

Article

Utilization of Bracing Arms as Additional Reinforcement in Pultruded Glass Fiber-Reinforced Polymer Composite Cross-Arms: Creep Experimental and Numerical Analyses

Muhammad Rizal Muhammad Asyraf ^{1,*} , Mohamad Ridzwan Ishak ^{1,2,3,*}, Salit Mohd Sapuan ^{3,4} and Noorfaizal Yidris ¹ 

¹ Department of Aerospace Engineering, Universiti Putra Malaysia, Serdang 43400, Selangor, Malaysia; nyidris@upm.edu.my

² Aerospace Malaysia Research Centre (AMRC), Universiti Putra Malaysia, Serdang 43400, Selangor, Malaysia

³ Laboratory of Biocomposite Technology, Institute of Tropical Forestry and Forest Products (INTROP), Universiti Putra Malaysia, Serdang 43400, Selangor, Malaysia; sapuan@upm.edu.my

⁴ Advanced Engineering Materials and Composites Research Centre (AEMC), Department of Mechanical and Manufacturing Engineering, Universiti Putra Malaysia, Serdang 43400, Selangor, Malaysia

* Correspondence: asyrafz96@gmail.com (M.R.M.A.); mohdrizwan@upm.edu.my (M.R.I.)

Abstract: The application of pultruded glass fiber-reinforced polymer composites (PGFRPCs) as a replacement for conventional wooden cross-arms in transmission towers is relatively new. Although numerous studies have conducted creep tests on coupon-scale PGFRPC cross-arms, none had performed creep analyses on full-scale PGFRPC cross-arms under actual working load conditions. Thus, this work proposed to study the influence of an additional bracing system on the creep responses of PGFRPC cross-arms in a 132 kV transmission tower. The creep behaviors and responses of the main members in current and braced PGFRPC cross-arm designs were compared and evaluated in a transmission tower under actual working conditions. These PGFRPC cross-arms were subjected to actual working loads mimicking the actual weight of electrical cables and insulators for a duration of 1000 h. The cross-arms were installed on a custom test rig in an open area to simulate the actual environment of tropical climate conditions. Further creep analysis was performed by using Findley and Burger models on the basis of experimental data to link instantaneous and extended (transient and viscoelastic) creep strains. The addition of braced arms to the structure reduced the total strain of a cross-arm's main member beams and improved elastic and viscous moduli. The addition of bracing arms improved the structural integrity and stiffness of the cross-arm structure. The findings of this study suggested that the use of a bracing system in cross-arm structures could prolong the structures' service life and subsequently reduce maintenance effort and cost for long-term applications in transmission towers.

Keywords: pultruded gfrp; cross-arm; bracing system; creep; Findley's power law model; Burger model



Citation: Asyraf, M.R.M.; Ishak, M.R.; Sapuan, S.M.; Yidris, N. Utilization of Bracing Arms as Additional Reinforcement in Pultruded Glass Fiber-Reinforced Polymer Composite Cross-Arms: Creep Experimental and Numerical Analyses. *Polymers* **2021**, *13*, 620. <https://doi.org/10.3390/polym13040620>

Received: 12 November 2020

Accepted: 3 December 2020

Published: 19 February 2021

Publisher's Note: MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<https://creativecommons.org/licenses/by/4.0/>).

1. Introduction

In electrical power grid systems, transmission towers are implemented to grasp and hold conductor cables from power generators to substations in continuous line connections. Transmission towers are divided and grouped into two major types, namely, latticed steel towers and monopole steel tubes. Latticed steel towers have been installed throughout Peninsular Malaysia since 1929 [1]. This type of transmission tower has remained in service for the transmission of electrical power to housing and industrial areas. Latticed steel transmission towers are composed of a peak, cross-arm, tower body, boom and cage. Cross-arms are installed and used to secure utility wires with their insulators, which hold lines directly, to maintain power cables above ground [2,3].

Wooden cross-arms made from Chengal wood (*Neobalanocarpus hemii*) were previously applied because they provided superior mechanical performance and arc quenching during

lightning strikes [4]. However, due to the appearance of natural wood defects [5–8] after long service times and the limited sources of Chengal timber [9], pultruded glass fiber-reinforced polymer composites (PGFRPCs) have been proposed as replacements for wood cross-arms. A kick-starter pilot project on GFRP composites in a 132 kV transmission tower in the Tanjung Batu line in Pekan Town has been initiated [10]. Fiber-reinforced polymer composites are commonly applied in automotive components [11,12], fire extinguishers [13] and household products [14,15]. These materials have been widely used in many sectors due to their good mechanical strength and stiffness [16,17].

Several research works involving computational simulation to evaluate the mechanical performance of PGFRPC cross-arm assemblies have been performed to obtain technical data on the effect of material properties on structural integrity. The computational simulation analysis of PGFRPC cross-arms has been applied to investigate the influence of static load and sleeve installation [18]; the effect of the stacking sequence of a laminate [19] on cross-arm assemblies; the effect of laminate properties on the failure of cross-arm structures under multiaxial load [20] and the influence of material configuration on the static deformation of composite cross-arms [21]. Long-term mechanical tests on the development of creep test rigs for cross-arms have also been conducted [22–24]. Despite the numerous studies involving the numerical simulations and development of test rigs, studies on the creep properties of PGFRPC cross-arms remain lacking.

Creep is a mechanical phenomenon that induces a pattern of deformation in any material under long-term constant stress. These deformations initiate from instantaneous deformation and are succeeded by primary (transient), secondary (steady-state) and tertiary (accelerated) and end in structural failure. In the primary creep stage, the creep rate decreases at function of time due to strain hardening or mobile dislocations. For the secondary creep stage, the creep rate remains almost constant as a state of balance is achieved between the rate of dislocation generation and the rate of recovery. Tertiary creep stage is followed as the creep rate increases rapidly until the material ruptures after undergoing a total of strain within a time. Over the long term, creep causes shear yielding, void formation and growth, chain slippage and fiber breakage. These phenomena subsequently allow the material to become fractured [25–27]. The current composite cross-arm is considered as an anisotropic material because it is fabricated from E-glass fiber-reinforced unsaturated polyester composite via pultrusion [28–30]. In some cases, this composite material experiences the instability of fiber interfacial strength, which disturbs the mechanical strength of the material structure because creep rupture is induced [27].

Composite cross-arms must be subjected to creep experiments to formalize, analyze and predict creep behaviors during long-time service systematically. In order to ensure better long-term durability of PGFRPC cross-arms, bracing systems are introduced in this research to compare and evaluate the long-term mechanical performance of the current design used in 132 kV transmission towers. Important data can be collected and assessed by using a full-sized cross-arm in the creep test under actual load conditions in an external tropical environment. This approach will contribute to the comprehension and forecasting of the long-term mechanical durability of existing cross-arm structures incorporated with bracing arms. Furthermore, it will provide a highly holistic and intuitive perspective for evaluating the behavior of whole structures.

PGFRPCs have only been recently applied in the cross-arm structures of latticed transmission towers to replace conventional wooden cross-arms. A literature survey revealed that no previous works have evaluated the creep behaviors of full-scale PGFRPC cross-arms in 132 kV transmission towers. This research aimed to analyze the influence of the bracing system on the creep behaviors and responses of PGFRPC cross-arms in transmission towers under actual loading conditions. Moreover, this work aimed to establish the baseline creep properties of full-scale PGFRPC cross-arms. Thus, the outcomes of this study are projected to provide a practical perspective to researchers and engineers for understanding the long-term mechanical behavior of PGFRPC cross-arms.

2. Methodology

The methodology of this research is divided into two stages: experimental works and numerical analyses. Further detail methods and steps of the research are discussed in the subsequent subsections. In general, Figure 1 shows the flow chart of the overall research methodology.

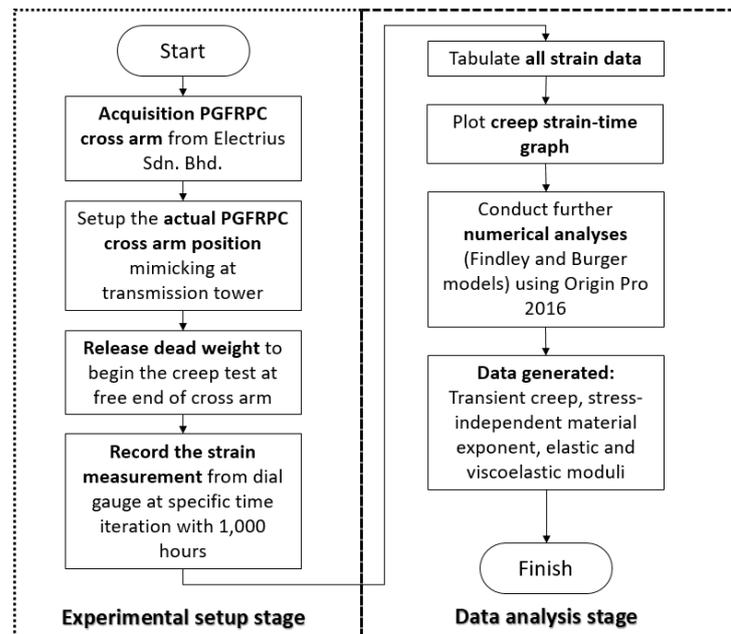


Figure 1. Flow chart of the research methodology.

