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Seasonal Dynamics of Algal Net Primary Production in Response to Phosphorus Input in a Mesotrophic Subtropical Plateau Lake, Southwestern China

Yue Wu^{1,2,3}, Jinpeng Zhang¹, Zeying Hou¹, Zebin Tian¹, Zhaosheng Chu^{1,*} and Shengrui Wang^{2,3}

- ¹ National Engineering Laboratory for Lake Pollution Control and Ecological Restoration, Chinese Research Academy of Environmental Sciences, Beijing 100012, China; ecustwy@126.com (Y.W.); jpzhangcraes@163.com (J.Z.); houzy@craes.org.cn (Z.H.); tianzb@craes.org.cn (Z.T.)
- ² Guangdong-Hong Kong Joint Laboratory for Water Security, Center for Water Research, Advanced Institute of Natural Sciences, Beijing Normal University, Zhuhai 519087, China; wangsr@bnu.edu.cn
- ³ Engineering Research Center of Ministry of Education on Groundwater Pollution Control and Remediation, College of Water Sciences, Beijing Normal University, Beijing 100875, China
- * Correspondence: chuzssci@yeah.net

Abstract: A comprehensive 3-dimensional hydrodynamic and eutrophication model, the environmental fluid dynamics code model (EFDC) with three functional phytoplankton groups, was applied to simulate the algal dynamics in a mesotrophic P-limited subtropical plateau lake, Lake Erhai, Southwestern China. Field investigations revealed the seasonal patterns in external total phosphorus (TP) input and TP concentration, as well as the composition of the phytoplankton community. The model was calibrated to reproduce qualitative features and the succession of phytoplankton communities, and the net primary production was calculated. The modeled daily net primary production (NPP) ranged between -16.89 and $15.12 \text{ mg C/m}^2/d$ and exhibited significant seasonal variation. The competition for phosphorus and temperature was identified as the primary governing factor of NPP by analyzing the parameter sensitivity and limitation factors of the lake. The simulation of four nutrient loading reduction scenarios suggested high phytoplankton biomass and NPP sensitivity to the external TP reduction. A significant positive correlation was found among NPP, total phytoplankton biomass and TP concentration. Overall, this work offers an alternative approach to estimating lake NPP, which has the potential to improve sustainable lake management.

Keywords: environmental fluid dynamics code (EFDC); net primary production; phosphorus; Lake Erhai; scenario analysis

1. Introduction

In recent decades, the global spread of water eutrophication has become a critical issue of importance and research interest [1–3]. Nutrients, referring to nitrogen (N) and phosphorus (P) and biogeochemical cycles in lake watersheds are strongly influenced by the input of anthropogenic nutrients via river runoffs [4–6]. The oversupply of nutrients always leads to eutrophication, which results in elevated gross primary productivity (*GPP*), net primary production (NPP) and a high level of chlorophyll (Chla) [7–9]. NPP, defined as the net accumulation rate of carbon, is among the critical properties of ecosystems, which not only forms the basis of food webs, but also influences ecosystem-scale biogeochemical cycling rates. Surveys of NPP across stressor gradients can also help to identify how environmental change and anthropogenic disturbance alter metabolism rates in aquatic ecosystems [10–12]. Accordingly, understanding and forecasting the changes in NPP in response to external forcings, such as phosphorus, are major challenges for both scientific issues and improving sustainable lake management.



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). To date, several approaches have been developed to estimate NPP, including bottle and chamber incubations [13,14], the diel open-water technique [15–17] and oxygen isotopes [18,19]. However, the high temporal and spatial heterogeneity of NPP has posed a challenge in generating a comprehensive assessment of NPP in large and deep lakes. In addition to direct measurement, indirect estimation using alternative metrics (e.g., Chla and algal biomass) has also been utilized, including mathematical modeling approaches [20–22]. NPP is generally regulated by several biochemical and physical processes, such as temperature, light, nutrient availability, and water current [23–28]. Consequently, most recent works modeling the NPP are concerned with related parameters [29–31]. In addition, NPP is also influenced by biochemical differences in the algal community; the dominant species composition varies seasonally, but fewer studies dealing with NPP change in response to the shifting of the dominant species composition.

The Environmental Fluid Dynamics Code (EFDC) [32] is a comprehensive multidimensional surface water model that has been widely utilized for a wide range of water body types. The eutrophication module of EFDC is a carbon-based sub-model, simulating carbon dynamics in the lake. Moreover, the simulation of phytoplankton in EFDC is divided into three algal groups (diatoms, green algae and cyanobacteria). The division makes it possible to achieve the seasonal algal group transitions to investigate the species-specific impact on NPP. Therefore, we believe that the EFDC model could be utilized to model the NPP of the lake and reflect the effects of dominant species changes in phytoplankton on NPP. Although few comparative studies are available, the results are promising. Qin and Shen [33] determined the impact of local and transport processes on phytoplankton primary production using the EFDC model. Camacho et al. [34] modeled the factors controlling NPP rates of phytoplankton in St. Louis Bay and evaluated estuarine responses to nutrient load modifications using a WASP-EFDC coupled model. Much of the work in this area is still focused on the water quality-related constituents or anticipating harmful algal blooms (HABs).

In this paper, an algal-dominated mesotrophic plateau lake, Lake Erhai, in Southwestern China, was chosen to study how NPP changes in response to external P input with a significant seasonal succession of dominant algal species. Field observations and models were utilized to address the following objectives: (1) to explore the variations of nutrient supply and the algal community to calibrate the EFDC model parameters with field data; (2) to model the seasonal NPP of Lake Erhai; (3) to analyze the influences of phosphorus reduction scenarios on algal biomass and NPP.

2. Materials and Methods

2.1. EFDC Model Description

The water quality model was established and applied using a commercial version of DSI LLC (EFDC Explorer Release 10.3) developed from the Environmental Fluid Dynamics Code (EFDC) [32]. EFDC is a comprehensive 3-dimensional model designed for simulating hydrodynamics, salinity, temperature, eutrophication dynamics and the fate and transport of toxicants.

