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Effects of Composition, Pressure, and Temperature on the Elastic Properties of SiO₂–TiO₂ Glasses: An Integrated Ultrasonic and Brillouin Study

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Abstract: We have systematically investigated the elastic properties (ρ , V_P , V_S , K, μ and σ) of eight SiO₂–TiO₂ glasses, varying in composition from 1.3 to 14.7 wt% TiO₂, as a function of pressure up to 0.5 GPa by the pulse superposition (PSP) ultrasonic technique, and two compositions (1.3 and 9.4 wt% TiO₂) up to ~5.7 GPa by Brillouin scattering in a diamond anvil cell. The parameters were also measured after annealing to 1020 °C. Composition–elasticity relationships, except for K and σ , are more or less linear; the annealing simply makes the relationships more uniform (less scatter). There is excellent agreement between the ultrasonic and Brillouin measurements at ambient and high pressure. The pressure-induced anomalous elastic behavior (negative dV_P/dP and dK/dP) becomes more negative (more compressible) with the increasing TiO₂ content. Correspondingly, the acoustic Grüneisen parameters become more negative with increases in the TiO₂ content, reaching a minimum near ~8–10 wt% TiO₂. The comparison of the low- and high-pressure ultrasonic and Brillouin V_P and V_S in two glasses (1.3 and 9.4 wt% TiO₂) shows excellent agreement, defining the reversible elastic behavior at low pressures and irreversible behavior at higher pressures (\geq 5.7 GPa) well. This result is consistent with our previous high-pressure Raman study showing an irreversible structural change in a similar pressure range.

Keywords: SiO₂–TiO₂ glasses; elastic properties; pressure-temperature dependences; ultrasonic method; Brillouin scattering; equation of state; anomalous compression behavior

1. Introduction

Interest in the SiO₂–TiO₂ glass system has continued to develop in view of its low thermal expansion properties and the ability to tune the coefficient of thermal expansion over wide ranges of temperature by varying compositions (TiO₂ content) and/or annealing. SiO₂–TiO₂ glasses containing up to ~11 wt% TiO₂ have been synthesized as apparently single homogeneous phases [1–3]. At relatively modest TiO₂ concentrations (>~3 wt%), TiO₂ plays the role of a network former just as SiO₂ does; thus, like Si, Ti is tetrahedrally coordinated with oxygen. A SiO₂–TiO₂ glass (ULE[®], Corning Code 7971) containing about 7.5 wt% TiO₂ has been demonstrated to have a nearly zero thermal expansion [4,5] in the temperature range of 0 to 300 °C. It has been shown [6–8] that moderate amounts of TiO₂ (up to 10 wt%) added to fused silica cause a systematic and linear decrease in the coefficient of



thermal expansion of silica glass. Such composition-dependent variations in the thermal expansion of SiO_2 -TiO₂ glasses have been plausibly correlated with changes in the structure and lattice vibrations in the glass network [6,9]. Schultz [7,8] successfully synthesized SiO_2 -TiO₂ glasses containing higher TiO₂ contents (up to 16.5 wt%) that were clear, and demonstrated unique annealing methods for developing the low-expansion properties of such glasses, containing even up to 20 wt% TiO₂, across wider ranges of temperature. The synthesized glasses with relatively high TiO₂ contents (16.5–20.0 wt%) were not, however, fully transparent due to phase separation and the presence of crystalline phases of TiO₂ (rutile/anatase).

A number of investigators [10–24] have studied the effects of TiO_2 content on the various physical, thermal, elastic and optical properties of SiO_2 – TiO_2 and other related glasses, such as those in the system Na₂O– TiO_2 – SiO_2 . Some of these studies [10,11] have thrown light on the roles of the structure and coordination of Ti and Si ions in the variations of glass properties. The infrared reflection and Raman scattering studies [23,25,26] on SiO_2 – TiO_2 glasses have enabled an elucidation of the structural variations caused by the addition of TiO_2 to SiO_2 .