2.1. Materials

The PGFRPC cross-arm was applied as the test subject in the preparation stage of the creep test. This cross-arm comprised one tie and two main members. The PGFRPC cross-arm for the 132 kV suspension tower was obtained from a local cross-arm manufacturer, Electrius Sdn Bhd, in Klang, Selangor, Malaysia. The PGFRPC cross-arm assembly members were fabricated via pultrusion by using unsaturated polyester resin as the matrix and E-glass as the reinforcement fiber. The physical size and dimensions of the cross-arm were determined in accordance with the actual standard of the Tenaga Nasional Berhad. Each member cross-arm was shaped in the form of a square hollow section ($102 \times 102 \text{ mm}^2$) with a thickness of 7.8 mm. The total length of the cross-arm's main member was 3651 mm and that of the tie member was 3472 mm. Each cross-arm member was assembled with bolts and nuts with their fastening brackets. After the assembly of the cross members, a whole set of cross-arm units were fitted inside the creep test rig with a constant load of 647 kg of bricks on the end side.

This study focused on the effect of the bracing system in a cross-arm assembly on creep properties. Thus, five additional beams were incorporated and connected to the main cross-arm structure. The bracing arms were fabricated with the dimensions of $50 \times 50 \text{ mm}^2$ from Balau timber wood. The cross-arm structure included two long members (connecting the middle of the tie member to the end of the main member) and three short members (joined at the middle to the middle of every member). The lengths of the long (tie–main), short (tie–main) and short (main–main) bracing members were 186, 50 and 40 cm, respectively. Figure 2 depicts (a) the existing cross-arm design and (b) the enhanced cross-arm design incorporating bracing arms.

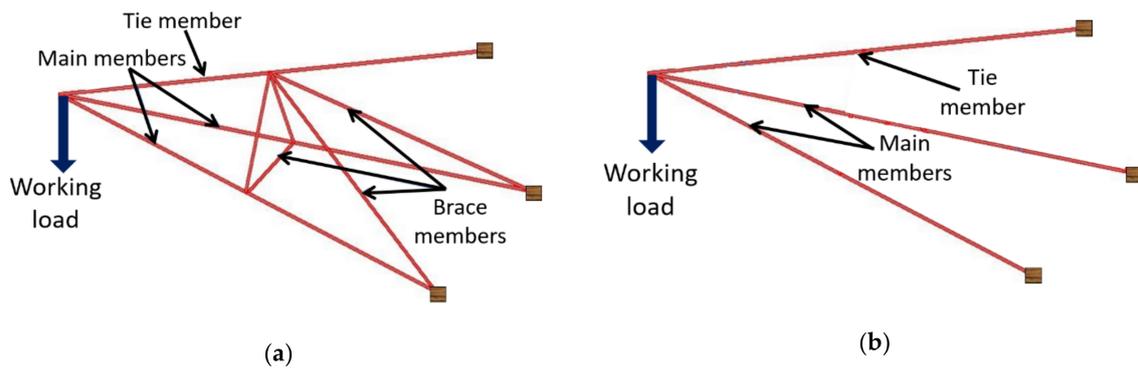


Figure 2. Cross-arm configurations: (a) with additional bracing arms—braced design; and (b) without bracing arms—current design.

2.2. Methods

A cantilever beam setup test condition implementing two-point bending application was executed to assess the creep properties of PGFRPC cross-arms. Dial gauges were positioned at five points of each main member of the cross-arm. As shown in Figure 3, the dial gauges were located at 0.61 m intervals between each point on the main members. The actual operational working load (mimicking the electric cables and its insulators loadings) of 6.347 kN was applied at the free end of the cross-arm to simulate the actual cross-arm loading condition in the transmission tower.

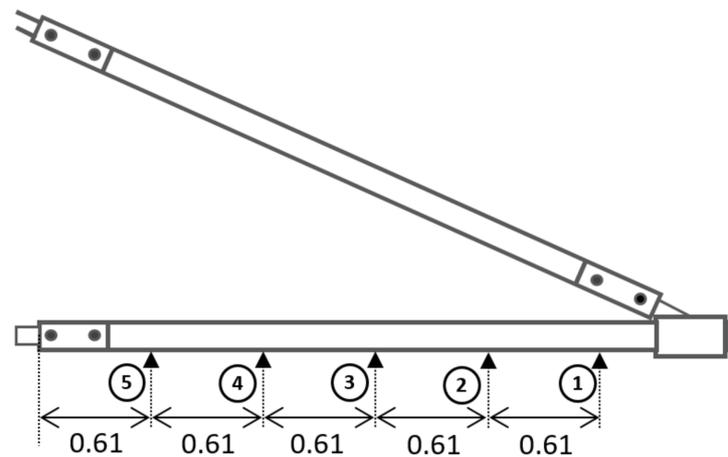


Figure 3. Positions of dial gauges under the cross-arm to measure creep strain pattern, in meters.

The creep test was performed in accordance with ASTM D2990 with 1000 h of test operation. The dial gauge readings for deformation were taken at 0, 0.1, 0.2, 0.5, 1, 2, 5, 20, 50, 100, 200, 500, 700, and 1000 h intervals. The initial strain was evaluated at 15 s after the working stress was loaded and considered as an instantaneous strain. The environmental condition was maintained and was influenced by actual tropical weather because the test was conducted outdoors (Aircraft Hangar, Faculty of Engineering, Universiti Putra Malaysia). At the end of the experiment, existing (without bracing members) and improved (with bracing members) cross-arm designs were subjected to creep strain and modulus comparison and creep numerical analysis. Figure 4 displays the (a) schematic and (b) actual positions of the PGFRPC cross-arms in the creep test rig.

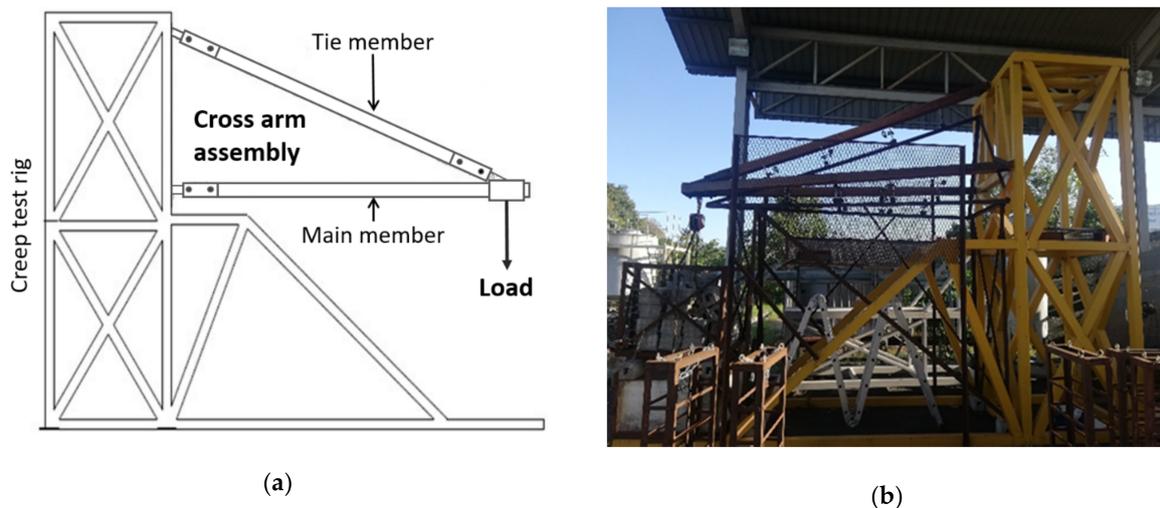


Figure 4. (a) Schematic diagram and (b) actual image of PGFRPC cross-arm used in the creep test rig.

2.2.1. Creep Properties of Cross-Arms

In this research, the cross-arm was assumed as a cantilever beam structure because it is horizontally extended from one end. Thus, cantilever beam equations and derivations were used to evaluate the cross-arm's long-term mechanical properties. The cross-arm structure was exposed to constant tension and compression reactions on its upper and bottom sides during the application of a downward constant load. This condition created a series of strain patterns corresponding to the location of load implemented at the free end of the beam. Given that the displacement movement was maintained at a certain position for a period of time, the beam exhibited a stress response pattern across its length. In this pattern, stress gradually decreased from the fixed point to the free ends. This behavior showed that the viscoelastic beam responded to the material's viscous characteristic; this response reduced the total stress [31,32].

