



Review Recent Advances in the Laser Forming Process: A Review

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Abstract: Laser forming is an emerging manufacturing process capable of producing either uncomplicated and complicated shapes by employing a concentrated heating source. The heat source movement creates local softening, and a plastic strain will be induced during the rise of temperature and the subsequent cooling. This contactless forming process may be used for the simple bending of sheets and tubes or fabrication of doubly-curved parts. Different studies have been carried out over recent years to understand the mechanism of forming and predicting the bending angle. The analysis of process parameters and search for optimized manufacturing conditions are among the most discussed topics. This review describes the main recent findings in the laser forming of single and multilayer sheets, composite and fiber-metal laminate plates, force assisted laser bending, tube bending by laser beam, the optimization technique implemented for process parameters selection and control, doubly-curved parts, and the analytical solutions in laser bending. The main focus is set to the researches published since 2015.

Keywords: laser forming process; laser bending; doubly-curved surfaces; optimization; tube bending

1. Introduction

Sixty years have passed since the day Theodore H. Maiman built the first laser in 1960 at Hughes Research Laboratories. Since then, different types of laser were invented and improved for use in industries and laboratories. Two recent review papers are currently published and address various aspects of using laser technology. Dixit et al. [1] and Das and Biswas [2] published review papers on laser forming in 2015 and 2018, respectively. However, laser technology, applied in manufacturing technology, can be viewed from a completely different prism. The "LASER" acronym stands for Light Amplification by Stimulated Emission of Radiation. A single phase-coherent beam can be focused on a tiny spot, and according to the power of the laser source, different processes are developed. The low magnitude power leads to surface treatment and annealing of the workpiece; increasing the laser power leads to the melting of the workpiece and welding. High power lasers melt and evaporate the workpiece, and metal cutting happens. The number of photons controls the power of the laser and the frequency emitted from the light source. The ability for industrial applications varies from 100 W to more than 5 kW. Forming is another type of process, which can be implemented by laser technology. The workpiece can be a flat plate (sheet) or tube.

Laser beam irradiation induces thermal stresses into the worksheet. Temperature gradient mechanism (TGM), buckling mechanism (BM), and upsetting mechanism (UM) are three proposed mechanisms that happen during the laser beam irradiation [3,4]. The cooling of the sheet, at last, leads to bending the sheet due to residual stresses and corresponding strains. By increasing the temperature during laser beam

irradiation, the physical properties of the sheet include yield strength, ultimate tensile strength, and the elastic (Young) modulus will also be decreased. The yield strength of the material decreases faster than the elastic modulus.

Consequently, the equivalent (von Mises, for instance) stress proportional to the elastic modulus overtakes the yield strength in some regions of the sheet. So, plastic deformation occurs over the irradiated zone. The amount of plastic deformation depends on both the pre-stress field and temperature distribution in the sheet. The more massive plastic strain will be obtained by higher peak temperatures and larger pre-stresses [5]. The laser beam specifications, the scan pattern, and the properties of the sheet determine the final shape of the workpiece. Reasonable attempts have been made by researchers in recent years to investigate the effect of laser irradiation path on the quality, productivity, and shape of the final workpiece. In the laser forming process, the heating of the workpiece is non-uniform and asymmetric. The beam irradiates from one point of the workpiece and scans along a defined path. The geometry condition is not constant along the heating line. So, an unwanted deformation will be created in the sheet called the "edge effect". This undesirable deformation reduces the forming accuracy. By introducing the laser forming technology, new applications responded in various industries. Bending of small parts with little bending angle (less than 1°), bending of complicated parts for aerospace industries such as tailor machined blanks (TMB), bending of low diameter tubes with minimum ovality and thickness variations, forming of composite parts with little delamination, and forming of doubly curved specimens to obtain the irradiating patterns which can be used in the flame forming of the dome and saddle-shaped parts in ship bodies are examples of the industrial applications of laser forming.

