## Supplementary Materials: Influence of pH, Temperature and Sample Size on Natural and Enforced Syneresis of Precipitated Silica

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**Figure S1.** Solubility  $\tilde{c}^*_{Si(OH)_4}$  of monomeric silicic acid as a function of pH, calculated according to Schlomach [1].



**Figure S2.** Solubility  $\tilde{C}^*_{Si(OH)_4}$  of monomeric silicic acid as a function of temperature, calculated according to Schlomach [1].



**Figure S3.** Relative shrinkage  $\Delta V/V_0$  of enforced syneresis for  $s_0 = 16$  mm and  $\vartheta = 40$  °C, acid-catalyzed (**a**) and base-catalyzed (**b**).



**Figure S4.** Relative shrinkage  $\Delta V/V_0$  of enforced syneresis for  $s_0 = 16$  mm and  $\vartheta = 60$  °C, acid-catalyzed (**a**) and base-catalyzed (**b**).



**Figure S5.** Relative shrinkage  $\Delta V/V_0$  of enforced syneresis for  $s_0 = 12$  mm and  $\vartheta = 40$  °C, acid-catalyzed (**a**) and base-catalyzed (**b**).



**Figure S6.** Relative shrinkage  $\Delta V/V_0$  of enforced syneresis for  $s_0 = 12$  mm and  $\vartheta = 60$  °C, acid-catalyzed (a) and base-catalyzed (b).

Pressure	Maximum shrinkage $\Delta V/V_0 _{max}/-$		Time constant τ/h		
difference	Acid-catalyzed	<b>Base-catalyzed</b>	Acid-catalyzed	<b>Base-catalyzed</b>	
$\Delta p/bar$	pH < pH <sub>iso</sub>	$pH > pH_{iso}$	$pH < pH_{iso}$	$pH > pH_{iso}$	
0.27-0.33	0.44	0.82	10.6	10.5	
0.60-0.67	0.52	0.82	3.7	2.6	
1.37-1.41	0.63	0.85	2.1	1.5	
2.16-2.25	0.66	0.87	1.3	1.1	
3.65-3.75	0.71	0.88	0.9	0.9	
6.19–6.30	0.77	0.91	0.7	0.8	
7.51-7.60	0.78	0.92	0.6	0.7	

**Table S1.** Maximum shrinkage  $\Delta V/V_0|_{\text{max}}$  and characteristic time constant  $\tau$ , enforced syneresis,  $s_0 = 16 \text{ mm}$  and  $\vartheta = 40 \text{ °C}$ .

**Table S2.** Maximum shrinkage  $\Delta V/V_0|_{\text{max}}$  and characteristic time constant  $\tau$ , enforced syneresis,  $s_0 = 16 \text{ mm}$  and  $\vartheta = 60 \text{ °C}$ .

Pressure	Maximum shrinkage $\Delta V/V_0 _{max}/-$		Time constant τ/h		
difference	Acid-catalyzed	<b>Base-catalyzed</b>	Acid-catalyzed	Base-catalyzed	
$\Delta p/bar$	pH < pH <sub>iso</sub>	pH > pH <sub>iso</sub>	pH < pH <sub>iso</sub>	pH > pH <sub>iso</sub>	
0.31-0.43	0.39	0.81	3.5	4.8	
0.60-0.80	0.52	0.84	2.1	1.9	
1.22-1.51	0.61	0.86	1.7	1.1	
2.24-2.28	0.67	0.88	1.2	0.9	
3.66-3.82	0.73	0.89	0.8	0.7	
6.15-6.24	0.75	0.90	0.5	0.6	
7.67–7.69	0.76	0.91	0.3	0.6	

**Table S3.** Maximum shrinkage  $\Delta V/V_0|_{\text{max}}$  and characteristic time constant  $\tau$ , enforced syneresis,  $s_0 = 12 \text{ mm}$  and  $\vartheta = 20 \text{ °C}$ .

