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Bridge Condition Deterioration Prediction Using the Whale Optimization Algorithm and Extreme Learning Machine

Liming Jiang¹, Qizhi Tang^{1,*}, Yan Jiang^{1,2,*}, Huaisong Cao³ and Zhe Xu⁴

- State Key Laboratory of Mountain Bridge and Tunnel Engineering, Chongqing Jiaotong University, Chongqing 400074, China; jlm1065155897@163.com
- ² College of Engineering and Technology, Southwest University, Chongqing 400715, China
- ³ Chongqing Yuhe Expressway Co., Ltd., Chongqing 400799, China; 19912422134@163.com
- ⁴ Guangxi Nanbai Expressway Co., Ltd., Nanning 530029, China; xz18844090147@163.com
- * Correspondence: tangqizhi1015@163.com (Q.T.); xnjtjiangyan@163.com (Y.J.)

Abstract: To address the problem in model computations and the limited accuracy of current bridge deterioration prediction methods, this paper proposes a novel bridge deterioration prediction method using the whale optimization algorithm and extreme learning machine (WOA-ELM). First, we collected a dataset consisting of 539 sets of bridge inspection data and determined the necessary influencing factors through correlation analysis. Subsequently, the WOA-ELM algorithm was applied to establish a nonlinear mapping relationship between each influencing factor and the bridge condition indicators. Furthermore, the extreme learning machine (ELM), back-propagation neural network (BPNN), decision trees (DT), and support vector machine (SVM) were employed for comparison to validate the superiority of the proposed method. In addition, this paper provides further substantiation of the model's exceptional predictive capabilities across diverse bridge components. The results demonstrate the accurate predictive capability of the proposed method for bridge conditions. Compared with ELM, BPNN, DT, and SVM, the proposed method exhibits significant improvements in predictive accuracy, i.e., the correlation coefficient is increased by 4.1%, 11.4%, 24.5%, and 33.6%, and the root mean square error is reduced by 7.3%, 18.0%, 14.8%, and 18.1%, respectively. Moreover, the proposed method presents considerably enhanced generalization capabilities, resulting in the reduction in mean relative error by 11.6%, 15.3%, 6%, and 16.2%. The proposed method presents a robust framework for proactive bridge maintenance.

Keywords: bridge engineering; inspection data; deterioration condition prediction; whale optimization algorithm; extreme learning

1. Introduction

The number of highway bridges in China exceeded 960,000 in 2023. With the passage of time, these bridge structures inevitably experience performance degradation, caused by the coupled effects of external service environment factors and internal material deterioration [1–3]. Accurately predicting bridge performance evolution holds great theoretical and practical importance for scientific maintenance and extending structural service life [4–6].

Extensive research has been conducted by a considerable number of scholars on the establishment of bridge condition prediction models, which are broadly categorized into deterministic and probabilistic models [7]. The former category assumes a fixed and deterministic degradation trend for bridge condition, and utilizes historical periodic inspection data to perform regression fitting of predefined deterioration decay equations. Through this process, the degradation rate of bridge performance under different conditions is estimated. For instance, Yang et al. [8] employed detection data from 398 reinforced concrete bridges to fit a bridge condition degradation model that reveals the changing characteristics of bridge performance during different operational phases. Similarly, Sahar et al. [9] established a degradation regression model for the superstructure of bridges based on extensive bridge



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). inspection data. Subsequently, the model considered eight influencing factors, including service time, span, and traffic volume, and the researchers also conducted sensitivity analysis on these factors. While deterministic models are relatively straightforward to construct, they can be adjusted and updated for different bridges. However, they still struggle to account for the stochastic nature of bridge degradation and demand high-quality historical inspection data. In contrast, the second type of model considers the degradation rate as a random variable and utilizes the theory of stochastic processes to simulate the deteriorating trends of bridge structural conditions. Moreover, most probability models have implemented Markov processes [7]. For example, Zhang et al. [10] used five years of continuous bridge inspection data from 445 hollow slab bridges and developed a bridge condition degradation prediction model based on a multi-stage Markov chain. Furthermore, their findings revealed that the state transition probability matrix in the model closely matched actual conditions. Additionally, Wellalage et al. [11] proposed a Metropolis-Hastings optimized Markov chain Monte Carlo method to calculate the state transition matrix of the typical components of railway bridges. Moreover, they compared it with regression and Bayesian models to demonstrate its superiority. In addition, Thanh et al. [12] addressed data insufficiency issues in Markov processes by incorporating a physical-empirical model. The results indicated that the model could derive the state transition matrix using the least squares method. Nevertheless, probabilistic models remain dependent on subjective engineering judgments and necessitate ongoing updates, constraining their potential for further optimization to ensure predictive efficacy.

In recent years, owing to the rapid development and extensive application of machine learning, various scholars have started adopting the extreme learning machine (ELM) model to enhance the predictive performance of models. For instance, Jiang et al. [13] utilized the ELM model to indirectly predict the remaining lifespan of lithium batteries, achieving an error control within 5%. Furthermore, He et al. [14] demonstrated that the ELM model could achieve a 94.44% accuracy in circuit fault prediction in just one millisecond, highlighting the significant advantages of ELM in predictive performance. Subsequently, researchers discovered that optimizing the initial weights and thresholds could further improve ELM's predictive capabilities.

The whale optimization algorithm (WOA) is a novel swarm intelligence and bioinspired optimization algorithm proposed by Mirjalili et al. [15] in 2016. It draws inspiration from the hunting behavior of humpback whales and simulates their unique spiral bubblenet hunting strategy, aiming to achieve optimization for complex problems. Additionally, WOA incorporates three independent population update mechanisms: search for prey, encircling prey, and spiral update. Effectively, WOA eliminates the need for manually setting various control parameter values. Consequently, this approach significantly enhances algorithm efficiency and reduces application complexity. In this context, Lu et al. [16] established a microgrid fault analysis model using the whale optimization algorithm-enhanced extreme learning machine (WOA-ELM). When compared to the backpropagation neural network (BPNN), radial basis function neural network, and conventional ELM, WOA-ELM demonstrated faster learning speed, stronger generalization capability, and higher recognition accuracy. Similarly, Li et al. [17] conducted experiments comparing various optimization algorithms for ELM prediction models, and their findings revealed that WOA-ELM outperformed ELM, genetic algorithm-optimized ELM, cuckoo search-optimized ELM, and dandelion algorithm-optimized ELM in terms of predictive performance. Certainly, there are many other effective metaheuristic algorithms. For instance, Nadimi-Shahraki et al. [18] analyzed the performance of the MTDE algorithm based on the multi-trial vector-based differential evolution method for problems such as the pressure vessel, welded beam, tension/compression spring, and three-bar truss. Their analysis demonstrated that the MTDE algorithm exhibits improved performance and high precision in finding the optimal solution. Liu et al. [19] conducted research on the agricultural drone route-planning problem using the grey wolf optimization algorithm. They discovered that this algorithm can

effectively generate drone trajectories that meet agricultural operational requirements, and exhibits improved performance and high precision in finding optimal solutions.

Considering the high data quality requirements, limited applicability, and the subjective influence on model updates in existing methods, this paper proposes a bridge deterioration prediction model based on WOA-ELM. To enhance the model's applicability beyond a single bridge, the study utilizes a dataset comprising 539 sets of diverse bridge inspection data. It establishes nonlinear mapping relationships between 11 influencing factors, including time, bridge type, span, and others, and the indicators representing the bridge's condition. By comparing the results of this paper's approach with various machine learning prediction models, its superiority is confirmed.

2. Extreme Learning Machine

The ELM [20–22] is a machine learning algorithm based on the construction of a feedforward neural network. Its fundamental principle involves randomly generating connection weights between the input layer and the hidden layer, as well as thresholds for the hidden layer nodes, and then obtaining the optimal solution through straightforward matrix computations. Compared to traditional feedforward neural network algorithms, ELM exhibits strong learning capabilities, superior generalization performance, and simplicity in parameter configuration. The network structure of ELM is illustrated in Figure 1.



Figure 1. Extreme learning machine network structure.

In consideration of the single-hidden-layer ELM network architecture illustrated in Figure 1, we assume the existence of *n* arbitrary samples (X_i, Y_i) . In this context, $X_i = [x_{i1}, x_{i2}, ..., x_{in}]^T \in \mathbb{R}^n$ represents the input matrix, and $Y_i = [y_{i1}, y_{i2}, ..., y_{im}]^T \in \mathbb{R}^m$ signifies the output matrix. The input layer of the ELM comprises *n* nodes, while the hidden layer consists of *l* nodes, and the output layer encompasses *m* nodes. The mathematical representation of the ELM can be succinctly articulated as follows:

$$\sum_{i=1}^{l} \beta_i g(\omega_i x_j + b_j) = y_j, j = 1, 2, \dots, n$$
(1)

In this equation, the symbol $\omega_i = [\omega_{i1}, \omega_{i2}, \dots, \omega_{in}]^T$ signifies the input weight matrix, while $\beta_i = [\beta_{i1}, \beta_{i2}, \dots, \beta_{im}]^T$ represents the output weight matrix. Additionally, the notations g(x) and b_i are employed to denote the activation function and bias of the hidden layer neurons correspondingly.

The primary objective of learning in a single-hidden-layer neural network is to minimize the output error. This objective necessitates identifying distinctive values for β_i , ω_i , and b_i that satisfy the requirements in Equation (2). Consequently, these values can be succinctly represented using matrices as follows:

$$H\beta = Y \tag{2}$$

$$H(\omega_1, \dots, \omega_l, x_1, \dots, x_l, b_1, \dots, b_l) = \begin{bmatrix} g(\omega_1 x_1 + b_1) & \dots & g(\omega_l x_1 + b_l) \\ \vdots & \dots & \vdots \\ g(\omega_1 x_N + b_1) & \dots & g(\omega_l x_N + b_l) \end{bmatrix}_{N \times l}$$
(3)

In this expression, $\beta_{l \times m} = [\beta_1, \beta_2, ..., \beta_l]^T$ represents the output weight matrix, and $T_{N \times m} = [T_1, T_2, ..., T_N]^T$ corresponds to the desired output matrix.

The learning process of ELM can be approximated as solving a nonlinear optimization problem. When the activation function is infinitely differentiable, the input weights and biases of ELM are stochastically determined. Simultaneously, the output matrix of the hidden layer becomes uniquely determined throughout the training process. Consequently, the ELM learning process is analogous to finding the least squares solution, which can be mathematically expressed as follows:

$$\hat{\beta} = H^+ \Upsilon \tag{4}$$

In this equation, H^+ stands for the Moore–Penrose pseudoinverse of the hidden layer output matrix.