2. Laser Bending of Monolithic Sheets

Sheet bending is a vital manufacturing process which can be performed using laser technology. The sheet is scanned along a straight line, and local heating of one of the sheet's surfaces leads to the plastic deformation of the sheet due to the stress gradient over the thickness direction. The process parameters affecting the bend angle are laser characteristics (laser power, spot size, scan speed, pulsed or continuous irradiation), the number of irradiation passes, material type, and the geometrical dimension of the sheet (thickness, width, length). The literature survey shows that laser power is the most influential process parameters in the laser forming process. The coating of the sheet is also necessary. Graphite is a typical coating that absorbs the irradiated beam effectively. The retention of heat in the coating layer for a longer duration affects the out-of-plane bending and minimizes the residual stresses [6]. The rougher surface (such as sandblasted surfaces) and thicker coating layer increase the absorptivity of the laser beam and lead to higher bending angle [7]. Microstructural observation using electron backscatter diffraction (EBSD) technique shows that the grain size does not influence the final bending angle [8]. Cement and lime are two other coatings used in experiments, and the results show that the cement coating creates more deformation and bending than the lime coating [9,10]. Pulsed or continuous irradiation of the laser beam is also essential. Pulsed irradiation beam with overlapping the pulses increases the bending angle, and the existence of a gap between the pulses reduces the final bending angle [11].

In the laser forming process, the sheet bends only with the laser beam, and no die, punch, or external tools except the mounting fixture are needed for forming. The forming is contactless. Here resides of the most significant advantages of this process. The small and local deformations by the laser beam form the part. Without a smooth deformation field, it is difficult to form a non-smooth component. The effect of varying the scan distance, the number of passes per scan line, and the number of scan lines on the profile of the bend are essential. Overlapping of the laser beam paths is required to create a continuous smooth bend [12]. The bending angle enhanced about 20% in multi-pass laser forming, but the bending rate decreased at higher passes. The numerical and experimental studies show that the relative variation of the residual plastic strain decreases with the increase in laser irradiation pass [13].

The material of the bent sheet is also important. Thermal and mechanical properties have a significant effect on the forming outcome. Steel alloys are the most common materials in published research [13–16]. Aluminum alloys, titanium, and magnesium are other common materials [4,8,17–25]. The main differences of different materials types are the melting temperature, mechanical properties variation by temperature, the heat conductivity of the material, and laser beam absorption. The forming of magnesium alloys is vital due to brittle material behavior and low elongation at failure. Dixit et al. [17] studied the bending of friction stir welded AA5052-H32 aluminum alloy sheets experimentally and numerically. The irradiation of the laser beam changes the mechanical properties of the welded zone hardness distribution. The input heat in the irradiated zone refines the microstructure of the bent zone, and small refined grains at the top layer, followed by large elongated grains, will be produced in the heat-affected zone. The grain refinement leads to an increase in micro-hardness. The slip and twinning mechanisms also can be activated in the heat-affected zone according to the processing condition. The input heat in laser forming improves the micro-hardness of the heat-affected zone in the sheet [8,15]. By increasing the thermal gradient and heat flux from a specified limit, the grains can grow, and the hardness will decrease with an increase in the grain size [19]. In the laser forming of steel sheets, ferrite and pearlite will form due to heating and cooling. The average grain size varies from 6 to 10 μ m [20]. The residual stress distribution is also affected by the input heat flux [21,23]. Fetene et al. [18] studied the effect of width and thickness on the multi-pass laser bending of AH36 steel strips experimentally and numerically. The absorption coefficient of the irradiated beam affects the bending angle. It can be obtained with experimental tests and inverse problem solution by finite element software such as ABAQUS, COMSOL MULTIPHYSICS, or ANSYS software [17,18,24]. The finite element analysis is usually carried out with a 3D nonlinear transient thermo-mechanical solver. The temperature and strain-rate dependent material properties of the sheet are required. The coupled thermal-structural analysis allows us to predict the bending angle with reasonable accuracy [24–26]. Safari and Ebrahimi studied the laser bending of perforated sheets [27] numerically. The results show that the bending angle decreases by increasing the diameters of the hole in the laser-formed perforated sheets. Figure 1 shows selected samples fabricated by laser forming.

The main challenge in the numerical modeling concerns the constitutive law to mimic the stress-strain behavior at elevated temperature, the heat transfer, and heat source models [4,25]. Higher material conductivity leads to higher heat transfer, and the heat-affected zone increasing. Consequently, the bending angle decreases. Air convection during beam irradiation is also essential [19]. Forced cooling by air and natural convection of air are compared [25], and results show that significant improvement had been obtained by forced cooling of air in the multi-scan laser bending process. The possibility of Martensite phase formation should be considered in the bending of steel alloys. Paramasivan et al. [24] investigated the simultaneous use of laser beam irradiation (at the top of the sheet) and a coaxial external cooling source (at the bottom of the sheet). The results showed that the bending angle increased by about 20% due to the increase in heat transfer and the temperature gradient between the top and the bottom of the sheet. The magnitude of induced residual stresses increased with an increase in cooling source diameters while the heat-affected zone decreased. The heat transfer in multi-pass laser forming is essential. Cooling time should be considered between repetitive passes to avoid surface oxidation and material melting. The conductivity of material and cooling conditions (forced or natural convection) can affect the production time and the productivity of the process in mass production [28]. Table 1 shows some of the main researches about the laser bending of single sheets.