In the eutrophication submodule, the EFDC model is capable of simulating 21 water column state variables (Figure S4 and Table S1), including phytoplankton, dissolved oxygen (DO), and various components of carbon, nitrogen, phosphorus, silicon, total active metals and bacteria. The main state variables of carbon, phosphorus and nitrogen are dissolved, labile particulate, and refractory particulate state, whereas total phosphate (PO4⁻), and two mineral forms of nitrogen (ammonia nitrogen, NH₄-N and nitrate NO₃⁻) are also included in the nutrients cycle. The total active metal (TAM) is defined as the total concentration of metals that are active in sorption and subsequent settling of phosphate and silica, which are primarily iron and manganese.

EFDC also includes a sediment diagenesis module capable of simulating kinetic processes in the sediment bed and its interactions with the water column. The governing equations of the water quality module of EFDC can be represented as follows:

$$\frac{\partial (m_x m_y HC)}{\partial t} + \frac{\partial}{\partial x} (m_y HuC) + \frac{\partial}{\partial y} (m_x HvC) + \frac{\partial}{\partial z} (m_x m_y wC) \\
= \frac{\partial}{\partial x} \left(\frac{m_y HA_x}{m_x} \frac{\partial C}{\partial x} \right) + \frac{\partial}{\partial y} \left(\frac{m_x HA_y}{m_y} \frac{\partial C}{\partial y} \right) + \frac{\partial}{\partial z} \left(m_x m_y \frac{A_z}{H} \frac{\partial C}{\partial z} \right) \\
+ m_x m_y HS_c \tag{1}$$

where *C* is the concentration of a water quality state variable (mg/L); *u*, *v* and *w* are velocity components in the curvilinear coordinates (m/s); *x* and *y* are the orthogonal curvilinear coordinates in the horizontal direction (m); *z* is the sigma coordinate (dimensionless); *t* is time (s); A_x , A_y and A_z are the diffusion coefficients in the *x*, *y* and *z* directions; *m*_x and *m*_y are the square roots of the diagonal components of the metric tensor (m); *S*_c is internal and external sources and sinks per unit volume; *H* represents water column depth; and *m* is the horizontal curvilinear coordinate scale factor.

2.1.1. Phytoplankton Kinetic

Phytoplankton was partitioned into three groups in the simulation, namely, green algae, diatom and cyanobacteria. The simulation of cyanobacteria was restricted to non- N_2 fixing species since *Microcystis* spp. is dominant in Lake Erhai [35].

The following kinetic equation governed the biomass of phytoplankton:

$$\frac{\partial B_x}{\partial t} = (P_x - BM_x - PR_x) \times B_x + \frac{\partial (WS_x \times B_x)}{\partial Z} + \frac{WB_x}{V}$$
(2)

where P_x is the production rate of algal group x (day⁻¹) (x = 1, 2 or 3, where 1 represents cyanobacteria, 2 represents diatoms and 3 represents green algae); BM_x is the basal metabolism rate of algal group x (day⁻¹); PR_x is the predation rate of algal group x (day⁻¹); WS_x is the positive settling velocity of algal group x (m/day); WB_x represents the external loads of algal group x (g C/day) and V is the cell volume (m³).

Several factors control the growth of algal; based on these differences, we distinguished the related parameters (growth, respiration and grazing) in model simulations.

In the EFDC model, it is expressed by multiplying the maximum growth rate of each algal group by the limiting factor, as shown in Equation (3).

$$P_x = PM_x f_1(N) f_2(I) f_3(T) f_4(S)$$
(3)

where PM_x (day⁻¹) is the maximum growth rate of algal group x, $f_1(N)$ is the effect of suboptimal nutrient concentration ($0 \le f_1 \le 1$), $f_2(I)$ is the effect of suboptimal light intensity ($0 \le f_2 \le 1$), $f_3(T)$ is the effect of suboptimal temperature ($0 \le f_3 \le 1$) and $f_4(S)$ is the effect of salinity ($0 \le f_4 \le 1$).

2.1.2. Nutrient Limitation

For Lake Erhai, the primary limiting factor is the nutrients, which is expressed as follows:

$$f_1(N) = \left(\frac{\mathrm{NH}_4 + \mathrm{NO}_3}{\mathrm{KNHC} + \mathrm{NH}_4 + \mathrm{NO}_3}, \frac{\mathrm{PO}_{4\mathrm{d}}}{\mathrm{KHPc} + \mathrm{PO}_{4\mathrm{d}}}\right) \tag{4}$$

where KNHc is the nitrogen half-saturation constant for cyanobacteria (mg/L); KHPc is the phosphate half-saturation constant for cyanobacteria (mg/L); PO_{4d} is the dissolved portion of total phosphate (mg/L); and $f_1(N)$ and $f_1(P)$ refer to the nitrogen and phosphorus limitation functions, respectively.

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2.1.3. Temperature Limitation

In addition to nutrient availability, the temperature plays a significant role in regulating the growth, basal metabolization and predation of zooplankton. Cooler waters are preferable to diatoms as they have higher growth rates and are metabolically more active than green algae and cyanobacteria. The growth rate of green algae is less than diatoms, but it can endure higher water temperatures. Comparatively, cyanobacteria grow better at higher temperatures (>25 °C) than the other two taxa [36–38]. The temperature dependency of algal growth can be represented by a Gaussian probability curve [39,40]:

$$f(T) = \begin{cases} e^{-KTG1_x(T-TM1_x)^2}T \leqslant TM1_x \\ 1TM1_x \leqslant T \leqslant TM2_x \\ e^{-KTG2_x(T-TM2_x)^2}T \geqslant TM2_x \end{cases}$$
(5)

where *T* represents the water temperatures (°C) from the hydrodynamic model; TM_x is the optimal temperature for algal growth in algal group *x*; *KTG*1 and *KTG*2 are parameters that describe the effect of temperature on the growth of algal group *x* below *TM*1 or above *TM*2, respectively.

2.1.4. Basal Metabolism and Predation

The basal metabolism in the present model is the sum of all internal processes that decrease algal biomass and consists of two parts: respiration and excretion.

$$BM_x = BMR_x exp(KTB_x[T - TR_x])$$
(6)

where KTB_x is the effect of temperature on the metabolism in algal group x (1/°C), and TR_x is the reference temperature for the basal metabolism in algal group x (°C).