Deflection could be assumed to occur in the cross-arm because the upper part of beam was in tension mode, whereas the bottom part is in compressive mode. Specifically, the cross-arm was exposed to non-uniform stress distribution in accordance with the beam's length and thickness. Given that the cross-arm comprised PGFRPC material, the profile of the material could be assumed to display uniform density across its length.

As shown in Figure 5, the static elastic modulus (E_e) of the cross-arm's beam can be generated based on Equation (1):

$$E_e = \frac{4PL^3}{yb^3} \quad (1)$$

where y is the deflection at the beam (m); E_e is the static elastic modulus (N/m^2); P is the force exerted on the beam (N); L is the total length (m) and b and h are the width and thickness of the beam (m), respectively.

Given that the y deflection is already known, the maximum bending stress can be predicted by using Equation (1) [33]. In general, the maximum stress experienced by the cross-arm is usually located at fixed point $x = 0$, whereas the minimum stress is exhibited at the loading end $x = L$. The maximum and minimum stresses of the beam can be formulated on the basis of Equation (2).

$$\sigma = \frac{P(L-x)\frac{h}{2}}{I} = \frac{6P(L-x)}{bh^3} \quad (2)$$

Equation (3), which is based on the equation of Hooke's law, can be used to calculate the creep strain at a specific time and location across the beam.

$$\epsilon_t = \frac{\sigma_n}{E_e} \tag{3}$$

where ϵ_t is the creep strain at a specific time and location point across the beam, σ_n is specific stress and E_e is the static elastic modulus at the specific point on the cross-arm.

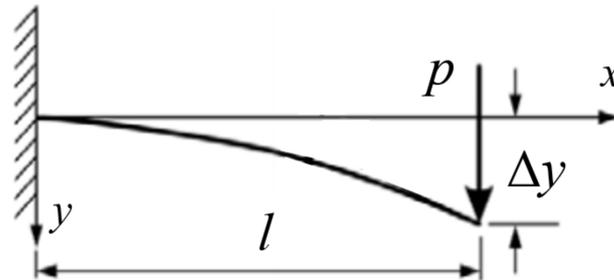


Figure 5. Schematic diagram of cross-arm’s beam when exposed applied force at the end of the cross-arm structure.

2.2.2. Constitutive Creep Models

The evaluation of creep trends and properties can be further extended by using established creep models, such as empirical and physical models.

In the empirical model, the nonlinear Findley power law model is used to justify and clarify transient creep in accordance with stress factor and material constants. Moreover, the Findley model can remove any exaggerated data deviation because the empirical model is simple and straightforward [34,35]. However, model applications are limited due to the direct and straightforward numerical calculation that is implemented universally to any system [26]. In this situation, the Findley model is considered to simulate the creep pattern of the PGFRPC cross-arm because the cross-arm is an anisotropic material [27]. The model is presented as Equation (4) [35].

$$\epsilon_t = At^n + \epsilon_0 \tag{4}$$

In Equation (4), A and n are the transient creep strain and time exponents, respectively, and ϵ_0 is the instantaneous strain after load exertion.

The Burger model is a physical model that is usually applied to describe and visualize the creep pattern with a spring and dashpot diagram to examine the viscoelasticity of creep. Perez et al. [36] and Chandra and Sobral [37] stated that creep strain is composed of three major strain components, including instantaneous strain (Maxwell spring); viscoelastic strain (Kelvin’s dashpot element) and viscous strain (Kevin–Voight element). Typically, the stress response on a viscoelastic material at the tip of displacement causes the strain to occur instantaneously. Figure 6 shows the Burger model, which includes three major elements.

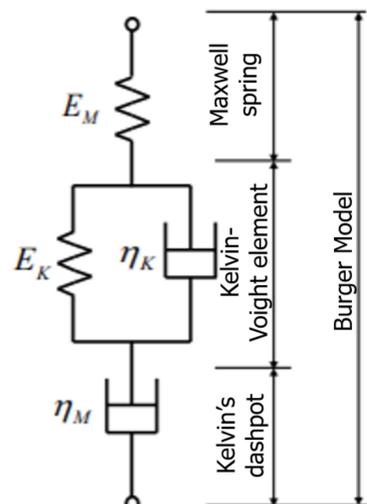


Figure 6. Schematic diagram of physical Burger model.

The presented model is presented as Equation (5).

$$\varepsilon_t = \varepsilon_e + \varepsilon_d + \varepsilon_v \quad (5)$$

The mathematical formulation in Equation (5) comprises ε_e , ε_d and ε_v , which are called the elastic strain, viscoelastic strain and viscous strain, respectively.

Equation (6) was derived on the basis of Equation (5) and the physical elements of Burger models, such as spring and dashpot elements.

$$\varepsilon_t = \frac{\sigma}{E_e} + \frac{\sigma}{E_d} [1 - \exp(-t/\tau)] + \frac{\sigma}{\eta_v} t; \quad \tau = \frac{E_d}{\eta_d} \quad (6)$$

where ε_t is the creep strain at a specific time; σ is the applied stress; E_e and E_d are the elastic moduli of the springs and η_d and η_v are the viscosities of the dashpots in this model. Meanwhile, t is the time, and τ is the retardation time for the Kelvin element to produce 63.21% (or $1-1/e$) of its total deformation [38].

The E_e , E_d , η_d and η_v parameters can be obtained by fitting experimental data with Equation (8) and used to characterize the creep behaviors of composite structures. The mathematical formulas show that the first term is a constant and is independent of time, whereas the second term elaborates on the early stage of creep but reaches a maximum quickly. The last term governs the long-term creep trend at a constant creep rate. Figure 7 displays the typical creep and relaxation of the Burger model for the polymeric composite.

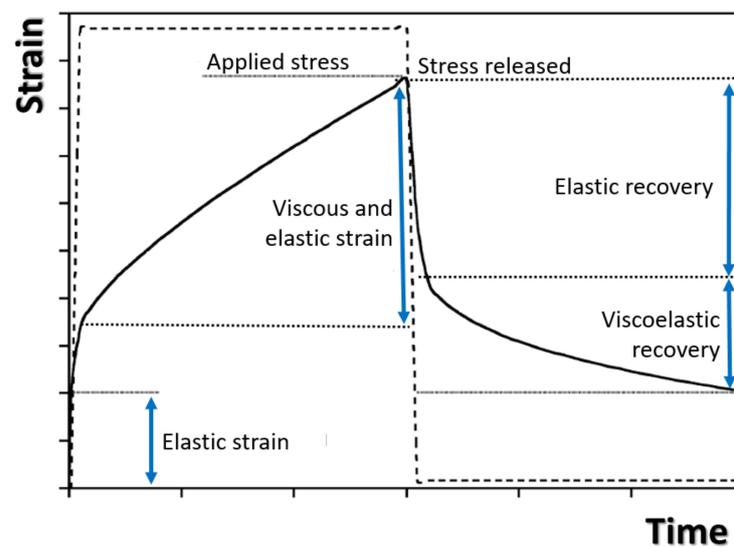


Figure 7. Typical creep and Relaxation Burger Model [39].

The specific behaviors, such as elastic, viscoelastic and viscous moduli, of the creep properties of the PGFRPC cross-arm can be determined on the basis of the Burger model. In this work, this model was suitable because the creep period was valid only for primary and secondary creep. These outcomes were meaningful for predicting the improvement of long-term mechanical properties through the inclusion of a bracing system in composite structures.

3. Results and Discussion

3.1. Strain-Time Curve

Figure 8 displays the comparison of the creep strain-time curves at five points on the current and braced composite cross-arm designs under actual working loads. Each point of the strain gauge exhibited various values of creep strain patterns in accordance with the effect of tension and compression along the main member beams during loading action [31]. The elastic strain values varied along the position of the main member beams as the stress along the beam was increased from the loading end to the fixed point [40].

This finding demonstrated that the highest value of creep strain was localized at y3, which was the center of the main members in the current and braced design cross-arms. This result was attributed to beam buckling given that the working load was implemented at the free end of the main member beams of the cross-arm structure [41,42].