Different aspects of laser bending have been investigated numerically and experimentally. The material of most of the researches is ductile. It seems that new methods of bending brittle materials are needed. Further aspects exist in the development of the laser forming process. The bending of pre-formed samples can be an advancement in this field. For example, the bending of a sheet with an elongated hole in the bending area (which was created by a cutting die) and bending the lateral edge of a stretch formed sheet such as a car body are two examples of pre-formed cases. The minimum radius of bending is essential. The problem is, "Can laser bending technology fabricate a sheet with zero

bending radius?". The possibility of using laser bending technology for assembling sheets is another interesting topic in this field. The behavior of laser-formed sheets in fatigue loading, creep condition, working at corrosive circumstance (high humidity, contact with the seawater, higher temperature), and comparison to conventional bending processes can help us judge the operational condition of laser-formed samples. Combining the laser bending with other laser-based processes such as laser beam machining (LBM) or laser beam welding (LBM), or even additive manufacturing and performing both processes simultaneously can produce more complicated and cheaper parts.



Figure 1. (a) Bending of the sheet by multi-pass irradiation [12], (Adapted from [12], with permission from Elsevier, 2020). (b) Laser bending by multi-scan laser bending [22], (Adapted from [22], with permission from Elsevier, 2020). (c) Laser bending of AH36 steel [18], (Adapted from [18], with permission from Elsevier, 2020). (d) Laser forming of AISI 304-stainless steel sheet with surface roughness and Cr₂O₃ oxide layer created [7], (Adapted from [7], with permission from Elsevier, 2020).

Reference	Material	Laser Specification	Blank Dimensions	
Zhang et al. [13]	DP980 steel	220 W laser; 2.5 mm spot diameter; 20 mm/min scan speed	80 mm × 80 mm, 1.8 mm thickness	
Zhang et al. [14]	DP980 steel	750–1250 W laser; 5.2 mm spot diameter; 2–5 m/min scan speed	100 mm × 50 mm, 1.4 mm thickness	
Maji et al. [15]	AISI 304 stainless steel	225–275 W laser; 0.5–0.75 mm spot diameter; 250–283 mm/s scan speed	120 mm × 40 mm, 0.5 mm thickness	
Song et al. [16]	Ultra-high strength steel sheet SPFC1180Y	500–1000 W laser; 5 mm spot diameter; 2–10 m/min scan speed	100 mm × 50 mm, 1.2 mm thickness	
Fetene et al. [18]	AH36 (mild) steel	500–700 W laser; 7.6–11.4 mm spot diameter; 800–1000 mm/min scan speed	120 mm length, 20–40 mm width, 1–2 mm thickness	
Mjali et al. [19,21]	Commercially pure grade 2 titanium alloy	1500–3500 W laser; 12 mm spot diameter; 1.6–2.6 m/min scan speed	200 mm × 50 mm, 3 mm thickness	
Kant and Joshi [22]	Magnesium M1A alloy	300–500 W laser; 3.87–7.74 mm spot diameter; 1–3 m/min scan speed	$70 \text{ mm} \times 40 \text{ mm}$, 1.9 mm thickness	
Kotobi and Honarpisheh [23]	Commercially pure grade 2 titanium alloy	1600 W laser; 3 mm spot diameter; 6 m/min scan speed	70 mm × 40 mm, 0.6 mm thickness	

Table 1. Comparison of the leading researches in the laser bending of monolithic sheets.