3. Optimization of the WOA Algorithm

Given the unknown nature of the optimal initial weights and thresholds for ELM, the present study employs WOA for optimization. By considering the optimal position of an individual within the initial whale population as the best candidate set for the target position, two essential steps are achieved. Firstly, the optimal individual's position serves as a reference for identifying the best candidate set. Secondly, the remaining individuals progressively converge towards this identified best candidate set, while iterative position updates are conducted to iteratively approach the optimal solution [23]. The mathematical expression for this stage is presented below:

$$X(t+1) = X^{*}(t) - A \cdot D, \ A = 2a \cdot r - a$$

$$D = |C \cdot X^{*}(t) - X(t)|, \ C = 2r, \ a = 2(1 - t/T)$$
(5)

In this equation, X(t + 1) represents the position vector of the individual whale after iterative updates at the current iteration. X(t) denotes the position vector of the individual whale at the current iteration. $X^*(t)$ signifies the position vector of the optimal individual within the current whale population. D stands for the random distance vector between the whale and the target. A and C are coefficient vectors. a represents the linearly decreasing attenuation coefficient of $2 \rightarrow 0$. r is a random value between 0 and 1. t represents the current iteration number, and T denotes the maximum number of iterations.

During each iteration update, a random individual whale is selected, and the distance between this whale and the target is calculated. Subsequently, a spiral equation is established between the individual whale and the target based on this distance calculation. The mathematical expression for this spiral equation is as follows:

$$X(t+1) = X^*(t) + D' \cdot e^{bl} \cdot \cos(2\pi l); \ D' = |X^*(t) - X(t)|$$
(6)

In the provided equation, D' represents the distance vector between the current individual whale and the target. The constant *b* defines the logarithmic spiral curve, and *l* is a random variable between 0 and 1.

In this study, a probability threshold *p* is set to simultaneously achieve both of the aforementioned approaches. This ensures that the sperm whale randomly selects either of

the two models with equal probabilities. The final mathematical expression for this stage is presented below:

$$X(t+1) = \begin{cases} X^*(t) - A \cdot D & p < 0.5\\ X^*(t) + D' \cdot e^{bl} \cdot \cos(2\pi l) & p \ge 0.5 \end{cases}$$
(7)

In this equation, *p* is a random variable between -1 and 1.

To enhance the search capability further, this study calculates the magnitude of A in real time during each iteration. When |A| is below the threshold 1, the selection of the optimal individual from the whale population as the target for position updates, in accordance with Equation (7), exemplifies the algorithm's local search capability. Additionally, when the magnitude of |A| surpasses a specific threshold of 1, the algorithm enhances its global search capability. This enhancement is achieved by adopting a strategy that involves randomly selecting a whale individual as the target position and updating the positions of other individuals accordingly. The mathematical expression for this process is provided below:

$$X(t+1) = X_{rand}(t) - A \cdot D; D = |C \cdot X_{rand}(t) - X(t)|$$
(8)

In this formula, the symbol $X_{rand}(t)$ represents the position vector of a randomly selected whale individual from the current whale population.

4. Bridge Condition Deterioration Prediction Model Based on WOA-ELM

The objective of this study is to establish a data-centric bridge health prediction model. In this context, a substantial amount of bridge inspection data are utilized within this study. However, the ELM model's initial weights and thresholds exhibit randomness and lack of consistency, thereby constraining the further enhancement of model accuracy. To address this challenge, WOA is introduced as a remedy. The initial phase entails data preprocessing. During this phase, 539 sets of bridge inspection data are organized into a dataset to facilitate training and testing with WOA-ELM. The subsequent phase involves leveraging the training set to calculate optimal hyperparameters for the ELM predictive model and establish the network topology. Following that, WOA is applied, utilizing the training set and network topology, to compute the most suitable model weights for this dataset. In the ultimate phase, optimized initial weights and thresholds are incorporated into the ELM model for training, culminating in the development of a bridge deterioration prediction model. Figure 2 illustrates the workflow of the regional bridge deterioration prediction model based on WOA-ELM.



Figure 2. Construction process of bridge state deterioration prediction model based on WOA-ELM.

5. Performance Metrics for Evaluation

To assess the performance of the model, this study employs the mean absolute error (MAE), mean relative error (MRE), root mean square error (RMSE), and correlation coefficient (R) as evaluation metrics for the predictive model [24,25]. The computations for each performance evaluation metric are as follows:

$$MAE = \frac{1}{N} \sum_{i=1}^{N} |y_i - \hat{y}_i|$$
(9)

$$MRE = \frac{1}{N} \sum_{i=1}^{N} \left| \frac{y_i - \hat{y}_i}{y_i} \right|$$
(10)

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (y_i - \hat{y}_i)^2}$$
(11)

$$R = \frac{N\sum_{i=1}^{N} y_i \hat{y}_i - \sum_{i=1}^{N} y_i \sum_{i=1}^{N} \hat{y}_i}{\sqrt{\left[N\sum_{i=1}^{N} y_i^2 - \left(\sum_{i=1}^{N} y_i\right)^2\right] \left[N\sum_{i=1}^{N} \hat{y}_i^2 - \left(\sum_{i=1}^{N} \hat{y}_i\right)^2\right]}}$$
(12)

where *MAE* measures the absolute deviation between the predicted values and the expected values. It effectively addresses the issue of error cancellation and serves as an indicator of the model's generalization capability. *MRE* measures the relative deviation between the predicted and expected values, providing valuable insights into the model's generalization ability. *RMSE* assesses the fluctuations in deviation between the predicted and expected values, thus serving as a reflection of the model's accuracy. *R* signifies the goodness of fit and predictive accuracy of the model. Here, y_i denotes the actual value of the *i*th sample, and \hat{y}_i represents the model's predicted value for the same sample. The variable *N* corresponds to the total number of samples, and |R| < 0.4 denotes a low-degree linear correlation. A correlation coefficient value within the range 0.4 < |R| < 0.7 indicates a moderate correlation, whereas a value within the range 0.7 < |R| < 1 signifies a high-degree linear correlation.

6. Method Validation

6.1. Dataset

Establishing a comprehensive bridge condition database serves as an essential foundation for investigating the evolutionary patterns of bridge deterioration. This article gathers documentary materials, including sets of periodic inspection reports, construction design drawings, repair drawings, and maintenance records, for 539 urban bridges situated from 2011 to 2019.

6.1.1. Data Preprocessing

When dealing with multi-source data, a key-value pair collection approach is employed to represent and store each individual bridge entity. The former specifies the specific features, while the latter assigns corresponding data to these features [26]. Bridge entity attributes should encompass information from three aspects: the route level, bridge level, and component level. Different attributes have varying data formats, such as text-based or numerical data. Text-based data typically represent the name or label of the subject under study, while numerical data indicate quantitative relationships between data points.

However, the integrated raw database cannot be directly used for subsequent analyses. This is primarily due to disparities in the quality of historical raw data, such as limited preservation time for paper-based records and instances of missing data. These issues significantly affect the continuity and traceability of data representation. Additionally, the storage of electronic data is constrained by technical standards and management practices, resulting in inconsistent storage formats, information gaps, and inconsistencies.

Therefore, it is necessary to preprocess the initial raw data to maximize the elimination of data noise's impact on subsequent evaluations and ensure the reliability and applicability of the database. The construction process of the regional bridge condition database proposed in this paper is illustrated in Figure 3. Common data cleaning methods include deletion, analogy filling, and mean filling.



Figure 3. Bridge condition database construction process.

6.1.2. Mathematical Representation of Bridge Condition Data

The bridge condition database encompasses diverse data types. The input variables adopted for modeling encompass numerical variables, such as bridge age and length. Moreover, textual variables are included in region and bridge type. Additionally, Boolean variables are employed to signify maintenance conditions. To ensure numerical stability and avert gradient explosions, the normalization technique will be applied to standardize the numerical variables, and eliminate their influence on the model. Concerning the textual variables, there is no explicit correlation or ordinal relationship among distinct values. Therefore, one-hot encoding will be utilized to transform them into $1 \times N$ binary vectors, where N denotes the number of categories for each variable.

For instance, in the context of bridge type, predefined categories will be used for encoding. These categories include hollow slab beam, T-beam, and box girder, which will be encoded as (1, 0, 0), (0, 1, 0), and (0, 0, 1), respectively, thereby serving as input neurons. Similarly, the area variable will be divided into three major regions within the primary urban area: Region 1, Region 2, and Region 3. These regions possess diverse climatic, spatial, geographical, and environmental characteristics. They will be encoded using the same methodology as previously mentioned. Furthermore, for the Boolean variable maintenance condition, a value of 1 will signify a year with maintenance performed, and a value of 0 will represent a year without maintenance.

6.1.3. Establishment of Bridge Condition Database

Secondary encoding, such as minimum-maximum normalization and one-hot encoding, will be performed on the data to prepare the input variables suitable for network training. The dataset will be randomly divided into a training set comprising 80% of the samples (430 cases) and a test set with 20% of the samples (109 cases). The ranges of values for each variable are presented in Table 1. The complete dataset is shown in Appendices A and B.

Variable	Value Ranges
Bridge Condition Index: y	[0, 100]
The service life of the bridge t /years	[0, 20] rounding
The regions {Region 1, Region 2, Region 3} T_a	$\{1, 0, 0\}, \{0, 1, 0\}, \{0, 0, 1\}$
The bridge types {Slab beam, T-beam, Box girder} T_b	$\{1, 0, 0\}, \{0, 1, 0\}, \{0, 0, 1\}$
The structural forms {Simply supported beam, Continuous beam} T_c	{0, 1}
Crossing l/m	[6, 54]
Bridge Length L/m	[8, 1650]
Bridge Width <i>B</i> /m	[7, 44]
Number of Lanes N	[1, 8] rounding
Maintenance Condition {No maintenance, Maintenance performed} M	{0, 1}

Table 1. Prediction model variable representation and value ranges.

6.2. Data Normalization

For numerical variables, there are significant differences in value ranges among different features [27]. Consequently, unequal weights are assigned to the variables, which leads to the phenomenon of feature dilution in variables with smaller value ranges. To address this, the minimum-maximum normalization method is employed to map the feature values of variables into the [0, 1] interval, as shown in Equation (13):

$$x_{i}^{j} = \frac{x_{i}^{j} - x_{i\min}}{x_{i\max} - x_{i\min}} \quad i = 1, 2, \dots, m \quad j = 1, 2, \dots, n \tag{13}$$

where *m* denotes the number of variables; *n* represents the number of samples for each variable; x_i^j is the original value of the *j*th sample for the *i*th variable; x_i^j is the normalized value corresponding to the variable after processing; and x_{imax} and x_{imin} are the lower and upper bounds, respectively, for the variable values.