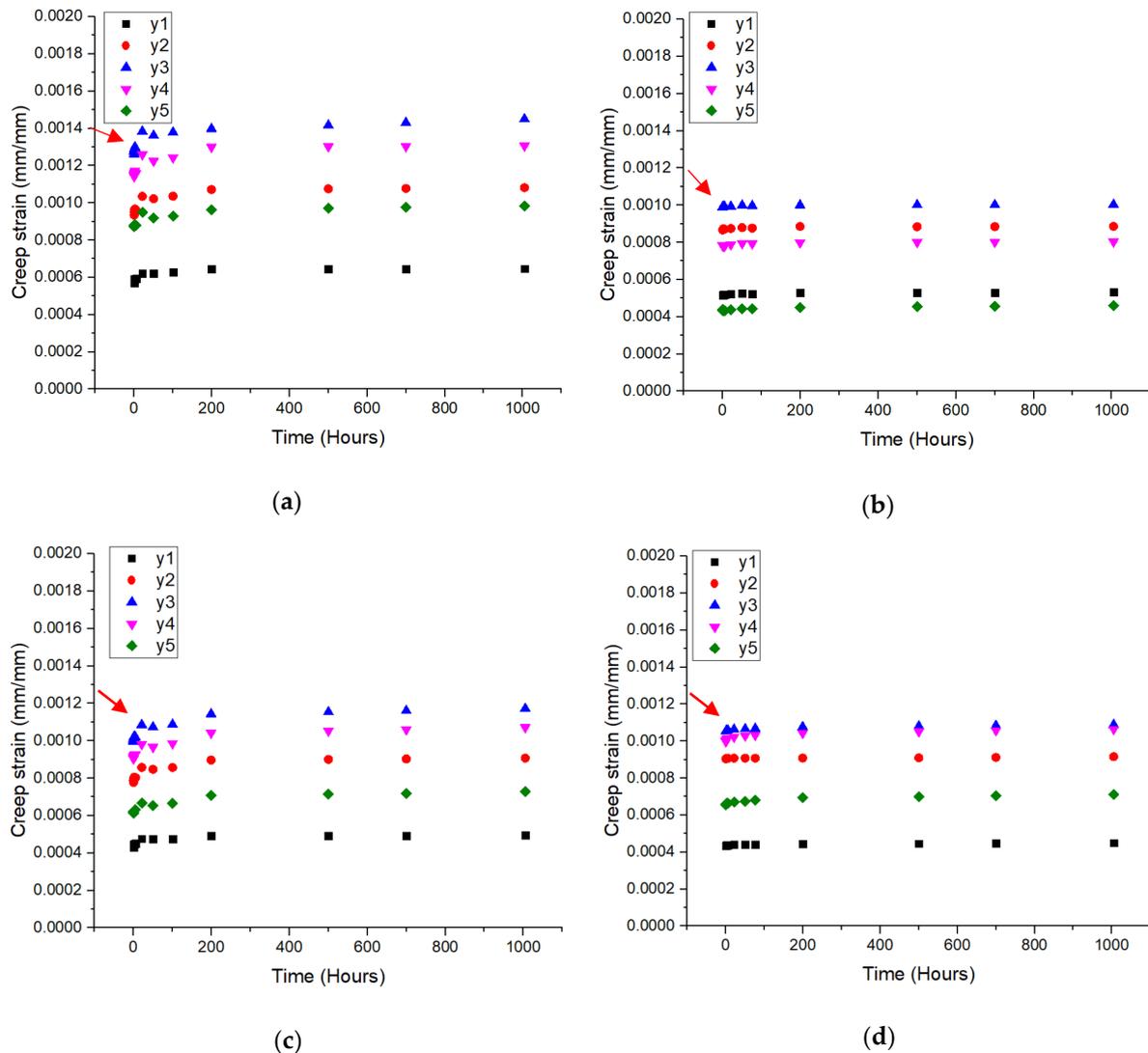


Figure 8. Creep strain-time curves for current PGFRPC cross-arm for (a) left and (c) right; braced PGFRPC cross-arm for left (b) and right (d) main member.

The braced cross-arm expressed a lower value of creep strain than the current cross-arm design. The beam laterally (buckling reaction) deflected at the middle of the beam as the force acted downward to the ground [43]. Overall, these results illustrated that the incorporation of additional bracing arms helped reduce the buckling reaction and subsequently provided improved structural integrity.

The creep strain patterns in Figure 8a–c, and d depicted a transitional phase from the elastic to the viscoelastic stage. At all points, the creep strain curves of the current composite cross-arm design indicated an extended transition period from the elastic to the viscoelastic phases as emphasized by the red arrows in Figure 8. Therefore, the incorporation of the bracing system into the cross-arm structure increased the stability of the viscoelastic stage. This effect reduced any failure potential within the structure.

Figure 8a,c show that the left and right main members of the current cross-arm design exhibited similar creep curve patterns. This result indicated that the main member arms of the existing cross-arm assembly must be symmetrical in shape, size and alignment to

sustain the working load. This finding was particularly obvious when the strain at y3 was higher in the current cross-arm design than in the braced cross-arm. All in all, the creep resistance performance of the cross-arm assembly could be improved by the incorporation of additional braced arms to counter the lateral force from dead weight, which caused the structure to buckle [44].

3.2. Findley Power Law Model

As discussed in this section, Findley’s power law was implemented to visualize the steady-state creep experienced by PGFRPC cross-arms (Table 1). Several parameters were evaluated on the basis of the model as represented by Equation (5). These parameters included transient creep A and stress-independent material exponent n .

Table 1. A parameter and stress independent material exponent, n from Findley power law for current and braced PGFRPC cross-arms.

Main Member Arm	Location	A		n		Adj. R^2	
		Current Cross-Arm	Braced Cross-Arm	Current Cross-Arm	Braced Cross-Arm	Current Cross-Arm	Braced Cross-Arm
Right	1	1.167×10^{-4}	1.321×10^{-5}	0.061	0.101	0.964	0.978
	2	1.506×10^{-4}	1.579×10^{-5}	0.088	0.107	0.942	0.942
	3	1.057×10^{-4}	4.573×10^{-6}	0.129	0.182	0.934	0.915
	4	1.183×10^{-4}	6.931×10^{-6}	0.119	0.208	0.903	0.928
	5	4.419×10^{-4}	8.299×10^{-6}	0.172	0.498	0.890	0.901
Left	1	3.207×10^{-4}	3.470×10^{-6}	0.021	0.220	0.961	0.982
	2	8.497×10^{-5}	2.116×10^{-6}	0.122	0.536	0.950	0.862
	3	5.602×10^{-5}	6.255×10^{-6}	0.195	0.265	0.959	0.993
	4	4.115×10^{-5}	1.825×10^{-6}	0.227	0.203	0.959	0.997
	5	2.663×10^{-5}	8.690×10^{-6}	0.232	0.277	0.951	0.988

The transient creep or A parameter of current and braced composite cross-arms were compared as depicted in Figure 9. The results showed that the A parameter of the current composite cross-arm design was higher than that of the braced cross-arm, accounting for the superior steady-state creep response of the existing design. This result indicated that retrofitting the PGFRPC cross-arm with additional braced arms would not influence the secondary stage of creep because the GFRP composite itself exhibited improved creep resistance performance [45–47].

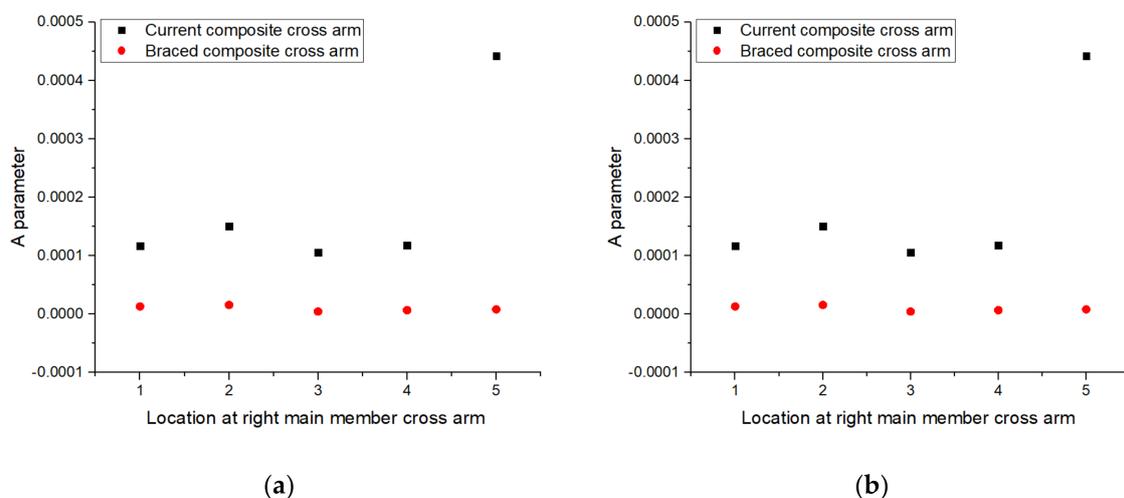


Figure 9. A parameter for current and braced PGFRPC cross-arms: (a) right; (b) left main members.