The purpose of this paper is to report more extensive information on the elastic properties of SiO_2 –TiO₂ glasses as a function of composition, annealing, pressure and temperature, and to correlate the results, in light of a structural model, with the variations in thermal expansion and other related anharmonic parameters. The pressure dependences of the ultrasonic elastic moduli of the glasses reported here have been described recently [24], but primarily in the context of possible coordination changes in TiO₂ at low titania concentrations. Here, we probe the behavior of the system on annealing, and particularly focus on the acoustic Grüneisen parameters and the minimal anelastic behavior in this system at frequencies exceeding the MHz range via a comparison of new Brillouin data with the ultrasonic measurements.

2. Materials and Methods

The eight SiO₂–TiO₂ glasses used in this study were prepared by the flame hydrolysis boule process [6–8] at the Corning Glass Works laboratory. The TiO₂ content of the glasses ranged from 1.3 to 14.7 wt% (Table 1). Further, a fused silica sample obtained from the Corning Glass Works (Corning Code 7940) is included in this study. The preparation of these glasses has been described in detail previously [6,8]. Briefly, compositions were determined by X-ray fluorescence, with net uncertainties in the compositions of ±0.03 wt% [8]. The abundance of Ti³⁺ in these glasses was minimal; prior to annealing, the abundance was estimated as ~10 ppm [8], and after annealing, the glasses became entirely water-white, implying that the amount of Ti³⁺ was negligible [8].

Glass Number	Composition in wt%		ρ	Vp (km/s)	Vs (km/s)	K (GPa)	μ(GPa)	E (GPa)	σ Poisson's Ratio
	SiO ₂	TiO ₂	(g/cm)						
7940A (fused silica)	100	0	2.2007	5.947	3.769	36.16	31.26	728.0	0.165
T4A	98.7	1.3	2.2005	5.911	3.746	35.71	30.88	79.11	0.164
T1A	97.2	2.8	2.2001	5.872	3.717	35.32	30.40	70.88	0.166
T5A	95.4	4.6	2.1995	5.833	3.692	34.87	29.98	69.70	0.166
T6A	94.0	6.0	2.1992	5.803	3.672	34.53	29.65	69.16	0.166
T2A	92.7	7.3	2.1986	5.758	3.635	34.15	29.0.5	67.90	0.169
ULE 7971A	92.5	7.5	2.1993	5.783	3.653	34.42	29.35	62.56	0.168
T3A	90.6	9.4	2.1985	5.719	3.607	33.77	28.60	66.91	0.170

Table 1. Chemical composition and ultrasonic elastic parameters of seven SiO_2 -Ti O_2 glasses at an ambient pressure and temperature. The measurements of these glasses after annealing are listed.

2.1. Density and Ultrasonic Measurements

The density of the glass specimens was measured by the Archimedes method, using distilled water. The density and velocity measurements were made on the glasses both in an "as received, unannealed state," as well as after annealing. The annealing process involved heating the glasses

to 1020 °C for about 1–1/2 h, and then cooling them slowly from 1020 to 700 °C at a rate of 5 °C/h, and then allowing them to cool inside the furnace from 700 °C to room temperature.

The ultrasonic velocities were measured by the pulse super-position method at pressures up to 0.5 GPa [19,24]. Samples of the acoustic path length of about 1 cm were employed. The two faces of the sample were lapped flat within about 1 μ m and parallel to within about 30 s of the arc. X- and Y-cut 20 MHz quartz transducers, 0.63 cm in diameter, were used for the compressional and shear wave velocity measurements, respectively. The details of the electronics and high-pressure and temperature equipment used, and the procedure to reduce the basic pulse repetition frequency data to obtain the elastic moduli are described elsewhere [19,24]. Briefly, Cook's [27] method (Equation (1)), which solves for the high-pressure density (ρ) at the pressure (P) from the adiabatic bulk modulus (K_S) corrected to isothermal conditions (using Δ , which is equal to $\alpha\gamma T$, the product of the thermal expansion, Grüneisen parameter and temperature), was used to iteratively solve for the density under pressure at progressive intervals of 0.0275 GPa.