6.3. Determination of Influencing Factors

Selecting the appropriate input variables is pivotal for ensuring accurate predictions of BCI. Inadequate input variables cannot adequately capture the core aspects of bridge degradation issues, while an excess of variables can lead to challenges like overfitting and model incongruity, simultaneously elevating the model's computational complexity [28]. Consequently, this study adheres to the methodology described in references [29–31], utilizing statistical analysis and mutual information correlation coefficients for the meticulous selection of input variables customized for diverse bridge components. Because whether the bridge structure has undergone maintenance is a crucial influencing factor in this study, we will focus on selecting variables from the remaining factors in the variable selection process.

The scatterplot distribution of sample feature variables and BCI established in this study is depicted in Figure 4.

Subsequently, an exploration of the relationships between various variables and the output was conducted. Appropriate correlation coefficients were chosen for statistical correlation analysis. We employed coefficients to determine the correlation between two categorical variables, used the Pearson correlation coefficient for computing the correlation between two interval variables, and typically applied eta-squared coefficients for the correlation between mixed variables involving both categorical and interval data. These findings are presented in Figure 5.



Figure 4. Scatter plot of dataset samples.



Figure 5. Bridge rating and variable correlation degree based on statistical correlation coefficients. (a) Bridge decking rating and correlation with variables; (b) superstructure rating and correlation with variables; (c) substructure rating and correlation with variables; (d) overall structural rating and correlation with variables.

Figure 5 depicts the correlation between bridge ratings, determined using statistical correlation coefficients, and various variables. Notably, a strong correlation is observed between the bridge deck, superstructure, and substructure variables and the overall structural rating. This correlation aligns with the bridge assessment methodology that takes into account the component weights. When examining the correlations between bridge decking, superstructure, and substructure, the highest correlations are observed in the following order: [bridge decking, superstructure], [superstructure, substructure], and [bridge decking, substructure]. This pattern emerges because, during the operational phase, the bridge decking and superstructure act as a unified entity, sharing the load, which results in the highest correlation among all combinations. Conversely, the superstructure and substructure are typically connected through supports, characterized by load transmission rather than simultaneous loading, resulting in slightly lower correlation coefficients. Additionally, the bridge decking and substructure lack a direct mutual interaction relationship, which accounts for the lower observed correlation. These findings reflect the inherent structural characteristics and common interaction patterns in bridges. Furthermore, it is worth noting that the overall structural rating is significantly affected by its service life. This is evident from correlation coefficients exceeding 0.6 for all variables, except for the substructure. Bridge age emerges as the primary factor influencing structural performance degradation. Additionally, the bridge type and structural form contribute to the rating to varying degrees. Effective combinations of hollow box girders, T-beams, box girders, simple supports, and continuous beams can enhance the bridge's service life throughout its full lifespan and provide sufficient performance reserves. Notably, the overall structural rating decreases with increasing bridge width and lane count, indirectly reflecting the unique contribution of traffic volume to the bridge deterioration process.

The aforementioned correlation analysis reveals the interdependencies between bridge age, region, bridge type, structural form, span, bridge length, bridge width, lane count, and the ratings for the bridge decking, superstructure, substructure, and overall structural performance. It highlights the unique contributions of each variable to the deterioration of bridge performance, forming the basis for extrapolation and prediction in long-term structural performance assessment. However, it is worth noting that some of the correlation coefficients are relatively low, indicating either weak or very weak correlations. This can be attributed, in part, to variations in rating data stemming from differences in inspection personnel's habits and cognitive levels in describing bridge defects. This leads to data inaccuracies and instability, resulting in pronounced data variability. Furthermore, Pearson correlation coefficients are inherently sensitive to linear data and may struggle to quantify and identify potential nonlinear relationships between variables. This may account for the lower correlation coefficients observed in certain cases.

The discrete distribution characteristics of the bridge inspection sample data are illustrated in Figure 6, which serves as an example of visualizing inherent relationships among variables. It is evident that a pronounced linear relationship exists between bridge age, span, superstructure, and the BCI of overall bridge structure, as indicated by robust Pearson correlation coefficients. Conversely, for bridge type and bridge length, the data exhibit a scattered and disorganized distribution, reflecting some nonlinear relationships. These nonlinear associations can be effectively identified and quantified using maximum mutual information coefficients, resulting in relatively high correlation coefficients.

Furthermore, taking into consideration the diverse correlation patterns existing among the data, we delve deeper into the intrinsic characteristics and associations among bridge data. Based on joint statistical analysis and mutual information correlation coefficients, we identify the degree of correlation between variables. Employing a correlation threshold of 0.2, variables with correlation coefficients lower than 0.2 are excluded from the subsequent modeling of bridge degradation states. This screening process results in a candidate feature set that exhibits higher correlation with bridge ratings. This serves to reduce the dimensionality and computational complexity in subsequent model training and prediction, thereby minimizing unnecessary computations. The comprehensive results of the correlation analysis, considering various correlation patterns, are presented in Figure 7. The variable candidate sets, ranked by correlation coefficient magnitude, are as follows: [bridge decking: bridge age, lane count, bridge type, structural form, bridge width, span, bridge length, region], [Superstructure: bridge age, lane count, bridge type, structural form, bridge width, span, bridge length], [substructure: bridge age, bridge type, structural form, lane count, bridge width, region], and [overall structure: bridge age, lane count, bridge width, bridge type, structural form, span, bridge length], region].



Figure 6. Discrete distribution characteristics of correlation analysis variables.



Figure 7. Discrete distribution characteristics of correlation analysis variables. (**a**) Bridge decking rating and correlation with variables; (**b**) superstructure rating and correlation with variables; (**c**) substructure rating and correlation with variables; (**d**) overall structural rating and correlation with variables.

To further substantiate the robustness of the aforementioned analysis, we have employed the quantile–quantile plot to visualize the predictive outcomes, both before and after the selective removal of specific input variables in Figure 8.



Figure 8. Quantile–quantile plot of BCI values. (a) Quantile–quantile plot of BCI values for bridge deck; (b) quantile–quantile plot of BCI values for superstructure; (c) quantile–quantile plot of BCI values for substructure.

From our examination of the plots, we can draw the following conclusions: for the predictions of BCI values pertaining to the bridge deck, superstructure, and substructure, data points exhibit a predominantly linear distribution along the diagonal line. This observation signifies that the predictive outcomes from the model remain largely consistent in terms of their distribution characteristics, irrespective of the inclusion or exclusion of specific input variables. More precisely, in the context of bridge deck BCI predictions, the mean difference between predictions with and without the exclusion of specific input variables is 2.1%, with a corresponding standard deviation variance of 3.7%. Similarly, for superstructure BCI value predictions, the mean difference stands at 2.7%, with a standard deviation variance of 2.0% after selective input exclusion. In the case of substructure BCI value predictions, the mean difference is 2.1%, accompanied by a standard deviation variance of 4.0% following the removal of specific inputs. These findings serve to further underline the rationality behind the removal of these specific input variables.

6.4. Establishment of the WOA-ELM Model

6.4.1. Selection of Activation Functions

Activation functions play a pivotal role in neural networks. Here are some of the most prevalent activation functions in neural networks, including the sigmoid function, the sine function, and the hardlim function [32,33], with specific details provided below:

$$Sigmoid(x) = \frac{1}{1 + e^{-x}} \tag{14}$$

$$Sine(x) = Sin(x)$$
 (15)

$$Hardlim(x) = \begin{cases} 0 \ x < 0\\ 1 \ x \ge 0 \end{cases}$$
(16)

In light of the findings in Figure 9, utilizing the sigmoid function as the activation function in the extreme learning machine model demonstrates improved learning efficiency and enhanced fitting precision. Following that, the performance of the sine function is observed, while among these three activation functions, the hardlim function displays inferior performance. Therefore, we have opted for the sigmoid function as the activation function for subsequent modeling.



Figure 9. Different Activation Functions' ELM Prediction Accuracy.

6.4.2. Determining the Number of Neurons in the Neural Network

In this study, we evaluated the predictive accuracy of the ELM model using the sigmoid activation function. The assessment was conducted for various numbers of neurons in the hidden layer, namely, 5, 10, 15, 20, 25, and 30. The obtained accuracy results exhibited a parabolic distribution, and it was observed that the highest accuracy was achieved when the number of neurons was set to 20 in the hidden layer. Consequently, we determined the number of neurons in the hidden layer as 20 for our model. The results are illustrated in Figure 10.



Figure 10. ELM prediction accuracy of different numbers of hidden layer neurons.

6.5. Forecasting Results and Comparisons

6.5.1. Prediction of BCI of Overall Bridge Structure

Before each training and testing process, a set of 430 data points was randomly chosen as training samples. Additionally, 109 data points were reserved as testing samples. Based on the previous research, the activation function of the ELM algorithm is set to the sigmoid function, with 20 hidden-layer neurons; the WOA population size is set to 20 individuals, and the maximum number of iterations is 50 times.

To mitigate the influence of random sample allocation on predictive results, the best outcome from 10 runs was adopted as the final result. Furthermore, a comparative analysis was conducted to validate the superiority of the proposed method. The analysis involved WOA-ELM, ELM, BPNN, decision trees (DT) and support vector machine (SVM) as the subjects of comparison.

The predictive model's performance was evaluated using several metrics, including MAE, MRE, RMSE, and R. The comparison between the predicted and expected BCI is illustrated in Figure 11. The input layer of the model comprised 11 neurons, while the output layer consisted of 1 neuron.



Figure 11. (a) Comparing the predicted overall structure BCI values from the WOA-ELM model with the expected values; (b) comparing the predicted overall structure BCI values from the ELM model with the expected values; (c) comparing the predicted overall structure BCI values from the BPNN model with the expected values; (d) comparing the predicted overall structure BCI values from the DT model with the expected values; (e) comparing the predicted overall structure BCI values from the SVM model with the expected values; (f) box plot of model error.

