



# **Review Fundamentals of Global Modeling for Polymer Extrusion**

Krzysztof Wilczyński <sup>1</sup>,\*<sup>D</sup>, Andrzej Nastaj <sup>1</sup>, Adrian Lewandowski <sup>1</sup>, Krzysztof J. Wilczyński <sup>2</sup> and Kamila Buziak <sup>1</sup>

- <sup>1</sup> Polymer Processing Department, Faculty of Production Engineering, Warsaw University of Technology, 02-524 Warsaw, Poland; a.nastaj@wip.pw.edu.pl (A.N.); a.lewandowski@wip.pw.edu.pl (A.L.); kami.buziak@gmail.com (K.B.)
- <sup>2</sup> Politech Ltd., 86-031 Bydgoszcz, Poland; wilczynski\_k@wp.pl
- \* Correspondence: k.wilczynski@wip.pw.edu.pl

Received: 25 October 2019; Accepted: 13 December 2019; Published: 15 December 2019



**Abstract:** A review paper is presented on modeling for polymer extrusion for both single screw and twin-screw extrusion. An issue of global modeling is discussed, which includes modeling for solid conveying, melting, melt flow, and co-operation of the screw/die system. The classical approach to global modeling of the extrusion process, which is based on separate models for each section of the screw, i.e., solid transport section, melting and pre-melting sections, and the melt flow section is presented. In this case, the global model consists of the elementary models. A novel continuous concept of global modeling based on CFD (Computational Fluids Dynamics) computations is also presented, and a concept of using the DEM (Discrete Element Method) computation coupled with CFD computations is discussed.

Keywords: polymers; extrusion; modeling

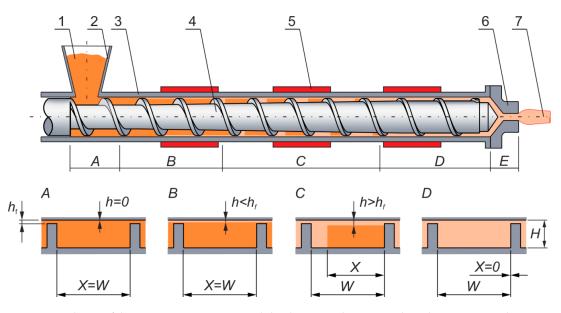
## 1. Introduction

Extrusion (Figure 1) is the most important and most massive technology in the polymer processing industry. It is widely used for the production of film, sheet, pipe, and profiles, as well as for specialty processing operations, such as compounding, mixing, granulating, chemical reactions, and more. These operations are applied for most polymeric materials, and extrusion is mainly used for these operations.

There are several important functions of extruding machines, polymer transport (from a hopper to a die), polymer melting, pressure generation, material mixing for thermomechanical and chemical homogenization, and, lastly, product forming. Melting should be quick to provide enough room for good material mixing. Melting and mixing are fundamental in polymer processing and crucial for the development of novel, advanced materials, polymer composites, or polymer blends, as well as for material recycling of plastics.

Single screw extruders are generally poor mixers and melting progresses slowly. In twin-screw extrusion, melting progresses faster and mixing action is considerably improved. In order to improve melting and mixing actions, various screw configurations are applied, using elements that intensify these actions, e.g., Maillefer, Barr, Maddock, and many others.

The design of polymer processing is currently supported by computer simulations based on the mathematical models of manufacturing processes. Modeling makes it possible to predict the course of these processes on the basis of process data (material, operating, and geometry).



**Figure 1.** Scheme of the extrusion process: 1—solid polymer, 2—hopper, 3—barrel, 4—screw, 5—heaters, 6—die, 7—extrudate, A—solid conveying zone, B—pre-melting zone (delay zone), C—melting zone, D—melt conveying zone, E—melt flow zone in the die, X—width of the solid bed, W—width of the screw channel, H—height of the screw channel, h<sub>f</sub>—clearance between the screw flights and the barrel, and h—polymer melt thickness.

Several fundamental books or book chapters have been devoted to an extrusion process, e.g., by McKelvey [1], Tadmor and Klein [2], White [3], White and Potente [4], Tadmor and Gogos [5], White and Kim [6], Potente et al. [7], Rauwendaal [8], Campbell and Spalding [9], Chung [10], Agassant et al. [11], Manas-Zloczower et al. [12], Osswald and Hernandez-Ortiz [13], and many others [14–33]. However, the subject of global modeling and the continuum approach to this was not considered. Some of these books also contain an excellent literature review, e.g., by White and Potente [4], Rauwendaal [8], and Agassant et al. [11].