$$\ln(\rho/\rho_0) = (1+) \int_{P_0}^{P} dP/K_S$$
(1)

The precision of the frequency (*f*) measurements is ~ 1 part in 10^5 . The phase angle correction, $\gamma/360 f$, due to the bond between the transducer and the specimen, is negligible (γ does not exceed 2° for a well-prepared bond) and was ignored. The errors in the ultrasonic velocity values reported here are between 0.05% and 0.14%; incorporating the errors in density, our uncertainties on the derived moduli are less than 0.24%. The pressure derivatives of the moduli were calculated from a combination of fits to the velocities and the iteratively-derived densities from Equation (1) [24].

2.2. Brillouin Scattering Measurements

The Brillouin scattering technique was used by deploying a 5-pass Fabry–Pérot interferometer (Sandercock design) coupled with an Ar⁺-ion laser (at 100 mW power) for the excitation of the approximately 120 μ m diameter sample. Measurements of the acoustic velocities were conducted at an ambient pressure and up to ~7.5 GPa in a diamond anvil cell. The apparatus and methodology are described elsewhere [28]: briefly, the modified platelet geometry approach was deployed with a ~20° external scattering angle, with the angle chosen to optimize the signal. A collection time of 45 min was used for each Brillouin data point. Diamond anvils with 0.8 mm size culets and a T301 stainless steel gasket were used, with a 4:1 methanol/ethanol mixture as the pressure medium. The ruby fluorescence technique was used for the in situ pressure measurements. Due to the relative sharpness and amplitude of the peaks, the compressional velocities were more accurately determined than the shear velocities in these experiments, with estimated accuracies of ±0.4–0.7% for the compressional velocities and ±0.8–1.5% for the shear velocities. The shear velocity error was somewhat larger than the compressional velocity because the lower amplitude of the shear peak generated a smaller signal-to-noise ratio relative to the strong and sharp compressional peak.

3. Results and Discussion

3.1. Elastic Parameters at 1 bar and 25 °C

(A) Effect of composition and annealing. The composition and measured elastic parameters of SiO_2 -TiO₂ glasses, including fused silica (Corning Glass Works Code 7940), are listed in Table 1. The data for fused silica and the ULE[®] SiO₂-TiO₂ glass (Corning Code 7971) containing 7.5 wt% TiO₂ are in good agreement with the previous measurements of McSkimin and Andreatch [29] and the published Corning Glass Works specification [3], but in less good agreement with those of Gerlich et al. [30] The density and bulk moduli values reported by Gerlich et al. for these glasses are appreciably lower.

For end-member fused silica, our results are in good accord with previous ultrasonic and Brillouin results at 300 K [30–32]. Notably, there are variations in the reported values of the velocity in fused silica of up to ~50 m/sec in compressional velocity [33], but velocities are known to vary depending on the thermal history/fictive temperature of the glass [34].

The compositional dependence of the compressional (*Vp*) and shear (*Vs*) velocities, density (ρ), Poisson's ratio (σ), and bulk, shear and Young's moduli (*K*, μ and *E*, respectively) for these glasses are shown in Figures 1–3. The relations between the TiO₂ content and the elastic parameters, particularly *K* and σ , are not as uniform and systematic for the unannealed glasses as for the annealed glasses.



Figure 1. Longitudinal (V_p) and shear wave (V_s) velocities versus TiO₂ content for unannealed (as received) and annealed glasses. For the compositions up to 9.4 wt% TiO₂, annealing causes an increase in V_s and a slight decrease in V_p . Squares are McSkimin's (unpublished) 1972 data for the CorningULE[®] 7971 glass. For the 14.7 wt% glass, which is partly crystalline, both velocities drastically decrease on annealing (see text for discussion).



