To reduce the computational burden, the Nelder-Mead method is used for the optimization. It is shown that the FaSHM demonstrates better field weakening capability, which can reduce the maximum current, power, and cost of the inverter power modules. At the same time, the FaSynRM requires less permanent magnet mass for the same torque density and is more resistant to irreversible demagnetization, which can reduce costs and improve the reliability of the electric machine.

Keywords: electric machine parameter optimization; energy-efficient subway trains; extended constant power speed range; ferrite magnet electric machines; finite element analysis of electric machines; multi-objective optimization of electric machines; Nelder-Mead method; synchronous homopolar machine; synchronous motor field excitation; synchronous reluctance machine; traction motor; urban rail transportation



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1. Introduction

1.1. Disadvantages of Induction Motors and Motors with Rare Earth Magnets

At present, most traction drives, including those of trains, trams, subways, and mining dump trucks, use induction motors (IM). However, traction drives with IMs have the following disadvantages:

- (1) Large loss and heating in the rotor [1,2], which can lead to unacceptably high temperatures of the rotor, shaft, and bearings, even despite the liquid cooling of the rotor [3];
- (2) Continuous torque capability is significantly worse than permanent magnet synchronous motors (PMSM) [4];
- (3) Higher inverter power rating with a required constant power speed range (CPSR) over 3:1 [5,6]. For example, a study [5] presents a traction drive based on an IM with a mechanical power of 50 kW and a CPSR of 3.5:1, and the power rating of the traction inverter is 125 kVA. Study [6] presents a traction drive based on an IM with a mechanical power of 50 kW and a CPSR of 4:1, and the power rating of the traction inverter is 125 kVA.

To overcome these disadvantages, rare earth permanent magnet synchronous motors (PMSM) are used, which have a larger specific torque, lower loss, and a higher power factor [7]. However, PMSMs have the following disadvantages:

- (1) The production of PMSMs necessitates costly rare-earth magnets, which experience significant price fluctuations within a short span of a year or two. This variability arises due to a limited pool of magnet suppliers in the global market [8–10];
- (2) In the near future, a shortage of materials for the production of rare earth magnets is predicted due to the rapid growth in the production of electric vehicles and wind turbines, which very often use rare earth permanent magnets [11];
- (3) Rare-earth element extraction has an adverse environmental impact [12];
- (4) The demagnetization of rare-earth magnets can occur in high-power density PMSMs due to the presence of strong magnetic fields and high temperatures;
- (5) The task of maintaining high efficiency at speeds near the maximum becomes challenging when aiming for a wide constant power speed range, primarily due to increased copper loss that occurs in the field weakening mode [13];
- (6) Furthermore, in electrical power applications such as subway and railway trains, the rotational motion of PMSM induces a significant uncontrolled electromotive force (EMF) in the winding. This situation presents a significant risk of fire in the event of an emergency short circuit. Given the high inertia of the trains, which makes them unable to stop in time in such critical situations, it is recommended to refrain from using the PMSM in this application.

Due to the disadvantages of IM and PMSM, the development of synchronous motors for the subway without rare earth magnets becomes relevant.

The utilization of ferrite magnets proves advantageous due to their significantly lower cost compared to rare-earth magnets and their widespread production across numerous countries worldwide [14,15].

In addition, ferrite magnets have no losses due to eddy currents and high-temperature strength [14,16]. A challenge of using ferrites in motor design is their low coercive force [14,17]. For this reason, when optimizing motors with ferrite magnets, special attention must be paid to limiting irreversible demagnetization.

1.2. Literature Overview on the Use of Ferrite-Assisted Synchronous Reluctance Motors in Traction Drives

Magnet-free synchronous reluctance motors (SynRMs) have lower losses than induction motors. However, in electric vehicles that require a wide CPSR, SynRMs have a reduced inverter utilization factor, which significantly increases the power rating and cost of the inverter power modules [6]. This drawback can be overcome, as well as the dimensions of the motor can be reduced by adding inexpensive ferrite magnets to the rotor [14]. Ferrite-assisted SynRMs (FaSynRMs) with high rotor magnetic anisotropy have proven themselves in pumping applications in which a wide CPSR is not required [18–20]. Moreover, FaSynRM is also an alternative to IPMSM in electric vehicle applications, with comparable torque capability, lower permanent magnet cost, and better field-weakening capability [21,22].

For example, in [21], the characteristics of PMSM and FaSynRM are theoretically compared in a Toyota Prius 2010 drive with a rated power of 60 kW and CPSR of 3.5:1. It is concluded that the FaSynRM has characteristics similar to the original V-shaped interior PMSM with the same overall dimensions, while the cost of its active materials is much lower, and the maximum operating temperature of the rotor is much higher. In [22], a theoretical comparison is made between V-shape rare-earth assisted SynRM and FaSynRM for a BMW i3 2016 drive with a rated power of 60 kW and CPSR of 3:1. It is shown that the use of ferrite magnets makes it possible to obtain lower peak mechanical stress, better field-weakening capability, higher peak efficiency, and comparable efficiency over the operating range.

It can be concluded that quite a lot of articles are devoted to the analysis of FaSynRM characteristics in light passenger vehicles. However, studies on optimizing FaSynRM design for a subway train drive have not been presented.

1.3. Literature Overview on the Use of Synchronous Homopolar Motors in Traction Drives and on the Use of Ferrite-Assisted Synchronous Homopolar Motors

Another alternative to PMSMs in electric vehicles is electrically excited wound rotor synchronous motors (WRSM), which solve many of the problems associated with rare earth magnets but require a solution to the problem of unreliable sliding contact [23].

By merging the advantages of permanent magnet synchronous machines (PMSMs) and wound rotor synchronous machines (WRSMs), synchronous homopolar machines (SHMs) eliminate the need for slip rings like in PMSMs and, similar to WRSMs, operate without magnets. They achieve a wide constant power speed range (CPSR) due to their adjustable excitation current. One advantage SHMs have over WRSMs is that the number of excitation coils is independent of the number of poles, whereas, in WRSMs, it increases with the number of poles, resulting in reduced excitation magnetomotive force (MMF) [14]. As a result, SHMs have lower mass and reduced losses in the excitation winding compared to WRSMs. Additionally, since SHMs have no losses in the rotor, there is no need for rotor cooling. SHMs find applications as highly reliable generators in various fields, including laser technology, pulse heating, welding units [24], automotive generators [25], railway passenger cars, ships, and aircraft [26].

In addition, the application of SHM in traction drives is being studied.

In [23,27], the utilization of SHMs as traction motors in mining trucks is discussed. Paper [27] presents and validates the computation method for the traction SHM, which relies on a set of 2D magnetostatic boundary problems. Furthermore, SHM optimization techniques for traction applications were developed [23] using the Nelder-Mead algorithm and the model proposed in [27]. Also, the performance of SHMs was compared with other types of motors. For example, in contrast to WRSMs, traction SHMs exhibit certain drawbacks, as highlighted in reference [27]. Firstly, the mass and dimensions of SHMs exceed those of WRSMs due to each rotor tooth covering roughly one pole pitch, leaving approximately half of the pole pitches unused for torque production. Secondly, SHMs necessitate a higher inverter power rating compared to WRSMs.

Several studies [28–31] have explored multi-pole SHMs that feature an excitation winding on the stator and rare-earth magnets housed in the rotor slots. These SHMs, equipped with rare-earth magnets, offer advantages over those without permanent magnets. The use of rare-earth magnets enhances the utilization of the rotor surface, while keeping the weight and dimensions comparable to conventional PMSMs. In traction drives with a wide constant power speed range (CPSR), SHMs with rare-earth magnets excel by exhibiting higher inverter utilization and lower costs for the inverter. The excitation winding enables the adjustment of the excitation flux across a wide range of speeds, utilizing the excitation winding current as an additional control signal to enhance SHM performance optimization. However, a notable drawback of SHMs with rare-earth magnets lies in their dependency on a limited number of rare-earth element suppliers, leading to high material costs. Moreover, the depth of the rotor slots in these SHMs is significantly smaller compared to those without magnets, compromising the saliency of the rotor. Consequently, although rare-earth magnets provide substantial additional torque, the primary torque generated by the interaction between the field of the excitation winding, modulated by rotor stacks, and the field of the stator winding is diminished.

To enhance the characteristics of SHMs with magnets, an alternative approach involves utilizing cost-effective ferrite magnets in their construction. Ferrite magnets are considerably less expensive than rare-earth magnets and are produced in numerous countries worldwide [10]. The application of ferrite magnets in SHMs is exemplified in [26], where they are employed as under-car generators for railway passenger cars. The use of SHM

with ferrite magnets, compared with those without magnets, offers such advantages as reducing the weight and dimensions of the machine, as well as minimizing power losses.

Research on synchronous homopolar motors featuring ferrite magnets (for brevity in this paper, we call them ferrite-assisted synchronous homopolar motors, FaSHMs) is relatively infrequent. For example, in [14], the characteristics of a FaSHM are compared with the characteristics of an SMH without magnets in the drive of a subway train bogie.

1.4. The Problem and Aim of the Study

An overview of the literature shows that although there are studies of the characteristics of FaSynRM and FaSHM in traction drives, a comparative analysis of the characteristics of these types of motors in the drive of a subway train bogie is not presented. In this paper, the characteristics of the FaSynRM and the FaSHM for a 370 kW subway train bogie drive are optimized, and their comparative analysis is provided. The optimization of the motor designs is carried out using the computationally efficient Nelder-Mead method, which makes it possible to consider the driving cycle of the train and not just the rated operating point. Optimization considers several criteria, such as cycle losses, maximum inverter current, torque ripple, and the degree of irreversible demagnetization of the permanent magnets.