3. Laser Bending of Bi-Layer and Tailored Blanks

The previous section discussed the forming of single, monolayer, homogenous sheets. The properties and thickness of the sheet were assumed as constant. However, different properties of the sheet can be obtained by increasing the number of layers (bi-layer sheets or multilayer sheets), manufacturing a composite sheet, or different thickness or material (tailor welded blanks (TWB), tailor machined blanks (TMB)). Doing so, the laser-induced bending mechanism and magnitude of bending will be different. Safari et al. [29] investigated the laser bending of tailor machined blanks (TMB) experimentally. Tailor-made blanks are sheet metal assemblies with different thicknesses and/or materials and/or surface coatings. The laser melts the sheet, and bending happens due to plastic deformation during solidification. The thickness affects the bending angle. Different thicknesses, start point of scan and absorbed power by the sheet (laser power and scanning speed) influence the bending magnitude of the TMB sheet. The thick-to-thin irradiation path creates a higher bending angle in comparison to the thin-to-thick irradiation path. Increasing the laser power, reducing the laser scan speed and irradiation of the laser beam from the back of the sheet (the side of the sheet that the step does not rely on) enhances the bending angle of tailor machined blanks. The bending angle of laser-formed tailor-machined blanks can be predicted by the artificial neural network (ANN) [30].

Seyedkashi et al. [31] investigated the laser forming of stainless steel 304 L and Copper 11000 clad sheets using 200 W laser power. Clad sheets are types of tailored properties sheets. The laser beam creates a high-temperature gradient along the thickness direction. The portion of heat received by the sheets is different, and due to non-uniform plastic deformation, the bending angle, residual stress distribution, and microstructure are different in clad sheets.

Kotobi and Honarpisheh [32] studied the laser forming of St-Ti bilayer sheets. The induced residual stress distribution along the thickness is measured experimentally by the slitting method. The bending angle increases by increasing the laser power and number of scanning passes and reducing the scanning velocity. The higher residual stress will be induced in the workpiece, and a higher bending angle will be obtained. A relation between the bending angle and maximum residual stress has been derived [33]. Research has shown that the thermal properties of layers affect the thermally affected depth and lead to the smaller plastic zone. Consequently, a smaller bending angle will be obtained [34–36].

The thickness is another critical process parameter. Higher laser power is needed for bending thicker sheets. The sheet bending creates due to the temperature gradient induced in the sheet. So, for the bending of thick sheets, a steeper temperature gradient across the sheet thickness should be produced. Higher laser power (2 to 3 kW) and lower scan speed create such temperature gradient and deform the sheet [37]. The springback decreases by increasing the thickness. Thinner sheets may be

bent with significantly lower laser power (about 400 W) and higher scan speed, but the springback will be increased. The authors propose that a comprehensive study performs the residual stress distribution along with the thickness for bi-layer and TMB bent samples. This residual stress distribution can be measured with experimental methods and used for assessing the performance of the fabricated parts. Moreover, by developing a new type of materials and parts like functionally graded materials (FGM), shaped memory alloys (SMA) parts, and powder metallurgy parts, more investigation is needed to understand the mechanism of bending by the laser beam.

4. Laser Forming of Composite Sheets

The effect of material type and layers configuration on the laser-formed sheets were discussed in previous sections. In this section, the laser forming of composite sheets will be discussed. The type of composite is essential. Fiber and matrix have different mechanical properties (yield strength, stress-strain behavior) and physical properties (melting point, density, conductivity). Seyedkashi et al. [38] investigated the laser forming of three-layered SUS430/C11000/SUS430 laminated composite sheets. The copper mid-layer has higher thermal conductivity than the stainless steel 430 sheets. The plastic strain, along with the thickness and the shear stress between the layers, is more complicated than a single monolithic layer. Warping is another problem in the laser bending of composite samples. During the laser forming of stainless steel-carbon steel composite plate in ANSYS software, the non-uniform heat distribution and different heat conductivity and heat loss produce a warping force which causes undesirable deformation of composite in addition to the edge effect [39]. The sequence of layers is also important and affects the bending angle of the multilayer composite samples [40].

Fiber–Metal Laminates (FML) are made of different layers of metal and composite material. The difference between the properties of fiber, matrix, and metal leads to complicated plastic deformation, bending, and unpredictable. The complicated deformation mechanisms, interfacial delamination, and thermal alteration of the layers are three main challenges in the laser forming of FMLs. However, using the experimental test and using an artificial neural network tool made it possible to predict the behavior of FMLs during the laser bending process [41,42]. Moreover, the deformation of FMLs can be predicted using Eigen-strain field prediction [43,44]. The composites are divided into three categories, polymer matrix composite (PMC), ceramic matrix composite (CMC), and metal matrix composite (MMC). By increasing the use of MMC parts and the easy fabrication of PMC parts, more study is needed to fabricate the MMC and PMC made parts by laser beam technology. The use of MMC materials is increasing rapidly in the aerospace industry.