#### 2. Modeling of the Extrusion Process

It is a particularly important challenge where the modeling of the two most important technologies are extrusion and injection molding. In these, there is a need for global modeling, i.e., description of the solid transport, polymer melting, and the melt flow. Polymer melt flows are relatively well understood. However, the transport of solid material as well as melting of the polymer are still poorly understood. The right polymer melting model is the basis for developing a comprehensive (global) model of the process.

#### 2.1. Solid Conveying Section

Solid conveying in the single screw extruder was described first by Darnell and Mol [34] who elaborated on the model for material transport and pressure development. In this model, the solid particles are assumed to be rapidly compacted, which forms a non-deformable solid bed. This solid bed flows due to frictional forces exerted by the barrel and screw surfaces on the solid polymer granules. It is assumed that the internal coefficient of friction (polymer/polymer) is larger than the external coefficient of friction (polymer/metal).

This fundamental approach was later extended by other researchers. Schneider [35] introduced anisotropy coefficients justifying that the pressure is not distributed equally in bulk materials. Tadmor et al. [2,36,37] introduced an energy balance considering the heat conduction into the solid bed. Campbell and Dontula [38] as well as Hyun and Spalding [39] defined an angle for the solid bed pressing force, which was not normal to the active flight of the screw. Chung [40,41] presented

a different approach assuming that the solid bed moves because of the presence of molten polymer films at the metal surfaces. Essentially, the solid polymer is coated by a thin layer of polymer melt. In addition, several studies were performed in which the material data for the solid conveying section were no longer assumed to be constant, e.g., by Spalding and Hyun [42]. The research on solid conveying was recently reviewed in detail by Schöppner et al. [43,44].

Although numerous researchers extended the work of Darnell and Mol, the basic analysis remained relatively unchanged and was the basis for modeling the extrusion process.

All the models of solid conveying presented so far were based on the assumption that the polymer granules are moving as a solid bed without relative movement of polymer granules. However, some investigations, e.g., performed by Fang et al. [45] showed that this assumption cannot be valid any longer since relative movement of individual granules occurs in the screw channel.

To solve the problem of modeling the solids' transport within a single screw extruder, the discrete element method (DEM) was proposed, which is well known within the field of granular mechanics. The first research using this method in the field of solid conveying the extrusion process was performed by Potente and Pohl [46] who studied the hopper inflow behavior in single screw extruders.

The fundamental studies on modeling the solid conveying in the single screw extruder with the use of the discrete element method were performed by Moysey and Thompson [47,48] who demonstrated the suitability of this 3D DEM approach for simulating single screw extruders. They presented the procedures for determining the coefficient of restitution [49], which is used as a material parameter in modeling, and performed the first simulations for compacting granules and the pressure/throughput relation in the feed section of the single screw extruder [50].

A further description of the solid conveying section based on the discrete element method (DEM) DEM was performed by Schöppner et al. [43,44] who developed the model, which fully comprehends the effects occurring in the solid conveying section and enables the calculation of a solid conveying zone with consideration of the pressure build-up and filling degree.

The discrete element method (DEM) is a very useful and powerful tool for modeling the solid conveying section of single screw extruders. However, it has two substantial drawbacks. It is time consuming and the material parameters, i.e., the coefficient of friction (CoF) and coefficient of restitution (CoR), are difficult to determine. Since it is time consuming, this method cannot be used for global modeling of the extrusion process, which requires hundreds of computing iterations.

Solid conveying in twin-screw extruders was studied, mainly for co-rotating extrusion, e.g., by Carrot et al. [51], Bawiskar and White [52], Potente et al. [53], and Wong at al. [54]. Studies of the solid conveying in counter-rotating extruders were relatively few. Doboczky first [55] discussed some of the problems of a solid conveying region, while Wilczyński and White [56] experimentally investigated it. Twin-screw extrusion systems are generally starved fed, and the solid conveying has less impact on global modeling than in flood fed single screw extruders.

## 2.2. Melting Section

The first melting tests in the single screw extruder were performed by Maddock and Street [57,58] who used the "screw pulling out technique," which involves stopping the screw, rapidly cooling the machine, and then pulling out the screw of the machine. An analysis of the cross-sections of the polymer removed from the screw allowed us to get to know the melting mechanism (contiguous solid melting). According to this mechanism, a melt layer is formed between the hot barrel and the solid polymer, which is scrapped off by the transverse flow in the screw, and accumulates at the active flight of the screw. The solid is gradually decreased by the effects of heat conducted from the hot barrel and viscous dissipation within the melt (Figure 2) [59].