As shown in Table 2, the average n value of the current composite cross-arm was 0.1366, whereas that of the current PGFRPC cross-arm was approximately 0.2697. The

average n value of the braced composite cross-arm (0.2597) was within the acceptable range of 0.20–0.29 [48–50]. However, the n value of the current PGFRPC cross-arm was 0.1366, which was less than the common range of stress-independent material exponents. Moreover, the stress exponent n of the braced composite cross-arm was higher than that of the current composite cross-arm, showing that the braced composite cross-arm had a poorer hardening capability, which resulted in increased flow rate along each individual arm [51,52].

Table 2. Stress independent material exponent, n for current and braced PGFRPC cross-arms.

Cross-Arm Configuration	Current		Braced	
	Right	Left	Right	Left
Stress independent material exponent, n	0.1138	0.1594	0.2192	0.3002
Average of n value	0.1366		0.2597	

All adjusted regression ($Adj. R^2$) values for Findley’s model for both cross-arms (current and braced designs) were close to 1, indicating that the Findley model fitted the experimental data very well. The braced PGFRPC cross-arm (0.997–0.862) exhibited higher $Adj. R^2$ values than the existing design (0.964–0.890). This result demonstrated that the braced composite cross-arm followed the creep principles in the primary and secondary creep stage and that the creep data produced showed reduced exaggeration due to improved structural integrity.

3.3. Burger Model

The Burger model was used to elaborate the elasticity and viscoelasticity parameters of the two configurations of the PGFRPC cross-arms in the current and braced designs. The computational software OriginPro 2016 was implemented to plot nonlinear curve fit functions to identify two estimation parameters (E_e and η_k) as shown in Table 3.

Table 3. Elastic and viscoelastic parameters from Burger model for current and braced PGFRPC cross-arms.

Main Member Arm	Location	E_e		η_k		$Adj. R^2$	
		Current Cross-Arm	Braced Cross-Arm	Current Cross-Arm	Braced Cross-Arm	Current Cross-Arm	Braced Cross-Arm
Right	1	1.338×10^{11}	1.539×10^{11}	1.185×10^{15}	5.396×10^{15}	0.416	0.544
	2	1.618×10^{11}	1.818×10^{11}	1.161×10^{15}	8.552×10^{15}	0.456	0.497
	3	1.809×10^{11}	2.387×10^{11}	1.410×10^{15}	1.921×10^{16}	0.544	0.552
	4	2.652×10^{11}	4.018×10^{11}	1.960×10^{15}	1.368×10^{16}	0.466	0.588
	5	4.392×10^{11}	8.993×10^{11}	3.609×10^{15}	1.535×10^{16}	0.545	0.786
Left	1	1.837×10^{11}	1.838×10^{11}	4.378×10^{15}	8.979×10^{15}	0.965	0.971
	2	2.013×10^{11}	1.753×10^{11}	3.073×10^{15}	2.139×10^{16}	0.938	0.951
	3	2.347×10^{11}	2.258×10^{11}	2.806×10^{15}	1.554×10^{16}	0.942	0.978
	4	3.443×10^{11}	3.156×10^{11}	7.908×10^{15}	8.298×10^{15}	0.947	0.974
	5	6.330×10^{11}	5.977×10^{11}	1.657×10^{16}	2.181×10^{16}	0.936	0.985

The elastic phase occurred after instantaneous strain directly after the load was applied on the cross-arm. A graph (Figure 10) indicating the values of the elastic modulus and E_e of the two arm configurations was plotted to visualize this phenomenon. Overall, the graph shows that the braced PGFRPC cross-arm had high elastic moduli at y1–y5, likely because the cross-arm was being supported by an additional bracing system, which subsequently increased the elastic critical moment of the beam as the force was exerted [53]. This result proved that buckling was resisted by additional bracing given that the stiffness of the main member beams had increased [54].

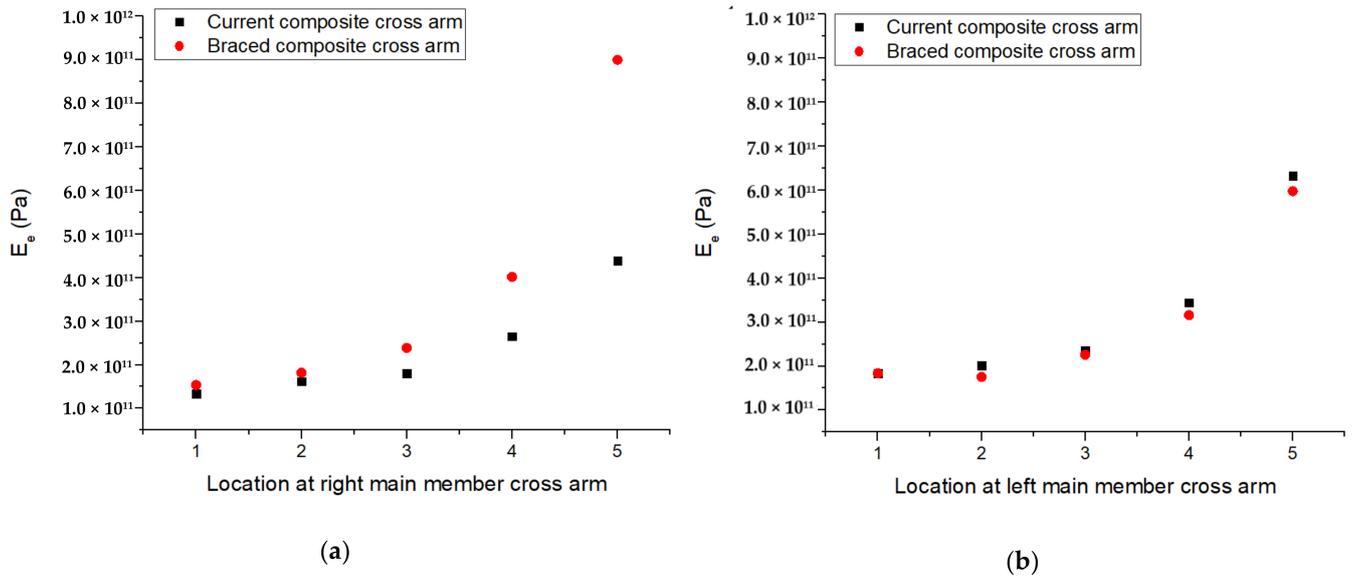


Figure 10. E_e parameter for current and braced PGFRPC cross-arms: (a) right; (b) left main members.

The viscoelasticity modulus was another parameter that was evaluated by using the Burger model. This parameter is vital for analyzing the relaxation response over time of a beam inside an interconnected structure, such as cross-arms. This parameter is also called the irrecoverable creep strain, which accounts for the relaxation coefficient of the viscoelastic property [55]. Figure 11 depicts the viscoelastic properties of the current and braced PGFRPC cross-arms in accordance with location along the main members. The viscoelastic modulus of the braced PGFRPC cross-arm had increased compared with that of the current PGFRPC cross-arm. This observation indicated that the addition of braced arms considerably improved the viscoelastic properties of the cross-arm structure; this improvement accounted for the enhancement in relaxation during creep [56].

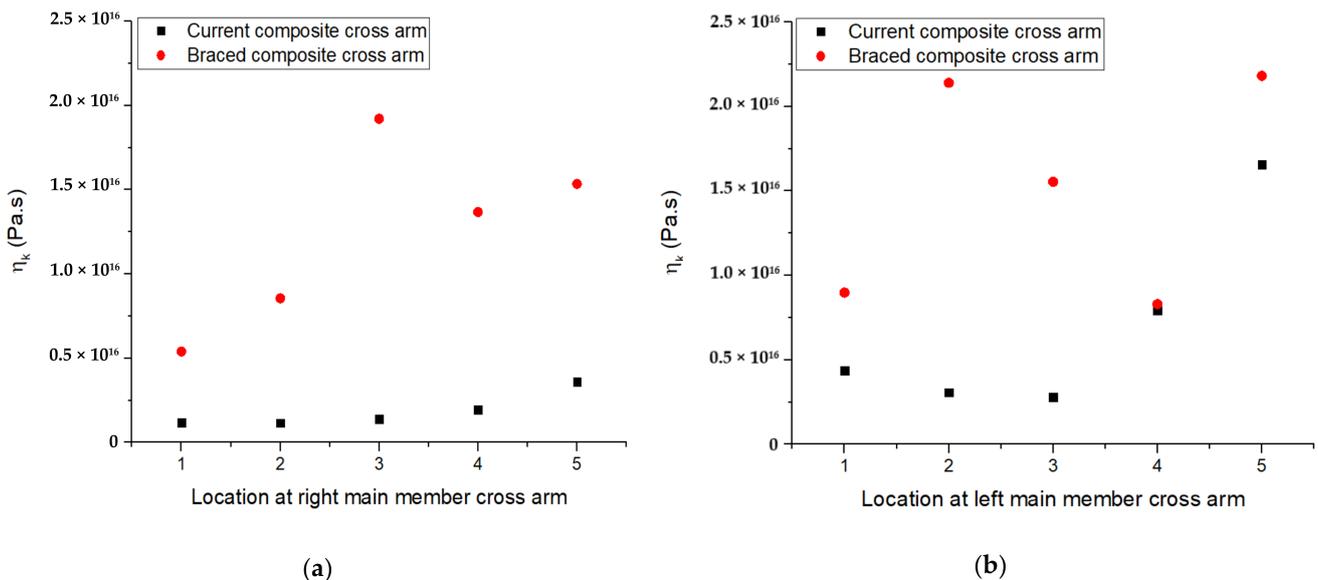


Figure 11. η_k parameter for current and braced PGFRPC cross-arms: (a) right; (b) left main members.