5. Force Assisted Laser Bending

To increase the bending angle of laser-formed sheets, applying an external force is a helpful solution. The applied force causes more bending, and sharp bending angles can be obtained [45]. The springback phenomenon is crucial, and the accuracy of forming is affected by the change in the angle of the bent sample after unloading. The springback has a close relation to the distribution of induced residual stresses during forming. The external force (bending moment) is created by a hydraulically driven tool, preload weight, or a screw-driven rod [46–48]. Fuzzy logic models and trained artificial neural network (ANN) with verified FEM models can predict the bending angle [49,50]. Figure 2 shows the mechanism of applying an external force for laser-assisted bending of titanium samples.

The proper combination of laser heating and external force increases the bending angle up to 140°, considerably decreases springback (10 times on titanium and 30 times on aluminum alloy), and reduces the risk of rupture during bending at high angles in comparison with conventional bending processes. Moreover, using an assistant force can decrease the edge effect in the laser bending process. Shi et al. [51] proposed a method consisting of applying two unequal concentrated forces, which reduce the edge effect up to 80% in comparison to the pure laser bending process. In a recent trial, the electromagnetic force is used for force assisted laser bending [52,53]. The electromagnetic

force is a non-contact tool that can bend the sheet more precisely by controlling the electric current and air gap between the electromagnet and sheet. Moreover, the straightening (unbending) of bent samples was carried out by the electromagnetic force. The distributed load instead of point load is the main advantage of electromagnetic force, despite the more challenging control of electromagnetic force.



Figure 2. Bending mechanism of titanium sheet by applying an external force and the final fabricated sample [46]. (Adapted from [46], with permission from Elsevier, 2020).

6. Laser Tube Bending

Tube bending was always a challenge in conventional bending. Usually, an internal plug is inserted inside the tube, and bending happens. However, a laser beam can also be used for tube bending. The laser beam is irradiated on the tube surfaces and may result in 2D or 3D tube bending. The amount of research about tube bending is low in comparison to the laser sheet metal forming. The effects of the irradiating length and the number of irradiating passes on tube bending have been studied. Three primary defects of the laser tube bending are lateral bending angle (especially when the scanning path is complicated like spirals), ovality, and thickness variation. The tube bending angle increased by increasing the irradiation length and number of passes. Moreover, the ovality percentage and the thickness variation will be increased by increasing the irradiation length [54]. The circular scanning method can be used for 2D and 3D tube bending. A scanning strategy has been developed to determine the scanning path using direct and reverse solution [55]. The effect of process parameters is like sheet metal forming, and the bending angle of the tube increases by increasing the laser power and beam diameter and with a decrease in the travel speed [56]. Figure 3 shows two samples of laser tube forming. Laser beam absorption can also be performed to improve the obtainable bending angle [57]. Different materials, such as carbon steel, stainless steel, and nickel tubes, can be formed and used in various industries such as aerospace industries, engines, heat exchangers, and air conditioners [54-60]. Statistical tools, such as Particle Swarm Optimization (PSO), can predict the bending angle and compensation of springback [58]. The Taguchi design of experiment, Artificial Neural Networks (ANN), and genetic algorithm (GA) are standard statistical tools which can find the optimized condition to obtain maximum bending angle, minimum ovality, minimum thickening, and minimum forming energy consumption [60].

The size of the tube is another essential process parameter. Normal sizes, such as 1/2 and 3/4 inch tubes, can be formed using a laser beam without difficulties. However, the laser forming of micro-tubes (for example, a tube with $635 \mu m$ outer diameter) needs more precise tools and controlled conditions [59,61]. The micro-tubes are thin-walled structures, due to high thermal conductivity and quick heat dissipation from the irradiated zone, short pulse, and high power laser beams utilized for inducing plastic strain and tube bending. It seems that researchers only focus on the bending of

round tubes. Rectangular tubes, especially the 3D bending of them, is an attractive subject of study. The ovality of 2D and 3D laser-formed tubes and thinning of the tube is also important and needs more investigation.



Figure 3. 2D and 3D tube bending [55]. (Adapted from [55], with permission from Elsevier, 2020).