We would like to highlight that although the optimization of the FaSHM for the subway drive was already considered by the authors in [14]. However, the losses in the section of the train running due to inertia (see Figure 1, “Coasting” section) that occur in the magnetic core, which are significant due to the long duration of this section of the cycle, were not taken into account. Therefore, when compared to the FaSynRM, this study re-optimized the FaSHM design to take this factor into account.

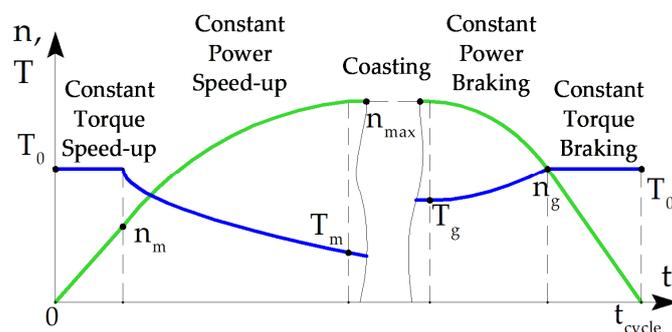


Figure 1. Dynamic speed (green line) and torque (blue line) profiles of the subway train’s traction motor.

2. Representation of the Train Flow Pattern in the Motor Optimization Routine

The movement of the subway train, as depicted in Figure 1, encompasses several stages: acceleration with a constant torque, acceleration with a constant power, coasting at a steady speed (with any minimal deceleration disregarded), deceleration with a constant power, and deceleration with a constant torque. The maximum torque remains constant at $T_0 = 1240 \text{ N}\cdot\text{m}$ for both motor and generator modes. The speed of transitioning between constant power and constant speed modes is $n_m = 1427 \text{ rpm}$ during acceleration and $n_g = 2854 \text{ rpm}$ during braking. The maximum attainable speed is $n_{max} = 4280 \text{ rpm}$.

Figure 2 illustrates the torque dependency on rotational speed, with two separate abscissa axes representing the motor and generator modes. The optimization routine of the FaSHM for specific operating points 1, 2, 3, 4, and 5 depicted in Figure 2 is detailed in [14]. This optimization process encompasses all stages of the operating cycle, excluding coasting. The optimization function incorporates objectives such as weighted average electric losses evaluated over the cycle, with the weight coefficients w_i determined using the trapezoid quadrature formula. Building upon this research, the present study further refines the optimization procedure for traction motors with magnets in subway trains, considering the core losses during coasting mode. Despite the motor being switched off, magnetic fluxes induced by the magnets still result in coasting-related losses. Therefore, this study

also considers the coasting mode (operating point 0). If coasting occupies 50% of the time required for travel between stations, integration of the speed reveals that coasting accounts for 63.3% of the total distance. In this case, the weighting coefficients are calculated as:

$$w^{ex}_0 = 1/2; w^{ex}_i = w_i/2, i = 1, 2, 3, 4, 5. \tag{1}$$

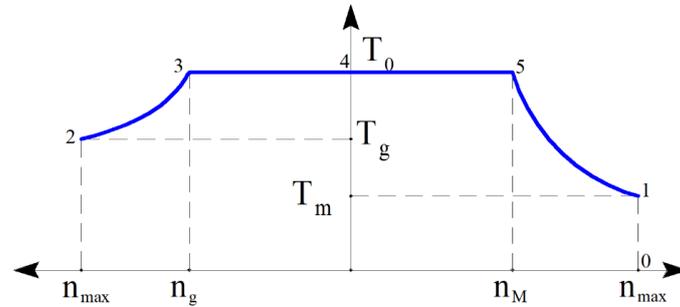


Figure 2. Demanded speed-torque characteristic of the subway train drive. The numbers 0–5 indicate the numbers of operating points of the electric machine, taken into account in the optimization process.

The average loss is calculated as:

$$\langle P_{loss} \rangle = \sum (w^{ex}_i \cdot P_{loss\ i}), \tag{2}$$

where $P_{loss\ i}$ is the total loss at the i -th operating point.

In each operating point, denoted as V_i , the maximum allowable line-to-line voltage is approximately equal to the DC voltage, although not precisely. In the operating points of generator mode, the voltage V_i slightly surpasses the DC voltage due to the switch voltage drop, while in the operating points of the motor mode, it slightly dips below the DC voltage. To quantify this relationship, we introduce the catenary ratio k_i , defined as $k_i = V_i / V_{DC\ rated}$ ($V_{DC\ rated} = 750\text{ V}$). It is assumed that in modes 1, 2, 4, and 5, the DC voltage is equivalent to that in the catenary, resulting in k_i being close to 1. The following margin values are selected: $k_2 = 1.01, k_1 = k_4 = k_5 = 0.97$. In operating point 3 (generator mode), k_3 can be chosen greater than in motor modes 1, 4, and 5, owing to the battery charge recuperation. For added safety, all the details pertaining to the specific modes are consolidated in Table 1.

Table 1. Points of the operating cycle of the subway train drive considered during the optimization.

Operating Point, i	Operating Point Name	Speed n_i , rpm	Torque, T_i , N·m	w_i	k_i	w^{ex}_i
0	Coasting mode; maximum speed	4280	0	-	-	0.5
1	Driving mode; maximum speed	4280	413.4	0.363	0.97	0.181
2	Braking mode; maximum speed	4280	826.9	0.091	1.01	0.046
3	Braking mode; changing from constant power to constant torque operation	2854	1240	0.182	1.1	0.091
4	Zero speed	0	1240	0.182	0.97	0.091
5	Driving mode; changing from maximum torque to constant power operation modes	1427	1240	0.182	0.97	0.091

3. Designs Features of the FaSHM and FaSynRM

The structure of the FaSynRM magnetic core is uniform along the axis of rotation; therefore, to describe it, it is sufficient to consider only its two-dimensional geometry (Figure 3a). The FaSHM consists of two pairs of stator and rotor stacks connected by axial elements that conduct the excitation magnetic flux. Therefore, to model the FaSHM, it

is necessary both to consider the two-dimensional geometry of a pair of stator and rotor packages (Figure 3b) and to consider the design of the axial elements: the stator housing and the rotor sleeve (Figure 3c).

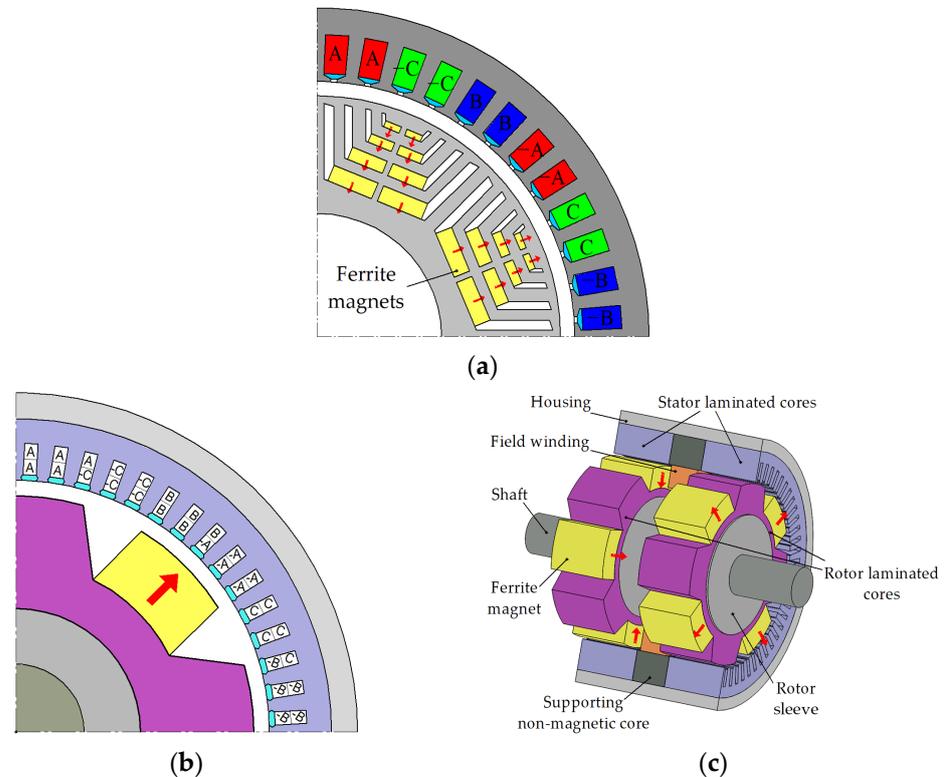


Figure 3. Motor design representation. Red arrows mark the directions of magnetization of the permanent magnets. (a) Ferrite-assisted synchronous reluctance motor (FaSynRM), 2-Pole area, red, blue and green colors indicate the different phases of the armature winding; (b) Ferrite-assisted synchronous homopolar motor (FaSHM), 1/4 cross-section and stator armature winding layout; (c) 3D cutout view of FaSHM with 1/2 stator cutout and unobstructed rotor.

Table 2 shows the main design parameters of the motors. Figure 3 illustrates the motor phases using capital letters A to C to indicate their order. The presence of a minus sign in Figure 3 signifies the reverse direction of the current within a winding layer. Both considered motors have a 3-phase 8-pole winding. The FaSHM stator has 60 slots, and the number of slots per pole and per phase $q = 60 / (8 \cdot 3) = 2.5$. The FaSynRM stator has 48 slots, and the number of slots per pole and per phase $q = 48 / (8 \cdot 3) = 2$. Unlike the FaSHM, the FaSynRM has only one set of stator and rotor stacks and does not have an excitation winding and its fastening elements, which makes it easier to assemble.

Table 2. Design features of the FaSHM and the FaSynRM.

Parameter	FaSHM	FaSynRM
Phase number		3
Pole number		8
Ferrite magnet grade		Y30H-2
Excitation winding	Yes	No
Number of sets of stator and rotor stacks	2	1
Stator slot number	60	48
Number of the armature winding layers	2	1

Table 2. Cont.