Figure 2. Density (ρ) and Poisson's ratio (σ) versus TiO₂ content. As shown, annealing causes an increase in ρ and decrease in σ for the SiO₂–TiO₂ glasses studied.



Figure 3. Bulk (*K*), shear (μ) and Young's (*E*) moduli versus TiO₂ content. Annealing causes an increase in *K*, and a decrease in μ and *E*. Squares are McSkimin's (unpublished) 1972 data. Error bars are smaller than the symbols.

As a result of annealing, the relations between the TiO_2 content and the elastic parameters become uniform and more or less linear for glasses containing up to 9.4% TiO₂ (Figures 1–3). The interesting aspect here is that the effect of annealing, which plausibly equilibrated the glasses closer to their glass transition temperature, T_g , has the effect of increasing the density of the glasses while lowering their compressional wave velocities, while also eliminating the unusually complex behavior of Poisson's ratio, σ , observed in the unannealed samples (Figure 2). Indeed, while the bulk moduli are greater in the unannealed samples, the shear moduli are substantially less (Figure 3), producing the anomalous behavior in the Poisson's ratio of these samples. The origin of the higher bulk moduli of the unannealed samples is not simple to explain: it is possible that there is a complex interplay between the internal strains and compressibility. Moreover, the lower density/higher temperature of the equilibration of the unannealed samples generates a substantial weakening of the shear modulus, implying that the lower density of the unannealed glasses has a particularly strong effect on the shear modulus. An explanation for these observations is that annealing causes the removal of strains and the rearrangement of the glass network such that the structure becomes more compact. This compaction effect of annealing, in particular, is dramatic in SiO_2 -TiO₂ glass (T 7) containing 14.7 wt% TiO₂ and, in contrast to the lower Ti-content glasses, results in increases in ρ , μ and E, but decreases in Vp, Vs, σ and K. Optical evidence shows that the annealing of the 14.7 wt% glass generates the unmixing of the glass and crystallization of TiO_2 , and hence the elastic results on this phase represent that of a two-phase aggregate. This unmixing is in full accord with the analysis that such high TiO₂ glasses are highly metastable and prone to unmixing to a crystalline TiO₂ phase and a coexisting glass at temperatures beneath the annealing point and as low as 750 °C [8]. The compaction effect in the T7 glasses may be related to an annealing-induced partial coordination change of Ti ions from four to six in the glass structure at high Ti contents. This reasoning is consistent with the infrared reflection [23] and Raman studies [23,25,26]. For the annealed glasses containing up to 9.4% TiO₂, the parameters, V_p , V_s , K, μ and E decrease linearly with the increase in the TiO₂ content; however, increases linearly with the TiO₂ content.

The decreases in the moduli are certainly caused by the weakening of the silica network. The Ti⁴⁺ ions have a lower field strength than the Si⁴⁺ ions, and the average length of the Ti–O bonds is larger than those of the Si–O bonds; hence, the Ti–O and Si–O–Ti bonds in SiO₂–TiO₂ glasses are weaker than the corresponding Si–O and Si–O–Si bonds in endmember silica glass. This view has been supported by infrared absorption studies [9,26].

The density of the glasses is particularly interesting in this respect: despite the larger mass of Ti, the effect of the increased Ti content is to weakly lower the density of these glasses.

Hence, the decrease in with the increasing TiO_2 content (Figure 2) seems, at first, surprising in view of the fact that the substituted Ti^{4+} ions are heavier than the Si^{4+} ions. In crystalline silica, Evans [1] clearly demonstrated that the additions of small amounts of TiO_2 to the SiO_2 – TiO_2 solid solution (cristobalite phase) cause the tetragonal a_0 and c_0 *d*-spacings of this phase to increase. Such an effect is consistent with the observed trend in the density of the SiO_2 – TiO_2 glasses. A decrease in density can thus be viewed as being due to the increasing openness of the structure as TiO_2 is added: while Ti may be present five-fold in coordination at low concentrations (below ~3 wt%), and four-fold at higher concentrations [24], it appears that the net effect of both larger Ti ions and potentially weaker polyhedral linkages for more highly coordinated species may each contribute to the unexpected decrease in density. The openness of the structure can also increase if the Si–O–Ti angles increase. This is exactly what is concluded from the optical studies [23,26].