For zooplankton and planktivorous fish, green algae and diatoms are essential groups in freshwaters. Diatoms are beneficial groups in freshwaters as they provide food sources for zooplankton and planktivorous fish. Similar to the metabolism, the temperature effect on the predation rate in algal is expressed as an exponentially increasing function of temperature:

$$PR_{x} = PRR_{x} \left(\frac{B_{x}}{B_{x}P}\right)^{\alpha P} exp(KTP_{x}[T - TR_{x}])$$
(7)

where PRR_x is the reference predation rate at B_xP and TR_x in algal group x (1/day), B_xP is the reference phytoplankton concentration for predation (g C/m³), P is the exponential dependence factor, KTP_x is the effect of temperature on predation in algal group x (1/°C) and BMR_x is the basal metabolism rate at TR_x in algal group x (1/day).

2.1.5. Calculation of NPP

The classic GPP definition is as follows:

$$GPP = NPP + R \tag{8}$$

In the single cell, for each time interval, the change in phytoplankton biomass ΔB is described by the equation below:

$$\frac{\Delta B}{\Delta t} = GPP - R - F \tag{9}$$

where *GPP* is the phytoplankton gross primary productivity in a given time interval (g C/m²), *R* is the time specific rate of total phytoplankton respiration and consumption (including respiration, grazing and settling, g C/m², *R* is the rate of total phytoplankton respiration and consumption over daily and monthly timescale, when $\Delta t = 1$ d and 30 d respectively) and *F* is the time specific rate of phytoplankton moving in or out of the cell by physical transport.

When we calculate the change in phytoplankton biomass for the whole lake, F is generally assumed to be negligible compared with other sources [41]. Thus, the NPP could be estimated in Equation (10) by summarizing the change in total biomass for each time interval.

$$NPP(t) = \int \int \int (P_{total}(t) - BM_{total}(t) - PR_{total}(t)) dx dy dz$$
(10)

where P_{total} is the production rate of all algal group (day⁻¹); BM_{total} is the basal metabolism rate of algal group (day⁻¹).

Our study conducted an NPP calculation through the Mass balance Tool and Mass Flux tool in the EFDC Explorer 10.3. These functions allowed the total phytoplankton mass balance and mass flux in the total model's water columns to be computed based on model output snapshots: the smaller the output snapshot interval, the more accurate the reported results. In our model, the time step was less than 150 s, so in the post-process, we converted the NPP into daily and monthly timescales.

2.2. Study Site

Lake Erhai is a subtropical plateau lake $(99^{\circ}32'-100^{\circ}27' \text{ E}, 25^{\circ}25'-26^{\circ}10' \text{ N}, 1965.5 \text{ m}$ a.s.l), located on the Yunnan-Guizhou Plateau, Southwestern China (Figure 1). The lake's surface area is approximately 252 km², with a total storage capacity of $29 \times 10^9 \text{ m}^3$ and an average depth of 10.8 m. The watershed area is approximately 2565 km². The climate type of Lake Erhai watershed is subtropical, moist monsoon, with a distinctly rainy season (June to September) and dry season (October to March). The annual precipitation of the watershed is 932 mm.



Figure 1. Location and map of Lake Erhai watershed, the two outflows are marked with light blue. The Xi'er river watershed in the southeast of the lake is circled with red dotted line, the natural runoff in this area do not flow into the lake.

There are 27 major inflows in the north part, west part and south part of the Lake, respectively. Two outlets drain the lake from the south and the east, respectively. In the north, the Muji River system is the largest sub-watershed, covering 61% of the lake watershed [42] and contributing most of the water inflow (50–55% of the total annual inflow) through 3 major rivers (Mijuriver, Yong'an river and Luoshi river). In the west, 18 streams from the Cangshan Mountains are distributed along the narrow coast, constituting important water sources of the lake (40–45% of total annual inflow). The southern water sources of the lake are the Boluo river and the Baita river, supplying an additional 4% of the total annual inflow.

Historically, the water quality of the lake is good and oligotrophic. However, the intensified and imbalanced economic development, rapid urbanization and pressures from anthropogenic activities have significantly impacted this plateau lake, resulting in water quality degradation and eutrophication since the 2000s (Figure S1). The lake water quality experienced a sharp deterioration in 2002–2003. After the explosions of two large algal blooms in 2002 and 2003, the ecosystem shifted greatly from a macrophyte-dominated to an algal-dominated state [43].

2.3. Sample Collection and Analysis

Eleven monitoring sites were designed for monthly routine sampling during 2016 and 2017, water temperature (T) and dissolved oxygen (DO) were measured in situ by using portable instrument (Multi 3420, WTW, Oberbayern, Germany). Samples for total nitrogen (TN), total phosphorus (TP), ammonia nitrogen (NH₄-N), Chla, and phytoplankton biomass measurement were collected in pre-cleaned, acid-washed, brown polyethylene bottles and stored at 4 °C before laboratory analysis. All the chemical parameters were analyzed with three replications following standard methods [44]. Phytoplankton samples were preserved with Lugol's iodine solution (2% final conc.) and mirror checked. The species of phytoplankton were identified under a microscope (CX21, 400×, Olympus, Tokyo, Japan) based on the protocol in the "Phytoplankton Manual" [45] and "Chinese Freshwater Phytoplankton System, Classification and Ecology" [46]. The algal biomass was calculated based on the cell bio-volume for each species [47]. Additionally, it was converted to biomass in mg C/L based on the carbon content of phytoplankton given by Reynolds et al. [48].

2.4. Model Setup

2.4.1. Grid Generation

The lake was discretized with a curvilinear grid using 1047 grids, in which the most minor grid was approximately 0.26 km², and the largest was approximately 7.4 km². The average depth was 9.98 m, and the deepest grid was approximately 21.2 m in the lake center at the water surface elevation of 1965 m above sea level (Figure 2).

Although there is only weak thermal stratification in Lake Erhai, phytoplankton is still influenced by vertical distribution in light; therefore, it is desirable to resolve variability in vertical light intensity and nutrients using a three-dimensional spatial resolution. In this model, the grid is vertically discretized into five layers, and a total of 5235 computational cells were generated from top to bottom to represent Lake Erhai in its entirety.