3.4. Creep Models Accuracy and Validation

The coefficients of determination or adjusted regression $Adj. R^2$ for each fitted model are tabulated in Tables 1 and 2. The $Adj. R^2$ coefficients for Findley’s power law model

ranged from 0.860 to 0.997 and were better than those of the Burger model, which ranged from 0.416 to 0.985. The forecasted value of the Burger model diverged from experimental data because this model forecasted the relationship of viscosity and time linearly [57]. Hence, this result established that Findley's power law model was the most suitable numerical model for evaluating the creep performance of PGFRPC cross-arms because the creep trend elucidated the steady-state creep behavior in the secondary phase [58,59]. The Burger model was still implemented in this research due to evaluation of the influence of additional bracing arms on the elastic and viscoelastic moduli of composite cross-arms. Both numerical models are essential for research applications to obtain a holistic view and understanding of the creep behaviors of both PGFRPC cross-arm configurations.

Each model was further evaluated and validated by comparing their instantaneous strain values with the experimental instantaneous strain. Instantaneous strain was obtained on the basis of Hooke's law principles, which state that the value of instantaneous stress is linearly proportional to the applied stress. Table 4 displays the comparison of instantaneous strain values at y_3 between the experimental outputs and numerical models of the current and braced PGFRPC cross-arms for model validation. The instantaneous strain at y_3 was selected because y_3 exhibited the highest strain among all locations in the cross-arms.

Table 4. Comparison of instantaneous strain value between experimental outputs and numerical models located at y_3 in current and braced PGFRPC cross-arms.

Configu- Ration	Model	Inst. Strain	Located at y_3 at Main Member			
			Right	Percentage Error (%)	Left	Percentage Error (%)
Current cross- arm	Experimental data	$\varepsilon (10^{-3})$	1.262	-	0.996	-
	Findley model	$\varepsilon_0 (10^{-3})$	1.190	6.050	0.963	3.427
	Burger model	$\varepsilon_0 (10^{-3})$	1.310	3.664	1.010	1.386
Braced cross- arm	Experimental data	$\varepsilon (10^{-3})$	0.990	-	1.053	-
	Findley model	$\varepsilon_0 (10^{-3})$	0.987	0.304	1.050	0.286
	Burger model	$\varepsilon_0 (10^{-3})$	0.993	0.304	1.050	0.286

As seen in Table 4, all presented percentage errors had less than 7% error. Sayahi et al. [60] and Zhang et al. [61] stated that the acceptable percentage error is approximately 25–20%. In general, the percentage errors for the validation of numerical data are divided into five classes, namely, highly acceptable (0.1–9.9% accuracy), good (10–14.9% accuracy), satisfactory (15–19.9% accuracy), fair (20–24.9% accuracy) and unsatisfactory (more than 25 accuracy) [60,61]. The Findley and Burger models revealed that the creep trends were within the highly acceptable range. This result indicated that both numerical models forecasted the creep values with high accuracy. This study established that the experimental data that were plotted to elaborate the creep properties of the PGFRPC cross-arms were verified with precise and consistent values from the Findley and Burger numerical models.

4. Conclusions

The time-dependent creep behavior of PGFRPC cross-arms implemented with bracing systems was reduced compared with that of the existing PGFRPC cross-arm design. Therefore, the bracing arms showed potential for installation in latticed transmission towers to grasp electric cables and insulators. Previous works have investigated the creep behaviors of coupon-scale PGFRPC cross-arms in the laboratory environment. This approach is typical for intended baseline characterizations. The creep behaviors of the braced and current designs of PGFRPC cross-arms under outdoor working conditions were compared. This comparison showed that the creep strain of the main member beams in the braced PGFRPC cross-arm had decreased by approximately 8–20% compared with those in the existing PGFRPC cross-arm design. Moreover, the incorporation of bracing systems in the cross-arm

structure would increase the stability of the viscoelastic stage. This effect could reduce any failure potential within the structure. Further analysis with the Findley and Burger models revealed that the braced PGFRPC cross-arm had a higher elastic modulus than the current design of the PGFRPC cross-arm. The braced systems increased the viscoelastic modulus of the cross-arm, thus enhancing relaxation during creep. Retrofitting the PGFRPC cross-arm with braced arms would not influence the secondary stage of creep given that the PGFRPC composite itself had improved creep resistance performance due to its high flexure strength and modulus. This characteristic could be advantageous for using bracing members inside cross-arm structures in the construction of transmission towers to prolong the structure's service life.

Findley's power law model was a useful tool for describing and predicting the creep responses of braced and current PGFRPC cross-arm designs under their working loads. This model predicted that both PGFRPC cross-arm designs showed low creep rates under their actual working loads. Meanwhile, the Burger model was very practical for explaining the elastic and viscoelastic behaviors of the composite structures. In future works, fatigue and electrical capacity tests should be conducted to evaluate the dynamic load exerted by the wind and the electrical resistance of braced PGFRPC cross-arms. These works could broaden the views and perspectives of researchers and engineers of braced PGFRPC cross-arms.

Author Contributions: Conceptualization, M.R.I. and M.R.M.A.; methodology, M.R.M.A.; software, M.R.M.A.; validation, M.R.I., S.M.S., and N.Y.; investigation, M.R.M.A.; resources, M.R.I.; writing—original draft preparation, M.R.M.A.; writing—review and editing, M.R.M.A., and M.R.I.; visualization, M.R.M.A.; supervision, M.R.I., S.M.S. and N.Y.; project administration, M.R.I.; funding acquisition, M.R.I. All authors have read and agreed to the submission version of the manuscript.

Funding: This research work was funded by Ministry of Higher Education, Malaysia for financial support through the enumerator service under Fundamental Research Grant Scheme (FRGS): FRGS/1/2019/TK05/UPM/02/11 (5540205) and Geran Putra: (9634000) by Universiti Putra Malaysia to carry out all research activities.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Acknowledgments: The authors are very thankful to Department of Aerospace Engineering, Faculty of Engineering, UPM for providing space and facilities for the project. Moreover, all authors are very appreciate and thankful to Jabatan Perkhidmatan Awam (JPA) and Kursi Rahmah Nawawi for providing scholarship award and financial aids to the first author to carry out this research project.

Conflicts of Interest: The authors declare no conflict of interest.

References

1. Rawi, I.M.; Ab-Kadir, M.Z.A. Investigation on the 132 kV overhead lines lightning-related flashovers in Malaysia. In Proceedings of the 2015 International Symposium on Lightning Protection (XIII SIPDA), Balneario Camboriu, Brazil, 28 September–2 October 2015; Institute of Electrical and Electronics Engineers (IEEE): Piscataway, NJ, USA, 2015; pp. 239–243.
2. Itam, Z.; Ishak, Z.M.; Yusof, Z.M.; Salwi, N.; Zainoodin, M.M. Effect on the temperature behavior of glass fiber reinforced polymer (GFRP) in various application—A review. *AIP Conf. Proc.* **2018**, *2031*, 1–5. [[CrossRef](#)]
3. Selvaraj, M.; Kulkarni, S.M.; Babu, R.R. Analysis and experimental testing of a built-up composite cross arm in a transmission line tower for mechanical performance. *Compos. Struct.* **2013**, *96*, 1–7. [[CrossRef](#)]
4. Rahman, M.S.A. Wood and fiberglass crossarm performance against lightning strikes on transmission towers. In Proceedings of the International Conference on Power Systems Transient (IPST), Seoul, Korea, 26–29 June 2017; Sung-Kyun-Kwan University: Seoul, Korea, 2017; pp. 1–6.
5. Ilyas, R.A.; Sapuan, S.; Atiqah, A.; Ibrahim, R.; Abrol, H.; Ishak, M.R.; Zainudin, E.S.; Nurazzi, N.M.; Atikah, M.S.N.; Ansari, M.N.M.; et al. Sugar palm (*Arenga pinnata* (Wurmb.) Merr) starch films containing sugar palm nanofibrillated cellulose as reinforcement: Water barrier properties. *Polym. Compos.* **2019**, *41*, 459–467. [[CrossRef](#)]