3.2. Densification

The pressure density data for a solid can be used for calculating its bulk modulus, *Ko* and initial pressure derivative $K'o = (\partial K/\partial P)P = 0$ through the Birch–Murnaghan equation of state [35]:

$$P = (3/2 \text{ Ko} \{(\rho o/\rho)7/3 - (\rho o/\rho)5/3\} \{1 - \xi [(\rho o/\rho)2/3 - 1]\}$$
(2)

where $\xi = 3(4 - K'o)/4$. Correspondingly, if *Ko* and *K'o* are known, ($\rho/\rho o$) can be evaluated as a function of pressure.

Using Equation (1) and the data for fused silica and the SiO₂–TiO₂ glasses containing 7.3 wt% TiO₂ (Table 2), ($\rho/\rho o$) was calculated as 6 GPa (Figure 4) using our elasticity data. Here, we deployed our values of the bulk modulus and its pressure derivative to calculate the relative densities: due to the importance of the bulk modulus in determining the compression curve in this pressure range, higher order derivatives do not notably impact the density offset between the two phases. Values of the derivative parameters in Table 2 are derived from the initial (zero-pressure) slopes of the respective elastic parameters (Figures 2 and 3). As shown in Figure 4, the glass containing TiO₂ shows higher densification ($\rho/\rho o$) under pressure, as anticipated from the lower bulk modulus of this material. At 2 GPa, the difference between the ($\rho/\rho o$) ratios is expected to be ~7%. Thus, despite the almost identical initial densities of the two glasses (differing by ~0.1% at ambient pressures: Figure 2, top), the effect of pressure is to produce markedly higher densities for the Ti-bearing glass under pressure. The net result that a glass that contains more of a more massive cation is comparable in density to silica at an ambient pressure but becomes denser at a high pressure (as anticipated from its higher mean atomic number) illustrates that the initial structural role of Ti is to expand the overarching Si-dominated network in these glasses, but this Ti-induced expansion of the glass network is reduced under pressure.



Figure 4. Comparison of the densification of fused silica and SiO_2 – TiO_2 glass containing 7.3 wt% TiO_2 up to 6 GPa using the Birch–Murnaghan equation of state.

Glass Number	Composition in wt%		dK/dP	dp/dP g/cm ³ Mbar ⁻¹	dµ/dP	dE/dP	dơ/dP Mbar ⁻¹
	SiO ₂	TiO ₂					
7940A (fused silica)	100	0	-5.37	6.68	-3.53	-8.82	-1.01
T4A	98.7	1.3	-5.68	6.78	-3.56	-9.00	-1.24
T1A	97.2	2.8	-5.42	6.80	-3.56	-8.87	-1.00
T5A	95.4	4.6	-5.97	7.01	-3.55	-9.13	-1.52
T6A	94.0	6.0	-5.85	7.06	-3.54	-9.05	-1.42
T2A	92.	7.3	-5.96	7.20	-3.60	-9.20	-1.47
ULE 7971A	92.5	7.5	-5.88	7.10	-3.60	-9.16	-1.36
T3A	90.6	9.4	-5.77	7.26	-3.59	-9.09	-1.30

Table 2. Pressure derivatives of the elastic parameters (moduli in Mbar) of the annealed SiO_2 -Ti O_2 glasses at ambient conditions.

