



Article Study on Influencing Factors of Paste Coating Thickness of Pervious Concrete

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Abstract: Pervious concrete (PC) is a multifunctional material with good water permeability, noise reduction, and heat absorption properties. The most critical performance indicators of the PC are permeability and strength, which are mainly affected by the cement paste coating thickness (PCT) on the aggregate surface. The experiment was carried out to study the influence of the watercement ratio, superplasticizer dosage, aggregate roughness, and aggregate size on PCT, and a new normalization method was proposed for grey correlation analysis to determine the influence degree of the above factors on PCT. Finally, fitting models for predicting the PCT were established based on experimental data. The experimental results indicate that the influence of the water-cement ratio on PCT can be divided into two stages, whereby the PCT shows a slow decline and then a rapid decline with the increase in water-cement ratio; with the increase in superplasticizer dosage, the PCT represents an exponentially decreasing trend; the PCT increases with the aggregate size and aggregate roughness. Based on the grey correlation analysis, the superplasticizer dosage exerts the greatest influence on PCT, followed by the water-cement ratio, aggregate size, and aggregate roughness. The results of this study revealed the change law of PCT under the action of the above factors, which established the premise of controlling the strength and permeability of PC from the perspective of the PCT and provided a reference for the mixture proportion design.

Keywords: pervious concrete; paste coating thickness; influence degree

1. Introduction

Nowadays, scientists and engineers are putting more effort into designing environmentally sustainable systems. To achieve sustainability, pervious concrete and other materials that use renewable resources have been extensively studied [1,2]. Pervious concrete (PC) is treated as a two-phase material composed of cement paste and aggregate [3]. In the case of today's large-area impermeable concrete pavement structure being applied, the rainwater cannot directly infiltrate into the underground, resulting in groundwater that cannot be compensated, which brings a series of ecological problems. The above problems can be solved by using PC instead of impervious concrete [4-7]. The large, open pore structure (typically in the range of 15–25% interconnected porosity, and pore size ranging from 2 to 8 mm) of pervious concrete allows air and fluids to pass easily from the surface to underlying layers [8]. Previous studies have shown that the typical water-cement ratio for PC is generally between 0.25 and 0.45, the aggregate size is between 5 and 20 mm, and the cement content ranges from 200 kg/m³ to 450 kg/m³ [2,9–12]. According to the needs of the working performance of the fresh mixture, materials such as superplasticizers can be added. Pervious concrete, which is well recognized as one of the key building materials of a sponge city [13], has been widely used in pavement, parking lots, ecological revetment, and other engineering scenarios [14-16]. Moreover, pervious concrete can contribute to



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). reducing the urban heat island effect and acoustic noise as well as improving driving safety on rainy days [17,18].

Previous research consistently focused on the pore structure of PC, which indirectly determines its permeability and strength [19–22], wherein the pore characteristics such as pore size, porosity, tortuosity, distribution, and specific surface were investigated to establish the relationship between pore characteristics and PC performance [23,24]. However, the pore structure of permeable concrete is complex and unpredictable. Different molding methods, mix proportions, and aggregate conditions will form different pore structures, which are challenging to characterize with a simple quantitative description [25]. Essentially, strength, permeability, and pore structure are determined mainly by the cement paste coating thickness (PCT) [26,27].

The PCT determines the pore distribution and the bond state among the aggregates wrapped with cement paste [26,28]. When the PCT increases, the pore size of the PC becomes smaller, and more cement paste is filled among the aggregates. Therefore, the PC strength is improved, but the permeability is correspondingly reduced. Conversely, a reduction in the strength of the PC raises engineering safety concerns when the PCT decreases. Zhongzhen Wang stated that the macroperformance and mesostructure of PC are mainly determined by the PCT and explored the influence of the PCT on the compressive strength, permeability, and characteristics of cement paste and pores [26]. Anthony Torres's study [29] correlated the fundamental properties of pervious concrete, such as the porosity, permeability, and compressive and tensile strengths, with the PCT, and the results showed that the porosity and permeability of the pervious concrete samples decreased with an increase in cementitious paste thickness, but the 28-day compressive strength and splitting tensile strength increased. In addition, the ideal paste thickness (IPT) was proposed [30], which characterized the ability of a cement paste to form a stable film on a smooth, nonabsorbent vertical surface, and the actual paste thickness (APT) represented the ability of cement paste to adhere to and remain on the aggregate surface. Betiglu E. Jimma's work introduced the concept of paste film-forming ability as an additional parameter for characterizing cement paste for pervious concrete applications [30]. However, relevant studies have investigated the relationship between PCT and the macroscopic properties of the PC, but the influence of cement and aggregate factors on PCT has not been fully revealed.