Figure 11 reveals differences between the predictions of BCI values for the technical condition of bridges by five different algorithms and their expected values, resulting in a substantial overlap among certain data points. In practice, the predictive models based on

the WOA-ELM algorithm and the ELM algorithm demonstrate remarkable proficiency in capturing sample characteristics, and exhibit especially favorable proficiency for forecasting trends in the technical state of bridges. Accurately predicting changes in bridge conditions will aid managers in taking preemptive measures to maintain bridge performance and enhance safety. Additionally, upon closer examination of the prediction error distribution for BCI values among the five algorithms, the WOA-ELM algorithm manages the magnitude of prediction errors significantly, with overall error fluctuations primarily concentrated around values near zero. Following this, the ELM algorithm exhibits relatively lower error levels. However, the SVM and BP neural networks, among the five algorithms, exhibit the most significant overall deviations in prediction errors and possess a larger number of outliers.

Figure 12 portrays scatter plots that exhibit the forecasted and anticipated BCI values, employing five algorithms: WOA-ELM, ELM, BPNN, DT, and SVM. The data points from all five models extend outward around the diagonal line. Additionally, five is a dense distribution near the diagonal, indicating a high degree of agreement between the predicted and expected values. Furthermore, the probability density distribution curves of the BCI prediction errors for the five algorithms are compared. The WOA-ELM algorithm exhibits a smaller extension range and a higher concentration of data points around the peak of the density curve. These observations indicate its superior ability to track the expected values. Moreover, the ELM and DT algorithms show a slightly lower capturing effect on the expected values, and the BPNN and SVM algorithms display a larger dispersion in the distribution of prediction data, indicating poorer control over error fluctuations.



Figure 12. Cont.



Figure 12. (**a**) Comparative analysis of deviation between predicted and expected BCI using the WOA-ELM model; (**b**) comparative analysis of deviation between predicted and expected BCI using the ELM model; (**c**) comparative analysis of deviation between predicted and expected BCI using the BPNN model; (**d**) comparative analysis of deviation between predicted and expected BCI using the DT model; (**e**) comparative analysis of deviation between predicted and expected BCI using the SVM model; (**f**) probability density analysis of prediction errors among the WOA-ELM, ELM, BPNN, DT, and SVM models.

The results depicted in Table 2 reveal significant advancements attained by the WOA-ELM model when compared to the ELM, BPNN, DT, and SVM models. In particular, the WOA-ELM model exhibits significant improvements in R, with enhancements of 4.1%, 11.4%, 24.5%, and 33.6%. Additionally, the model demonstrates reductions in MAE by 9.9%, 13.6%, 5.4%, and 15.7%, and MRE by 11.6%, 15.3%, 6%, and 16.2%, respectively. Furthermore, the RMSE is lower by 7.3%, 18.0%, 14.8%, and 18.1% for the corresponding evaluations. The obtained results establish a remarkable level of consistency between the proposed WOA-ELM model and the other four models concerning the predictions of BCI values. When compared to other models, the proposed model exhibits superior performance in various aspects. It shows superiority in terms of both absolute and relative deviations in predictions. Additionally, the proposed model demonstrates better performance in deviation fluctuation and goodness of fit measures. The proposed model exhibits the lowest level of deviation between predicted and expected values. This signifies its high prediction accuracy and remarkable generalization capability. As a result, the model enables the effective forecasting of bridge states under various time points and feature variables. These achievements can be primarily attributed to the optimization of the initial weights and thresholds of the extreme learning machine through the whale optimization algorithm. Following this, the network undergoes training and testing on the dataset with the optimized initial weights and thresholds. As a consequence, commendable performance is achieved in both accuracy and generalization capability.

Table 2. Summary of predictive performance indicators of different models.

Category	Prediction Model	MAE	MRE (%)	RMSE	R
	WOA-ELM	2.412	2.632	3.003	0.768
0 11	ELM	2.676	2.978	3.241	0.738
Overall	BPNN	2.791	3.106	3.661	0.689
structure	DT	2.549	2.800	3.151	0.616
	SVM	2.862	3.14	3.667	0.575

6.5.2. Prediction of BCI of Bridge Components

Similarly, employing the WOA-ELM model with consistent parameters, predictions were made for the degradation scores of the bridge deck, superstructure, and substructure. A comparative analysis between the predicted BCI and the expected values is presented in Figures 12–14. Specifically, the bridge deck model incorporates an input layer consisting of nine neurons, the superstructure model features an input layer comprising eight neurons, and the substructure model is equipped with an input layer comprising seven neurons. Each of these models has an output layer consisting of one neuron.



Figure 13. (a) Comparing the predicted bridge deck BCI values from the WOA-ELM model with the expected values; (b) comparing the predicted bridge deck BCI values from the ELM model with the expected values; (c) comparing the predicted bridge deck BCI values from the BPNN model with the expected values; (d) comparing the predicted bridge deck BCI values from the DT model with the expected values; (e) comparing the predicted bridge deck BCI values from the SVM model with the expected values; (f) box plot of model error in the bridge deck BCI ratings.



Figure 14. (a) Comparing the predicted superstructure BCI values from the WOA-ELM model with the expected values; (b) comparing the predicted superstructure BCI values from the ELM model with the expected values; (c) comparing the predicted superstructure BCI values from the BPNN model with the expected values; (d) comparing the predicted superstructure BCI values from the DT model with the expected values; (e) comparing the predicted superstructure BCI values from the SVM model with the expected values; (f) box plot of model error in the superstructure BCI ratings.

According to Figures 13–15, the WOA-ELM algorithm demonstrates excellent generalization performance and fitting accuracy in the evaluation of various components and overall ratings of bridges. It also exhibits a minimal presence of outliers and high applicability across diverse data features. While the DT model shows low error variance and dispersion in predicting BCI values for upper structural elements, there is room for improvement in other performance aspects. It is worth noting that the model exhibits relatively lower fitting accuracy in the evaluation of lower structural components. This is primarily due to the fact that, within the entire regional road network, most bridge substructures remain in good condition, with no localized minor damage or deterioration. As a result, BCI values tend to be uniformly high, and the variability is low, making the algorithm susceptible to noise interference and, thus, challenging in accurately capturing the relationship between structural states and feature variables. Especially taking bridge decks as an example, the WOA-ELM model demonstrates a significant advantage in terms of R-squared, with improvements of 9.5%, 12.7%, 16.7%, and 19.7%, respectively. Furthermore, the model exhibits reductions of 4.3%, 6.5%, 1.7%, and 12.5% in terms of MAE, and reductions of 6.4%, 6.7%, 2.8%, and 13.3% in terms of MRE. Additionally, the corresponding RMSE evaluations show reductions of 5.4%, 9.0%, 4.3%, and 12.7%, respectively.



Figure 15. (a) Comparing the predicted substructure BCI values from the WOA-ELM model with the expected values; (b) comparing the predicted substructure BCI values from the ELM model with the expected values; (c) comparing the predicted substructure BCI values from the BPNN model with the expected values; (d) comparing the predicted substructure BCI values from the DT model with the expected values; (e) comparing the predicted substructure BCI values from the SVM model with the expected values; (e) comparing the predicted substructure BCI values from the SVM model with the expected values; (e) comparing the predicted substructure BCI values from the SVM model with the expected values; (f) box plot of model error in the substructure BCI ratings.

Given that the randomness of the data can affect the model to some extent, we conducted ten random splits of the dataset and generated a box plot of the errors between predicted values and expected values, as illustrated below.

According to Figure 16, after ten runs, the WOA-ELM algorithm demonstrated that the median errors in both the overall bridge structure and component ratings were primarily within proximity to zero, reaffirming the model's outstanding predictive performance. Additionally, WOA-ELM exhibited the lowest number of outliers among the five models, indicating strong generalization capabilities. While the BPNN and SVM models had relatively good error distributions, the presence of too many outliers was deemed unacceptable. Furthermore, despite the ELM and DT models showcasing solid generalization and accuracy under ideal conditions, an overall examination of ten runs revealed more scattered error distributions and a higher occurrence of outliers, indicative of the lower stability of these two models.



Figure 16. (**a**) Box plot of model error in the overall structure BCI ratings; (**b**) box plot of model error in the bridge deck BCI ratings; (**c**) box plot of model error in the superstructure BCI ratings; (**d**) box plot of model error in the substructure BCI ratings.

7. Conclusions

In this study, a comprehensive dataset of bridge condition deterioration was meticulously collected by the aggregation of extensive bridge inspection data. The dataset encompasses 11 significant input features, including bridge service time, region, and bridge type. Leveraging this comprehensive dataset, a data-driven WOA-ELM bridge condition deterioration prediction model was successfully constructed. To ensure the reliability and robustness of the proposed method, it was subjected to rigorous validation using a substantial volume of inspection data. The extensive validation process has enabled us to draw the following concluding insights:

(1) The foundation of this study rests upon a comprehensive dataset of bridge inspection data, which facilitates the establishment of complex nonlinear connections between essential features and bridge conditions. This research effectively harnesses and explores the inherent data patterns within the long-term bridge inspection data. Setting itself apart from other prediction models that focus solely on individual bridges, the proposed model demonstrates exceptional proficiency in precisely forecasting the states of diverse bridges within the region.

- (2) In this study, we conducted correlation analysis, taking into consideration several key factors, including the bridge's age, lane count, bridge width, bridge type, structural form, span, bridge length, geographic location, and maintenance status. The aim was to enhance the accuracy of BCI prediction. Furthermore, the WOA-ELM prediction model proposed in this paper outperforms the ELM, BPNN, DT, and SVM models in terms of sample fitting capability and accuracy. Specifically, the model presented in this paper exhibited improvements in R-values by 4.1%, 11.4%, 24.5%, and 33.6%, reductions in RMSE by 7.3%, 18.0%, 14.8%, and 18.1%, decreases in MAE by 9.9%, 13.6%, 5.4%, and 15.7%, and reductions in MRE by 11.6%, 15.3%, 6%, and 16.2%. These results clearly demonstrate a significant enhancement in the model's performance for bridge condition prediction.
- (3) In the context of predicting the BCI for bridge components, we utilized Pearson correlation analysis and mutual information theory to identify the critical influencing factors that need to be taken into account for each specific component. For instance, within the realm of the bridge superstructure, it was imperative to consider variables such as bridge age, lane count, bridge width, bridge type, structural form, span, bridge length, geographic location, and maintenance status. When undertaking the prediction BCI for various bridge components, our proposed method consistently demonstrated remarkable advantages, surpassing the performance of the ELM, BPNN, DT, and SVM models in terms of predictive accuracy. Specifically, with regard to bridge decking components, our method resulted in significant improvements in R-values, with increases of 9.5%, 12.7%, 16.7%, and 19.7%. Additionally, there were reductions in RMSE by 5.4%, 9.0%, 4.3%, and 12.7%, decreases in MAE by 4.3%, 6.5%, 1.7%, and 12.5%, and reductions in MRE by 6.4%, 6.7%, 2.8%, and 13.3%. These outcomes prominently underscore the exceptional predictive prowess of our methodology across diverse bridge component conditions. The significance of this research lies in the provision of a more dependable technical assessment tool for bridge management and maintenance, poised to assume a pivotal role in practical applications.