Figure 2. Diagram of computational grids of hydrodynamic water quality simulation in Lake Erhai: the distribution of 29 major rivers and streams; simplified agricultural ditches are represented with circle and x mark; 2 outflows are represented with red filled circle and x mark.

2.4.2. Boundary Condition and Nutrient Input

The boundary conditions are the external driving forces of the model. The boundary conditions include the flow rates, water temperature and concentrations of water quality parameters within the inflow tributaries. The flow rates and water quality variables were monitored monthly by the local government of the Ecological and Environmental Bureau of Dali Bai Autonomous Prefecture for major rivers and streams. The boundary conditions were established using these data.

Nutrient loads from non-point pollution were estimated based on local monitoring since 2016 (Figure S2) and a flow balance analysis using the hydrodynamic model. There are nearly 200 agricultural ditches around the lake. These drainage ditches are particularly nutrient rich in the rainy season. Large-scale agricultural non-point pollutants were transported into the lake via these drainage ditches. The flow rates, water temperature, concentration of total nitrogen (TN), total phosphorus (TP) and ammonia–nitrogen (NH₄-N) were measured during the rainy season and dry season, respectively. The yearly nutrient input from the agricultural ditches were calibrated since the loading from ditches could account for 40–50% of the total yearly flux (Figure S3). In the model, we simplified these agricultural drainage ditches as 70 inflows evenly spaced along with the western (40 points), northern (20 points) and southern (10 points) lakeshores (Figure 2). The surface boundary

conditions included air temperature, atmospheric pressure, evaporation, precipitation, solar radiation, cloud cover, wind speed and direction on a daily to hourly basis. The meteorological data were sourced from China's Meteorological Scientific Data Sharing Service Network (http://data.cma.cn/, accessed on 5 December 2021).

Prior research has shown that sediment release in Lake Erhai is mainly triggered by overlying water conditions that vary with the seasons. Sediments can act as a pollutant source for the overlying water [49–51]. Thus, we set varied flux rates of PO₄ and ammonia for each season following reported diffusion experiments in the laboratory and in situ measured data [52–54].

2.4.3. Model Calibration and Validation

The generated EFDC model needed to be calibrated before it could simulate water quality compliance scenarios and offer quantitative information on the extent of cropping system change. The hydrodynamic module was first calibrated and the daily water elevation and temperature validated. Then, monthly monitoring data from eight sites were selected to calibrate and validate the Lake Erhai water quality simulation (Figure S2). TN, TP, Chla and DO were chosen to carry out the calibration. The calibration procedure was repeated until the simulated values could reproduce the temporal and spatial distributions of observed water quality indexes. The model performance was evaluated by the relative error% (*RE*%) based on the data of three lake center sites in 2017. The calibrated parameters were given in Appendix A (Table A1)

$$RE\% = \left| \frac{X_i^{observed} - X_i^{Simulated}}{X_i^{observed}} \right|$$
(11)

where $X_i^{observed}$ is the observed value of water variables, and $X_i^{Simulated}$ is the simulated value of water variables.

2.5. Sensitivity Analysis

To examine the sensitivity of our model, Latin Hypercubic sampling (LHS) combined with distribution-based sensitivity analysis (PAWN) were employed [55]. The selected parameters were first propagated by LHS, and then the output uncertainty was characterized by executing the LHS-created model. Finally, PAWN was used to determine the relative contribution of each parameter to output uncertainties.

The fundamental concept behind the PAWN method is that an input factor's effect is proportionate to the amount of change in the output distribution caused by correcting that input [56,57]. More specifically, the sensitivity of *y* to x_i is defined as the difference between the unconditional distribution of *y* caused by simultaneously varying all input factors and the conditional distribution induced by varying all input factors except x_i . The PAWN sensitivity index for the *i*-th input factor is calculated as follows:

$$KS(x_i) = \max_{y} |F_y(y) - F_{y|x_i}\left(\frac{y}{x_i}\right)|$$
(12)

where $F_y(y)$ and $F_{y|x_i}(y/x_i)$ are the unconditional and conditional CDFs of $F_{y|x_i}(y/x_i)$, respectively; *y* is the output; and stat is a statistic (e.g., maximum, median or mean) defined by the user.

Due to the large number of parameters involved in simulating water quality using EFDC, conducting a global sensitivity analysis on all parameters was computationally prohibitively expensive [58,59]. Therefore, a literature review was conducted to select parameters. To conduct the sensitivity analysis, 21 critical factors relating to phytoplankton growth and sink, as well as the carbon, nitrogen and phosphorus cycles in the aquatic environment, were chosen [60–65]. Table 1 summarizes the ranges of the determined parameters and their descriptions. The LHS sampling and analysis of the output by

the PAWN algorithm were performed by using the non-commercial 'SAFE' Toolbox in MATLAB [56].

Parameters	Units	Description	Min	Max
PMc	1/day	Maximum growth rate for cyanobacteria	1.5	2
PMd	1/day	Maximum growth rate for diatom	1.0	2
PMg	1/day	Maximum growth rate for green algae	1.5	2.5
BMRd	1/day	Basal metabolism rate for diatom	0.15	0.3
BMRg	1/day	Basal metabolism rate for green algae	0.06	0.12
PRRd	1/day	Predation rate for diatoms	0.01	0.1
PRRg	1/day	Predation rate for green algae	0.01	0.1
TMc1	°C	Lower optimal temperature for growth of cyanobacteria	20	25
TMc2	°C	Upper optimal temperature for growth of cyanobacteria	26	30
KTG1c	/	Suboptimal temperature effect coefficient for growth of cyanobacteria	0.001	0.01
KHNc	mg/L	Nitrogen half-saturation for cyanobacteria	0.1	0.35
KHPc	mg/L	Phosphorus half-saturation for cyanobacteria	0.0015	0.0025
KHPg	mg/L	Phosphorus half-saturation for phytoplankton:greens	0.002	0.004
WSd	1/day	Settling velocity for diatoms	0.3	0.5
WSrp	1/day	Settling velocity for Refractory particulate organic matter (RPOM)	0.0	0.15
CPprm1	g c/g P	Minimum algae carbon to phosphorus ratio	40	60
rNitM	1/day	Maximum nitrification rate	0.15	0.3
KHNitN	gN/m^3	NH ₄ half-saturation constant for nitrification	0.3	0.8
KHNitDO	$\mathrm{gO}^2/\mathrm{m}^3$	Oxygen half-saturation constant for nitrification	0.5	1
KHORDO	gO^2/m^3	Oxygen half-saturation constant for algal respiration	1.5	2.5
KDC	1/day	Minimum dissolution rate of dissolved organic carbon (DOC)	0.0015	0.0025

Table 1. Description of parameters for sensitivity analyses.