This study aimed to investigate the influence of cement paste and aggregate factors on PCT. In particular, the cement paste factors include water–cement ratio and superplasticizer dosage, and the aggregate factors include aggregate roughness and aggregate size. The experiment was carried out to study the influence of the above factors on PCT. A new normalization method was proposed for grey correlation analysis, and the influence degree ranking of each factor was obtained. Finally, a fitting model for predicting PCT was established.

2. Materials and Methods

2.1. Materials

The P.O 42.5 ordinary Portland cement was used, and its chemical compositions are listed in Table 1. The superplasticizer (SP) was produced by Tianjin Weihe Technology Development Co., Ltd., and its recommended dosage ranged from 0.1% to 0.5% (mass ratio of superplasticizer to cement). Dolomite was chosen as the aggregate because its white cross-section will be used for image analysis (Section 2.4). In previous studies, the main problem encountered with image analysis was that because the hardened cement paste color was similar to the aggregate, it caused certain difficulties and errors in image analysis [26,31,32]. The dolomite aggregates with white cross-sections can be better distinguished from the color of cement paste and pores. Three kinds of dolomite aggregate size on PCT. All aggregates were kept in a saturated, surface-dried condition (SSD) to avoid the influence of aggregate moisture content. Tap water was used throughout the experiment.

Components	Mass Ratio (%)
CaO	51.42
SiO ₂	24.99
Al_2O_3	8.26
Fe ₂ O ₃	4.03
MgO	3.71
SO_3	2.51
Loss on ignition	3.31

Table 1. Chemical composition of cement.

Table 2. Properties of aggregate.

Aggregate Size (mm)	Apparent Density (kg/m ³)	Bulk Density (kg/m ³)	Void Content (%)
5-10		1755	38.57
10-15	2857	1733	39.34
15–20		1691	40.81

2.2. Preparation and Measurement of Aggregate Roughness

A vibration polishing machine was used to produce dolomite aggregates with different roughness (Figure 1) to explore the influence of aggregate roughness on PCT. Aggregates with different roughness (Figure 2) were prepared by adding emery with varying mesh numbers into the vibrating polisher container for polishing. The parameters of polishing are tabulated in Table 3. Given the problem that the aggregate size became smaller during the polishing process, the aggregates were sieved again after polishing.



Figure 1. Vibration polishing machine to produce aggregates with different roughness.



Figure 2. Four groups of aggregates with different roughness.

Group	Mesh Number of Emery	Size of Ceramic Abrasive	Time of Polishing (Hour)	Ra ¹ (µm)	
R1	-		-	342	
R2	240	$3 \times 3 \text{ mm}$	24	209	
R3	400	Regular tri-prism	24	121	
R4	800		24	52	

Table 3. Polishing parameter of four groups of aggregates.

¹ Ra is calculated from Equation (1).

A probe-type surface roughness tester cannot measure the roughness of the aggregate well because of the complex spatial surface of the aggregate, which exceeds the equipment's measuring range. As an emerging technology, the 3D scanner can be utilized to solve this problem because of its fast scanning speed and high scanning accuracy [33]. A DAVID SLS-2 structured light scanner was used to scan four groups of aggregates, R1, R2, R3, and R4, respectively, to obtain their high-density point cloud information for calculating the aggregate roughness. Moreover, the index Ra (the arithmetic mean deviation of the profile [34,35]) is used to characterize the roughness of the aggregate surface, as shown in Equation (1), and the calculation process of the Ra can be seen in Figure 3. First, a random cut plane is inserted into the point cloud of the aggregate. Then, the point cloud coordinates located on the cut plane are extracted and sorted clockwise. Third, a random point is selected from the extracted points as the starting point, and other points are selected clockwise as the calculation objects. When the distance between the last point and the starting point is closest to 2 mm, the Ra is calculated by all the previously selected calculation objects. Fourth, the same method can be used to calculate the Ra value of the remaining points in this cut plane. Fifth, insert a new cut plane and continue to calculate the Ra using the above method. The above steps are implemented by computer programs. In this experiment, the Ra value of a single group of aggregates is the average value after 300 times of sampling using the program. The roughness index Ra for R1, R2, R3, and R4 groups is listed in Table 3 and Figure 2. Four groups of aggregates with different roughness.