Parameter	FaSHM	FaSynRM
Number of the stator slots per pole and phase q	2.5	2
Rotor slot number	4	-
Rotor flux barrier number per pole	-	4

Figure 4 illustrates the power supply circuit for the FaSHM, comprising a standard three-phase inverter for the multiphase armature winding and a chopper for the excitation winding. On the other hand, the FaSynRM solely necessitates a three-phase inverter without the need for a chopper.

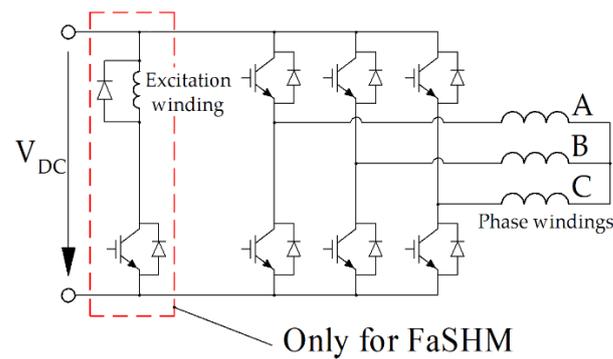


Figure 4. Layout of the three-phase inverter with a DC breaker designed to supply the excitation winding; letters A, B, and C represent the armature winding phases.

4. Objectives and Parameters of the Optimization

Since the external dimensions of the motor are essentially determined by the corresponding dimensions of the car bogie and correspond to the commercial induction motors already used in the drive under consideration, the main emphasis in optimizing the performance is on reducing losses in the duty cycle (see Figure 1) and on reducing the current rating power modules of the traction inverter. When optimizing, it is also necessary to limit torque ripple and prevent irreversible demagnetization of weakly coercive ferrite magnets. Since the applied Nelder-Mead method is an unrestricted method, the constraints are also set by additional terms of the optimization function.

Therefore, the objective function is formulated based on four objectives:

- (1) Minimizing the average electrical losses, denoted as $\langle P_{loss\ el} \rangle$, which is calculated as a weighted average of losses at different operating points;
- (2) Minimizing the maximum armature winding current, indicated by $\max(I_{arm\ i})$, across operating points 1–5;
- (3) Minimizing the maximum torque ripple, indicated by $\max(TR_i)$, across operating points 1–5;
- (4) Reducing to zero δ_{demag} , which represents the cross-section area of magnets exposed to a demagnetization magnetic field stronger than the marginal demagnetization field H_0 , relative to the overall cross-section area of the magnets.

When developing an electric motor, it is important to consider the discrete nature of certain parameters, such as the number of turns (N_{sec}) in the armature winding section and the standardized values of rectangular wire width and height outlined in [32]. However, this study disregards the discreteness of these values and allows them to have any positive real value, aiming to provide a more objective assessment. Random factors arising from different technical specifications in motor development can lead to optimal values of these parameters varying between designs. Specifically, the number of turns in the armature winding (N_{sec}) is chosen so that $V_{DC\ rated} = \max(V_i/k_i)$ [23].

An additional target for FaSHM is the maximum nonsymmetrized torque ripple $\max(TR_{nonsym_i})$. This type of torque ripple is generated by a single pair of stator and rotor stacks, whereas a symmetrized torque ripple is produced by the entire FaSHM, involving all pairs of stator and rotor stacks. The details of the terms TR and TR_{sym} are elaborated in [27].

In the FaSynRM, a significant contribution to the torque is generated by the reluctance torque, and the ferrite magnets play an assisting role. Therefore, when properly designed, the FaSynRM is comparatively strong to irreversible demagnetization. To ensure the strength of FaSynRM to such factors as temperature decrease, transients, or failures of the control system with an overcurrent, the maximum value of the demagnetizing field is constrained to $H_0 = 2$ kOe.

In [14], for the FaSHM, the demagnetizing field was not constrained in the objective function, but it was shown that the demagnetizing field does not exceed 3.2 kOe, while the coercive force of ferrite magnets can be 4 kOe. In contrast to [14], in this paper, H_0 is constrained for the FaSHM as well since it is under comparison with the FaSynRM, in which irreversible demagnetization is also possible. Moreover, in the FaSHM, the magnets make up for the disadvantage of a magnet-free SHM using only half the poles for torque production [14]. Therefore, in the FaSHM, the magnets are subjected to a greater demagnetizing effect compared to the FaSynRM. Trial runs of the optimization routine with a constraint of $H_0 = 2$ kOe showed an unacceptable reduction in efficiency and an increase in the maximum current of the armature winding. For this reason, a constraint of $H_0 = 2.5$ kOe was adopted for the FaSHM, which is somewhat larger than for the FaSynRM.

Also, in contrast to [14], when optimizing both machines, losses in the coasting mode (see Figure 1) with the motor turned off are considered. Even when the motor is turned off, the losses induced by permanent magnets in the magnetic core are not equal to zero, which is significant due to the long duration of this section of the working cycle.

Hence, the objective function of the FaSHM takes the following form:

$$F = \ln(\langle P_{loss} \rangle) + 0.7 \ln(\max(I_{arm\ i})) + 0.025 \ln(\max(TR_{sym_i})) + 0.01 \ln(\max(TR_i)) + 150 \max(\delta_{demag}), \quad (3)$$

where $\langle P_{loss} \rangle$ is the average total loss calculated in accordance with (2); $\max(I_{arm})$ is the maximum armature current; $\max(TR_{sym})$ is the maximum value of the symmetrized torque ripple; $\max(TR)$ is the maximum value of the nonsymmetrized torque ripple; $\max(\delta_{demag})$ is the maximum ratio of the area of permanent magnets with $H > H_0$ to the total area of magnets.

The objective function for the FaSynRM is as follows:

$$F = \ln(\langle P_{loss} \rangle) + 0.7 \ln(\max(I_{arm\ i})) + 0.1 \ln(\max(TR_i)) + 0.1 \ln(M_{rot}) + 0.1 \ln(M_{mag}) + 150 \max(\delta_{demag}), \quad (4)$$

where M_{rot} is the mass of the rotor, and M_{mag} is the mass of the permanent magnets.

The weight constants 150, 1, 0.7, 0.1, 0.025, and 0.01 in Equations (3) and (4) indicate the significance of specific objectives. These values represent the approximate relative priorities assigned to each optimization goal, drawing from the author's experience in designing comparable machines.

A coefficient of 150 at δ_{demag} ensures the selection of designs in which there is no irreversible demagnetization of permanent magnets. The next most important goal (loss $\langle P_{loss} \rangle$) has a weight coefficient equal to unity.

The constant 0.7 signifies that a 1% decrease in the maximal current holds the same value as a 0.7% reduction in average loss. The objectives of minimizing symmetrized and unsymmetrized torque ripples hold relatively lesser significance. The constants 0.025 and 0.01 indicate that all else being equal, designs with lower torque ripples are favored. Additionally, to enhance clarity, the natural logarithm of Equations (3) and (4) is employed.

The fminsearch optimization procedure according to the Nelder-Mead method [33], implemented in the MATLAB software, is described in detail in [34]. The fminsearch (F, x_0)

optimization procedure is launched to minimize the value of the objective function F by successively varying the vector x of electric machine parameters, where x_0 is the vector of initial values of the electric machine parameters.

The procedure for calculating the objective function F , implemented in MATLAB, includes the steps shown in the flowchart in Figure 5. This flowchart is valid for both FaSHM and FaSynRM. However, for FaSHM, the objective function is calculated according to (3), and for FaSynRM, according to (4). Table 3 shows the list of variable parameters for FaSHM and Table 4 for FaSynRM. After building the geometry of the electric machine corresponding to the current value of the vector x , varied by the fminsearch function, its characteristics are calculated at operating points 0–5 (see Figure 2), necessary to calculate the terms of the objective function.

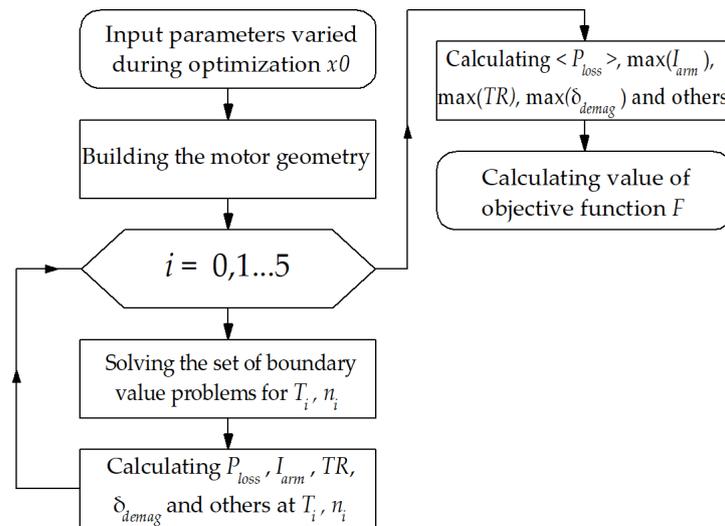


Figure 5. Objective function calculation block diagram.

Table 3. Variable FaSHM parameters.

Parameter	Before Optimization	After Optimization
Housing thickness h , mm	15.6	14.8
Total stator stacks length L_{stator} , mm	219.6	227
Stator slot depth h_p , mm	35.9	31.0
Stator slot width b_p , mm	9.0	7.63
Air gap width δ , mm	4.4	2.98
Rotor slot thickness, α_1	$0.423 \cdot t_z^*$	$0.547 \cdot t_z^*$
Rotor slot thickness, α_2	$0.664 \cdot t_z^*$	$0.706 \cdot t_z^*$
Current angles at operating points 1,2,3,4, electrical radians	0.943; 0.921; 0.404; 0.118	0.726; 0.834; 0.304; 0.0772
Current ratio **	10.55	9.77

Notes: * the FaSHM rotor tooth pitch $t_z = 360^\circ / 4 = 90$ mechanical degrees; ** the current ratio is the ratio of the current in the armature winding layer to the current in the excitation winding cross-section.