Although our proposed method exhibits significant advantages over other models, there is still room for further improvement in the predictive performance of our model (e.g., enhancing the optimization precision and learning efficiency of meta-learning). Therefore, we will focus on exploring meta-learning algorithms to further enhance the performance of our model in the field of BCI prediction in future research.

Author Contributions: L.J. contributed to methodology, conceptualization, data curation, formal analysis, investigation, and writing. Q.T. was involved in data curation, methodology, validation and the preparation of the original draft. Y.J. contributed to conceptualization, investigation and supervision. H.C. was involved in conceptualization, the preparation of the original draft, and data collection. Z.X. participated in validation, reviewing and data collection. All authors have read and agreed to the published version of the manuscript.

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Data Availability Statement: The data presented in this study are available on request from the corresponding author.

Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

Table A1. Dataset.

NO.	Α	В	С	D	Ε	F	G	н	Ι	J	К	NO.	Α	В	С	D	Ε	F	G	Н	Ι	J	К
1	2	1	4	3	35	365	8	2	0	0	0	271	1	2	13	1	8	20	31	8	0	0	0
2	1	2	15	1	10	20	25	6	0	1	0	272	1	2	19	1	6	8.3	31	8	1	0	0
3	1	2	10	1	10	20	25	6	1	0	1	273	1	2	13	1	6	8.3	31	8	0	0	0
4	1	2	8	1	10	20	25	6	0	0	0	274	2	2	19	3	21	59	9	1	1	0	0
5	1	2	12	1	10	21	24.5	6	1	1	0	275	2	2	15	3	21	59	9	1	0	0	0
6	1	2	7	1	10	21	24.5	6	0	0	0	276	1	3	16	1	20	39.5	33	8	0	1	1
7	1	2	5	1	10	21	24.5	6	0	0	0	277	1	3	13	1	20	39.5	33	8	1	0	0
8	1	2	16	1	20	85	31	8	0	1	0	278	1	3	10	1	20	39.5	33	8	0	0	0
9	1	2	14	1	20	85	31	8	0	0	0	279	1	3	16	1	20	33	31.5	8	1	0	0
10	1	2	18	1	20	52	35	8	0	1	0	280	1	3	13	1	20	33	31.5	8	0	1	0
11	1	2	13	1	20	52	35	8	0	0	0	281	1	3	10	1	20	33	31.5	8	1	0	0
12	1	2 1	11	1	20 4E	52 45	35	0	0	0	0	282	1	3	10	2	20	41	31.5 21 E	0	1	0	0
13	2 1	2	-± 18	2	40	180	315	8	1	1	0	203	1	3	15	1	20	41 35	31.5	8	0	1	0
14	1	3	18	2	30	230	85	2	1	0	0	285	1	3	10	1	20	35	31.5	8	1	0	0
16	1	3	13	2	30	230	85	2	0	0	0	285	1	3	10	1	20	35	31.5	8	0	0	0
17	1	3	18	1	20	66	11	3	0	0	0	287	2	2	18	3	19	93	7	1	1	1	0
18	1	3	13	1	20	66	11	3	0	Õ	0	288	2	2	14	3	19	93	7	1	0	0	Õ
19	1	3	11	1	20	66	11	3	Õ	0	Õ	289	1	2	18	3	24	29	7	1	1	Õ	Ő
20	2	3	18	3	20	65	11	3	Õ	0	Õ	290	1	2	14	3	24	29	7	1	0	Õ	Õ
21	2	3	13	3	20	65	11	3	0	0	0	291	2	2	18	3	24	176	7	1	1	0	0
22	2	3	11	3	20	65	11	3	0	0	0	292	2	2	14	3	24	176	7	1	0	0	0
23	1	3	18	1	20	57	24.5	6	1	1	0	293	1	2	13	2	50	768	24.5	6	1	0	0
24	1	3	13	1	20	57	24.5	6	1	0	0	294	1	2	10	2	50	768	24.5	6	0	0	0
25	2	1	3	3	23	73	8	1	0	0	0	295	1	3	12	2	40	379	32.6	8	1	0	1
26	1	3	18	1	25	84	19.3	4	0	1	0	296	1	3	9	2	40	379	32.6	8	0	0	0
27	2	1	3	3	40	289	35	8	0	0	0	297	1	3	7	2	40	379	32.6	8	0	0	0
28	2	3	18	3	24	236	9.5	2	1	1	0	298	2	2	11	3	30	350	10	2	0	0	1
29	2	3	13	3	24	236	9.5	2	0	0	0	299	2	2	8	3	30	350	10	2	0	0	0
30	2	3	11	3	24	236	9.5	2	0	0	0	300	1	2	19	2	30	234	31	8	0	0	0
31	1	3	18	1	20	29	24.5	6	1	0	0	301	1	2	14	2	30	234	31	8	0	0	0
32	1	3	13	1	20	29	24.5	6	1	0	0	302	1	3	16	2	20	59	31.5	8	1	1	0
33	2	1	20	3	40	100	16	3	1	0	0	303	1	3	10	2	20	125	31.5	0	1	1	0
25	2	1	13	2	40	100	10	2	1	0	0	205	2 1	2	20	1	20 16	102	0 7	2 1	0	1	0
36	2	1	14	3	40	100	10 16	3	1	0	0	305	1	2	20 16	2	20	192	21 5	1	1	1	0
37	1	1	20	1	20	35	31	6	1	0	0	307	1	3	10	2	20	95 95	31.5	8	0	0	0
38	1	1	15	1	20	35	31	6	0	0	0	308	1	3	11	2	20	95	31.5	8	0	0	0
39	1	1	14	1	20	35	31	6	0	0	0	309	2	1	4	3	25	194	9	2	1	0	0
40	1	1	12	1	20	35	31	6	0	Õ	0	310	2	1	4	3	24	57	9	2	0	0	Õ
41	2	1	3	3	23	73	8	1	0	0	0	311	1	3	16	2	20	94	31.5	8	0	1	1
42	1	1	20	3	20	54	31	6	0	1	0	312	1	3	13	2	20	94	31.5	8	1	0	0
43	1	1	15	3	20	54	31	6	1	0	0	313	2	2	4	3	28	62	9	2	0	0	0
44	1	1	12	3	20	54	31	6	0	0	0	314	2	2	4	3	34	263	9	2	1	0	0
45	1	1	20	2	25	38	31	6	0	0	0	315	2	2	4	3	29	236	9	2	0	0	0
46	1	1	15	2	25	38	31	6	1	0	0	316	2	2	4	3	35	122	9	2	0	0	0
47	1	1	14	2	25	38	31	6	1	1	0	317	2	2	4	3	36	52	9	2	0	0	0
48	1	1	12	2	25	38	31	6	0	0	0	318	2	2	4	3	35	265	9	2	0	0	0
49	2	1	4	3	35	275	8	1	0	0	0	319	2	2	18	2	20	94	31.5	8	0	0	0
50	2	1	3	3	30	42	9	2	0	0	0	320	2	2	15	2	20	94	31.5	8	1	0	0
51	2	1	3	3	35	111	9	2	0	0	0	321	2	2	18	3	28	294	7	1	0	0	0
52	2	3	6	3	27	207	8	2	0	0	0	322	2	2	15	3	28	294	7	1	1	0	0
55 E4	2	1	3	3	33	12	9	2	0	0	0	323	2	2	18	3	38 20	200	9	2	1	0	0
54	2	1 2	3	2	24 20	420 00	9	2	0	0	0	324	2	2	13 14	2	20 25	∠00 122	ソワ	ے 1	1	0	0
55 56	∠ 2	∠ 1	3	3 2	∠0 37 5	90 373	יד 11 5	2	0	0	0	325	∠ 2	2	14 14	3 2	33	153	55	1	0	0	0
57	2	1	3	3	24	68	7	2 1	0	0	0	327	2	2	18	3	24	176	7	1	0	1	n
58	2	1	3	3	27	407	9	2	0	0	0	328	2	2	15	3	24	176	7	1	1	0	Ő
59	2	1	4	3	35	465	9	2	õ	õ	õ	329	2	2	18	3	33	262	9	2	0	1	õ
60	2	3	6	3	37	150	8	2	õ	Ő	õ	330	2	2	15	3	33	262	9	2	Ő	0	Ő

Table A1. Cont.