**Figure 2.** CSM melting mechanism (Contiguous Solid Melting) observed for flood fed single screw extrusion of polypropylene [59].

The experiments showed that two steps of melting can be distinguished, including the delay section (or pre-melting), which corresponds to forming and growing the polymer melt layer, and the melting section (or plasticating), which corresponds to the accumulation of the molten polymer at the active flight of the screw.

Several years later, Tadmor et al. [60–62] completed a similar experimentation and developed the first melting model for single screw extrusion, which was a crucial contribution to the theory of extrusion and allowed us to formulate the first computer extrusion model EXTRUD [63]. This fundamental melting model was built by determining the velocity and temperature profiles in the melt film and temperature profile in the solid bed (Figure 2). Then, an energy balance at the interface melt/solid and the mass balance in the melt film and the solid were performed, which allowed us to predict the melting rate. Later, these studies were extended, and more detailed models were developed for a solid conveyance [36,37] and for the delay zone [64]. Then, the basic extrusion model was improved.

Many researchers repeated the "screw pulling out" experiments, and, in the majority of cases, they confirmed the Tadmor melting model. However, there were some exceptions, especially in the case of melting PVC, which were reported by Menges and Klenk [65] and Mennig [66] who observed the location of the melt pool at the passive flight of the screw, which is opposite than in the classical model where the melt pool is located at the active flight (Figure 2). Dekker [67] observed that, in the case of PP, the solid bed is surrounded by the polymer melt and did not detect a melt pool on any side of it.

The fundamental model of Tadmor was later extended by other researchers. Donovan [68] relaxed the assumption of the constant velocity of a solid bed and introduced some acceleration parameters. Edmondson and Fenner [69] as well as Cox and Fenner [70] proposed a model which allows the solid bed to accelerate naturally, and allows for the presence of a melt film between the bed and the screw. Lindt et al. [71,72] assumed that the rigid solid bed is suspended in the melt, which was later improved by Elbirli et al. [73,74] by considering the solid bed deformation, and allowing for transverse flow of the melt around the solid. Pearson et al. [75,76] generalized this approach by formulating the most elaborate extension of the Tadmor model in the 5-zone model in which the solid bed, melt pool, and the melt films are analyzed separately. In addition, the melt film thickness on the barrel varies. Analytical melting models were also developed. The models of Vermeulen et al. [77], Pearson [78], and Mount et al. [79] analyzed the melting on the barrel surface. Potente [80] included the melting on the screw surface into his model.

Housz and Meijer [81,82] pioneered the modeling of melting in multiflighted screws by modifying the classical Tadmor model. Elbirli et al. [83] as well as Amellal and Elbirli [84] developed non-Newtonian non-isothermal models that assumed the coexistence of fourth regions in a screw channel: solid bed, melt conveying, melt film at the inner barrel surface, and melt film surrounding the solid bed. Han et al. [85] considered the presence of six regions: solid bed, melt conveying, and four melt films at the inner barrel surface, screw root, barrier gap, and screw flights, respectively. Rauwendaal [86] has evaluated the performance of various barrier designs.

These studies presumed that the beginning of the barrier section coincides with the onset of melting, and the melting rate follows the rate of change of the cross-channel areas for solids or melt,

which is not consistent with experiments. Gaspar-Cunha and Covas [87,88] developed a melting model where the onset and rate of melting are decoupled from the start and the cross-channel location of the barrier, and inserted this model into a global package describing flow and heat transfer along the extruder from the hopper to the die exit.

Single screw extruders may have barrels with a grooved feed zone and a grooved melting zone. Numerous experiments were performed to study the effect of the grooved barrel on extrusion performance, e.g., by Grünschloß [89,90], Chung [91], and Jin et al. [92]. It was validated that this system shows more efficient melting, higher specific throughput, uniform pressure buildup, and lower processing costs compared to other high-performance extruders. Avila-Alfaro et al. [93,94] presented the mathematical model for melting in the grooved plasticating unit, which was a revised version of the classic model of Tadmor with some improvements made by Vermeulen et al. [77] and Pearson [78].