2.6. Statistical Analysis

In the study, Origin 2018 software was used for statistical studies, including calculating mean values, standard deviations, *t*-tests, Pearson correlation and linear/nonlinear correlations. The spatial distribution of water quality-related factors was obtained using EEMS Explorer 10.3 and ArcGIS 10.2. Linear fitting and *t*-test results with p < 0.05 are considered significant. Means are given with plus/minus standard deviations.

3. Results and Discussion

3.1. Seasonal Variation of Phosphorus Load and Algal Biomass

The field investigation revealed clear seasonal changes in external TP loading, TP concentration and total biomass in Lake Erhai. External TP loading was substantially associated with precipitation, with summer inflow accounting for 63% and 74% of the total TP load in 2016 and 2017, respectively. The TP concentration in the lake increased as the TP input increased. The highest value of TP reached 0.057 mg/L in autumn. Then, the TP concentration decreased with the settling of phytoplankton and elevated water level, and the lowest TP was 0.02 mg/L in spring.

The wet algal biomass during 2016–2017 ranged from to 0.41 to 9.97 mg/L, with an average of 2.23 mg/L (Figure 3b). The biomass in the summer (June to August) and autumn (September to November) was significantly higher than that in the spring (March to May)

and winter (December to next February). The species compositions of phytoplankton in the lake were mainly diatoms, green algae and cyanobacteria (Figure 3b). The succession of dominance taxa was diatom, green algae and cyanobacteria, representing 45%, 57% and 52% of the total biomass in the spring, summer and autumn of 2017, respectively.



Figure 3. Seasonal variation of phosphorus concentration, phosphorus inflow and main algal groups in 2016–2017: (a) the seasonal average phosphorus concentration, total phosphorus load and precipitation; (b) the variation of total biomass and composition of algal groups.

3.2. Model Results with Calibration and Validation

The hydrodynamic simulation of the lake was calibrated through the water level and surface water temperature. The average relative error of the water level simulation and water temperature is 0.3% and 7.74%, respectively, indicating that the established model can accurately reflect the water mass balance and thermodynamic process in the lake (Figures 4a,f and S5). Possible reasons for the error include incomplete data availability, fluctuating water temperature during sampling and sampling errors. Overall, the results of water elevation and temperature simulation showed that the established model performs with sufficient reliability in hydrodynamic and thermodynamic processes.

In terms of water quality and phytoplankton, the simulated concentrations of water quality variables are shown in Figure 4. The average relative errors of TN, TP, Chla and DO of all calibration sites were 12.94, 27.84, 33.72 and 13.96%, respectively. The average relative errors of TN, TP, Chla and DO of 11 validation sites in 2017 were 17.63, 31.82, 36.11 and 17.43%, respectively. Hence, the water quality model developed in this study generally reproduced the variation of water quality over the simulation period, which can be used to analyze the impact of external nutrient load reduction changes on the Lake Erhai water quality.

27.5

25.0

22.5

20.0

17.5 15.0

12.5

10.0

7.5

Jar

Jan

Feb

Temp /°C



Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec



27.5

25.0

22.5

15.0 12.5

10.0

7.5

(a)

RE% = 5.3%

Mar Apr May Jun Jul Aug Sep Oct Nov Dec

°C 20.0

Temp / 17.5

Figure 4. Calibration of water quality in Lake Erhai: (a-e) temp/DO/TN/TP/Chla in Southern lake center; (f-j) temp/DO/TN/TP/Chla in northern lake center.

3.3. The Seasonal Dynamic of Phytoplankton Biomass and Net Primary Production

Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec

In 2017, the converted algal biomass in Lake Erhai varied between 0.11 and 0.37 mg C/L, with the lowest value occurring in June and the largest value occurring in November. The simulated algal biomass of the model yielded good agreement with the observation. The presence of two peaks corresponds to the massive proliferation of diatom and green algae in spring and the bloom of cyanobacteria in the autumn to winter, respectively. According to Equation (12), the daily, monthly and seasonal net primary production was estimated. The average monthly NPP in 2017 ranged between -34.53 and 31.91 mg C/m²/d and exhibited seasonal congruence. Seasonal fluctuation in total NPP indicates that Lake Erhai is net heterotrophic in spring and net autotrophic in the other three seasons. In summer, the total NPP exceeded 200 t C, which equates to 2500 t in wet weight, approximately. In contrast, the NPP implied a more balanced situation between respiration and growth

in autumn and winter. The difference in seasonal NPP can be attributed to the dynamics of the phytoplankton community within the year. In spring, the loss of phytoplankton is primarily related to the grazing and death of diatom, and the decrease in green algae is due to the depletion of bioavailable phosphorus in the lake. In the late summer to autumn, the cyanobacteria became dominant in the lake and thrived as the suitable water temperature and sufficient phosphorus was available. Consequently, the net NPP reached the highest level. In winter, the growth of cyanobacteria was limited by temperature again. The decline in cyanobacteria was the primary cause of negative NPP.