NO.	A	В	С	D	Ε	F	G	Н	Ι	J	K	NO.	Α	В	С	D	Е	F	G	Н	Ι	J	K
61	2	3	4	3	37	491	6	1	0	0	0	331	2	2	18	3	23	204	9.5	2	1	0	0
62	2	3	6	3	46	171	11.7	2	0	0	0	332	2	2	15	3	23	204	9.5	2	0	0	0
63	2	1	5	3	32	443	13	3	0	0	0	333	2	2	14	3	23	204	9.5	2	1	0	0
64	2	3	6	3	30	142	8	2	0	0	0	334	2	2	18	3	23	140	14.5	3	0	0	0
65	2	3	2	3	33	391	7	1	0	0	0	335	2	2	18	3	28	294	9.5	2	0	0	0
66	2	3	6	3	27	118	9	1	0	0	0	336	1	2	18	3	24	29	13	2	0	1	0
67	2	3	6	3	29	289	9 12 9	2	0	0	0	228	2	2	10	2	38 28	200	9	2 1	1	1	0
69	2	3	4	3	38 40	236 526	12.0	1	0	0	0	339	2	2	10	3	20 24	294 176	7	1	1	0	0
70	2	3	4	3	50	660	7	1	0	0	0	340	2	2	5	3	25	157	8	1	0	0	0
71	2	3	2	3	39	228	7	1	0	Ő	Õ	341	2	2	5	3	26	270	8	1	Õ	Õ	Õ
72	2	3	4	3	39	400	7	1	0	0	0	342	2	2	5	3	28	171	8	1	0	0	0
73	2	3	2	3	36	530	7	1	0	0	0	343	2	2	5	3	25	25	13.5	3	0	0	0
74	2	3	4	3	39	618	7	1	0	0	0	344	2	2	5	3	30	243	8	1	0	0	0
75	2	3	2	3	32	370	7	1	0	0	0	345	2	2	5	3	31	301	8	1	0	0	0
76	2	3	2	3	38	645	9	2	0	0	0	346	2	2	5	3	28	233	8	1	0	0	0
77	2	3	2	3	50	580	9	2	0	0	0	347	2	2	11	3	20	292	9.5	2	0	0	0
78 79	2	3	4	3	30 36	238 147	7	1	0	0	0	348 349	2	2	12	3	20 40	109	9 24 5	2	0	0	0
80	2	3	4	3	50	465	95	2	0	0	0	350	1	2	7	2	40	430	24.5	6	0	0	0
81	2	1	4	3	36	350	10	2	0	0	0	351	1	1	20	1	20	58	31	6	1	0	0
82	2	1	3	3	32	452	27	6	Ő	0	0	352	1	1	17	1	20	58	31	6	0	0	0
83	2	1	5	3	32	1038	9	2	0	0	0	353	1	2	19	1	20	31	31	8	0	0	0
84	1	1	3	3	30	46	40	8	0	0	0	354	1	2	16	1	20	31	31	8	1	0	0
85	2	3	6	3	54	285	9.5	2	0	0	0	355	1	2	14	1	20	31	31	8	0	1	0
86	2	1	4	3	35	115	17.5	4	0	0	0	356	2	3	4	3	30	71	35	6	0	0	0
87	1	1	4	3	36	151	35	8	0	0	0	357	1	2	17	1	20	70	16	4	0	0	0
88	2	1	4	3	40	168	35	8	0	0	0	358	2	2	17	3	30	150	9.5 10 F	2	0	0	0
89 90	2	1	4	3	40 35	100	35 35	8	0	0	0	359	2	2	9	3	32 40	220	19.5	4	0	0	0
90 91	2	1	4	3	35	180	17.5	4	0	0	0	361	1	2	9	2	35	437	20	4	0	0	0
92	1	1	4	3	36	396	40	8	0	0	0	362	2	2	9	3	30	120	9.5	2	0	0	0
93	2	1	3	3	35	259	37	8	0	Ő	Õ	363	2	2	9	3	33	258	19.5	4	Õ	Õ	Õ
94	2	1	3	3	28	340	10	2	0	0	0	364	2	1	9	3	22	27	9	2	0	0	0
95	2	1	3	3	35	145	11.5	2	0	0	0	365	2	1	9	3	47	148	9	2	0	0	0
96	2	1	3	3	31	475	11.5	2	0	0	0	366	2	1	9	3	32	126	9	2	0	0	0
97	2	1	3	3	42	130	11.5	2	0	0	0	367	2	1	9	3	30	400	9	2	0	0	0
98	1	1	3	2	40	296	21	4	0	0	0	368	2	1	9	3	33	182	9	2	0	0	0
99 100	2	1	3	3	30 21	367	9	2	0	0	0	369	2	1	9	3	35	345 170	9	2	1	1	0
100	2	1	3	3	35	321	9	2	0	0	0	370	2	1	9	3	30	170	9	2	0	0	0
101	2	1	3	3	35	328	9	2	0	0	0	372	2	1	9	3	30	1650	18.5	4	0	0	0
103	1	3	20	2	20	162	15.8	4	1	1	Ő	373	2	1	9	3	30	353	18.5	4	1	0	0
104	2	1	5	3	30	124	8	1	0	0	0	374	2	1	9	3	30	1560	18.5	4	0	0	0
105	2	1	5	3	35	115	33	8	0	0	0	375	2	1	9	3	33	626	18.5	4	1	0	0
106	2	1	5	3	32	128	8	1	0	0	0	376	2	1	7	3	38	113	11.5	2	1	0	0
107	2	1	4	3	30	120	8	1	0	0	0	377	2	1	4	3	38	113	11.5	2	0	0	0
108	1	1	4	3	36	617	37	8	0	0	0	378	2	1	7	3	40	1537	21.5	4	0	0	0
109	2	1	4	3	35	285	8	1	0	0	0	379	2	1	4 7	3	40	245	21.5 11 5	4	1	0	0
110	2	2	3	3	30	373	9	2	0	0	0	381	2	1	4	3	40	245 245	11.5	2	0	0	0
112	2	2	3	3	31	70	38	8	0	0	0	382	2	1	7	3	30	190	8	1	1	0	0
113	1	3	18	2	40	260	31.5	8	Ő	1	0	383	2	1	13	3	30	343	10	1	1	0	0
114	1	3	13	2	40	260	31.5	8	1	0	0	384	2	1	7	3	29	143	8	1	1	0	0
115	1	3	11	2	40	260	31.5	8	0	0	0	385	2	1	13	3	23	155	8	1	1	0	0
116	1	3	14	1	20	28	20	4	1	0	0	386	2	1	13	3	22	276	8.5	1	1	0	0
117	1	3	12	1	20	28	20	4	0	0	0	387	2	1	13	3	30	310	8	1	1	0	0
118	1	3	18	2	40	400	31.5	8	0	0	0	388	2	1	9	3	23	61	8	1	1	0	0
119	1	3	13	2	40	400	31.5	8	0	1	0	389	2	1	6	3	23	61 190	8	1	1	0	0
120 121	1	3	11 19	2 1	40 20	400 20	31.3 31	ð	0	0	0	390 301	2	1	9	3	25 25	180	ð	1	1	0	0
121 122	1 1	3	13	1 1	20 20	20 20	31	8	1	1	0	392	∠ 2	1 1	9	3	∠3 33	171	8	1 1	1	0	0
123	1	3	11	1	20	20	31	8	0	0	0	393	2	1	6	3	33	171	8	1	0	0	0
124	1	3	18	1	16	27	32.5	8	1	Ő	0	394	2	1	9	3	25	74	8	1	0	0	0
125	1	3	13	1	16	27	32.5	8	1	0	0	395	2	1	6	3	25	74	8	1	0	0	0
126	1	3	11	1	16	27	32.5	8	0	0	0	396	2	1	9	3	25	92	8	1	1	0	0
127	2	3	18	3	24	403	9.5	2	0	0	0	397	2	1	6	3	25	92	8	1	0	0	0

Table A1. Cont.

NO.	Α	В	С	D	Е	F	G	Н	Ι	J	К	NO.	Α	В	С	D	Е	F	G	Н	I	J	K
128	2	3	18	3	24	419	9.5	2	0	0	0	398	2	1	9	3	25	191	8	1	1	0	0
129	1	3	18	1	16	73	31.5	8	0	0	0	399	2	1	6	3	25	191	8	1	0	0	0
130	2	3	18	3	24	138	15.8	4	1	0	0	400	2	1	9	3	30	278	8	1	1	0	1
131	2	3	13	3	24	138	15.8 15.8	4	0	0	0	401	2	1	6	3	30 25	278	8	1	0	0	0
132	2	1	10	3	24	100	12.5	2	0	0	0	402	2	1	6	3	25	100	8	1	0	0	0
134	1	3	17	1	20	37	31	8	1	0	1	404	2	2	11	3	33	90	7.8	1	0	0	0
135	1	3	12	1	20	37	31	8	0	0	0	405	2	2	11	3	30	90	7.8	1	0	0	0
136	1	3	10	1	20	37	31	8	0	0	0	406	2	2	11	3	30	30	7.8	1	0	0	0
137	1	3	17	1	30 30	74	19 10	4	1	0	0	407	2	2	11 11	3	30	40	17.8	4	0	0	0
139	1	3	10	1	30	74	19	4	0	0	0	409	2	2	11	3	35	110	7.8	1	0	0	0
140	1	3	18	1	25	30	29	8	1	0	0	410	2	2	11	3	33	350	7.8	1	Õ	0	0
141	1	3	13	1	25	30	29	8	0	1	0	411	2	2	11	3	30	30	7.8	1	0	0	0
142	1	3	11	1	25	30	29	8	0	0	0	412	2	2	7	3	40	374	9.5	2	0	0	0
143	1	2	18	1	20	20	30 20	8	1	0	0	413	2	2	7	3	38	440	9.5	2	1	0	0
144	1	2	13	1	20	20	30	8	0	0	0	414	2	2	4 7	3	18	70	9.5 8	1	0	0	0
146	1	3	18	1	13	13	31	8	1	0	1	416	2	2	7	3	17	38	8	1	Õ	0	Ő
147	1	3	13	1	13	13	31	8	0	0	0	417	2	1	11	3	35	80	41.5	8	0	0	0
148	1	3	11	1	13	13	31	8	0	0	0	418	2	1	9	3	30	105	33	8	0	0	0
149 150	1	1	16 14	1	20	50 50	31	8	1	1	0	419	2	1	6	3	20	40	8	2	0	0	0
150	1	1	14	1	20	50 50	16	4	1	0	0	420	2	3	9	3	25	100	31.5	8	1	0	0
152	1	1	14	1	20	50	16	4	0	1	1	422	2	3	9	3	31	98	12.5	2	1	1	0
153	1	1	11	1	20	50	16	4	0	0	0	423	2	1	6	3	45	305	24.5	6	0	0	0
154	1	1	19	1	20	50	16	4	0	0	1	424	2	1	6	3	45	90	14	2	0	1	0
155	1	1	14	1	20	50	16	4	1	0	0	425	2	1	67	3	46	97 125	14	2	0	0	0
156	1	2	10	1	16	60 60	12.5	3	0	1	0	426 427	2	1	13	3	25 30	90	9 22	4	0	0	0
158	1	2	9	1	16	60	12.3	3	0	0	0	428	2	1	12	3	33	450	13	2	0	0	0
159	1	2	15	1	16	24	12.3	3	0	0	0	429	2	2	14	3	30	78	13	2	1	0	0
160	1	2	10	1	16	24	12.3	3	1	0	0	430	2	2	14	3	30	210	14	2	1	0	0
161	1	2	9 12	1	16 20	24	12.3	3	0	0	0	431	2	1	11	3	45 12	255 40	20	4	0	0	0
162	1	2	7	1	20	80 80	12.3	3	0	0	0	432	1	1	15	3	27	40 60	17	4	0	1	0
164	1	2	6	1	20	80	12.3	3	0	0	0	434	1	1	15	3	27	60	17	4	0	0	0
165	1	2	15	1	20	109	12.3	3	0	0	1	435	2	1	11	3	33	298	17	4	0	0	0
166	1	2	10	1	20	109	12.3	3	1	1	0	436	1	1	11	3	30	170	17	4	0	0	0
167 168	1	2	9 15	1	20	109	12.3	3	0	0	0	437	1	1	11	1	20	20	10	2	0	0	0
169	1	2	10	1	10	20	12.3	3	0	0	0	439	1	1	4	3	20	280	23 14	3	0	0	0
170	1	2	9	1	10	20	12.3	3	1	0	0	440	2	1	4	3	30	186	9	2	Õ	0	Ő
171	1	2	15	1	10	20	39	8	1	1	0	441	1	1	15	1	30	111	33	6	0	0	0
172	1	2	10	1	10	20	39	8	1	1	0	442	1	1	15	1	20	40	33	6	1	0	0
173	1	2	9 14	1	10 20	20 120	39 12 3	8	0	0	0	443	2	1	7	3	38	417 417	9	2	1	0	0
174	1	2	9	1	20	120	12.3	3	0	1	0	445	2	1	7	3	35	370	9	2	0	0	0
176	1	2	8	1	20	120	12.3	3	0	0	0	446	2	1	7	3	35	259	9	2	0	Õ	0
177	1	2	9	1	20	32	12.3	3	0	1	0	447	2	1	5	3	35	259	9	2	0	0	0
178	1	2	15	1	10	20	12.3	3	1	1	0	448	2	1	7	3	35	182	9	2	0	0	0
179	1	2	10 13	1	10 20	20	12.3	3	0	0	0	449 450	2	1	5	3	35	182	9	2	0	0	0
181	1	3	9	3	20	40	8.5	1	0	0	1	451	2	1	7	3	30	246	9	2	0	0	0
182	2	2	13	3	20	50	19	4	0	0	0	452	2	1	7	3	25	167	9	2	0	0	0
183	2	2	9	3	20	50	19	4	0	0	0	453	1	1	17	1	20	152	11	2	1	0	0
184	2	2	13	3	20	40	13	2	0	0	1	454	1	1	17	2	30	150	11	2	1	0	0
185 186	2	2	9	3	20 20	40 40	13	2	0	0	0	455 456	1	1	17 17	2	30 20	$\frac{485}{248}$	17	4	0	0	0
187	2	2	7	3	44	141	8	1	0	0	0	457	2	1	7	3	30	240 90	7.8	1	0	0	0
188	2	2	3	3	44	141	8	1	0	Õ	Õ	458	2	1	7	3	32	172	7.8	1	0	Õ	0
189	1	2	7	3	25	25	8	1	0	0	0	459	2	1	7	3	30	161	7.8	1	0	0	0
190	1	2	3	3	25	25	8	1	0	0	0	460	2	1	9	3	30	120	15	4	0	0	0
191 192	2	2	/ 3	3 3	44 44	141 141	8 8	1 1	0	0	0	461 462	2	1 1	9	3 3	27 30	75 318	7.8 7.8	1 1	0	0	0
193	1	2	13	3	35	45	8	1	0	0	1	463	2	1	9	3	30	110	7.8	1	0	0	0
194	1	2	9	3	35	45	8	1	0	0	0	464	2	1	9	3	27	100	10.5	1	0	0	0
195	2	2	13	3	36	260	8	1	0	0	0	465	1	1	17	1	20	573	21	4	0	0	0