The "screw pulling out technique" is a relatively time consuming and expensive method of studying melting in extruders. Therefore, other approaches were applied for observing the melting behavior directly in the extrusion process. For example, Zhu et al. [95,96] used glass windows in the barrel. Noriega et al. [97] applied advanced optical methods for visualizing the melting profile, and Wang and Min [98] used an ultrasound-based system for monitoring the polymer melting in a twin-screw extruder. Aigner et al. [99] developed a non-invasive ultrasonic measurement system for determining the melting behavior in a single screw plasticating unit. Very recently, Yu et al. [100] presented a visualization technique with a global transparent barrel equipped with four cameras to capture the flow patterns of a viscoelastic fluid in a novel type of co-rotating non-twin-screw geometry.

Similarly, as in the case of Darnell and Mol's work for solid conveying, even though numerous researchers extended the work of Tadmor and Klein, the basic analysis remained relatively unchanged and was usually the basis for modeling the extrusion process. However, the models of the type presented so far are based on a prior assumed melting mechanism, which are not universal, and cannot be valid for all polymers, various operating conditions, and various screw configurations. These models can be useful only in qualitatively predicting the trends in melting polymers in single screw extruders.

Instead of the melting mechanism previously assumed, melting of a polymer in single screw extruders can be simulated by solving the conservation equations of mass, motion, and energy along with a constitutive equation for the polymer being used.

This different approach was proposed first by Viriyayuthakorn and Kassahun [101] who developed a three-dimensional FEM model without assuming any particular melting mechanism. The problem of the phase change was solved by using a functional dependence of the specific heat on temperature. The solution of equations of motion and energy provided the solid/melt distribution, which was defined by the temperature distribution. Syrjala [102] performed a two-dimensional attempt for simulating melting without any melting mechanism assumed. However, in both cases, the simulations were not verified experimentally.

This novel approach based on solving the conservation equations without an assumed melting mechanism seems to be very promising for the future work on modeling the melting, even though it requires very large computational capabilities.

Altinkaynak et al. [103] performed intensive experimental and theoretical studies on modeling melting using this approach. The two-phase solid/melt flow was considered with the Cross-WLF model, which allows us to define a solid material as a high-viscous fluid, while a molten material allows us to define the material as a low-viscous fluid. Hopmann et al. [104] solved the equations of motion and energy using the finite volume method FVM with the Carreau model. Recently, Kazmer et al. [105] applied this approach to modeling melting in barrier screws, and Lewandowski and Wilczyński applied this approach to modeling in conventional screws [106].

Contrary to melting in single screw extruders, the studies on melting in twin-screw extruders were much more limited. These studies involved mainly modular self-wiping co-rotating twin-screw extruders, both experimentally (Bawiskar and White [52], Todd [107], Sakai [108], and Gogos [109–111])

and theoretically. Potente and Melish [112] as well as Bawiskar and White [113] proposed the models principally based on the classical Tadmor model [2] for a single screw extrusion, while assuming the progressive development of a molten layer from the barrel toward the screw root. Bawiskar and White [113] considered the formation of two stratified layers of melt in contact with the hot barrel and solid pellets in contact with the relatively colder screw. Potente and Melisch [112] proposed a model based on the melting of particles uniformly suspended in the polymer melt. A similar approach was presented by Liu et al. [95]. Vergnes et al. [114,115] and Zhu et al. [116] proposed the dispersive models based on the analysis of flow of the solid/liquid mixture with an equivalent viscosity.

Melting in counter-rotating twin-screw extruders is much less understood. Only limited observations were presented by Janssen [117]. White et al. [118,119] indicated that melting occurs much more rapidly than in intermeshing co-rotating twin-screw extruders. Wilczyński and White [56] revealed the mechanism of melting in intermeshing counter-rotating twin-screw extruders. According to this mechanism, melting is initiated both between the screws and at the barrel. The melting action between the screws is initiated by frictional work on the pellets by the calendering stresses between the screws. The melting action at the barrel is induced by a barrel temperature higher than the melting point and propagated by viscous dissipation heating of the melt film produced. Based on these observations (Figure 3), the models were developed for melting in both those regions [120]. Further studies of melting were reported by Wang and Min [98,121] and by Wilczyński et al. [122].

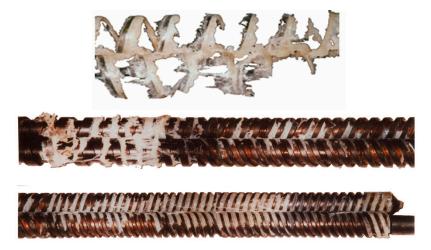


Figure 3. Melting mechanism for counter-rotating twin-screw extrusion [120].