$$Ra = \frac{1}{n} \sum_{i=1}^{n} |Z_i| \tag{1}$$

where *n* is the total number of data points, Z_i is the distance that the *i*th point deviates from the midline, and the midline is a line fitted from these *n* points by the least squares method, that is, the fitting line when $\epsilon = \sum (Z_i)^2$ takes the minimum value.



Figure 3. The calculation process of Ra.

2.3. Sample Preparation

The mixture proportion design of the experiment is presented in Table 4, and the cement content of all groups is 300 kg/m^3 . The pouring process can be summarized in two steps: the first step is to place the calculated aggregate (saturated surface dried condition) and 40% of the water into the mixer and stir for 60 s, which keeps moisture on the aggregate surface; the second step is to add the cement and the remaining water

with superplasticizer into the mixer and stir for 120 s. The size of the sample mold is $100 \times 100 \times 100$ mm. There are three main molding methods for PC: the vibration molding method, the manual poking molding method, and the static pressure molding method [36]. The manual poking molding method was used in this experiment. The production process of the specimens is shown in Figure 4. Furthermore, all samples were cured for 28 days under standard curing conditions.

Group	Water–Cement Ratio	Superplasticizer Dosage (%)	Aggregate Size (mm)	Ra (µm)
W/C 1	0.28			
W/C_2	0.30			
W/C_3	0.32	0.1%	10-15	342
W/C_4	0.34			
W/C_5	0.36			
SP_1		0		
SP_2		0.10%		
SP_3	0.28	0.20%	10-15	342
SP_4		0.30%		
SP_5		0.50%		
Size_1			5-10	
Size_2	0.36	0.1%	10-15	342
Size_3			15-20	
R1				342
R2	0.26	0.1%	10–15	209
R3	0.36			121
R4				52

Table 4. Mixture proportion designs of the experiment.



Figure 4. The production process of the specimens. (a) Pour out the fresh mixture from the mixer; (b) put the fresh mixture into the mold and poke the mixture manually; (c) flatten the specimen surface; (d) demold the specimens.

2.4. Image Analysis Method

The PCT can be measured by using a grid and digital measurement calipers [29], the semi-manual hand measurement method [31], the high-precision CT image analysis method [26,32,37], and the cross-sectional image analysis method [23,38]. In contrast, the results obtained by the high-precision CT image analysis method and the cross-sectional image analysis method are more accurate than other methods. The former can obtain the

PCT without damaging the specimen, but the price is high. On the contrary, the latter cuts the specimen into several slices, which is more convenient to operate and less expensive [39]. Hence, the cross-sectional image analysis method was used in this experiment, and the PCT can be calculated as the total area of cement paste divided by the total perimeter of aggregate in a cross-sectional image. ImageJ, the software used to calculate a series of geometric features of the analyzed object within the selected area of an image, was applied to analyze the geometric information of aggregate and cement paste.

In this experiment, the cement content of all specimens was 300 kg/m³. If the cement paste can be evenly wrapped on each aggregate, a change in the water–cement ratio, superplasticizer dosage, aggregate size, and aggregate roughness will not cause the change in the PCT. However, in the preliminary experiments, when the superplasticizer dosage was high, the cement paste flowed with great fluidity to the bottom of the specimen. It caused a blockage, and the PCT of the specimen's upper part changed with the superplasticizer dosage. If the average value of PCT is calculated using all parts of the specimen sections, the PCT of each specimen may be the same due to the same cement content in all specimens, but the vertical PCT distribution of each specimen is different. Therefore, the cross-sectional image analysis method can be used to obtain the change law of PCT of the specimen's upper part under the action of cement and aggregate factors. The specimen was cut into four equal parts ($100 \times 100 \times 25$ mm) along the height. Finally, six cross-section images were obtained, and the four cross-sectional images of the upper part of the specimen were taken as the image analysis objects.