Pressure	Maximum shrinkage $\Delta V/V_0 _{max}/-$		Time constant τ/h		
difference	Acid-catalyzed	Base-catalyzed	Acid-catalyzed	Base-catalyzed	
$\Delta p$ /bar	$pH < pH_{iso}$	$pH > pH_{iso}$	$pH < pH_{iso}$	$pH > pH_{iso}$	
0.14-0.26	0.40	0.71	10.4	3.8	
0.55 - 0.74	0.53	0.75	6.2	2.2	
1.36-1.40	0.63	0.80	2.9	1.3	
2.19-2.21	0.68	0.82	1.5	1.1	
3.75-3.81	0.74	0.84	1.1	0.8	
5.93-6.12	0.77	0.85	1.0	0.6	
7.09-7.20	0.79	0.86	0.8	0.5	

**Table S4.** Maximum shrinkage  $\Delta V/V_0|_{\text{max}}$  and characteristic time constant  $\tau$ , enforced syneresis,  $s_0 = 12 \text{ mm}$  and  $\vartheta = 40 \text{ °C}$ .

Pressure	Maximum shrinkage $\Delta V/V_0 _{max}$		Time constant τ/h		
difference	Acid-catalyzed	Base-catalyzed	Acid-catalyzed	Base-catalyzed	
$\Delta p/bar$	$pH < pH_{iso}$	$pH > pH_{iso}$	$pH < pH_{iso}$	$pH > pH_{iso}$	
0.26-0.31	0.42	0.71	7.0	3.6	
0.73-0.78	0.51	0.78	3.1	1.7	
1.45-1.63	0.63	0.83	1.6	1.1	
2.28-2.28	0.67	0.85	0.9	0.9	
3.51-3.88	0.73	0.86	1.0	0.7	
6.04-6.51	0.77	0.89	0.7	0.7	
6.87–7.66	0.78	0.89	0.5	0.5	

Pressure	Maximum shrin	kage $\Delta V/V_0 _{max}/-$	Time constant τ/h		
difference	Acid-catalyzed	<b>Base-catalyzed</b>	Acid-catalyzed	Base-catalyzed	
$\Delta p/bar$	$pH < pH_{iso}$	$pH > pH_{iso}$	$pH < pH_{iso}$	$pH > pH_{iso}$	
0.33-0.42	0.35	0.78	5.8	3.4	
0.73-0.80	0.51	0.85	1.8	1.2	
1.42-1.43	0.50	0.84	1.2	0.7	
2.20-2.25	0.60	0.86	0.8	0.6	
3.41-3.56	0.61	0.87	0.5	0.4	
5.54-6.14	0.70	0.89	0.4	0.4	
7.04-7.55	0.74	0.90	0.2	0.3	

**Table S5.** Maximum shrinkage  $\Delta V/V_0|_{\text{max}}$  and characteristic time constant  $\tau$ , enforced syneresis,  $s_0 = 12 \text{ mm}$  and  $\vartheta = 60 \text{ }^{\circ}\text{C}$ .

**Table S6.** Fitting parameters *A*–*F* of Equations (4) and (5) for the acid-catalyzed gel.

Temperature ∂/°C	A/-	B/bar	C/bar	D/h	E/h·bar	F/bar
20	0.808	-0.322	0.634	0.642	3.026	0.161
40	0.786	-0.277	0.460	-0.057	3.014	0.175
60	0.749	-0.411	0.749	-0.141	2.127	0.101

Table S7. Fitting parameters *A*–*F* of Equations (4) and (5) for the base-catalyzed gel.

Temperature ∂/°C	A/-	B/bar	C/bar	D/h	E/h·bar	F/bar
20	0.867	-0.113	0.399	0.469	1.225	0.094
40	0.902	-0.121	0.311	0.445	0.981	0.026
60	0.911	-0.145	0.939	-0.024	1.432	0.108



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