Table 4. Variable FaSynRM parameters.

Parameter	Initial Design	Optimized Design
Inner stator radius R_{stat} , m	0.2	0.1943
Stator slot bottom radius R_{bot} , m	0.23	0.2218
Stator slot thickness α_{stat1}	$0.4 \cdot t_{z1}$	$0.622 \cdot t_{z1}$
Air gap, mm	1	2.23
$a_{st i}$, mm	4	6.35
$b_{st i}$, mm	1	1.59
$a_{cut i}$, mm	4	6.95

Table 4. Cont.

Parameter	Initial Design	Optimized Design
$b_{cut\ i}$, mm	1	1.64
c	1.07	1.117
g	1.07	1.113
β , rad	0.01	0.021
b	$0.0777 \cdot \alpha_p$ *	$0.0755 \cdot \alpha_p$
Current angle, electrical degrees	50; 50; 50; 50	66.0; 67.7; 58.2; 55.1

Note: * α_p is the FaSynRM pole pitch; t_{z1} is the FaSynRM stator tooth pitch $t_{z1} = 360^\circ / 48 = 7.5$ mechanical degrees.

5. FaSHM Optimization Parameters and Results

5.1. FaSHM Optimization Parameters

The parameters varied during the optimization of the FaSHM, and fixed ones are shown in Figure 6. Their detailed description and the initial design are given in [14]. Table 5 provides parameters unchanged during the optimization, and Table 3 provides the initial and optimized values of varied ones.

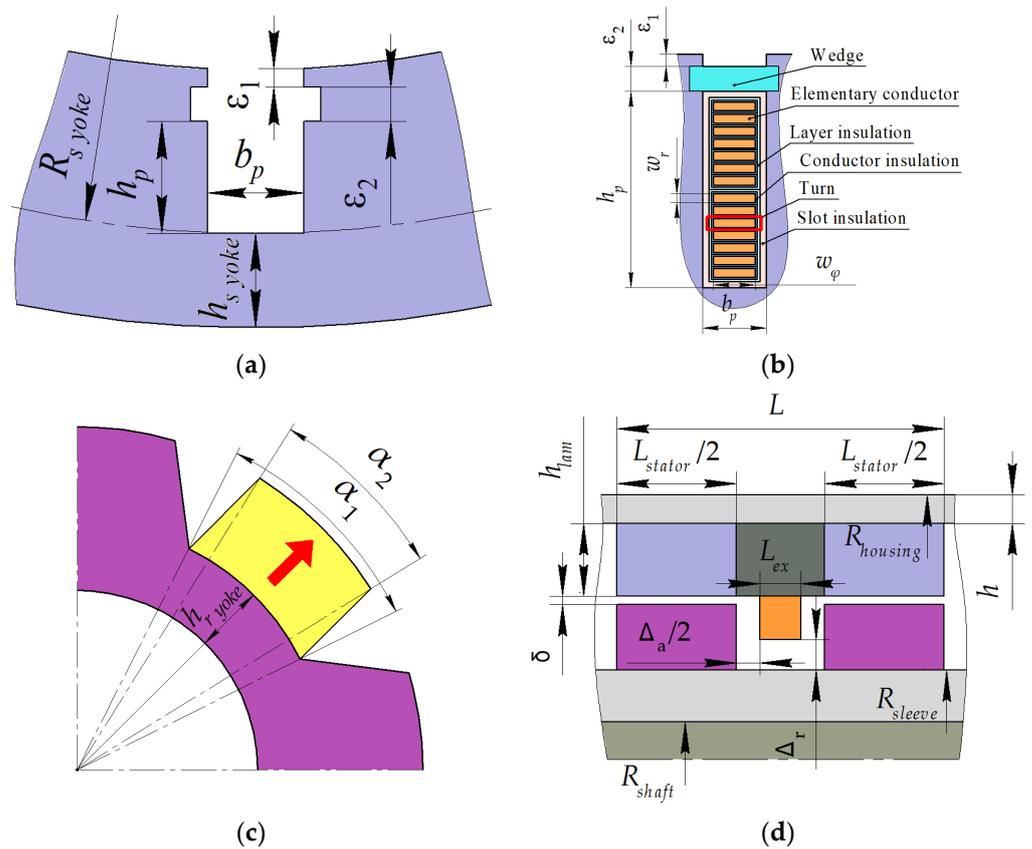


Figure 6. FaSHM parameters. (a) Stator, the red arrow marks the direction of magnetization of the permanent magnet.; (b) Armature winding; (c) Rotor; (d) Axial plane.

Table 5. FaSHM parameters were unchanged during optimization.

Parameter	Value
Machine length excluding winding end parts L , mm	260
Stator housing radius, mm	267
Axial clearance between excitation winding and rotor, Δ_a , mm	29
Radial clearance between field winding and rotor Δ_r , mm	22

Table 5. Cont.

Parameter	Value
Shaft radius R_{shaft} , mm	40
Stator lamination yoke $h_{s\ yoke}$, mm	21
Rotor lamination yoke $h_{r\ yoke}$, mm	17
Stator wedge thickness, ϵ_2 , mm	2
Stator unfilled area thickness, ϵ_1 , mm	3

5.2. FaSHM Optimization Results

As Figure 7 shows, the FaSHM optimization process took 180 calls of the objective function, and its value was significantly reduced.

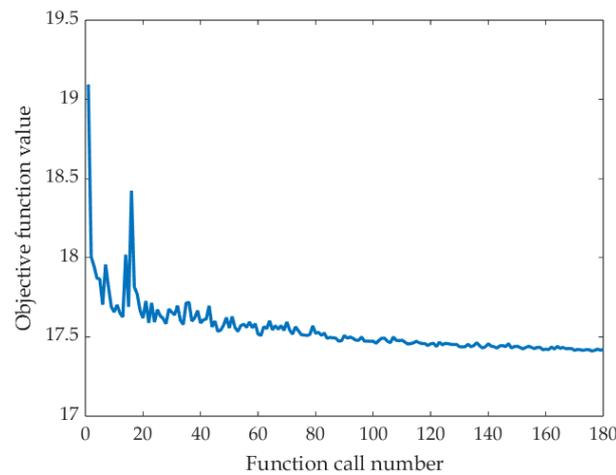


Figure 7. FaSHM optimization progress.

The losses in coasting mode are mainly concentrated in the stator laminated stacks. Its value is 705 W in the design presented in [14] and 639 W in the new design. Other motors' performance characteristics are presented in Table 6.

Table 6. FaSHM optimization results.

Parameter	Design Optimized in [14]					New Design				
	1	2	3	4	5	1	2	3	4	5
Operating Point, i										
Rotational speed n , rpm	4280	4280	2854	0	1427	4280	4280	2854	0	1427
Amplitude of the armature phase current I_{arm} , A	370	541	541	529	531	331	536	537	530	532
Efficiency, %	95.0	95.7	96.5	0	95.7	95.0	95.6	96.4	0	95.5
Output mechanical power P_{mech} , kW	185.3	-370.6	-370.6	0	185.3	185.3	-370.6	-370.6	0	185.3
Torque, N·m	413.4	-826.9	-1240	1240	1240	413.4	-826.9	-1240	1240	1240
Input electrical power, kW	195.0	-354.8	-357.7	5.6	193.6	195.0	-354.4	-357.2	6.1	194.1
Mechanical loss, kW *	3.55	3.55	1.06	0	0.14	3.55	3.55	1.06	0	0.14
Armature DC copper loss, kW	2.20	4.71	4.71	4.49	4.53	1.85	4.83	4.87	4.74	4.78
Armature eddy-current copper loss, kW	1.11	2.70	1.99	0	0.55	0.61	1.78	1.33	0	0.36
Stator lamination loss, kW	2.26	3.56	3.81	0	1.90	3.04	4.46	4.57	0	2.12
Rotor lamination loss, kW	0.04	0.09	0.07	0	0.02	0.11	0.23	0.19	0	0.05
Excitation copper loss, kW	0.55	1.21	1.21	1.13	1.14	0.51	1.37	1.38	1.32	1.33
Total loss, kW	9.72	15.81	12.85	5.62	8.27	9.68	16.22	13.41	6.06	8.77
Average losses according to Formula (2), kW			7.05					7.16		
Number of turns in armature winding			6.58					5.70		
Power factor	0.949	-0.989	-0.963	1.0	0.906	0.99	-0.99	-0.96	1.00	0.93
Line-to-line voltage amplitude V_{arm} , V	640	758	797	10	467	687	757	792	11	452

Table 6. Cont.

Parameter	Design Optimized in [14]					New Design				
	1	2	3	4	5	1	2	3	4	5
Nonsymmetrized torque ripple, %	16.3	15.4	13.5	13.6	13.6	24.0	-22.6	-20.5	21.6	21.6
Symmetrized torque ripple, %	2.50	2.50	2.42	2.61	2.61	9.7	6.9	6.0	6.3	6.2
Magnetic flux density in the housing and the sleeve, T	0.30	0.71	1.04	1.15	1.15	0.36	0.76	1.29	1.43	1.43

Note: * Assuming a proportionate relationship, mechanical losses increase with the cube of speed, reaching a maximum of 3.55 kW at n_{max} .

Figure 8 shows the instantaneous magnitude of the magnetic flux density of the design presented in [14] and the new design. Figure 9 shows the minimum value (with maximum absolute value) of the demagnetization field over the machine cycle in operating point 4 since a short-term application of the demagnetization field stronger than the coercivity of the magnets results in their demagnetization. The entire magnet area in the new design is not subjected to the demagnetization field with an absolute value of more than 2.5 kOe, while the large area of the magnets in the design presented in [14] is. The absolute value of the demagnetization field does not exceed 3 kOe in this case.