In order to obtain the perimeter of the aggregate, the general procedures of the image analysis have been displayed in Figure 5. First, photograph four cross-sections of the specimen in sequence. A bracket is used to fix the camera and provide annular lighting conditions to ensure imaging quality. Then, keep the bracket position and the camera focal length unchanged, and take a picture of a steel ruler for the next step to obtain the ratio of the actual distance to the pixel size in the picture. Second, import the pictures into the ImageJ software, and the ratio of the actual distance to the pixel size is calibrated according to the picture of the steel ruler in the previous step. Third, convert the image to an 8-bit type. Fourth, perform a threshold segmentation on the image, at which time the aggregates will be marked as a red area. Fifth, perform a binarization operation on the image; and there is some noise in the picture, which can be dealt with by smoothing and noise reduction. The black area in the picture represents aggregates, and the white area represents pores and cement paste. Finally, extract the perimeter of the black area (i.e., the perimeter of the aggregates).



Figure 5. Extraction of the perimeter of aggregate.

For the extraction of the cement paste area, $CaCO_3$ powder was used to fill the pores on the slices, making each pore appear white in the photo, similar to the aggregate color (Figure 6a). In addition, the process shown in Figure 5 can be used to extract the area of cement paste. The processed picture is shown in Figure 6b, where the black area represents the cement paste and the white area represents pores and aggregates. In this way, the area of cement paste is extracted.



Figure 6. Extraction of the area of cement paste. (**a**) Filling CaCO₃ powder into pores; (**b**) the cement paste is selected in the image.

The aggregate perimeter and cement paste area in four sections were determined based on the above process. The average value of the cement area divided by the aggregate perimeter on the four sections is taken as the PCT of this specimen.

3. Results and Discussion

3.1. Influence of Cement Paste and Aggregate Factors on PCT

The experiment was carried out to study the influence of the water–cement ratio, superplasticizer dosage, aggregate roughness, and aggregate size on PCT, which established the premise of controlling the strength and permeability of PC from the perspective of PCT and provided a reference for the mixture proportion design.

3.1.1. The Influence of Water–Cement Ratio on PCT

Figure 7 reflects the influence of the water–cement ratio on PCT. The PCT showed a downward trend when the water–cement ratio increased from 0.28 to 0.36. Furthermore, when the water–cement ratio is between 0.28 and 0.32, the decline of PCT is relatively slow, accounting for 30.5% of the total decline; when the water–cement ratio is greater than 0.32, the decrease is larger, accounting for 69.5% of the total decline. During the experiment (Figure 4), aggregates with their paste coating were taken out for close observation. When the water–cement ratio was low, the fluidity of the paste was poor. It can be seen that the contour characteristics of the aggregate itself are covered by the paste coating. The paste coating showed more irregular protrusions and high roughness, as shown in Figure 8a. When the cement fluidity increases due to the rise in the water–cement ratio, less cement paste can be wrapped on the aggregate surface. As shown in Figure 8b, the cement paste forms a smooth, relatively thin paste coating on the aggregate surface, and the original contour characteristics of the aggregate can be seen at this time.

Based on existing research [40], the initial fluidity of fresh cement paste depends mainly on the free water content. At any mix proportion (water–cement ratio and superplasticizer– cement ratio), the cement paste can flow only if the free water content is greater than a critical value (called critical free water content, denoted as W_0/C); when the system is bleeding, even if the free water is increased (by increasing the water–cement ratio or superplasticizer–cement ratio), all the additional free water will be bleeding and will no longer affect the initial fluidity. At this time, the free water content is called saturated free water content, denoted as W_1/C . The necessary condition for the proper fluidity of fresh cement paste is that its free water content is within the range of $(W_0/C, W_1/C)$. In this range, the higher the free water content, the greater the initial fluidity [41]. In this experiment, with the increase in the water–cement ratio, the free water content in cement paste increases, which enhances the fluidity of cement paste and reduces the yield stress and apparent viscosity of cement paste, so the cement paste wrapped on the surface of aggregate decreases accordingly.



Figure 7. Change law of PCT under the action of water–cement ratio. Error bars are standard deviations based on 4 replicates.



* Both aggregates with paste-coating were taken out from the fresh mixture in the experiment.

Figure 8. Shape changes of paste-coating under the action of water-cement ratio.