7. Optimization

The selection of process parameters is crucial in laser forming. A comprehensive analytical model which determines the bending angle of the sheet during laser forming has not been derived until now. This is mostly due to the complicated nature of laser forming. Interaction between structural and thermal loadings and coupled thermo-elastic-plastic loading prevents a specified and comprehensive analytical model. In this way, statistical tools are powerful tools for finding the effect of process parameters and determining the behavior of the sheet during laser forming. Full factorial design of experiments, response surface methodology, fuzzy logic strategy, Particle Swarm Optimization (PSO), Artificial Neural Network (ANN), Taguchi approach, Genetic Algorithm (GA), and other statistical tools are implemented to derive an equation for prediction of bending angle [4,15,28,41,49,60,62–71]. The number of experiments is vital in the accuracy of the derived equation. The number of process parameters for laser forming (including laser power, pulse or continuous irradiation, beam diameter, scan speed, irradiation scheme, number of passes, material type, thickness, etc.) is high, and studying the effect of process parameters is not possible experimentally. So, in most studies, a finite element analysis using commercial FEM codes (ABAQUS, ANSYS, COMSOL MULTIPHYSICS, ...) is verified by experimental tests and the other set of experiments simulated by FEM. If two levels are selected for investigation for eight listed laser forming parameters, 28 experiments (256 experiments) should be carried out by full-factorial design, which is almost impossible to be carried out experimentally. Reducing the number of experiments leads to neglecting the interaction of some process parameters.

For example, Omidvar et al. [64] used the Taguchi orthogonal design of experiments (four factors-five levels) to find a maximum bending angle for a 1 mm thick AA6061-T6 sheet. Twenty-five experiments had been carried out to find the maximal bending angle of 28.7°. Similar research was conducted by Behera et al. [71]. The main difference between Taguchi and other designs of experiments is the aim of the Taguchi method, in which the robust control of parameters leads to less uncertainty in the fabricated workpiece. Kant et al. [65] developed an integrated FEM-ANN approach to calculate the bend angle with an artificial neural network (ANN) tool. Ponticelli et al. [49] used a fuzzy logic model to forecast the inherent uncertainties in the laser-assisted bending process and control of the springback. The optimal condition is determined according to the least-cost planning methodology (LCPM) to reduce the number of passes and use the highest laser power. Moreover, a combination of fuzzy logic controller and particle swarm optimization (PSO) methods is proposed by the researchers to find the proper set of input parameters to catch a predefined bending angle [67]. In laser forming, the bending angle and thickening of the sheet due to shrinkage are essential. Combining the genetic algorithm (GA) and neural network (genetic algorithm-based neural network (GANN)) helps for the proper determination of the effect of the input parameters on bending angle and thickening [68].

In most of the statistical models, the effectiveness of process parameters on output can be determined. The portion of each process parameters differ. Usually, laser-induced heat characteristics (laser power, pulse duration, and scan speed) are the most significant process parameters. However, the laser power cannot be increased above the melting point of the material, which will lead to the burning of material or formation of spongy debris on the surface of the sheet [69]. ANalysis Of VAriance (ANOVA) is a powerful tool for determining the effectiveness of each input parameter. Typically, a regression equation is derived which relates the output parameter to any arbitrary input parameters. The fitting quality and the range of process parameters affect the precision of estimation. Multi-objective optimization can be used to find the maximum temperature, maximum bending angle, and/or maximum residual stress. The optimization technique used in the above references focuses on the classical and standard optimization technique used frequently in manufacturing processes. By developing new optimization techniques such as grey wolf optimization (GWO), ant colony optimization (ACO), scatter search (SS), self-organizing migrating algorithm (SOMA), and combined metaheuristic optimization techniques such as simulated annealing-artificial neural networks (SA-ANN) and Powell simulated annealing with combinatorial optimization (PSACO) algorithm, it is possible to find the optimized condition for the fabrication of complicated shapes by the laser forming process.