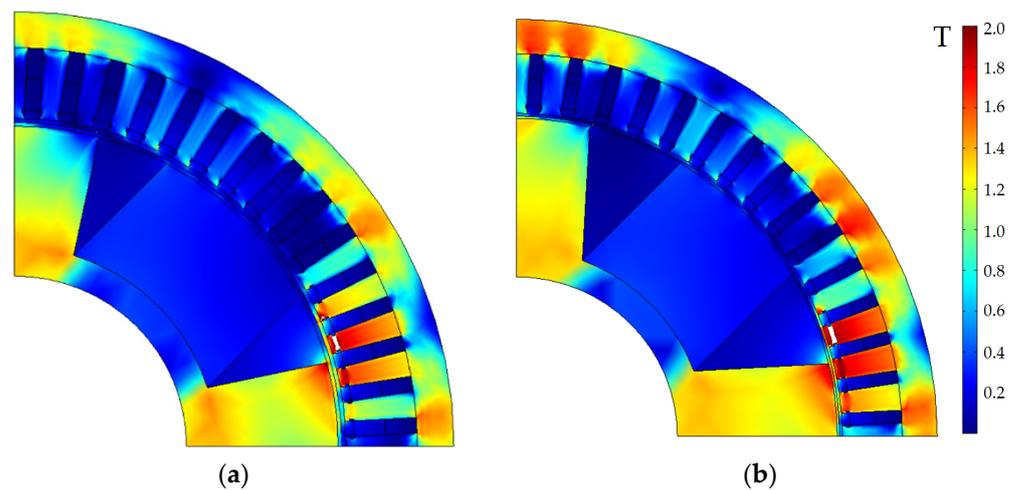


Figure 8. The cross-section of the optimized designs of the FaSHM and the plot of flux density magnitudes at operating point 4; saturation areas (>2 T) are shown with white. (a) Design optimized in [14]; (b) New FaSHM design.

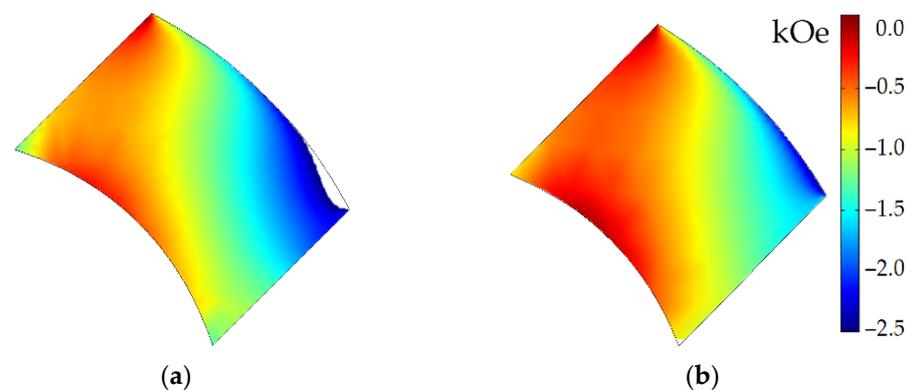


Figure 9. Operating point 4 demagnetizing force (kOe) in the FaSHM permanent magnet zone. Field stronger than -2.5 kOe is not shown (white color is used) (a) Design optimized in [14]; (b) New FaSHM design.

Figure 10 shows the calculated waveforms of the FaSHM: torque ripples at operating points with minimum and maximum torque; cogging torque; back EMF at the operating point where its maximum amplitude is reached, and back EMF at coasting.

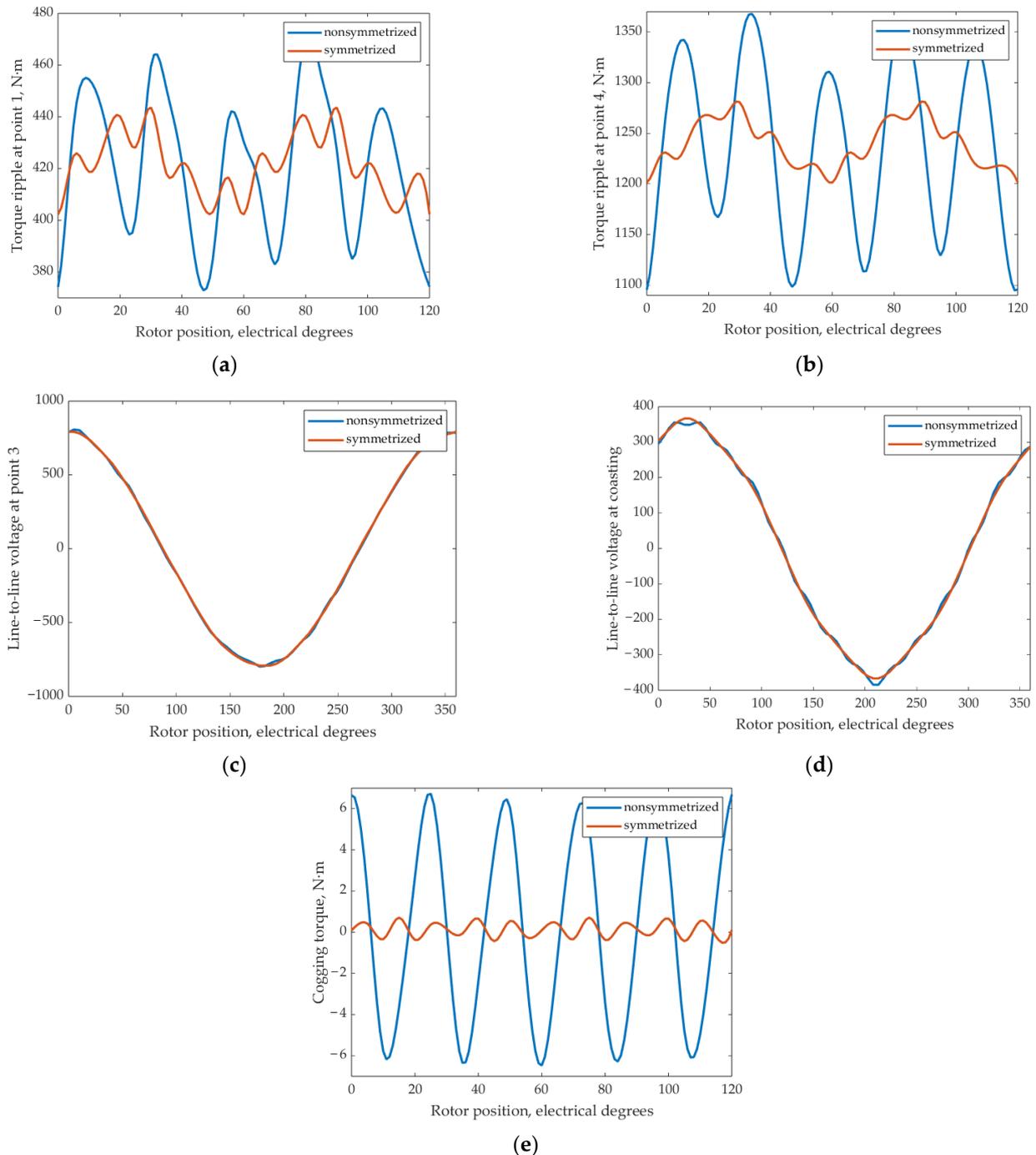


Figure 10. FaSHM calculated waveforms. (a) Torque ripple at operating point 1; (b) Torque ripple at operating point 4; (c) Line-to-line back EMF at operating point 3 (maximum EMF amplitude); (d) Line-to-line back EMF at coasting (operating point 0); (e) Cogging torque.

Comparing the results in Table 6, the differences in the characteristics of the FaSHM design optimized in [14] and the new design are not very large and consist of the following:

- (1) The maximum current decreased slightly by $100\%(541 - 539)/541 = 0.4\%$;

- (2) The main advantage of the new FaSHM design is a significantly increased resistance to demagnetization of magnets. The coercive force of the Y30H-2 magnet is about 4 kOe [35]. In the design optimized in [14], the maximum demagnetizing field is 3 kOe, and the margin is $(4 - 3) = 1$ kOe. In the new design, the maximum demagnetizing field is 2.5 kOe, and the margin is 1.5. Therefore, we can conclude that the new design is one and a half times more reliable for demagnetization of magnets. This is due to an increase in the width of the magnet (equal to the depth of the rotor slot) from 7.5 cm to 8.3 cm [14]. In addition, the lengths of the stator and rotor lamination have increased, which redistributed the flux over a larger area. Reducing the cross-sections of the housing and sleeve led to an increase in flux density;
- (3) Core losses during coasting have been reduced by $100\%(705 - 639)/705 = 9.4\%$, which contributes to the reduction of the average losses;
- (4) However, due to achieving better reliability with respect to demagnetization, the average losses slightly increased by $100\%(7.16 - 7.05)/7.16 = 1.5\%$.

6. FaSynRM Optimization Parameters and Results

6.1. FaSynRM Optimization Parameters

Figure 11 illustrates the parameters that define the FaSynRM geometry. The rotor has 4 magnetic flux barriers per pole. They are numbered 1, 2, 3, 4, starting from the outer barrier and ending with the inner one. The geometry of the magnetic flux barrier is shown in Figure 11b.