3.4. Limiting Factors of Algal Growth in Erhai

The further analysis of limiting factors of algal growth clearly explains NPP changes within the year. In Figure 5, smaller values of the limiting factor functions indicated the more substantial control of algal growth (i.e., f = 0 means strong limit and f = 1 means no limit) (Figure 6). In Lake Erhai, nitrogen limit factors in the upper water layer (0–1 m below the surface) were more than 0.7 throughout the year, indicating that nitrogen availability does not limit algal growth. In contrast, P restricted the algal growth throughout the year, except in winter. In winter and spring, water temperature limited cyanobacterial growth (limitation function < 0.4), while diatom showed a high primary production and reached the maximum biomass; the production rate of green algae was relatively low, as the temperature also did not favor its growth. They constitute the main parts of the NPP in spring. Then, the phosphorus limitation became stronger from February to May as the settling of diatom gradually exhausted the most bioavailable PO₄ in the surface layer, and external P input was limited in the dry season. The relative growth rate of diatom and green algae decreased to negative. From June to October, when the water temperature reached the optimal growth range of cyanobacteria, it took advantage of quicker phosphorus uptake rates and the buoyancy from gas vesicles, and became dominant in the lake NPP. Finally, in late autumn and winter, the limiting factors gradually changed from P to water temperature again (Figures 6a and 7). Cao et al. [66] also concluded that the pulse of nutrient input after the rainstorm in the summer, together with high temperatures and decreased radiation, was the leading cause of the sustained growth of phytoplankton in the autumn and triggered blooms in favorable meteorological conditions. Generally, water temperature controlled algal growth in Lake Erhai in winter and early spring, while phosphorus had a major impact in summer and autumn.



Figure 5. Simulated total biomass of phytoplankton and net primary production in Lake Erhai: (**a**) the simulation of phytoplankton biomass in Lake Erhai; (**b**) phytoplankton net primary production in Lake Erhai in each month and season of 2017. The daily average NPP of every month and total seasonal net primary production (including basal metabolism, grazing and settling, in ton) is represented by a dark blue dot and column, respectively.



Figure 6. Time variation of phytoplankton communities and limitation factors of 3 algal groups in Lake Erhai; (a) Diatom; (b) Green Algae; (c) Cyanobacteria; (*T*), f(I), f(N) and f(P) represent water temperature, irradiation, nitrogen and phosphorus limitation, respectively.



Figure 7. (a) Time plot of average algal biomass concentration and TP concentration in Lake Erhai under different reduction scenarios; (b) load reduction curve for average algal biomass, average TP concentration and annual NPP.

3.5. Model Sensitivity

The first six most sensitive parameters for the biomass of total phytoplankton communities and three algal groups are listed in Table 2. The parameters were ranked according to their mean Kolmogorov-Smirnov (KS) statistics. Their values are significantly larger than the "dummy sensitivity", a threshold indicating that this input factor is indeed influential [57].

Table 2. The rankings of the first six most influential parameters for Chla concentration (ug/L) and cyanobacteria biomass (CHC), diatom biomass (CHD) and green algae biomass (CHG) derived from the PAWN indices.

Parameters	Rank of Sensitivity					
Variables	1	2	3	4	5	6
Total Biomass	KHPg	PRRg	KHPc	PMc	WSrp	PMg
KS value	0.274	0.241	0.212	0.211	0.196	0.188
Biomass (cyanobacteria)	PRRg	KHPg	KHPg	KHPc	PMc	BMRg
KS value	0.292	0.290	0.234	0.212	0.211	0.196
Biomass (diatom)	BMRd	PRRd	PMd	KHNc	KHPc	PRRg
KS value	0.342	0.236	0.230	0.200	0.193	0.192
Biomass (green)	PRRg	BMRd	KHPc	BMRg	KHNc	PMd
KS value	0.275	0.220	0.219	0.214	0.204	0.200

The total biomass was mainly determined by the utilization capacity of limited resources, precisely, the phosphorus half-saturation concentration and maximum growth rate of green algae and cyanobacteria. Surprisingly, cyanobacteria biomass was strongly influenced by the predation rate and phosphorus half-saturation concentration of green algae. In contrast, the basal metabolism rate of diatom was ranked as the second and third influential parameters on green algae. We attributed this discrepancy to the fact that phytoplankton groups competed against each other by using different strategies of nutrient, light and temperature uptake. Therefore, the results for those phytoplankton growth rate, respiration, predation, and uptake of available nutrients. Diatom, in contrast, was controlled by its rates of respiration, predation and maximum growth rate. A possible reason for this is the different ecological niches other than the two phytoplankton groups.

Moreover, our model simulated the dynamic of phytoplankton biomass and NPP; however, several uncertainties remain in the model. The first arises from a significant lack of actual monitoring data of NPP to calculate and verify our model, as only Chla concentration and biomass data could be collected from the monitoring data. We were constrained to assuming that the *GPP* data obtained from the literature represent the annual average concentration. This was still not sufficient to build an accurate model.

The second arises from the uncertainties of boundary conditions, especially the measure and estimation of the nutrient from cropland via runoff to rivers and ditches. In addition, there is incongruence between the classification of water quality variables from lab water analysis and the EFDC model. We had to estimate the proportion of refractory and liable organic components in particulate nitrogen/phosphorus using empirical conversion factors.

Furthermore, the complex and incompletely understood ecological mechanisms underlying phytoplankton community dynamics, such as growth rate, resource competition, grazing rate and the inherent plasticity of the organism C: N: P stoichiometry, may lead to bias in the predictions of the community's response to external changes as a result of the model's intrinsic structure. For example, Yu et al. [67] reported that the bloom-forming cyanobacteria in Lake Erhai include seven *Microcystis*, four *Dolichospermum* and two *Aphanizomenon* species. The coexistence of N₂-fixer and non-N₂-fixer, as well as various strategies in nitrogen and phosphorus competition, increased the uncertainties and challenges of the mechanistic model in reproducing algal dynamics and Chla concentration during the high-risk period [68]. The parameters in our analysis are consistent for the whole lake. Some optimization approaches, such as employing time- and space-varying parameters, have succeeded in improving the simulation accuracy [62,69]. These are the issues that should be addressed in our future research.

3.6. Response of NPP to the Phosphorous Load Reduction

The results of our model indicate that the water quality of Lake Erhai would not be able to attain the targeted water quality standards (maintain <0.025 mg/L (Class II) for the whole year) under current watershed TP loading. It is necessary to provide reasonable predictions required for nutrient management in the lake. Accordingly, we designed four scenarios with the phosphorus reduced by 15% to 75% to evaluate the effect on TP concentration in the lake and phytoplankton production (Table 3).

	Loading Reduction Ratio	Reduction in TP t/a
LO	/	0
L1	15% reduction in TP	22.35
L2	25% reduction in TP	37.25
L3	50% reduction in TP	74.5
L4	75% reduction and TP	111.8

 Table 3. Four reduction scenarios under the existing watershed loading conditions.