8. Doubly Curved Parts

The laser beam irradiation path is an important parameter that can be used for shaping complicated parts including bowl-shaped surfaces, cylindrical surfaces, saddle-shaped surfaces, and intricate 3D shapes. In the laser-bending of sheets, the beam is irradiated along a straight line and bend the sample. However, using different scanning paths like spiral movement, concentric circles, crossed lines, spider pattern movement, and other developed scanning strategies make a complicated plastic strain field in the sheets and form the sheet to the desired shape. The tolerance of forming is a challenge that affects the effectiveness of the laser forming process. The curved parts can be used in shipbuilding, a cranial prosthesis (from Ti-6Al-4V titanium alloy for use in the skull) [72], Origami Spoon [73,74], and cylindrical shells. Gisario et al. [75] used radial paths to fabricate a dome from flat stainless steel blank. Maji et al. [68] used response surface methodology (RSM) to find the optimum process parameters to fabricate dome-shaped surfaces. The thickness of the sheet is crucial in doubly curved parts. Kant et al. [3] used a curvilinear path for forming of thick and thin sheets. The results show that the bend angle increases with a decrease in scanning path curvature in thick sheets. Different scanning paths can be utilized for the fabrication of curved parts. Table 2 shows some of the leading research in this field [76]. Several pieces of research have been published by the authors, which focus on the forming of saddle shapes by the spiral movement of the laser beam source [76–85]. The experience of the authors shows that concurrent consideration of the process parameters leads to better prediction of curvature. The proposed method for the design of experiments is response surface methodology (RSM). A comparison of spiral path movement with a circular irradiation path shows that a smoother curvature will be obtained while using a spiral path strategy. Moreover, the radial circular path forms the workpiece according to the buckling mechanism (BM), whereas the spiral irradiation pattern will result in a gradient mechanism (GM) [85,86]. Different materials, including mild steel, AISI 316 stainless-steel sheet [87], Galvanized iron [88], and AISI 304 stainless steel [89], were successfully formed by the researchers. Some researchers developed general scanning paths according to the circular irradiation path and showed that a precise workpiece could be fabricated using finite element modeling [90,91]. Figure 4 shows examples of doubly curved parts manufactured by laser forming. Most of the researchers focus on finding a proper irradiation scheme for forming of doubly curved shapes from a straight blank. However, forming doubly-curved specimens in multi-steps—for example, forming one curve and then re-irradiating the specimen to obtain the desired curvature in the perpendicular plane—is missed. It seems that independent control of curvature in multi-step bending can produce more complicated shapes and can be an exciting topic for researchers.

Table 2. Comparison of the irradiation scheme for laser forming of curved sheets	[70]	6]	l
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Reference	Fabricated Shape	Irradiation Scheme	Material	Laser Specification	Blank Dimensions
Chakraborty et al. [92]	bowl-shaped surface	Radial scan	AISI 304 stainless steel	350 W laser; 2.8 mm spot diameter; 0.45 mm/min scan speed	φ100 mm, 1 mm thickness
Liu and Yao [93]	pillow and saddle-shaped surfaces	Calculated paths	1010 mild steel	1000–1500 W laser; 6 mm spot diameter; 20–60 mm/s scan speed	140 mm \times 80 mm \times 0.89 mm
Na and Kim [94] and Kim and Na [95]	saddle-shaped surface	Calculated paths	mild steel	100 W laser; 2 mm spot diameter; 4–10 mm/s scan speed	$30 \text{ mm} \times 30 \text{ mm} \times 0.8 \text{ mm}$
Gao et al. [96]	ship hull shape	Calculated paths	S275 steel	400–500 W laser; 3–5 mm spot diameter; 20–40 mm/s scan speed	$100~\mathrm{mm}\times100~\mathrm{mm}\times1.5~\mathrm{mm}$
Imani Shahabad et al. [97,98]	Dome-shaped surface	Spider scanning paths	AA 6061-T6 aluminum alloy	2500–3000 W laser; 5–7 mm spot diameter; 60–100 mm/s scan speed	φ 150 mm, 2 mm thickness
Shen et al. [99,100]	Pillow, warped and saddle shape	Computational scanning path	304 stainless steel	200 W laser; 1.7 mm spot diameter	100 mm × 100 mm × 2 mm; 100 mm × 100 mm × 1 mm
Maji et al. [101]	Dome-shaped surface	Cross (axial and diagonal) scanning paths	AISI 304 stainless steel	400–500 W laser; 2–3 mm spot diameter; 30–40 mm/s scan speed	60 mm × 60 mm × 1 mm; 90 mm × 90 mm × 1 mm; 120 mm × 120 mm × 1 mm



(**c**)

(**d**)

Figure 4. (a) Fabrication of a bowl shaped surface by laser forming [92], (Adapted from [92], with permission from Elsevier, 2020). (b) Origami Spoon [73], (Adapted from [73], with permission from Elsevier, 2020) (c) Pillow, and warped shape [99], (Adapted from [99], with permission from Elsevier, 2020). (d) Dome and saddle shaped surfaces [76,95]. (Adapted from [95], with permission from Elsevier, 2020).