Table A1. Cont.

NO.	Α	В	С	D	Ε	F	G	Н	Ι	J	K	NO.	Α	В	С	D	Е	F	G	Н	Ι	J	К
196	2	2	9	3	36	260	8	1	0	0	0	466	1	1	18	1	20	393	21	4	0	0	0
197	1	3	18	1	20	132	15	4	0	1	1	467	1	1	20	2	20	420	11	2	1	1	0
198	1	3	14	1	20	132	15	4	0	0	0	468	1	1	7	3	20	25	8.8	2	0	0	0
199	1	3	12	1	20	132	15	4	0	0	0	469	2	1	17	1	20	172	9	2	0	0	0
200	1	3	17	1	20	146	15.5	4	1	1	0	470	2	1	17	1	20	172	9	2	0	0	0
201	1	3	13	1	20	146	15.5 15.5	4	0	0	0	471	2	1	9 10	3	30	180	22	2	0	0	0
202	1	3	11	2	20	140	15.5 31	4	0	0	1	472	2	1	5	2	20	91 125	32 8	2	1	0	0
203	1	3	12	2	30	180	31	8	0	1	0	473	2	1	4	3	25	300	11	2	0	0	0
205	1	3	10	2	30	180	31	8	0	0	0	475	2	1	7	3	38	225	17.8	4	0	0	0
206	1	3	16	2	30	347	31	8	0	1	1	476	2	1	4	3	30	100	9	1	0	0	0
207	1	3	12	2	30	347	31	8	0	0	0	477	2	2	3	3	35	233	8	1	0	0	0
208	1	3	10	2	30	347	31	8	0	0	0	478	2	1	11	3	30	190	9	2	0	1	0
209	1	3	16	2	30	190	31	8	0	1	0	479	2	1	7	3	40	442	18.5	4	0	0	0
210	1	3	12	2	30	190	31	8	0	0	0	480	1	2	10	1	20	32	24.5	6	0	1	0
211	1	3	10	2	30	190	31	8	0	0	0	481	1	2	10	2	30	254 51	24.5	6	0	0	0
212	1	3	10	2	40	200 288	31	0 8	0	0	0	402	1	1	12	1	20	50	315	6	0	0	0
213	1	3	10	2	40	288	31	8	0	0	0	484	1	2	16	1	8	20	31	8	0	0	0
215	1	2	16	1	25	50	35	8	1	0	Õ	485	2	1	12	3	23	53	10	2	0	0	Õ
216	1	2	12	1	25	50	35	8	0	0	0	486	2	1	7	3	34	196	8	1	Õ	0	0
217	1	2	17	1	30	240	31	8	1	0	1	487	1	3	16	2	30	70	19	4	0	0	0
218	1	2	13	1	30	240	31	8	0	0	0	488	2	3	16	1	25	84	19	4	0	1	0
219	1	2	11	1	30	240	31	8	0	0	0	489	1	3	13	1	16	60	31.5	8	0	0	0
220	1	2	19	1	16	45	23	4	0	0	0	490	2	3	13	3	24	403	9.5	2	0	0	0
221	1	2	17	1	20	74	38	8	0	1	1	491	1	3	13	2	40	180	31.5	8	1	0	0
222	1	2	13	1	20	74	38 28	0	1	1	0	492	2	5	2	2	24 16	419	9.5 14	2	0	0	0
223	1	1	20	1	20	19	31	8	0	1	0	493	2	1	3	3	40 46	305	14 24	2 4	0	0	0
225	1	1	16	1	8	19	31	8	1	0	0	495	2	3	6	3	25	100	35.5	6	0	0	0
226	1	1	14	1	8	19	31	8	0	0	0	496	2	1	3	3	45	90	14	2	Õ	0	0
227	1	3	20	1	30	60	31	8	1	0	0	497	2	1	5	3	28	100	9.5	2	0	0	0
228	1	3	16	1	30	60	31	8	1	0	0	498	1	1	13	1	20	50	31	6	0	0	0
229	1	3	14	1	30	60	31	8	0	1	0	499	1	1	12	1	27	91	32.5	6	0	0	0
230	1	1	20	1	6	9.3	24	6	0	1	0	500	1	1	13	1	20	40	16	3	0	0	0
231	1	1	16	1	6	9.3	24	6	1	0	0	501	2	2	8	3	20	50	9.75	2	0	0	0
232	1	1	14	1	6 20	9.3	24 19 E	6	0	1	0	502	1	1	10	3	48	190 52	9 10	2	0	0	0
233	1	2	10 16	3	20	27	18.5	4	0	0	0	503	2	1	10	2	25 20	280	10	2	1	1	0
235	1	2	18	1	20	65	31	8	1	0	0	505	2	1	9	3	30	200	22	4	0	1	0
236	1	2	14	1	20	65	31	8	0	0	1	506	1	1	5	3	20	25	8.8	2	0	0	0
237	1	2	12	1	20	65	31	8	0	1	0	507	2	1	5	3	32	172	7.8	1	0	0	0
238	1	1	16	1	25	43	38	8	1	1	0	508	2	1	5	3	30	90	7.8	1	0	0	0
239	1	1	7	3	25	125	40	8	0	0	0	509	2	1	15	1	23	300	9	2	0	1	0
240	1	1	3	3	25	125	40	8	0	0	0	510	2	1	15	1	22	172	9	2	0	1	0
241	1	1	16	3	25	150	9	2	0	1	0	511	2	1	5	3	30	161	7.8	1	0	0	0
242	1	1	12	3	25	100	9	2	0	0	0	512	2	1	15	1	23	152	11	2	0	1	0
243	1	1	20	1	30 20	28	33	8	1	1	0	515	1	1	15	2	30 10	100	11 17	4	1	1	0
244	1	3	16	1	20	28	32	8	0	0	0	515	2	1	15	1	20	248	17	4	0	0	0
246	1	3	14	1	20	28	32	8	Ő	Õ	Ő	516	1	1	18	1	20	420	11	2	0	1	Õ
247	1	3	17	2	40	140	31	8	0	0	1	517	1	1	15	1	20	573	24	4	0	0	0
248	1	3	13	2	40	140	31	8	1	1	0	518	1	1	16	1	20	393	24	4	0	1	0
249	1	3	11	2	40	140	31	8	1	0	0	519	2	3	11	3	24	419	9.5	2	0	1	0
250	1	3	17	2	40	150	31	8	0	0	1	520	1	3	11	1	16	60	31.5	8	0	0	0
251	1	3	13	2	40	150	31	8	1	0	0	521	2	3	11	1	24	403	9.5	2	0	1	0
252	1	3	11	2	40	150	31	8	1	0	0	522	1	3	11	2	40	180	31.5	8	0	1	0
253	1	3	17	2	50	280	31.5 21.5	8	1	1	1	523	1	3	15	2	25 20	84 71	19	4	0	0	0
254 255	1 1	3	13	∠ 2	50	200 280	31.5	8	0	0	0	524 525	1 1	2	15	∠ 1	30	71 40	17 32	4 8	0	0	0
256	2	3	13	3	24	116	9.25	2	0	0	0	526	1	2	15	1	25	70	35	8	0	0	0
257	2	3	9	3	24	116	9.25	2	õ	õ	õ	527	2	1	7	3	48	158	9	2	õ	õ	õ
258	2	3	7	3	24	116	9.25	2	0	0	0	528	2	1	5	3	32	182	9	2	0	0	0
259	2	3	16	3	28	110	8.5	1	1	1	0	529	2	1	5	3	35	345	9	2	0	0	0
260	2	3	12	3	28	110	8.5	1	0	0	0	530	2	1	5	3	35	170	9	2	0	0	0
261	2	3	10	3	28	110	8.5	1	0	0	0	531	2	1	5	3	30	106	9	2	0	0	0
262	2	3	13	3	25	278	8.5	1	1	0	0	532	2	1	7	3	30	400	9	2	0	0	0
263	2	3	9	3	25	2/8	8.5	1	U	U	U	533	1	1	15	3	30	30	32	8	U	U	0