3.3. Comparison between Ultrasonic and Brillouin Measurements

A representative Brillouin spectrum from these results, using an apparatus described elsewhere [29], is shown in Figure 5, and Table 3 compares the Brillouin scattering results on two of these glasses within the diamond anvil cell with the lower pressure ultrasonic data. Figure 6 shows the elastic results under pressure from the two techniques. Clearly, on this scale, the two sets of results are in outstanding agreement. The larger pressure range of the Brillouin results reveals the well-known velocity minima occurring under compression in silica-rich glasses, and shows that the minima both shift to slightly higher pressures and the amplitude of the depression increases with higher TiO₂ contents. The pressure at which such minima occur has generally been correlated with the degree of polymerization of the glass [36], and the possible implication here thus might be that progressively more Ti enrichment may induce a greater polymerization of glasses. We speculate that it is more likely that the role of increased Ti is rather to broaden the average T–O–T (tetrahedral cation-oxygen-tetrahedral cation) angles in the glass relative to pure silica, producing a broader pressure range over which these angles may undergo a relatively easy contraction (and softening) of the glass [37].



Figure 5. Representative Brillouin spectrum of an SiO_2 – TiO_2 glass at 2.77 GPa; P and S represent compressional and shear peaks, respectively. Peaks generated by different orders of the grating are also present, as is a peak produced from the pressure medium between the P and S peaks. The higher signal-to-noise of the compressional peak relative to the shear peak produces a smaller error bar for the compressional velocity determination relative to the shear velocity.

Composition TiO ₂ , wt%	g/cm ³	Brillouin <i>Vp</i> (km/s)	Scattering Vs (km/s)	Ultrasonic <i>Vp</i> (km/s)	Ultrasonic <i>Vs</i> (km/s)	ΔVp; %	ΔVs; %
1.3	2.2005	5.933	3.743	5.911	3.746	0.4	-0.08
2.8	2.2001	5.890	3.732	5.872	3.717	0.3	0.4
4.6	2.1995	5.828	3.683	5.833	3.692	-0.09	-0.2
6.0	2.1992	5.800	3.656	5.803	3.672	-0.05	-0.4
7.3	2.1986	5.751	3.622	5.758	3.635	-0.1	-0.3
9.4	2.1985	5.746	3.616	5.719	3.607	0.5	0.2

Table 3. Comparison of the ultrasonic and Brillouin scattering measurements of V_p and V_s in SiO₂-TiO₂ glasses at ambient conditions.



Figure 6. Pressure dependence of the compressional (V_P) and shear (V_S) velocities measured by the ultrasonic method up to 0.5 GPa (inverted filled triangles) and Brillouin scattering (triangles, circles) up to ~5.7 GPa for two SiO₂–TiO₂ glasses. Black filled symbols are compression data and the open are decompression data that have been compressed to pressures below that at which irreversible deformation occurs. Red triangles are decompression points for irreversibly densified glasses compressed to slightly above 5.5 GPa. Error bars for the Brillouin data are in the order of, or smaller than, the size of the symbols; for the ultrasonic data, they are smaller than the symbol sizes.

While Table 3 shows generally excellent agreement between the Brillouin and ultrasonic data sets, there is a small but systematic offset between the two sets of the velocity determinations. Table 3 shows the relative ambient pressure velocities determined within each glass and the offset between the optical and ultrasonic measurements. Here, the Brillouin measurements are observed to yield average compressional velocities higher by ~0.15% relative to the ultrasonic results. Although these velocity differences are small and close to the sums of the respective errors of the two measurements (and, with the less-well determined Brillouin shear velocities, the average velocities are within error), their average sign is in accord with the possible presence of dispersive effects. Notably, the two sets of

measurements differ in the frequency of their probes by between a factor of ~450–750, or approaching three orders of magnitude. The average magnitude of difference for compressional velocities is roughly comparable to the ~0.2–0.3% difference across a factor of a ~7 larger frequency range that is observed in silica glass at 300 K [38], and our results thus indicate that weak dispersive effects might be present at ambient temperatures in Brillouin measurements in silica-rich glasses. The origin of these dispersive effects has been proposed to be via anharmonic interactions with localized vibrational states (termed "network viscosity" in [38]), although tunneling between nearly energetically equivalent local structural configurations could also play a significant role [38,39]. If the latter effect predominates, higher temperatures could produce a greater offset between the Brillouin and ultrasonic results in glassy materials, which could produce noticeable discrepancies between highly accurate experiments deploying these respective techniques.