Although the flood fed single screw extrusion was extensively investigated and modeled, little information was presented on the starve fed single-screw extrusion. Several basic studies were performed by Lopez-Latorre and McKelvey [123], Isherwood et al. [124], Strand et al. [125], and Thompson et al. [126]. Recently, Wilczyński et al. [59,127] based on the experimental studies proposed the melting mechanism and melting model for the starve fed single-screw extrusion, and then developed the first computer model of this process SSEM-Starve [128]. According to this melting model, two stages of melting are distinguished. In the partially-filled region of the screw, the polymer granules are collected at the active flight and are generally melted by conduction. In the fully filled region, the unmolten solid particles are suspended in the previously molten material, and melting progresses through heat dissipation (Figure 4).

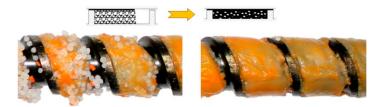
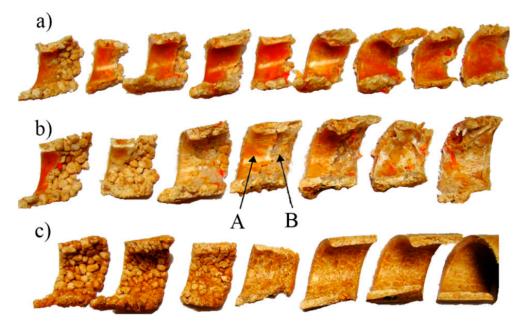


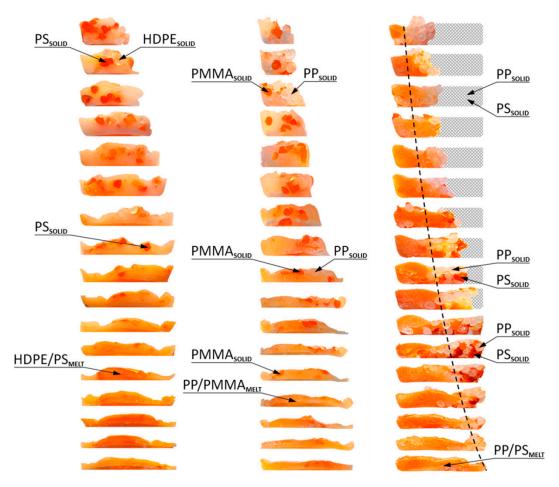
Figure 4. Melting mechanism for starve fed extrusion of polypropylene [59].

Recently, Wilczyński et al. [129–131] observed different melting mechanisms in single screw extrusion, both flood-fed and starve fed, in the case of wood-polymer composites (Figure 5) and polymer blends (Figures Figure 6 and 7).

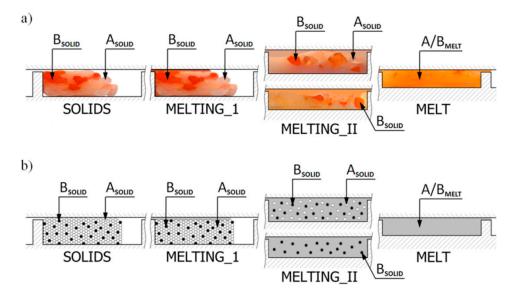


**Figure 5.** Melting of a wood-plastic composite of polypropylene PP and wood flour WF of a different composition in the single screw extrusion: (**a**) 25% WF, (**b**) 50% WF, (**c**) 75% WF, A—molten material, B—solid material [129] (with permission from Int. Polym. Process. 2015, 30, 113-120, by Wilczyński, K.; Nastaj, A., Lewandowski, A., Wilczyński, K.J., Buziak, K. © Carl Hanser Verlag GmbH & Co. KG, Muenchen).

The methods of investigating and modeling the extrusion process were adapted to modeling injection molding. Experimental studies of melting in injection molding machines were performed first by Donovan et al. [132], who revealed that the screw recharge process is a transient plasticating extrusion process, which gradually approaches the equilibrium extrusion behavior as the screw rotates. If the screw rotation time is a high fraction of the total cycle time, the plasticating behavior is similar to the extrusion behavior. However, if the screw rotation time is a small fraction of the total cycle time, the plasticating behavior is significantly different. Donovan [133,134] also proposed a heuristic model for predictive simulations, which required experimental evaluation of an empirical parameter, specific to a particular material over the tested range of operating conditions. Lipshitz et al. [135] developed a theoretical model for melting, which was built upon the detailed physical mechanisms taking place in the reciprocating screw injection molding machine. This model permits the calculation of the solid bed profile as a function of time during the injection cycle. It consists of a dynamic extrusion melting model for the rotation period, a transient heat conduction model with a phase transition for the screw rest period, and a model for the drifting of the beginning of melting during the injection cycle.