It can be seen in Figure 7 that the change in PCT with the increase in the water–cement ratio can be divided into two stages. When the water–cement ratio is between 0.28 and 0.32, the free water content in the cement paste is only slightly higher than or equal to the critical free water content, and the fluidity of the cement paste is small. Hence, the PCT slowly decreases with the increase in the water–cement ratio, which means the water–cement ratio has less influence on the PCT. When the water–cement ratio is between 0.32 and 0.36, the free water content in the cement paste gradually increases, so the PCT begins to decrease relatively quickly, which means the water–cement ratio has a certain influence on PCT.

3.1.2. The Influence of Superplasticizer Dosage on PCT

After the superplasticizer was added to the concrete mixture, it exerted a dispersing effect on the cement particles, which can improve the workability and fluidity of the cement mixture [42]. The influence of superplasticizer dosage on PCT is illustrated in Figure 9, where the PCT showed a declining exponential trend with the increase in superplasticizer dosage. The reason is that a large superplasticizer dosage in the mixture proportion significantly improves the fluidity of cement paste, thus reducing the limit value of the PCT on the aggregate surface, which manifests as a rapid decrease in PCT with the increase in superplasticizer dosage.



Figure 9. Change law of PCT under the action of superplasticizer dosage. Error bars are standard deviations based on 4 replicates.

Without the superplasticizer, the cement and water are mixed to form a cement suspension system. The charge characteristics of different mineral phases and the surface of early hydration products in the system are different, attracting each other to form a flocculation structure and wrapping large amounts of mixed water, thereby reducing the fluidity of the paste [43,44]. After adding the superplasticizer, the superplasticizer molecules dissociate into macromolecular anions in water and adsorb on the surface of cement particles and their hydration products so that the absolute value of the zeta potential of particles increases, the electrostatic repulsion between particles increases, the formation of flocculation structures in the system is destroyed and inhibited, and the free water in the system increases [45]. Macroscopically, the fluidity of the paste has improved. Thus, the greater the superplasticizer dosage, the greater the absolute value of the zeta potential, and the better the superplasticizer dosage increases the fluidity of cement paste, which is consistent with the experimental results. The superplasticizer dosage exerts a great effect on PCT, showing a declining exponential trend with the increase in the superplasticizer dosage.

The guiding significance of this conclusion for practical engineering is that, when designing the mixture proportion of PC, it is necessary to control the superplasticizer dosage precisely. An excessive superplasticizer dosage will lead to extreme fluidity of the mixture, and the cement paste during pouring will flow to the bottom of the material because of its gravity and the vibration of the vibrating process, thereby resulting in blockage at the bottom of the material (Figure 10). On the contrary, adding too little superplasticizer is not advantageous for the workability of the fresh mixture, particularly when the water–cement ratio is low.



Figure 10. Blockage at the bottom of the PC sample.

3.1.3. The Influence of Aggregate Roughness on PCT

The influence of aggregate roughness on PCT is shown in Figure 11. With the increase in aggregate roughness index Ra, the PCT rapidly increased and tended to be stable in the end, which reflects that the cement paste was more likely to adhere to the rough aggregate surface. On the micro scale, with the increase in aggregate roughness index Ra, the aggregate surface is more tortuous, which increases the actual area of the aggregate surface, thus increasing the anti-slide force between the aggregate surface and cement paste. From a macro perspective, the friction coefficient of the aggregate surface increases with the aggregate roughness index Ra, thereby enhancing the anti-slide force. The abovementioned mechanism explains the phenomenon that the PCT increase with aggregate roughness index Ra. When the index Ra of aggregate is larger than 200 μ m, the anti-skid force between the aggregate surface and fresh cement paste will gradually reach the maximum value, so the PCT tends to be stable with the increase in the index Ra.



Figure 11. Change law of PCT under the action of aggregate roughness index Ra. Error bars are standard deviations based on 4 replicates.

Based on the existing research [46], the bond tensile strength of the aggregate-mortar interface increases with the aggregate roughness and tends to a constant value; the shear strength of the aggregate-mortar interface increases with the aggregate roughness; and the splitting tensile strength and the axial compressive strength of concrete increase with the aggregate roughness. Thus, the shear and tensile strengths of the aggregate-fresh cement

paste interface will decrease with the decrease in the aggregate roughness, and the bond strength of the aggregate–cement paste interface after cement hardening will also decrease with the decrease in the aggregate roughness, which ultimately affects the overall strength of PC. Therefore, too-round and smooth aggregates should be avoided in PC production.