Figure 6 also shows results on decompression from compression to near 6 GPa: this pressure has been previously identified from Raman results as the pressure at which irreversible structural changes within these glasses take place [37]. Such irreversibility is well-documented in silica glass, with the onset of irreversible densification occurring near 9 GPa [40,41]: our results indicate that the onset of irreversible densification occurs at lower pressures within titania-bearing glasses relative to the SiO₂ endmember. The rationale for this lower onset pressure of irreversible densification is almost certainly associated with the weaker Ti–O bonds (and Si–O–Ti linkages) within the glass network: irreversible changes in the ring statistics associated with compaction are likely to be generated more readily due to the presence of titanium in the framework. As an important aside, this irreversible densification will also augment the difference in densities between titania-bearing glasses and silica above 6 GPa (Figure 4).

3.4. Mode Grüneisen Parameters yHT and yLT

The mode Grüneisen parameters γi are evaluated from the pressure dependence of the acoustic mode velocities, *Vi*:

$$\gamma i = (K_T / V i) (dV i / dP)$$
(3)

where K_T is the isothermal bulk modulus. Assuming only contributions from the acoustic modes, the high- and low-temperature limiting values of the Grüneisen parameters, γ HT and γ LT, can be evaluated from (d*Vs*/d*P*) and (d*Vp*/d*P*) using well-established relations [35,42]. As in fused silica, the γ HT values for all the SiO₂–TiO₂ glasses are negative (Figure 7).



Figure 7. Variation of the low-temperature and high-temperature limits of the acoustic Grüneisen parameter as a function of the TiO_2 content.

Indeed, both γ HT and γ LT become more negative with the TiO₂ content. Here, the acoustic mode Grüneisen parameters reflect the low-frequency response of the glass, and demonstrate that the near-zero thermal expansion of these glasses reflects a balance between the strongly negative Grüneisen parameters associated with the acoustic modes and the generally positive Grüneisen parameters of the optical modes within these glasses [37]. Hence, the anomalously small thermal expansions of these glasses are generated by the competing and compensating effects of the low-frequency acoustic modes and high-frequency optic modes, and the decrease in thermal expansion with the addition of TiO₂ is likely related to the influence of TiO₂ on the acoustic lattice vibration frequencies.

4. Conclusions

The elastic properties and their pressure derivatives of the SiO₂–TiO₂ glasses studied systematically vary with composition. In general, Vp, Vs, ρ , E, K and μ decrease more or less linearly with the increases in the TiO₂ content. Further, both the acoustic γ HT and γ LT become more negative with the TiO₂ content. The effect of annealing is to increase ρ , decrease V_P and increase V_S . Nonetheless, the net effect of annealing is complex, and indicates that the annealing of glasses at temperatures closer to their glass transition may generate markedly more systematic elastic behavior relative to higher temperature quenching.

The excellent agreement between the ultrasonic and Brillouin measurements at ambient and high pressure enables a well-defined demonstration of the anomalous, as well as (elastically) the reversible and irreversible, pressure-induced compression behavior, as observed in V_P and V_S vs. the pressure plots for two selected glasses containing 1.3 and 9.4 wt% TiO₂ up to ~5.7 GPa, supporting our previous Raman study regarding the irreversible structural change near \geq 5.7 GPa [37].

Further studies of the elastic, thermodynamic and structural properties of the SiO_2 -TiO₂ glasses, involving acoustic and spectroscopic, simultaneously under in situ high-P-T environments, would enhance our understanding of their anomalous elastic and irreversible compressional behavior and structural changes under a high pressure and temperature.

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