9. Analytical Approaches

Several pieces of research have been implemented to determine the bending angle analytically. One of the oldest articles in this field is Liu et al. [102]. Some of the research focuses on combined analytical and numerical methods for estimation of bending angle. Analytical models use equations of the elastic-plastic bending moment and equilibrium of force and moment [103]. Li and Wang [35] developed an analytical model to predict the bending angle of laminated plates accurately (stainless steel-carbon steel laminated plate). The piecewise function predicts the temperature distribution along with the thickness of the sheet. The zones in which the temperature is above the recrystallization temperature will experience a plastic deformation during cooling. The bending angle will be calculated analytically by determining the depth of the plastic zone, yield strength function, and the equilibrium equations. In a recent study, an analytical approach for predicting the bending angle of a laser-formed sheet with a single laser scan has been developed. The temperature field has been determined by

solving the 1-D transient heat conduction equation. The thermal strain and the induced thermal stress are obtained, and finally, the bending moment is assessed. The angle of sheet bending is determined according to the strain energy created due to the bending moment during the laser heating [104]. Recently, Kumar and Dixit [105] proposed an approach for the estimation of the temperature-dependent yield strength and modulus of elasticity. The approach consists of a straightforward solution and an inverse solution that relates the experimental data and finite element method to each other. Moreover, in another study, they developed a model to estimate the hardness of the laser bent parts. The kinetics of diffusional and non-diffusional phase transformation, latent heat generation during phase transformations, and the interaction of temperature and phase fraction on the variation of thermomechanical properties are three metallurgical phenomena should be considered in the analytical analysis [106]. The effect of preload during laser forming is essential. As discussed, force-assisted laser forming can bend sheets more effectively. An analytical model proposed by Guo et al. [107] for prediction of the bending angle in the presence of preload. The model is developed according to the buckling mechanism (BM) using thermal and preload stress and strain relationship in the heating zone and the buckling mechanism [107]. The edge effect is undesirable in laser forming, and the bending angle is not constant along the scanning line. An analytical solution to consider the edge effects in laser bending is suggested by Fauzi et al. [108].

The main challenges in the analytical model are the determination of the laser forming mechanism (thermal gradient mechanism (TGM), buckling mechanism (BM), the upsetting mechanism (UM), among others), analytical definition of mechanical properties (the definition of stress function according to strain, strain rate, temperature), non-linearity in geometry and properties, coupled thermal-structural analysis of bending, the effect of phase transformation, the residual stress remained in the workpiece, and stress relief during heating. Several developments can be attained in the field of the analytical model for the prediction of bending angle, strain field, residual stress distribution, and curvature radius. Joudaki and sedighi [109] proposed an analytical approach to predict residual stress during the bending of sheets. The model is developed to determine the effect of different material behavior on residual stress distribution. New analytical models can be derived by considering the stress as a function of temperature, strain, and coupled solving the structural and heat transfer equations.

10. Other Applications of Laser Beam Technology

A short pulse laser beam can be employed to fabricate micro-sized parts like MEMS parts [110]. Metal foams can be formed by laser forming [111–119]. Metal foams are a new category of materials which has a low density and good geometrical flexibility. Instead of applying a mechanical load, the laser irradiation heat produces a temperature gradient along with the thickness. The results show that the temperature gradient mechanism (TGM) is the primary mechanism of the closed-cell metal foams [113]. Stiffened parts and reinforced panels can be formed by laser beam irradiation [120–122]. The laser beam can be used in various processes like laser peen forming (LPF) [123–127], laser shock peening (LSP) [128,129], Laser solid forming (LSF) [130,131], laser folding [132], modification of mechanically bent parts (correction of spring back, over-bending or distortion of sheet [133]) and measuring the bending angle [134].

11. Conclusions

This review has briefly described the most remarkable and recent developments in laser-forming technology and applications involving single-layer, multilayer, and composite sheets. Topics covered include sheet bending by laser beam irradiation, tube bending, force assisted laser bending, optimization of process parameters, and analytical models in modeling. Doubly-curved parts have an essential role in the shipbuilding and aerospace industries and were discussed in a separate section. The laser beam technology can be used more creatively to fabricate special parts, such as saddle-shaped surfaces or the bending of micro-tubes. The experiences of the authors show that developing analytical solutions can help researchers to fabricate simple bending, but analytical solutions are not effective enough to

manufacture accurate and complicated shapes. Combining numerical methods, statistical approaches, and experimental knowledge can be a proper solution for the manufacturing of intricate shapes.

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