NO.	Α	В	С	D	Е	F	G	Н	Ι	J	К	NO.	Α	В	С	D	Е	F	G	Н	Ι	J	К
264	2	3	7	3	25	278	8.5	1	0	0	0	534	2	2	15	1	20	95	11.5	2	0	1	1
265	2	3	13	3	25	159	8.5	1	0	0	0	535	2	1	7	3	32	298	17.5	4	0	0	0
266	2	3	9	3	25	159	8.5	1	0	0	0	536	1	2	18	2	30	240	44	6	0	1	1
267	2	3	16	2	30	347	8.5	1	0	0	0	537	2	2	6	3	30	109	10	2	0	0	0
268	2	3	14	2	30	347	8.5	1	0	0	0	538	1	2	5	2	30	254	24.5	6	0	0	0
269	1	3	16	1	20	179	31.5	8	0	0	0	539	1	1	14	1	25	42	38.5	8	0	0	0
270	1	2	19	1	8	20	31	8	1	1	0	-	-	-	-	-	-	-	-	-	-	-	-

In this Appendix, A represents Structural Style, B represents District, C represents Age of Bridge, D represents Type of Bridge, E represents Span, F represents Length of Bridge, J represents Width of Bridge, H represents Number of Lanes, I represents Maintenance of Bridge Deck, J represents Maintenance of Superstructure, K represents Maintenance of Substructure. In column A, 1 represents Simply Supported Beam, 2 represents Continuous Beam. In column B, 1, 2, and 3 represent three different regions, respectively. In column D, 1 represents Plate Girder, 2 represents T-Girder, 3 represents Box Girder. In columns I, J, and K, 0 represents no maintenance, and 1 represents maintenance conducted during that year.

Appendix B

Table A1. Cont.

Table A2. BCI Values Set.

NO.	BCI														
1	97.82	69	92.68	137	87.93	205	82.14	273	83.84	341	96.06	409	96.72	477	92.19
2	88.92	70	94.68	138	90.75	206	86.07	274	87.26	342	97.41	410	94.88	478	96.71
3	89.16	71	95.94	139	90.78	207	82.68	275	89.88	343	93.59	411	93.06	479	89.76
4	80.57	72	91.35	140	86.72	208	83.22	276	88.89	344	99.66	412	97.85	480	88.36
5	94.78	73	94.52	141	87.24	209	82.96	277	87.65	345	99.29	413	94.14	481	87.74
6	86.05	74	95.39	142	81.61	210	80.2	278	90.22	346	95.01	414	93.46	482	87.59
7	85.64	75	94.74	143	87.18	211	81.17	279	85.5	347	92.69	415	89.71	483	85.46
8	93.29	76	91.76	144	86.65	212	89.02	280	85.99	348	89.96	416	89.78	484	83.66
9	83.57	77	98.57	145	80.87	213	89.13	281	83.57	349	87.96	417	91.77	485	87.62
10	85.95	78	97.18	146	87.9	214	89.37	282	84.29	350	89.47	418	88.87	486	94.65
11	85.16	79	92.71	147	81.76	215	83.09	283	86.13	351	81.45	419	97.08	487	88.98
12	86.88	80	91.71	148	85.31	216	87.55	284	86.57	352	84.63	420	89.37	488	88.18
13	93.12	81	95.6	149	89.13	217	85.17	285	84.2	353	85.94	421	93.95	489	95.3
14	94.29	82	92.42	150	83.24	218	84.82	286	80.21	354	86.74	422	93.25	490	89.42
15	88.88	83	92.51	151	88.1	219	86.56	287	83.61	355	87.74	423	94.73	491	93.98
16	85.42	84	85.07	152	89.4	220	83.18	288	82.97	356	98.39	424	93.41	492	87.98
17	81.73	85	88.36	153	88.64	221	89.29	289	85.65	357	89.51	425	90.3	493	98.13
18	91.38	86	93.45	154	87.18	222	83.78	290	87.15	358	88.72	426	89.32	494	97.38
19	91.86	87	88.31	155	86.75	223	84.32	291	82.23	359	89.56	427	89.43	495	97.08
20	83.63	88	91.49	156	88.64	224	86	292	84.26	360	88	428	89.95	496	99.33
21	91.38	89	96.31	157	88.15	225	88.18	293	84.47	361	89.96	429	82.38	497	95.43
22	91.22	90	94.82	158	86.43	226	86.63	294	88.8	362	89.92	430	84.49	498	86.59
23	86.54	91	93.97	159	85.97	227	88.28	295	87.04	363	89.03	431	95.73	499	88.88
24	81.59	92	96.07	160	91.47	228	88.15	296	82.51	364	89.34	432	85.89	500	85.51
25	99.75	93	93.18	161	88.78	229	92.32	297	84.39	365	92.39	433	90.61	501	90.6
26	88.13	94	94.81	162	89.55	230	87.36	298	91.87	366	93.97	434	90.8	502	94.36
27	96.63	95	93.38	163	88.34	231	84.77	299	91.85	367	93.29	435	89.72	503	85.17
28	89.64	96	97.58	164	92.4	232	87.88	300	84.66	368	87.63	436	90.75	504	87.46
29	85.59	97	89.28	165	89.46	233	87.57	301	86.71	369	89.74	437	88.65	505	89.24
30	86.64	98	84.71	166	85.38	234	87.5	302	90.17	370	89.23	438	96.12	506	92.94
31	83.22	99	94.94	167	82.9	235	85.43	303	89.41	371	88.7	439	90.18	507	99.2
32	88.66	100	99.05	168	87.23	236	86.72	304	82.9	372	88.89	440	89.56	508	95.61
33	89.29	101	98.64	169	83.93	237	84.66	305	83.96	373	89.4	441	81.44	509	85.25
34	89.03	102	91.3	170	83.37	238	86.3	306	87.14	374	89.23	442	84.7	510	86.89
35	87.14	103	87.94	171	89.34	239	89.88	307	83.01	375	90.17	443	88.95	511	97.84

NO.	BCI														
36	92.97	104	89.29	172	88.91	240	92.52	308	86.64	376	98.07	444	89.69	512	87.72
37	85.63	105	93.42	173	82.67	241	89.02	309	97.08	377	97.44	445	89.84	513	87.73
38	84.71	106	94.07	174	89.31	242	88.74	310	97.41	378	95.52	446	96.92	514	89.79
39	86.52	107	95.25	175	87.4	243	88.11	311	86.41	379	96.01	447	98.5	515	84.39
40	88.59	108	95.31	176	84.21	244	86.73	312	85.58	380	98.51	448	96.44	516	84.4
41	99.75	109	96.14	177	86.32	245	80.25	313	90.9	381	97.12	449	96.85	517	88.92
42	88.69	110	94.67	178	89.65	246	80.85	314	95.05	382	93.54	450	95.05	518	89.19
43	88	111	95.55	179	86.5	247	85.55	315	94.65	383	89.1	451	98.9	519	94.49
44	89.43	112	98.92	180	89.07	248	83.02	316	96.06	384	93.62	452	94.08	520	89.86
45	90.04	113	88.79	181	92.35	249	82	317	90.08	385	89.15	453	89.66	521	95.46
46	91.9	114	86.72	182	91.26	250	88.75	318	94.66	386	86.92	454	88.09	522	94.79
47	91.84	115	87.76	183	93.5	251	87.6	319	84.19	387	89.78	455	89.48	523	84.33
48	85.68	116	84.19	184	90.7	252	86.69	320	86.39	388	97.26	456	89.5	524	89.6
49	98.36	117	83.75	185	91.7	253	92.28	321	86.12	389	99.63	457	97.16	525	85.47
50	92.04	118	81.47	186	97.25	254	82.04	322	88.54	390	89.73	458	98.16	526	89.6
51	96.55	119	86.07	187	91.28	255	84.05	323	80.66	391	96.98	459	98.64	527	94.24
52	97.05	120	84.67	188	98.24	256	97.99	324	85.04	392	88.76	460	96.9	528	91.83
53	94.85	121	81.64	189	95.43	257	97.96	325	87.06	393	96.27	461	94.92	529	90.54
54	95.24	122	90.21	190	97.98	258	98.99	326	87.34	394	93.21	462	93.2	530	88.42
55	91.71	123	85.58	191	96.94	259	89.89	327	91.56	395	95.9	463	96.22	531	89.8
56	92.96	124	83.71	192	98.28	260	86.71	328	93.25	396	89.88	464	95.18	532	90.8
57	97.92	125	83.38	193	89.5	261	87.63	329	84.52	397	94	465	89.17	533	88.32
58	98.98	126	89.56	194	88.12	262	96.34	330	85.46	398	95.84	466	88.79	534	98.5
59	91.91	127	88.68	195	82.04	263	96.03	331	81.66	399	95.46	467	89.58	535	95.33
60	94.18	128	88.9	196	89.35	264	99.55	332	82.84	400	96.93	468	92.71	536	85.6
61	94.21	129	88.12	197	87.63	265	95.74	333	84.67	401	93.97	469	87.51	537	93.27
62	96.3	130	88.67	198	82.16	266	96.59	334	85.72	402	89.76	470	88.11	538	90.12
63	93.84	131	87.17	199	87.33	267	85.36	335	84.3	403	96.85	471	90.73	539	82.58
64	94.6	132	87.82	200	84.61	268	97.71	336	88.37	404	89.69	472	83.75	-	-
65	93.38	133	87.2	201	81.88	269	86.9	337	86.56	405	94.26	473	95.71	-	-
66	87.73	134	89.54	202	81.05	270	88.54	338	84.82	406	93.51	474	92.71	-	-
67	94.52	135	83.36	203	82.49	271	83.86	339	87.75	407	96.06	475	93.02	-	-
68	89.9	136	89.13	204	83.63	272	86.41	340	99.33	408	94.6	476	91.49	-	-

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