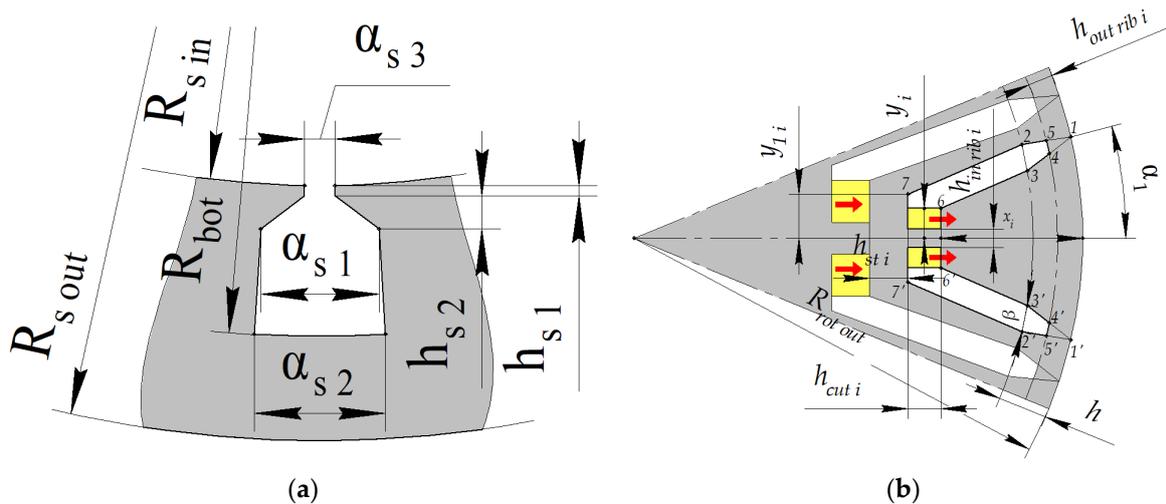


Figure 11. Geometric parameters of the FaSynRM. (a) Stator slot; (b) Rotor flux barrier, red arrows mark the direction of magnetization of the permanent magnets. Areas occupied by ferrite magnets are marked in yellow.

The integrity of the rotor is ensured by internal ribs with thickness $h_{in\ rib\ i}$ in the middle of each barrier and external ribs with thickness $h_{out\ rib\ i}$, adjoining the air gap. On the surface of the rotor, points at a distance α_i of the barrier symmetry axis are 1 and 1', which define the barrier geometry. Points 2, 2', 3, 3' are marked at a distance h from the surface of the rotor. The angular distance between points 2 and 3 and between 2' and 3' is equal to β . A circle of $455'4'$ at a depth equal to the thickness of the outer ribs $h_{in\ rib\ i}$ cuts off triangles $1'4'5'$ and $1'4'5'$ from the barrier. For the outermost edge, points 6 and 6' coincide with points 3 and 3', that is, line $66'$ is drawn between points 3 and 3'. With this exception, the depth x_i of the line is set to $66'$, and the length of this line is $2y_i$. Line $77'$ is drawn at depth $(x_i + h_{cut\ i})$, where $h_{cut\ i}$ is the width of the magnetic flux barrier. The length of this line is $2y_{1i}$. Line $77'$ of the deepest gap limits the area allocated for cutouts in general. Its angular size ϵ is a fixed parameter. Therefore, the parameter y_{1i} is set only for three external magnetic flux barriers.

In this case, $x_{i+1} = x_i + h_{cut\ i} + h_{st\ i}$, where $h_{st\ i}$ is the steel thickness deep behind the barrier. Behind barriers 1, 2, 3 are the following barriers. Behind barrier 4 is the circumference of the inner radius of the rotor. To reduce the optimization parameters, we accept the following relations:

$$\begin{aligned} \alpha_i &= a + b(i - 1/2), i = 1, 2, 3, 4; \\ y_{1i} &= y_i \cdot c, i = 1, 2, 3; \\ y_i &= y_{1i} \cdot g, i = 1, 2, 3, 4; \\ h_{cut\ i} &= a_{cut\ i} + b_{cut\ i}(i - 1), i = 1, 2, 3, 4; \\ h_{st\ i} &= a_{st\ i} + b_{st\ i}(i - 1), i = 1, 2, 3, 4. \end{aligned} \tag{5}$$

The ratio of the widths of the stator slot $\alpha_{stat1} / \alpha_{stat2}$ also does not change. In addition, the variable parameters include the current control angles in operating points 1, 2, 3, 4. Table 7 shows the FaSynRM parameters that are not changed during the optimization. Table 4 shows the FaSynRM parameters that are varied during the optimization.

Table 7. FaSynRM parameters were unchanged during optimization.

Parameter	Value
Machine length excluding winding end parts L , mm	240
Stator outer radius, mm	250
Stator parameter h_{stat1} , mm	1
Stator parameter h_{stat2} , mm	3
Outer rotor ribs thickness h_{outrib} , mm	1
Inner rotor ribs thickness $h_{inrib\ i}$, mm	1.5; 2.5; 3.5; 4
Rotor parameter h , mm	3
Rotor parameter ε	$0.8 \cdot \alpha_p$
Stator slot thickness ratio $\alpha_{stat1} / \alpha_{stat2}$	1.05
Rotor parameter a	$0.4777 \cdot \alpha_p$

6.2. FaSynRM Optimization Results

As Figure 12 shows, the FaSynRM optimization process took 180 calls of the objective function, and its value was significantly reduced.

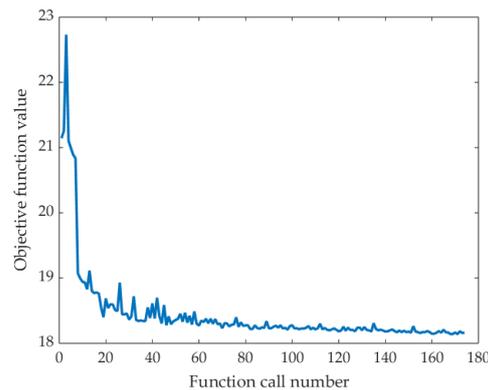


Figure 12. FaSynRM optimization progress.

Table 8 shows the characteristics of the initial and optimized FaSynRM designs. In the open-circuit coasting mode, the voltage at the motor terminals in the initial design and after optimization is 171 V and 207 V, respectively. The magnetic loss density is mainly concentrated in the stator magnetic core and is equal to 840 W and 490 W, respectively. Figure 13 shows the FaSynRM geometry and flux density amplitude at operating points 1–5 listed in Table 1. Figure 14 shows the geometry and flux density amplitude after the FaSynRM optimization. Figure 15 shows the demagnetizing field in the area of permanent magnets on the rotor before and after optimization.

Table 8. FaSynRM Optimization Results.

Parameter	Before Optimization					After Optimization				
	1	2	3	4	5	1	2	3	4	5
Operating Point, <i>i</i>										
Rotational speed <i>n</i> , rpm	4280	4280	2854	0	1427	4280	4280	2854	0	1427
Amplitude of the armature phase current I_{arm} , A	492	886	1381	1393	1402	450	693	833	832	839
Efficiency, %	91.6	93.0	94.1	0	93.4	94.7	95.4	96.0	0	95.3
Output mechanical power P_{mech} , kW	185.30	370.60	370.60	0	185.30	185.30	370.60	370.60	0	185.30
Torque, N·m	413.4	826.9	1240.0	0.2	1240.0	413.4	826.9	1240.0	0.2	1240.0
Input electrical power, kW	202.27	344.75	348.63	8.96	198.50	195.63	353.52	355.95	6.22	194.42
Mechanical loss, kW *	3.55	3.55	1.06	0	0.14	3.55	3.55	1.06	0	0.14
Armature DC copper loss, kW	1.05	3.76	8.96	8.96	8.96	1.76	4.44	6.37	6.22	6.22
Armature eddy-current copper loss, kW	-	-	-	-	-	-	-	-	-	-
Stator lamination loss, kW	11.14	16.61	10.75	0	3.80	4.25	7.88	6.89	0	2.70
Rotor lamination loss, kW	1.24	1.93	1.20	0	0.30	0.77	1.21	0.33	0	0.07
Excitation copper loss, kW	-	-	-	-	-	-	-	-	-	-
Total loss, kW	16.97	25.85	21.97	8.96	13.20	10.33	17.08	14.65	6.22	9.12
Average losses $\langle P_{loss} \rangle$, kW			10.46					7.40		
Number of turns in armature winding			5.95					9.76		
Power factor	0.846	0.678	0.609	1	0.684	0.910	0.791	0.735	1	0.769
Line-to-line voltage amplitude V_{arm} , V	654	757	583	7	297	621	757	665	9	356
Torque ripple, %	27	29	33	33	33	16	16	11	10	10

Note: * The mechanical losses are assumed to be proportional to the speed with a maximum value of 3.55 kW at n_{max} .