3.1.4. The Influence of Aggregate Size on PCT

In practical projects, the aggregate size ranges from 5 mm to 20 mm [31,47]. Therefore, three types of aggregates with particle sizes ranging from 5–10 mm, 10–15 mm, and 15–20 mm were used to investigate the influence of the aggregate size on PCT. The influence of the aggregate size on PCT is shown in Figure 12. With the increase in the aggregate size, the PCT shows a gradual increase, characterized by relatively slow growth at first and then rapid growth.



Figure 12. Change law of PCT under the action of aggregate size. Error bars are standard deviations based on 4 replicates.

During the experiment, the cement paste volume (denoted as V) and the aggregate mass (denoted as M) are fixed. However, the specific surface area (denoted as S) of the aggregate with a small size is larger than that of the aggregate with a large size. Assuming that the cement paste is uniformly wrapped on each aggregate, then the PCT can be expressed as $V/(S \times M)$. Therefore, under the same cement paste volume and aggregate mass, the larger the aggregate size is, the greater the PCT is. However, the increase in PCT caused by the increase in aggregate size does not promote PC strength but exerts the opposite effect. The PC strength decreases with the rise in aggregate size [12,48–51]. It is because the specific surface area of an aggregate with a small size is larger, thereby increasing the bonding region [26] between aggregate and improving the material strength. In practical application, selecting an aggregate with medium particle size is beneficial to maintain a balance between strength and permeability.

3.2. Influence Degree of Cement Paste and Aggregate Factors on PCT

The influence law of different factors on the PCT has been explored in the previous chapters, but the specific influence degree is unknown. For example, suppose the engineers want to improve the PC strength. In that case, it is possible to reduce the water–cement ratio, reduce the superplasticizer dosage, increase the aggregate size, and use the aggregate with higher a roughness from the perspective of increasing the PCT. However, it is necessary further to analyze the influence degree of various factors on PCT to determine which way is more effective, which is of great significance for the mixture proportion design of PC

and even the balance of the material strength and permeability. In this section, the grey correlation degree method [52,53] was used to determine the influence degree of various factors on PCT.

3.2.1. Grey Relational Analysis

The grey system theory [54], founded by Chinese scholar Julong Deng in 1982, is a new method to study the problems of fewer data, poor information, and uncertainty. The grey system theory provides a new statistical analysis method—grey relational analysis (GRA). The GRA uses the order of grey correlation degree to describe the strength, size, and order of the relationship between factors to judge each factor's influence on the system's development. The greater the grey correlation degree γ_i of a factor, the greater the contribution of the factor to the development of the system, and vice versa. The influence of the four factors (water-cement ratio, superplasticizer dosage, aggregate roughness, and aggregate size) on PCT can be understood as a grey system, which could use the grey correlation degree to manifest the influence degree of each factor on PCT. The calculation process of the grey correlation degree can be divided into four steps. First, taking PCT as the reference sequence X0, the water-cement ratio, superplasticizer dosage, aggregate roughness, and aggregate size are considered the comparison sequences X1, X2, X3, and X4, respectively. Second, in order to eliminate the gap caused by the non-uniform dimension of each factor, all data sequences are normalized by Equation (2). Third, the grey correlation coefficient $\xi_i(k)$ of all data in each comparison sequence is calculated by Equation (3). $\xi_i(k)$ reflects the degree of difference between the comparison sequence Xi and the reference sequence X0 on the *k*th value. Last, the grey correlation degree γ_i of each comparison sequence is calculated by Equation (4).

$$f(x(k)) = \frac{x(k)}{\overline{x}}$$
(2)

where x(k) is the *k*th value of the data sequence to be normalized, \overline{x} is the average value of the data sequences.

$$\xi_i(k) = \frac{\min_i \min_k |x_0(k) - x_i(k)| + \rho \cdot \max_i \max_k |x_0(k) - x_i(k)|}{|x_0(k) - x_i(k)| + \rho \cdot \max_i \max_k |x_0(k) - x_i(k)|}$$
(3)

where $|x_0(k) - x_i(k)|$ is the absolute difference between sequence X0 and sequence Xi, $min_imin_k|x_0(k) - x_i(k)|$ is the two-level minimum absolute difference, $max_imax_k|x_0(k) - x_i(k)|$ is the two-level maximum absolute difference, ρ is the resolution coefficient, which is usually taken as 0.5.

$$\gamma_i = \frac{1}{n} \sum_{k=1}^n \xi_i(k) \tag{4}$$

where *n* is the data number of the comparison sequence Xi, $\xi_i(k)$ is the grey correlation coefficient corresponding to each data point in the comparison sequence Xi.