The time series plot of the four scenarios is illustrated in Figure 7. The results showed that the annual average concentrations decreased by 5, 8, 17 and 26% for algal biomass, and 3, 6, 20 and 30% for TP, respectively. Due to the fact that the majority of phosphorus input occurred during the summer, the algal biomass and TP concentration in spring were not significantly affected by load reduction, and the difference in NPP between the scenarios was negligible. In summer and autumn, the NPP steadily decreased with the increase in the load reduction ratio.

Based on the modeled results, we analyzed the relationship between the reduction and change in algal biomass, TP and NPP. As illustrated in Figure 7b, the average biomass and TP concentration are linearly related to loading reduction percentage. It can be concluded that phosphorus loading reduction directly affects the water quality of Lake Erhai, and the efficiency of improvement is proportionate to the degree of load decrease, which implied that external loads contribute most to variations in net algal growth in Lake Erhai, while other factors, such as meteorological conditions and physical transport, play a less significant role [70–72]. Based on load–response curves, it is possible to determine the required load of phosphorus in order to reach a desired level of eutrophication. Considering the relative error of our model, TP loads from influent tributaries and agriculture ditches of Lake Erhai would have to be reduced by at least 25% to enable the water quality to reach Grade II for TP.

Meanwhile, reduced phosphorus further restrained the growth of phytoplankton and led to decreased annual NPP. As predicted by our model, the yearly production/biomass ratio (e.g., kg produced per year per kg biomass) of lake Erhai will less than 1 when the inflow TP concentration is reduced by 45%. These results are helpful for the mitigation of eutrophication. Recent investigations indicated that Lake Erhai had undergone a transition from the mesotrophic to the preliminary stages of the eutrophic state [73], implying that its current environmental carrying capacity is quite limited. There will be great challenges associated with remediating the aquatic environment through intensive restoration activities if the transition of ecological status and new ecological stability are reached [74–76] Therefore, controlling the lake's NPP is critical for the protection of Lake Erhai.

4. Conclusions

1. A 3D hydrodynamic and water quality model was developed for Lake Erhai, China. In the field investigation, the water surface elevation, temperature, nutrients and algal biomass concentration in the lake were accurately simulated by the numerical model, revealing a reasonable picture of the lake's hydrodynamics and eutrophication process. The model is suitable to calculate the seasonal NPP in the lake.

- 2. According to the modeling results, the average daily NPP ranged from -3.45 and $3.19 \text{ mg C/m}^2/d$. The seasonal fluctuation in total NPP indicates that Lake Erhai is net heterotrophic in spring and net autotrophic in summer, autumn, and winter. The difference in seasonal NPP can be attributed to the combined impact of phosphorus supply and temperature limitation of the phytoplankton community within the year.
- 3. The results of loading reduction scenarios indicate that phosphorus loading reduction directly affects the water quality of Lake Erhai, and the efficiency of improvement in TP concentration and NPP is proportionate to the degree of load decrease.

Supplementary Materials: The following supporting information can be downloaded at: https: //www.mdpi.com/article/10.3390/w14050835/s1, Figure S1: Trends of Gross domestic product (GDP) in Lake Erhai watershed, total nitrogen (TN)/total phosphorous (TP) concentration and average Secchi depth in Lake Erhai. (1997–2019); Figure S2: location of water quality monitoring sites in Lake Erhai and sampled agricultural ditches around the lake; Figure S3: External loading of TP and NH₄-N to Lake Erhai during the study period; Figure S4: Schematic diagram of EFDC water quality model; Figure S5: simulated and observed water elevation of Lake Erhai; Table S1: Variables used in EFDC model. References [77,78] are cited in the Supplementary Materials.

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Appendix A

Model parameters.

Table A1. The model parameters of Lake Erhai EFDC model and calibrated values.

Parameters	Unit	Description	Calibrated Value	Range
Pc	1/day	Maximum growth Rate for Cyanobacteria	1.35	0.2–9.0
Pd	1/day	Maximum growth Rate for Diatoms	0.95	0.2-9.0
Pg	1/day	Maximum growth Rate for Greens	1.7	0.2-9.0
BMc	1/day	Basal Metabolism Rate for Cyanobacteria	0.013	0.01–0.92
BMd	1/day	Basal Metabolism Rate for Diatoms	0.15	0.01-0.92
BMg	1/day	Basal Metabolism Rate for Greens	0.13	0.01-0.92
PRc	1/day	Predation Rate on Cyanobacteria	0.01	0.01-0.06
PRd	1/day	Predation Rate on Diatoms	0.155	0.03-0.3
PRg	1/day	Predation Rate on Greens	0.14	0.03-0.3
Keb	1/m	Background Light Extinction Coefficient	0.38	0.25-0.45

 Table A1. Cont.