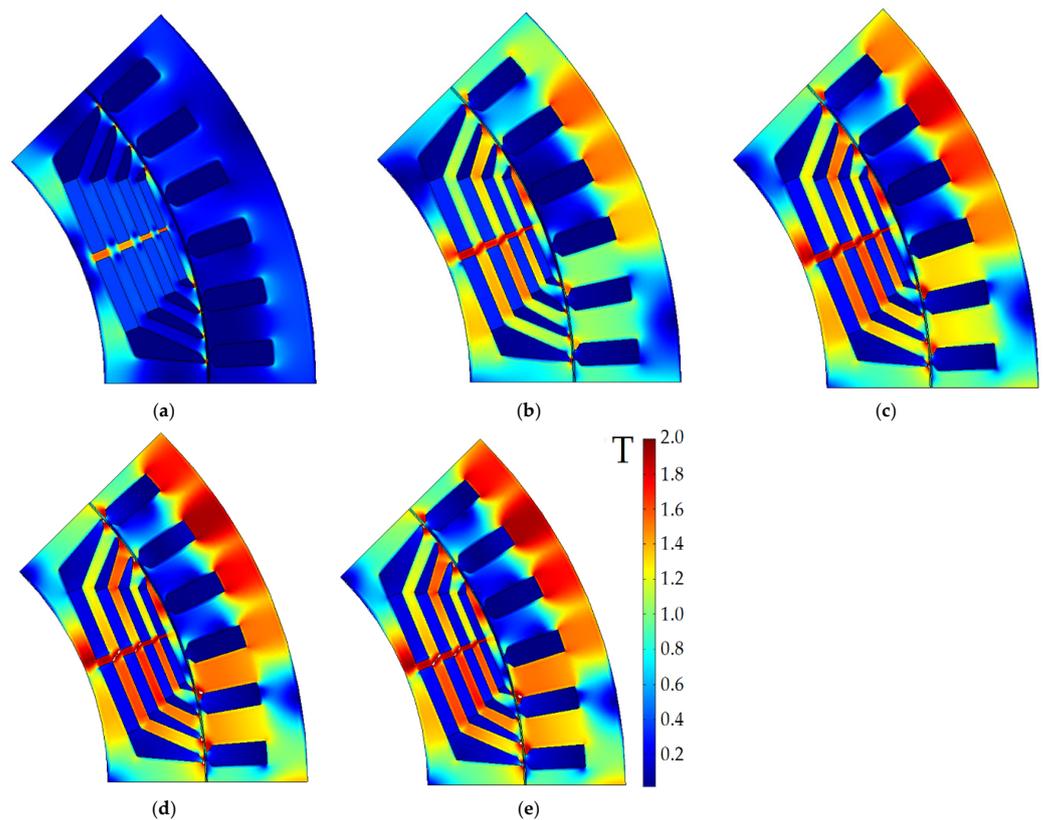


Figure 13. FaSynRM cross-section before optimization, with a plot of flux density modulus at saturation limit (>2 T) highlighted in white. (a) Operating point 1; (b) Operating point 2; (c) Operating point 3; (d) Operating point 4; (e) Operating point 5.

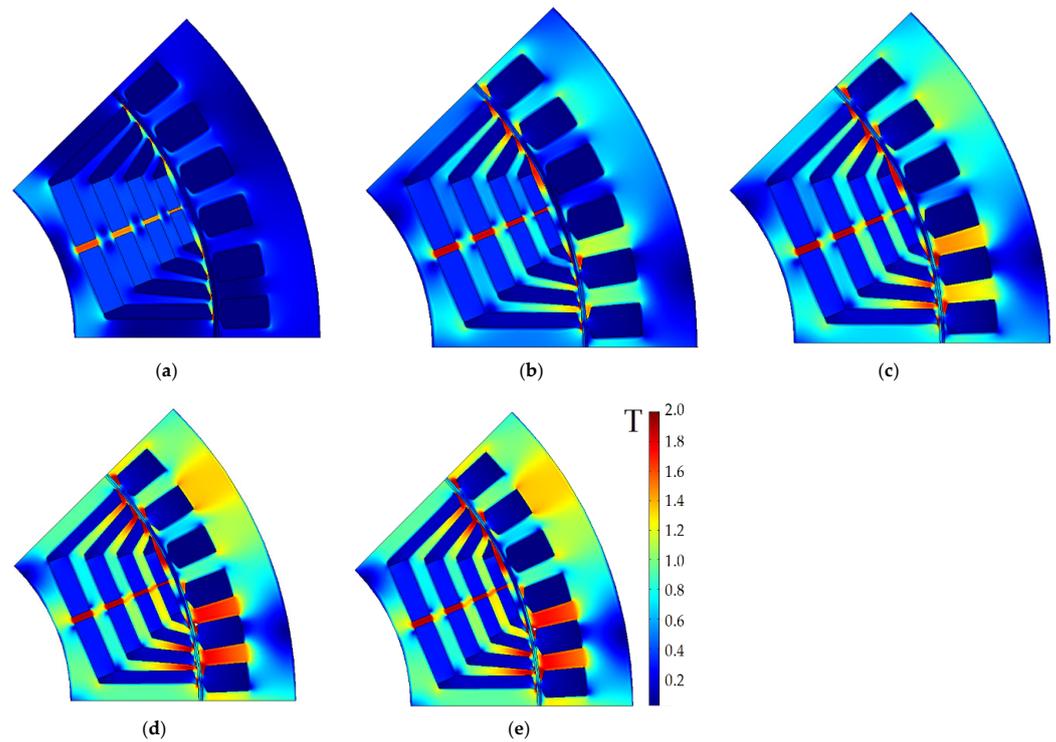


Figure 14. FaSynRM cross-section after optimization, with a plot of flux density modulus at saturation limit (>2 T) highlighted in white. (a) Operating point 1; (b) Operating point 2; (c) Operating point 3; (d) Operating point 4; (e) Operating point.

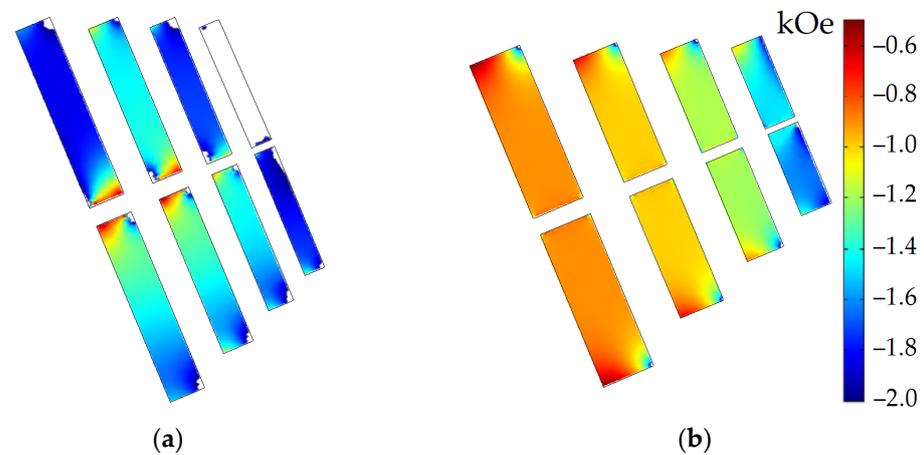


Figure 15. The demagnetizing field in the area of permanent magnets of the PMaSynRM rotor. Areas with the strongest demagnetization (<-2 kOe) are highlighted in white. (a) Before optimization; (b) After optimization.

Figure 16 shows the calculated waveforms of the FaSynRM: torque ripples at operating points with minimum and maximum torque; cogging torque; back EMF at the operating point where its maximum amplitude is reached, and back EMF at costing.

Comparing the characteristics of the FaSynRM before and after optimization, we can draw the following conclusions:

- (1) Average losses were reduced by $100\%(10.46 - 7.4)/10.46 = 29.3\%$;
- (2) Maximum armature winding current decreased by $100\%(1402 - 839)/1402 = 40\%$;
- (3) Maximum torque ripple decreased by $(33 - 10) = 23\%$;
- (4) The share of magnets δ_{demag} exposed to a demagnetizing field of more than 2 kOe decreased from 8.6% to almost zero (0.06%). As can be seen from Figure 15, the -2 kOe

level is reached only in the corners of the magnets, and it can be concluded that the demagnetization of this small share of magnets is not critical. Therefore, we can conclude that with a coercive force of 4 kOe, the optimized design has a large safety margin $(4 - 2) = 2$ kOe. The achievement of a higher resistance to demagnetization of the design after optimization, apparently, was facilitated by an increase in the thickness of the magnets, as well as an increase in the number of turns, and hence a decrease in the turn voltage and magnetic flux in the magnetic circuits.