After calculation, the grey correlation degree γ_i of the water–cement ratio, superplasticizer dosage, aggregate roughness, and aggregate size are 0.898, 0.739, 0.879, and 0.914, respectively. Based on the above calculation result, the grey correlation degree of the superplasticizer dosage is the lowest, indicating that the influence degree of the superplasticizer dosage on PCT is the lowest, which is inconsistent with the experimental phenomenon and data. It is because the above calculation results only conform to the mathematical relationship between the reference sequence and the comparison sequence and do not take into account the common value range of each factor.

Therefore, a new normalization method is proposed to normalize the sequence data, as shown in Equation (5). We can use this equation instead of Equation (2) mentioned above, then continue to calculate the grey correlation coefficient $\xi_i(k)$ (Equation (3)) and grey correlation degree γ_i (Equation (4)) of each comparison sequence. The new result after grey relational analysis considers the common value ranges of each factor, which means

that the new result is no longer limited to reflecting the mathematical relationship between the reference sequence and the comparison sequence but can provide better guidance for practical application.

$$f(x(k)) = \frac{V_{max} - x(k)}{V_{max} - V_{min}}$$
(5)

where V_{max} and V_{min} are the maximum and minimum values of the common value range of the factor, respectively. x(k) is the *k*th value of the data sequence to be normalized.

3.2.2. Grey Relational Analysis by New Normalization Method

Based on the literature about pervious concrete [2,5,9–12], the common value range of the water–cement ratio in PC is generally 0.25–0.45; the superplasticizer dosage is about 0.1–1% based on the type and brand, and 0.1–0.5% is considered the common value range of the superplasticizer used in this experiment; the aggregate size is usually 5–20 mm. According to the calculation method of aggregate roughness in Section 2.2, the roughness index Ra of rough aggregates is about 350 μ m, and the index Ra is around 50 μ m in smooth pebbles.

The new normalization method introduced in Section 3.2.1 was used to normalize the sequence data, and the grey correlation coefficient $\xi_i(k)$ and grey correlation degree γ_i of each comparison sequence were calculated by Equations (3) and (4). The calculated $\xi_i(k)$ and γ_i of each comparison sequence (X1, X2, X3, X4) are shown in Table 5. The results show that the degree of influence of cement paste-related factors on PCT is greater than that of aggregate-related factors on PCT in general. Particularly, the superplasticizer dosage exerts the greatest influence on PCT, followed by the water–cement ratio, aggregate size, and aggregate roughness. It can be concluded that the most effective way to control PCT in practical applications is to change the superplasticizer dosage. However, it is necessary to pay attention to the excessive superplasticizer that will cause severe bottom blockage. In contrast, the aggregate roughness performs the slightest influence on PCT.

Xi	X1 Water–Cement Ratio	X2 Superplasticizer Dosage	X3 Aggregate Roughness	X4 Aggregate Size
$\xi_i(k)$	0.520	1.000	0.378	0.544
	0.533	0.956	0.542	0.558
	0.560	0.879	0.798	0.588
	0.607	0.784	0.791	0.640
	0.560	0.879	0.399	0.879
	0.455	0.792	0.343	0.337
	0.680	0.822	0.348	0.484
	0.750	0.665	0.365	0.518
	0.944	0.604	0.406	0.604
	0.831	0.448	0.457	0.725
	0.680	0.822	0.348	0.484
	0.609	0.822	0.348	0.484
	0.566	0.854	0.354	0.495
	0.542	0.927	0.365	0.518
γ_i	0.631	0.804	0.446	0.561

Table 5. The grey correlation coefficient $\xi_i(k)$ and grey correlation degree γ_i of each comparison sequence.