Parameters	Unit	Description	Calibrated Value	Range
Sc	m/day	Settling velocity for Cyanobacteria	0.02	0.01-0.3
Sd	m/day	Settling velocity for Diatoms	0.12	0.01-0.3
Sg	m/day	Settling velocity for Greens	0.1	0.01-0.3
SRP	m/day	Settling velocity for refractory particulate organic matter (RPOM)	0.05	0.02–9.0
SLP	m/day	Settling velocity for liable particulate organic matter (LPOM)	0.01	0.02–9.0
CChlc	mg C/ug Chl	C:chlorophyll ratio for Cyanobacteria	0.02	0.01-0.05
CChld	mg C/ug Chl	C:chlorophyll ratio for Algae:Diatoms	0.033	0.01-0.05
CChlg	mg C/ug Chl	C:chlorophyll ratio for Algae:Greens	0.033	0.01-0.05
CPprm1		Constant1 used in Determining Algae C:P Ratio (gC/gP)	45	30-65
Keb	1/m	Background Light Extinction Coefficient	0.38	0.15-0.45
KHNc	mg/L	Nitrogen Half-Saturation for Cyanobacteria	0.045	0.01-0.25
KHNd	mg/L	Nitrogen Half-Saturation for Algae:Diatoms	0.05	0.01-0.25
KHNg	mg/L	Nitrogen Half-Saturation for Algae:Greens	0.1	0.01-0.25
KHPc	mg/L	Phosphorus Half-Saturation for Cyanobacteria	0.0033	0.001-0.05
KHPd	mg/L	Phosphorus Half-Saturation for Algae:Diatoms	0.0043	0.001-0.05
KHPg	mg/L	Phosphorus Half-Saturation for Algae:Greens	0.0035	0.001-0.05
TMc1	°C	Lower Optimal Temperature for Growth, Cyanobacteria	23	20–25
TMc2	°C	Upper Optimal Temperature for Growth, Cyanobacteria	30	25–30
TMd1	°C	Lower Optimal Temperature for Growth, Diatoms	10	10–15
TMd2	°C	Upper Optimal Temperature for Growth, Diatoms	22	10–15
TMg1	°C	Lower Optimal Temperature for Growth, Greens	20	22–25
TMg2	°C	Upper Optimal Temperature for Growth, Greens	25	22–26
TMp1	°C	Lower Optimal Temperature for Predation, Diatoms	15	15–25
TMp2	°C	Upper Optimal Temperature for Predation, Diatoms	20	15–26
KTG1c		Suboptimal Temperature Effect Coeff for Growth, Cyanobacteria	0.2	0.001-0.01
KTG2c		Superoptimal Temperature Effect Coeff for Growth, Cyanobacteria	0.03	0.001–0.01
KTG1d		Suboptimal Temperature Effect Coeff for Growth, Diatoms	0.069	
KTG2d		Superoptimal Temperature Effect Coeff for Growth, Diatoms	0.1	
KTG1g		Suboptimal Temperature Effect Coeff for Growth, Greens	0.1	
KTG2g		Superoptimal Temperature Effect Coeff for Growth, Greens	0.01	

Table A1. Cont.	
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Parameters	Unit	Description	Calibrated Value	Range
FNRc		Fraction of Metabolized Nitrogen Produced as RPON, Cyanobacteria	0.15	
FNRd		Fraction of Metabolized Nitrogen Produced as RPON, Diatoms	0.15	
FNRg		Fraction of Metabolized Nitrogen	0.15	
Ū.		Fraction of Metabolized Nitrogen		
FNLc		Produced as LPON Cyanobacteria	0.25	
		Fraction of Metabolized Nitrogen		
FNLd		Produced as LPON, Diatoms	0.25	
FNLg		Fraction of Metabolized Nitrogen Produced as LPON, Greens	0.25	
FNDc		Fraction of Metabolized Nitrogen	0.5	
FINDC		Produced as DON, Cyanobacteria	0.5	
FNDd		Fraction of Metabolized Nitrogen	0.5	
11124		Produced as DON, Diatoms	0.0	
FNDg		Fraction of Metabolized Nitrogen	0.5	
0		Produced as DON, Greens		
FNIc		Produced as DIN Cyanobacteria	0.1	
		Fraction of Metabolized Nitrogen		
FNId		Produced as DIN, Diatoms	0.1	
17 N 1 I		Fraction of Metabolized Nitrogen	0.1	
FINIg		Produced as DIN, Greens	0.1	
FPR		Fraction of Metabolized Phosphorus	0	
I'I KC		Produced as RPOP, Cyanobacteria	0	
FPRd		Fraction of Metabolized Phosphorus	0	
		Produced as RPOP, Diatoms		
FPRg		Produced as PPOP Croops	0	
		Fraction of Metabolized Phosphorus		
FPLc		Produced as LPOP. Cvanobacteria	0	
		Fraction of Metabolized Phosphorus	0	
FPLd		Produced as LPOP, Diatoms	0	
FPLo		Fraction of Metabolized Phosphorus	0	
1125		Produced as LPOP, Greens	0	
FPDc		Fraction of Metabolized Phosphorus	0.95	
		Produced as DOP, Cyanobacteria		
FPDd		Produced as DOP Diatoms	0.9	
		Fraction of Metabolized Phosphorus		
FPDg		Produced as DOP, Greens	0.9	
EDI-		Fraction of Metabolized Phosphorus	0.05	
FFIC		Produced as P4T, Cyanobacteria	0.05	
FPId		Fraction of Metabolized Phosphorus	0.1	
1110		Produced as P4T, Diatoms	0.1	
FPIg		Fraction of Metabolized Phosphorus	0.1	
VDD	1/day	Produced as P41, Greens	0.005	0.001 0.01
KKP KI P	1/day	Minimum Hydrolysis Rate of LPOP	0.005	0.001 = 0.01
KLI	1/day	Minimum Mineralization Rate of	0.005	0.01-0.1
KDP	1/day	DOP	0.008	0.01–0.3
KRPALG	m ³ (gc)/d	Constant relating Hydrolysis Rate of RPOP to Algae:	0.005	
KLPALG	m ³ (gc)/d	Constant relating Hydrolysis Rate of LPOP to Algae:	0.01	
KDPALG	m ³ (gc)/d	Constant relating Mineralization Rate of DOP to Algae:	0.01	

Parameters	Unit	Description	Calibrated Value	Range
KRN	1/day	Minimum Hydrolysis Rate of RPON	0.005	0.001-0.01
KLN	1/day	Minimum Hydrolysis Rate of LPON	0.0075	0.01 - 0.1
KDN	1/day	Minimum Mineralization Rate of DON	0.01	0.01-0.08
KRNALG	$m^3(gc)^{-1}d^{-1}$	Constant relating Hydrolysis Rate of RPON to Algae	0.005	0.0001- 0.01
KLNALG	$m^3(gc)^{-1}d^{-1}$	Constant relating Hydrolysis Rate of LPON to Algae	0.005	0.0001- 0.02
KDNALG	$m^3(gc)^{-1}d^{-1}$	Constant relating Mineralization Rate of DON to Algae	0.01	0.001-0.01
KHORDO	gO_2/m^3	oxygen Half-Sat Constant for Algal Respiration	1	0.5–2
KHDNN	gN/m ³	half-sat. constant for denitrification	0.001	0.05-0.2
KHCOD	mg/LO_2	oxygen half-saturation constant for COD decay	0.7667	1–1.5

Table A1. Cont.

The literature range of the parameters are obtained from references [58,63,64,79–83].

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