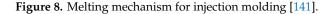
**Figure 6.** Melting of polyblends: (**a**) high density polyethylene/polystyrene blend (HDPE/PS)—starve fed extrusion, (**b**) polypropylene/polymethyl methacrylate blend (PP/PMMA)—starve fed extrusion, and (**c**) polypropylene/polystyrene blend (PP/PS)—flood fed extrusion [131].



**Figure 7.** Melting of polymer blends in starve fed single-screw extrusion: (**a**) melting visualization, (**b**) melting model: A—major component of polyblen (HDPE), B—minor component of polyblend (PS), A/B—polyblend (HDPE/PS), MELTING\_I—by heat conduction, MELTING\_II—by energy dissipation [131].

Later, the basic research in this field was performed first by Potente et al. [136,137], and then by Steller et al. [138,139] as well as by Covas et al. [140]. Recently, Wilczyński et al. [141] performed experimental studies on the melting mechanism of polymers in injection molding machines. It has been observed that melting in the injection molding machine occurs to some extent, according to the Tadmor mechanism, with clearly visible starvation (Figure 8).





The existing models of the injection molding process (plasticating unit) [136–140] differ from the extrusion models in that they involve the static and dynamic phases of melting (stationary and rotating screw) with an axial screw movement. However, it is assumed that the screw is fully filled with a material such as in the flood fed extrusion (Figure 2), which is inconsistent with Figure 8 where starvation is clearly seen in the starve fed extrusion (Figure 4).

## 2.3. Melt Conveying Section

The first analysis of flow in a single screw machine (screw pump) was performed by Rowell and Finlayson [142] for viscous oils who modeled the drag flow and pressure flow for an isothermal Newtonian fluid. This analysis was rediscovered by Carley et al. [143] and applied to the screw extrusion of polymers. It is not well known among the experts that Maillefer [144] developed nearly the same equations ahead of the publication of Carley et al. [143].

These basic studies analyzed one-dimensional flow through a rectangular channel of infinite width. Later, these models were improved by considering the transverse flow caused by the screw flights (Carley and Strub [145], Squires [146]), the effect of channel curvature (Booy [147], Squires [148]), and the effect of flight clearance (Mallouk and Mc Kelvey [149], Maddock [150]).

In later analyses, the simplest non-Newtonian case was considered, which is a one-dimensional isothermal flow of the power-low fluid in a channel of infinite width, both analytically (Kroesser and Middleman [151], Middleman [152]) and numerically (Colwell and Nicholls [153]). Afterward, two-dimensional flow was considered (Griffith [154], Zamodits and Pearson [155]). These basic studies were summarized and expanded first by McKelvey [1] and then by Tadmor and Klein [2].

Since the pioneering and fundamental work of Tadmor and Klein [2], many researchers have attempted to improve the basic models by considering two-dimensional or three-dimensional flow, taking into account the non-Newtonian characteristics of the polymer melt and the actual screw geometry or using a better approach for the thermal analysis, while considering mechanical/thermal coupling (Fenner [156], Lindt et al. [157,158], Lawal and Kalyon [159], Spalding et al. [160], Syrjala [161,162], and Ilinca and Hetu [163]). Recently, Miethlinger et al. [164–166] proposed a heuristic method for two-dimensional or three-dimensional modeling of the flow of power-law fluids in metering sections of single screw extruders.

In addition to the primary flow field in the metering section of the single-screw extruder, for sharp flight screw root corners, Polychronopoulos and Vlachopoulos [167] determined a secondary flow in front of the root of the pushing flight and behind the root of the trailing flight, akin to what is known in fluid mechanics as Moffatt eddies. Due to extremely large times required for fluid particles to travel along the helical Moffatt eddy path lines, degradation is likely.

It should be noted in this case that, when modeling the flow in the melt conveying section, most authors assume the screw is stationary and the barrel rotates. Campbell and Spalding [9] take the position that the rotating barrel and rotating screw produces significantly different results in modeling. The detailed discussion of these two approaches has been performed by Rauwendaal [8].