3.3. Statistical Model for Predicting PCT

Based on the experiment results, taking the water–cement ratio, superplasticizer dosage, aggregate roughness, and aggregate size as independent variables, the PCT is considered the dependent variable for linear regression analysis. The predicting model was established to predict the PCT under different factors, as shown in Equation (6). The fitting statistics of the model are shown in Table 6. The predicting model passed the F test (F = 77.824, p = 0.000 < 0.05). The F value is the statistical value of the F test. The regression model is statistically significant when the *p*-value corresponding to the F value is less than

0.05. The multicollinearity test of the model found that all the VIF (variance inflation factor) values in the model were less than 5, which means that there is no collinearity problem. The D-W (Durbin-Watson test) value is near 2, indicating no autocorrelation in the model and no correlation between the sample data. Overall, the proposed predicting model has a high degree of accuracy and shows a good fit. Based on the fitting statistics, aggregate size and aggregate roughness exert a significant positive effect on PCT, and superplasticizer dosage and water–cement ratio perform a significant negative effect on PCT. According to the grey correlation analysis results in Section 3.2.2, the influence of the aggregate roughness on the PCT is the lowest. Therefore, the contour maps are used to represent the prediction of the PCT by Equation (6) under the change in the water–cement ratio, superplasticizer dosage, and aggregate size (the default aggregate roughness Ra is 342 μ m), as shown in Figure 13.

$$PCT = 0.37980 + 0.00022R + 0.00900S - 36.44127SP - 0.41405WC$$

$$R^{2} = 0.972$$
(6)

where R is the aggregate roughness, S is the aggregate size, SP is the superplasticizer dosage, and WC is the water–cement ratio.

Standard VIF D-W p-Value (Durbin-Watson Test) Error (Variance Inflation Factor) 0.04151 0.000007 Intercept Aggregate roughness 0.00003 0.000099 1.352 0.000129 Aggregate size 0.00141 1.000 2.244 0.000000 Superplasticizer dosage 1.232 2.51412 0.001665 Water-cement ratio 0.09362 1.608



Figure 13. Prediction of the PCT under the change of water–cement ratio, superplasticizer dosage and aggregate size (the default aggregate roughness Ra is $342 \ \mu\text{m}$). (a) aggregate size ranges from 5–10 mm; (b) aggregate size ranges from 10–15 mm; (c) aggregate size ranges from 15–20 mm.

4. Scope for Future Research and Conclusions

The experiment was carried out to study the influence law and degree of the watercement ratio, superplasticizer dosage, aggregate roughness, and aggregate size on PCT. The most critical performance indicators of PC are permeability and strength, which are mainly affected by the PCT. The work carried out in this study is only the first step in exploring the seepage and strength characteristics of pervious concrete from the perspective of the PCT. In the future, researchers can continue exploring the PCT's non-uniform distribution along the height direction of specimens under different mixture proportions. Try to describe the

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Table 6. Fitting parameters of the prediction model.

non-uniform distribution of the PCT along the height direction of the specimens through several distribution functions, and then establish a series of numerical models of pervious concrete that consider the non-uniform distribution of the PCT. Further, the numerical simulation can be used to verify the experimental results and explore the influence of the PCT on the performance of pervious concrete.

The main conclusions of this study are summarized below:

- (1) The influence of the water-cement ratio on PCT can be divided into two stages. When the water-cement ratio is between 0.28 and 0.32, the PCT decreases slowly with the increase in the water-cement ratio; when the water-cement ratio is between 0.32 and 0.36, the PCT begins to decrease relatively quickly. The PCT shows a declining exponential trend with the increase in superplasticizer dosage. When designing the mix proportion of PC, it is necessary to control the superplasticizer dosage precisely.
- (2) The PCT increases with the increase in aggregate roughness. Under the same circumstances, the larger the aggregate size, the larger the PCT.
- (3) A new normalization method is proposed for grey relational analysis. The common value ranges of different factors are considered in this new method, which is more suitable for multi-factor impact analysis on the PCT.
- (4) The result of the grey relational analysis shows that the superplasticizer dosage exerts the greatest influence on PCT, followed by the water–cement ratio, aggregate size, and aggregate roughness.
- (5) Taking the water-cement ratio, superplasticizer dosage, aggregate roughness, and aggregate size as independent variables and the PCT as a dependent variable, a predicting model was established to predict the PCT under different factors.

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