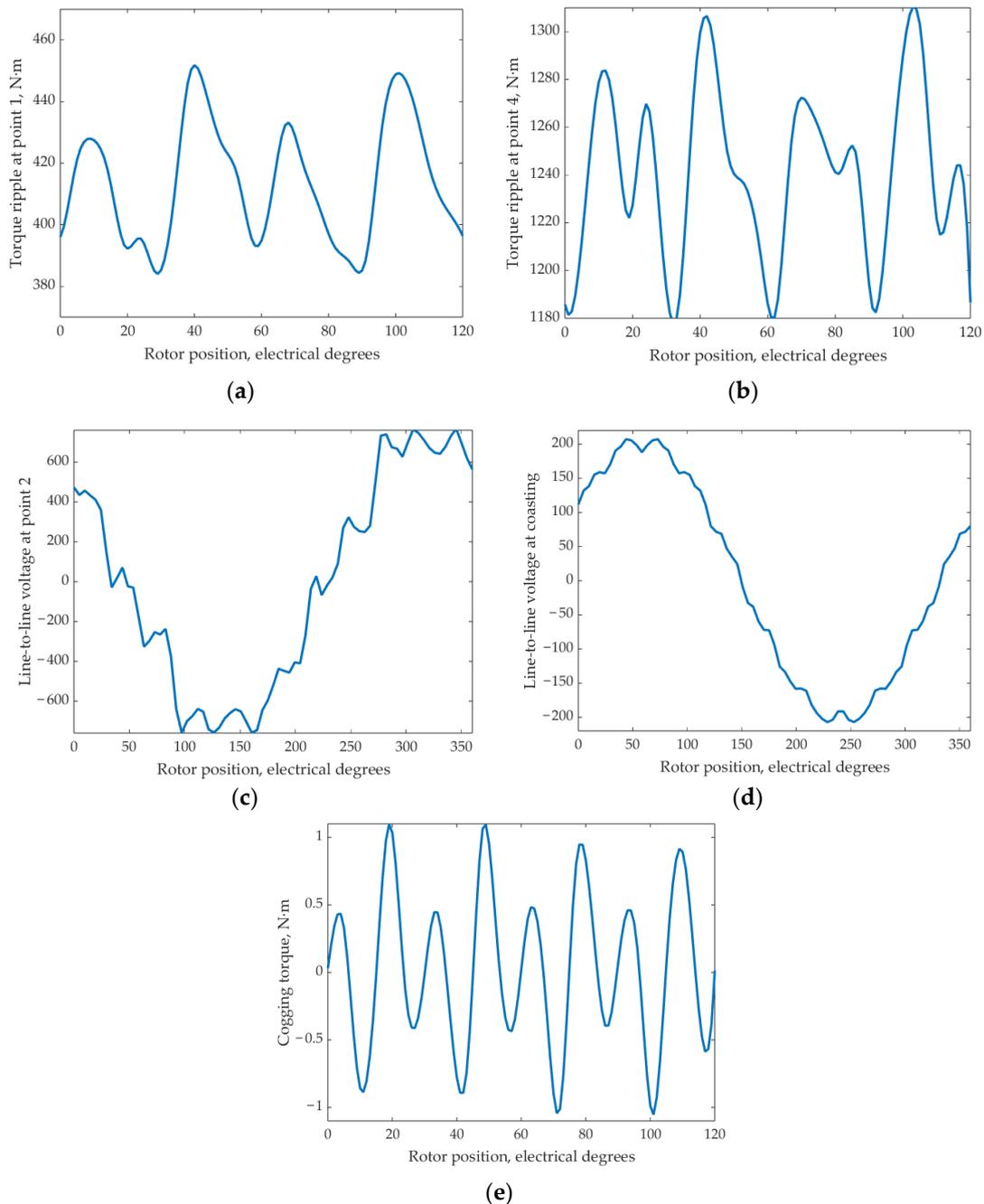


Figure 16. FaSynRM calculated waveforms. (a) Torque ripple at operating point 1; (b) Torque ripple at operating point 4; (c) Line-to-line back EMF at operating point 2 (maximum EMF amplitude); (d) Line-to-line back EMF at coasting (operating point 0); (e) Cogging torque.

7. Comparison of Characteristics of FaSHM and FaSynRM

This section discusses the comparison of the characteristics of the considered electrical machines after optimization. Table 9 compares the performance of the optimized FaSHM and FaSynRM. The FaSHM characteristics are taken from Table 6. The FaSynRM characteristics are taken from Table 8. Table 10 shows a comparison of masses, dimensions, and active material costs.

Table 9. Comparison of the characteristics of the optimized FaSHM and FaSynRM.

Parameter	FaSHM					FaSynRM				
	1	2	3	4	5	1	2	3	4	5
Operating Point, i										
Rotational speed n , rpm	4280	4280	2854	0	1427	4280	4280	2854	0	1427
Amplitude of the armature phase current I_{arm} , A	331	536	537	530	532	450	693	833	832	839
Efficiency, %	95.0	95.6	96.4	0	95.5	94.7	95.4	96.0	0	95.3
Output mechanical power P_{mech} , kW	185.30	370.60	370.60	0	185.30	185.30	370.60	370.60	0	185.30
Torque, N·m	413.4	826.9	1240.0	0.2	1240.0	413.4	826.9	1240.0	0.2	1240.0
Input electrical power, kW	195.0	−354.4	−357.2	6.1	194.1	195.63	353.52	355.95	6.22	194.42
Mechanical loss, kW *	3.55	3.55	1.06	0	0.14	3.55	3.55	1.06	0	0.14
Armature DC copper loss, kW	1.85	4.83	4.87	4.74	4.78	1.76	4.44	6.37	6.22	6.22
Armature eddy-current copper loss, kW	0.61	1.78	1.33	0	0.36	-	-	-	-	-
Stator lamination loss, kW	3.04	4.46	4.57	0	2.12	4.25	7.88	6.89	0	2.70
Rotor lamination loss, kW	0.11	0.23	0.19	0	0.05	0.77	1.21	0.33	0	0.07
Excitation copper loss, kW	0.51	1.37	1.38	1.32	1.33	-	-	-	-	-
Total loss, kW	9.68	16.22	13.41	6.06	8.77	10.33	17.08	14.65	6.22	9.12
Average losses $\langle P_{loss} \rangle$, kW			7.16					7.40		
Power factor	0.99	0.99	0.96	1.00	0.93	0.910	0.791	0.735	1	0.769
Line-to-line voltage amplitude V_{arm} , V	687	757	792	11	452	621	757	665	9	356
Torque ripple, %	9.7	6.9	6.0	6.3	6.2	16	16	11	10	10
Maximum demagnetizing force, kOe			2.5					2		

Note: * The mechanical losses are assumed to be proportional to the speed with a maximum value of 3.55 kW at n_{max} .

Table 10. Comparison of masses, costs, and dimensions of parts of the FaSynRM.

Parameter	FaSHM	FaSynRM
Stator lamination mass, kg	110.5	104.6
Rotor lamination mass, kg	66	78.4
Armature copper mass, kg	41.7	38
Excitation copper mass, kg	8.1	-
Magnets mass, kg	34	20
Weight of the rotor sleeve and motor housing without bearing shields, kg	98.9	-
The total mass of the active materials, rotor sleeve, and motor housing, kg	359.2	241
Stator lamination cost, USD	110.5	104.6
Rotor lamination cost, USD	66	78.4
Armature copper cost, USD	291.9	266
Excitation copper cost, USD	56.7	-
Magnets cost, USD	627.64	369.2
Rotor sleeve and motor housing cost, USD	98.9	-
The total cost of the active materials (electrical steel, copper, permanent magnets), USD *	1152.7	818.2
The total cost of the active materials (electrical steel, copper, permanent magnets) and structural steel of the rotor sleeve and motor housing, USD *	1251.64	818.2
Total length of the stator lamination L , mm	227	240
Total length of the machine, excluding the winding end parts (including spaces for the excitation coils), mm	260	-
Stator lamination outer diameter D , mm	504.4	500
Air gap, mm	2.98	2.23
Active core volume $\pi \cdot L \cdot D^2 / 4$, liters	45.4	47.1

* In the analysis, the following material cost assumptions were considered: copper at 7 USD/kg, laminated electrical steel at 1 USD/kg, non-laminated structural steel (for housing and rotor sleeve of the FaSHM) at 1 USD/kg, and Y30H-2 grade ferrite magnet at 18.46 USD/kg [14,36].

Comparing the characteristics of the FaSHM and FaSynRM from Tables 9 and 10, we can draw the following conclusions:

- (1) In this application, the average loss of the FaSHM is $100\%(7.4 - 7.16)/7.4 = 3.4\%$ less than that of FaSynRM;
- (2) By adjusting the excitation flux, the maximum armature current for the FaSHM is $833/539 = 1.54$ times less than for the FaSynRM, which potentially makes it possible to significantly reduce the cost of power modules of the traction inverter;
- (3) The active volume of magnetic cores, excluding the stator housing, in the FaSynRM is $100\%(47.1 - 45.4)/47.1 = 3.9\%$ higher than in the FaSHM;
- (4) The length of the FaSHM stator laminations is less than that of FaSynRM by $100\%(240 - 227)/240 = 5.4\%$; the length of the FaSHM, taking into account the gap for installing the excitation winding, is greater by $100\%(260 - 240)/260 = 7.7\%$;
- (5) The mass of active materials of the FaSHM is greater than that of the FaSynRM by $100\%(359.2 - 98.9 - 241)/(359.2 - 98.9) = 7.4\%$ excluding the housing and sleeve;
- (6) The cost of the FaSHM active materials is $100\%(1152.7 - 818.2)/818.2 = 29.0\%$ higher than that of the FaSynRM (excluding the housing and sleeve) due to the greater mass of copper and magnets;
- (7) The maximum modulus of the demagnetizing force in the case of the FaSHM is greater than in the case of the FaSynRM by $(2.5 - 2) = 0.5$ kOe. In this case, the demagnetization margin for the FaSynRM is $(4 - 2) = 2$ kOe, and for the FaSHM is $(4 - 2.5) = 1.5$ kOe, where 4 kOe is the coercive force of ferrite magnets. Therefore, the FaSHM requires a more careful design of control algorithms to avoid demagnetization during failures and transients.

8. Conclusions

The article provides a comparative analysis of the optimized designs of the traction ferrite-assisted synchronous reluctance machine (FaSynRM) and the traction ferrite-assisted synchronous homopolar machine (FaSHM) in a subway train drive with a power rating of 370 kW. The machines have an approximately equal outer diameter of the stator lamination. When optimizing the machines, the train movement cycle is considered. To reduce the computational burden during optimization, the computationally efficient Nelder-Mead method is used. Moreover, each time the optimization function is called, the characteristics of one of these machines are calculated only at 6 operating points, from which, using quadrature formulas, the integral characteristics of the machines can be calculated throughout the whole moving cycle.

The goals of machine optimization are to reduce losses in the train moving cycle, the maximum current of the semiconductor inverter, and the torque ripple. In addition, the goal of optimization is to prevent irreversible demagnetization of the ferrite magnets in the rotor.

For the FaSHM, compared with the FaSynRM, the losses are reduced by 3.4%, and the maximum current of the traction inverter is reduced by 1.54 times. For the FaSynRM, compared to the FaSHM, the active core volume is higher by 3.9%. However, for the FaSynRM, the mass of active materials is reduced by 7.4%, and the cost of active materials is reduced by 29% due to the smaller mass of magnets. Also, the FaSynRM has less risk of irreversible demagnetization of the ferrite magnets in the rotor.

In general, it can be concluded that the machines in question have comparable performance. However, the FaSHM has better field weakening capability, which reduces the maximum current, power, and cost of inverter power modules, while the FaSynRM requires fewer permanent magnets at the same torque density and is more resistant to irreversible demagnetization, which reduces its cost and improves reliability.

Future work will involve conducting a comprehensive comparison of the FaSHM with other types of electrical machines utilized in subway drives and other applications.

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V.P.; visualization, V.D. and V.K.; review and editing, V.D., V.K. and V.P. All authors have read and agreed to the published version of the manuscript.

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