6. Ilyas, R.; Sapuan, S.; Norrrahim, M.N.F.; Yasim-Anuar, T.A.T.; Kadier, A.; Kalil, M.S.; Atikah, M.; Ibrahim, R.; Asrofi, M.; Abral, H.; et al. Nanocellulose/Starch Biopolymer Nanocomposites: Processing, Manufacturing, and Applications. In *Advanced Processing, Properties, and Applications of Starch and Other Bio-Based Polymers*; Elsevier BV: Amsterdam, The Netherlands, 2020; pp. 65–88.
7. Ilyas, R.; Sapuan, S.; Atikah, M.; Asyraf, M.; Rafiqah, S.A.; Aisyah, H.; Nurazzi, N.M.; Norrrahim, M. Effect of hydrolysis time on the morphological, physical, chemical, and thermal behavior of sugar palm nanocrystalline cellulose (*Arenga pinnata* (Wurmb.) Merr). *Text. Res. J.* **2020**, *004051752093239*. [[CrossRef](#)]
8. Ilyas, R.A.; Sapuan, M.S.; Norizan, M.N.; Norrrahim, M.N.F.; Ibrahim, R.; Atikah, M.S.N.; Huzaifah, M.R.M.; Radzi, A.M.; Izwan, S.; Azammi, A.M.N.; et al. Macro to nanoscale natural fiber composites for automotive components: Research, development, and application. In *Biocomposite and Synthetic Composites for Automotive Applications*; Sapuan, M.S., Ilyas, R.A., Eds.; Woodhead Publishing Series: Amsterdam, The Netherlands, 2020.
9. Forestry Department of Peninsular Malaysia. *Annual Report 2018: JPSM*; Forestry Department of Peninsular Malaysia: Kuala Lumpur, Malaysia, 2018.
10. Abu-Bakar, M.S.; Mohamad, D.; Ishak, Z.M.; Yusof, Z.M.; Salwi, N. Durability control of moisture degradation in GFRP cross arm transmission line towers. *AIP Conf. Proc.* **2018**, *2031*, 020027. [[CrossRef](#)]
11. Sapuan, S.M. A Conceptual Design of the Concurrent Engineering Design System for Polymeric-Based Composite Automotive Pedals. *Am. J. Appl. Sci.* **2005**, *2*, 514–525. [[CrossRef](#)]
12. Ishak, N.M.; Malingam, S.D.; Mansor, M.R. The application of TRIZ on natural fibre metal laminate to reduce the weight of the car front hood. *J. Braz. Soc. Mech. Sci. Eng.* **2018**, *40*, 105. [[CrossRef](#)]
13. Asyraf, M.R.M.; Rafidah, M.; Ishak, M.R.; Sapuan, S.; Yidris, N.; Ilyas, R.; Razman, M.R. Integration of TRIZ, morphological chart and ANP method for development of FRP composite portable fire extinguisher. *Polym. Compos.* **2020**, *41*, 2917–2932. [[CrossRef](#)]
14. Mazani, N.; Sapuan, S.; Sanyang, M.; Atiqah, A.; Ilyas, R. Design and Fabrication of a Shoe Shelf from Kenaf Fiber Reinforced Unsaturated Polyester Composites. In *Lignocellulose for Future Bioeconomy*; Elsevier BV: Amsterdam, The Netherlands, 2019; pp. 315–332.
15. Ilyas, R.; Sapuan, S.; Asyraf, M.; Atikah, M.; Ibrahim, R.; Dele-Afolabi, T.; Hazrol, M. Introduction to Biofiller-Reinforced Degradable Polymer Composites. In *Biofiller-Reinforced Biodegradable Polymer Composites*; Informa UK Limited: London, UK, 2020; pp. 1–23.
16. Omran, A.A.B.; Mohammed, A.A.B.A.; Sapuan, S.M.; Ilyas, R.A.; Asyraf, M.R.M.; Kolor, S.S.R.; Petrú, M. Micro- and Nanocellulose in Polymer Composite Materials: A Review. *Polymers (Basel)* **2021**, *13*, 231. [[CrossRef](#)]
17. Alsubari, S.; Zuhri, M.Y.M.; Sapuan, S.M.; Ishak, M.R.; Ilyas, R.A.; Asyraf, M.R.M. Potential of Natural Fiber Reinforced Polymer Composites in Sandwich Structures: A Review on Its Mechanical Properties. *Polymers (Basel)* **2021**, *13*, 423. [[CrossRef](#)]
18. Mohamad, D.; Syamsir, A.; Beddu, S.; Abas, A.; Ng, F.C.; Razali, M.F.; Seman, S.A.H.A. Numerical Study of Composite Fiberglass Cross Arms under Statics Loading and Improvement with Sleeve Installation. *IOP Conf. Ser. Mater. Sci. Eng.* **2019**, *530*, 012027. [[CrossRef](#)]
19. Mohamad, D.; Syamsir, A.; Sa'Don, S.N.; Zahari, N.M.; Seman, S.A.H.A.; Razali, M.F.; Abas, A.; Ng, F.C. Stacking Sequence Effects on Performance of Composite Laminate Structure Subjected To Multi-Axial Quasi-Static Loading. *IOP Conf. Ser. Mater. Sci. Eng.* **2019**, *530*, 1–6. [[CrossRef](#)]
20. Mohamad, D.; Syamsir, A.; Beddu, S.; Kamal, N.L.M.; Zainoodin, M.M.; Razali, M.F.; Abas, A.; Seman, S.A.H.A.; Ng, F.C. Effect of Laminate Properties on the Failure of Cross Arm Structure under Multi-Axial Load. *IOP Conf. Ser. Mater. Sci. Eng.* **2019**, *530*, 012029. [[CrossRef](#)]
21. Mohamad, D.; Syamsir, A.; Itam, Z.; A Bakar, H.; Abas, A.; Ng, F.C.; Razali, M.F.; Seman, S.A.H.A. Numerical Simulation on the Statics Deformation Study of Composite Cross Arms of Different Materials and Configurations. *IOP Conf. Ser. Mater. Sci. Eng.* **2019**, *530*. [[CrossRef](#)]
22. Asyraf, M.; Ishak, M.R.; Sapuan, S.; Yidris, N. Conceptual design of multi-operation outdoor flexural creep test rig using hybrid concurrent engineering approach. *J. Mater. Res. Technol.* **2020**, *9*, 2357–2368. [[CrossRef](#)]
23. Asyraf, M.; Ishak, M.R.; Sapuan, S.; Yidris, N. Conceptual design of creep testing rig for full-scale cross arm using TRIZ-Morphological chart-analytic network process technique. *J. Mater. Res. Technol.* **2019**, *8*, 5647–5658. [[CrossRef](#)]
24. Asyraf, M.R.M.; Ishak, M.R.; Sapuan, S.M.; Yidris, N.; Ilyas, R.A.; Rafidah, M.; Razman, M.R. Evaluation of design and simulation of creep test rig for full-scale cross arm structure. *Adv. Civ. Eng.* **2020**, 6980918. [[CrossRef](#)]
25. Asyraf, M.R.M.; Ishak, M.R.; Razman, M.R.; Chandrasekar, M. Fundamentals of creep, testing methods and development of test rig for the full-scale crossarm: A review. *J. Teknol.* **2019**, *81*, 155–164. [[CrossRef](#)]
26. Asyraf, M.R.M.; Ishak, M.R.; Sapuan, S.; Yidris, N.; Ilyas, R. Woods and composites cantilever beam: A comprehensive review of experimental and numerical creep methodologies. *J. Mater. Res. Technol.* **2020**, *9*, 6759–6776. [[CrossRef](#)]
27. Asyraf, M.R.M.; Ishak, M.R.; Sapuan, S.M.; Yidris, N.; Shahroze, R.M.; Johari, A.N.; Rafidah, M.; Ilyas, R.A. Creep test rig for cantilever beam: Fundamentals, prospects and present views. *J. Mech. Eng. Sci.* **2020**, *14*, 6869–6887. [[CrossRef](#)]
28. Nadhirah, A.; Mohamad, D.; Zainoodin, M.; Nabihah, S.; Mubin, N.; Itam, Z.; Mansor, H.; Kamal, N.M.; Muda, Z.C.; Nasional, U.T.; et al. Properties of fiberglass crossarm in transmission tower—A review. *Int. J. App. Eng. Res.* **2017**, *12*, 15228–15233.
29. Fairuz, A.M.; Sapuan, S.M.; Zainudin, E.S.; Jaafar, C.N. Polymer composite manufacturing using a pultrusion process: A review. *Am. J. Appl. Sci.* **2014**, *11*, 1798–1810. [[CrossRef](#)]