Contrary to melt conveying in single screw extruders, the studies on melt conveying in twin-screw extruders were limited. The first experimental studies of flow in co-rotating twin-screw extrusion were performed by Erdmenger [168,169] who observed that material moved forward in the machine in a roughly helical eight-figure motion. The pumping mechanism of the co-rotating twin-screw extruder is a drag-induced flow much like that of the single-screw extruder. The geometry of the co-rotating intermeshing twin-screw configuration was studied in detail by Booy [170]. Newtonian flow models for fully filled elements were developed by Booy [171], Denson and Hwang [172], Szydłowski and White [173,174], and Tayeb et al. [175,176]. Later, non-Newtonian models were developed, e.g., by White et al. [177–180] and Potente et al. [181]. Todd [182] discussed the drag and pressure flows in twin-screw extruders. Recently, fully three-dimensional non-Newtonian FEM (Finite Element Method) computations were performed and the state-of-the-art tool was discussed by Ilinca and Hetu [163], Malik et al. [183], and Vergnes et al. [184] who compared the results of 3D simulations to the results issuing from the 1D Ludovic software. The 3D simulation method was found to be more accurate to describe flows in kneading discs, but the 1D model provided very satisfactory results for flows in screw elements. Several recent papers on modeling of co-rotating twin-screw extrusion may also be cited in this case [185–191].

Intermeshing counter-rotating twin-screw extruders are fundamentally different from single-screw machines, as well as from co-rotating twin-screw machines. They were first discussed by Kiesskalt [192], Montelius [193], and Schenkel [16] as positive displacement pumps whose throughput is controlled by screw geometry and screw speed. Doboczky [55,194] and Janssen et al. [117,195,196] developed flow pumping characteristics for these machines, and they gave primary attention to understanding the leakage flows between the screws, and between the screws and barrel. White and Adewale [197] developed a more general flow model considering the level of intermeshing in the machine. A numerical FEM simulation for an intermeshing counter-rotating twin-screw extruder was presented by Li and Manas-Zloczower [198], and by Kajiwara et al. [199]. However, no attention was given to screw pumping characteristics. Hong and White [200,201] presented a FAN analysis (Flow Analysis Network) of flow in this machine, and applied this method to non-Newtonian flow behavior. They have determined screw characteristic curves for various screw elements. This allowed us to model the flow for various modular screw designs and calculate pressure, fill factor, and temperature profiles. Schneider presented the historical development of the counter-rotating twin-screw extrusion [202]. Recently, Wilczyński and Lewandowski [203] performed a fully three-dimensional non-Newtonian FEM computation to design the screw pumping characteristics for counter-rotating extruders. An analysis included the flow in the C-chamber, and the leakage flows were identified over the calender gap, tetrahedron gap, flight gap, and side gap.

Currently, 3D FEM computations are available for single-screw extrusion and twin-screw extrusion, for which flow simplifications are minimized. These approaches accurately describe the velocity and temperature distributions and the pressure/flow rate relationships, but they require large computing resources and major calculation time. The POLYFLOW software package [204] can be used for simulating various aspects of extrusion including SSEs, TSEs, and die flows including viscoelastic effects.

For the major calculation time, these approaches cannot be used for global modeling of the extrusion process, which requires hundreds of computing iterations. In order to avoid the time-consuming computations during each iterative computing loop, the concept of screw pumping characteristics was developed, which are defined as the functional dependencies of the dimensionless flow rate and dimensionless pressure gradient [4]. These characteristics can be modeled by regression analysis and then implemented into the iterative computations by providing reasonable computation accuracy and computation time. Such characteristics were developed both for single-screw extrusion and twin-screw extrusion, e.g., by White and Potente [4], Rauwendaal [8], and by Wilczyński et al. [128,203,205,206], which are shown in Figure 9.