30. Jahangiri, T.; Wang, Q.; da Silva, F.F.; Bak, C.L. Fiber Reinforced Plastic (FRP) Composite Selection for the Composite Cross-Arm Core. In *Lecture Notes in Electrical Engineering*; Springer Science and Business Media LLC: Berlin/Heidelberg, Germany, 2019; Volume 557, pp. 15–65.
31. Hunt, J.F.; Zhang, H.; Huang, Y. Analysis of Cantilever-Beam Bending Stress Relaxation Properties of Thin Wood Composites. *Bioresource* **2015**, *10*, 3131–3145. [[CrossRef](#)]
32. Feng, S.H.; Zhao, Y.K. The summary of wood stress relaxation properties and its influencing factors. *WoodProc. Mach.* **2010**, *25*, 39–40.
33. Liu, H.W. *Mechanics of Materials*; China Machine Press: Beijing, China, 2004.
34. Fu, H.; Dun, M.; Wang, H.; Wang, W.; Ou, R.; Wang, Y.; Liu, T.; Wang, Q. Creep response of wood floor-high-density polyethylene/laminated veneer lumber coextruded composites. *Constr. Build. Mater.* **2020**, *237*, 117499. [[CrossRef](#)]
35. Findley, W.N. Creep characteristics of plastics. *Symp. Plast. ASTM* **1944**, 118–134.
36. Perez, C.J.; Alvarez, V.A.; Vázquez, A. Creep behaviour of layered silicate/starch–polycaprolactone blends nanocomposites. *Mater. Sci. Eng. A* **2008**, *480*, 259–265. [[CrossRef](#)]
37. Chandra, P.K.; Sobral, P.J.D.A. Calculation of viscoelastic properties of edible films: Application of three models. *Food Sci. Technol.* **2000**, *20*, 250–256. [[CrossRef](#)]
38. Hao, A.; Chen, Y.; Chen, J.Y. Creep and recovery behavior of kenaf/polypropylene nonwoven composites. *J. Appl. Polym. Sci.* **2014**, *131*, 8864–8874. [[CrossRef](#)]
39. Hakimeh, S.; Vaidyanathan, T.K. Flexural creep deformation and recovery in dental composites. *J. Dent.* **2001**, *29*, 545–551. [[CrossRef](#)]
40. Sezgin, F.; Tanoglu, M.; Eğilmez, O.; Dönmez, C. Mechanical Behavior of Polypropylene-based Honeycomb-Core Composite Sandwich Structures. *J. Reinf. Plast. Compos.* **2009**, *29*, 1569–1579. [[CrossRef](#)]
41. Sayyad, A.S.; Ghugal, Y.M. Bending, buckling and free vibration of laminated composite and sandwich beams: A critical review of literature. *Compos. Struct.* **2017**, *171*, 486–504. [[CrossRef](#)]
42. Bozkurt-Ömer, Y.; Bulut, M.; Erkliğ, A.; Faydh, W.A. Axial and lateral buckling analysis of fiber reinforced S-glass/epoxy composites containing nano-clay particles. *Compos. Part B Eng.* **2019**, *158*, 82–91. [[CrossRef](#)]
43. Kanyilmaz, A. Role of compression diagonals in concentrically braced frames in moderate seismicity: A full scale experimental study. *J. Constr. Steel Res.* **2017**, *133*, 1–18. [[CrossRef](#)]
44. Patil, D.M.; Sangle, K.K. Seismic Behaviour of Different Bracing Systems in High Rise 2-D Steel Buildings. *Structure* **2015**, *3*, 282–305. [[CrossRef](#)]
45. Asyraf, M.R.M.; Ishak, M.R.; Sapuan, S.M.; Yidris, N.; Ilyas, R.A.; Rafidah, M.; Razman, M.R. Potential application of green composites for cross arm component in transmission tower: A brief review. *Int. J. Polym. Sci.* **2020**, 8878300. [[CrossRef](#)]
46. Loni, S.; Stefanou, I.; Valvo, P.S. Experimental study on the creep behaviour of GFRP pultruded beams. In *Proceeding of AIMETA 2013–XXI Congresso Nazionale dell’Associazione Italiana di Meccanica Teorica e Applicata, Torino, Italy, 17–20 September 2013*; Politecnico di Torino: Torino, Italy, 2013; pp. 1–10.
47. Johari, A.; Ishak, M.; Leman, Z.; Yusoff, M.; Asyraf, M. Influence of CaCO₃ in pultruded glass fiber/unsaturated polyester resin composite on flexural creep behavior using conventional and time-temperature superposition principle methods. *Polimery* **2020**, *65*, 792–800. [[CrossRef](#)]
48. Sá, M.F.; Gomes, A.; Correia, J.; Silvestre, N. Creep behavior of pultruded GFRP elements—Part 1: Literature review and experimental study. *Compos. Struct.* **2011**, *93*, 2450–2459. [[CrossRef](#)]
49. Anand, A.; Banerjee, P.; Prusty, R.; Ray, B.C. Lifetime Prediction of Nano-Silica based Glass Fibre/Epoxy composite by Time Temperature Superposition Principle. *IOP Conf. Ser. Mater. Sci. Eng.* **2018**, *338*, 012020. [[CrossRef](#)]
50. D’Antino, T.; Pisani, M.A. Long-term behavior of GFRP reinforcing bars. *Compos. Struct.* **2019**, *227*, 227. [[CrossRef](#)]
51. Takagi, H.; Dao, M.; Fujiwara, M. Prediction of the Constitutive Equation for Uniaxial Creep of a Power-Law Material through Instrumented Microindentation Testing and Modeling. *Mater. Trans.* **2014**, *55*, 275–284. [[CrossRef](#)]
52. Ahmad, M.; Curiel-Sosa, J.; Rongong, J. Characterisation of creep behaviour using the power law model in copper alloy. *J. Mech. Eng. Sci.* **2017**, *11*, 2503–2510. [[CrossRef](#)]
53. Richardson, J.N.; Nordenson, G.; Laberrenne, R.; Coelho, R.F.; Adriaenssens, S. Flexible optimum design of a bracing system for façade design using multiobjective Genetic Algorithms. *Autom. Constr.* **2013**, *32*, 80–87. [[CrossRef](#)]
54. Bastami, M.; Jazany, R.A. Development of Eccentrically Interconnected Braced Frame (EIC-BF) for seismic regions. *Thin Walled Struct.* **2018**, *131*, 451–463. [[CrossRef](#)]
55. Segovia, F.; Blanchet, P.; Laghdir, A.; Cloutier, A. Mechanical behaviour of sugar maple in cantilever bending under constant and variable relative humidity conditions. *Int. Wood Prod. J.* **2013**, *4*, 225–231. [[CrossRef](#)]
56. Nakai, T.; Toba, K.; Yamamoto, H. Creep and stress relaxation behavior for natural cellulose crystal of wood cell wall under uniaxial tensile stress in the fiber direction. *J. Wood Sci.* **2018**, *64*, 745–750. [[CrossRef](#)]
57. Yang, J.; Zhang, Z.; Schlarb, A.K.; Friedrich, K. On the characterization of tensile creep resistance of polyamide 66 nanocomposites. Part II: Modeling and prediction of long-term performance. *Polymery* **2006**, *47*, 6745–6758. [[CrossRef](#)]
58. Siengchin, S. Dynamic mechanic and creep behaviors of polyoxymethylene/boehmite alumina nanocomposites produced by water-mediated compounding. *J. Thermoplast. Compos. Mater.* **2012**, *26*, 863–877. [[CrossRef](#)]

-
59. Siengchin, S.; Karger-Kocsis, J. Structure and creep response of toughened and nanoreinforced polyamides produced via the latex route: Effect of nanofiller type. *Compos. Sci. Technol.* **2009**, *69*, 677–683. [[CrossRef](#)]
 60. Sayahi, M.; Sghaier, S.; Hedi, B.S. Finite element analysis of ball burnishing process: Comparisons between numerical results and experiments. *Int. J. Adv. Manuf. Technol.* **2012**, *67*, 1665–1673. [[CrossRef](#)]
 61. Zhang, Z.; Zhang, W.; Zhai, Z.J.; Chen, Q.Y. Evaluation of Various Turbulence Models in Predicting Airflow and Turbulence in Enclosed Environments by CFD: Part 2—Comparison with Experimental Data from Literature. *HVAC&R Res.* **2007**, *13*, 871–886. [[CrossRef](#)]