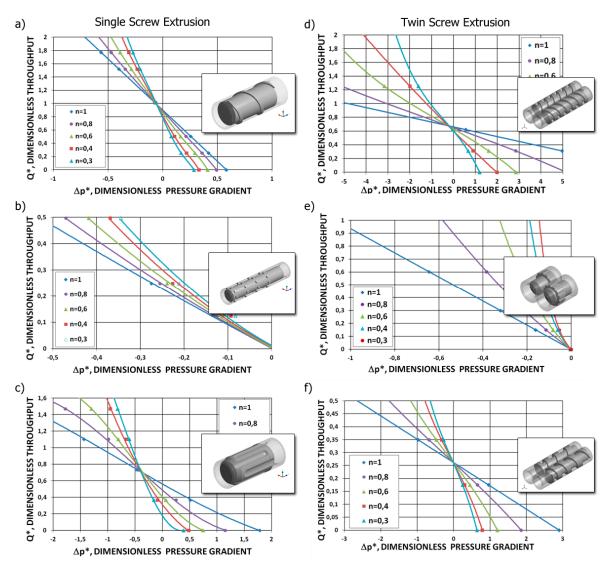


Figure 9. Screw pumping characteristics [128,206]: single-screw extrusion, (a) conventional screw, (b) mixing section, (c) Maddock section, counter-rotating twin-screw extrusion, (d) thick flighted section, (e) shearing section, and (f) thin flighted section.

# 3. Computer Models of Extrusion

In the modeling of polymer processing, the models are generally deterministic, transport phenomena-based, either steady (continuous processes) or unsteady (cyclic processes), and of distributed parameters or locally lumped parameters. For engineering purposes, the lumped parameter models may be generally sufficient. The main goal of engineering designs is to predict the pressure and mean polymer melt temperature profiles along the machine for a given screw and die geometry as a function of the process operating conditions. In these models, the screw channel is usually divided into short axial segments (increments), where the input temperature and pressure parameters come from the calculation in the previous segment. In addition, the output parameters from the current segment are the input parameters for the next segment. Within each segment, the local parameters are assumed to be constant.

The lumped parameter approach becomes particularly useful when dealing with plasticating processes, like extrusion and injection molding, where, in addition to the melt flow, we are faced with the solids' transport and melting of the material.

With immense progress in the computational fluid dynamics, the current trends in modeling polymer processing apply very sophisticated numerical (e.g., finite element) methods. This

includes both two-dimensional and three-dimensional computations of velocity, stress, pressure, and temperature fields with a variety of boundary conditions for shear-thinning and temperature-dependent, sometimes viscoelastic, fluids. In real extruders and injection molding machines, however, there is a lot of other problems that are still unsolved, and, at present, these methods are generally not applied for comprehensive (global) modeling of these screw processes.

The state-of-the-art for composite modeling of screw processes was presented in some fundamental books, e.g., by White and Potente [4], Rauwendaal [8], and Agassant et al. [11], as well as in some review papers, e.g., by Ariffin et al. [207], Wilczynski et al. [208], Teixeira et al. [209], and Malik et al. [183]. Single-screw extrusion, twin-screw extrusion, both co-rotating and counter-rotating, and injection molding were considered. The flood fed and starve fed operations were also discussed.

Tadmor and Klein [63] developed the first computer program EXTRUD for simulation of the extrusion process, which was described in Reference [2]. Afterward, Klein and Klein [210] presented the SPR (Scientific Process Research) extrusion simulation system. Next, several other computer programs for a single-screw extrusion were developed, e.g., Agur and Vlachopoulos [211] developed the NEXTRUCAD program, Potente et al. [212,213] built the REX program, Sebastian and Rakos [214] presented the PASS system (Polymer Analysis Simulation System), and Wilczyński [215,216] developed the SSEM program (Single Screw Extrusion Model). Other computer models were developed by Fukase and Kunio [217], Zavadsky and Karnis [218], Vincelette et al. [219], and Amellal and Lafleur [220]. Recently, Wilczyński et al. [221] developed the computer program for simulating the single-screw extrusion of wood polymer composites.

Research on the co-rotating twin-screw extrusion was initiated by White and his co-workers. On the basis of the melt flow studies [173,174] and the polymer melting studies [52,113], the computer model of co-rotating twin-screw extrusion Akro-Co-Twin [222–224] was developed. Independent studies performed by Potente [53,112,181] led to the development of the SIGMA program [225,226]. The research carried out by Vergnes et al. [114,115,176] led to the development of the LUDOVIC program [227]. Canedo [228] built TXSTM program, and Teixeira et al. [209] developed the global software for co-rotating extruders.

Research on the counter-rotating twin-screw extrusion was also initiated by White and his co-workers. Based on the melt flow studies [200,201] and the polymer melting studies [56,120] (Figure 3), the first computer model of counter-rotating twin-screw extrusion Akro-Counter-Twin was developed [229,230]. These studies were continued by Wilczyński et al. [231,232] who developed the TSEM program (Twin Screw Extrusion Model).

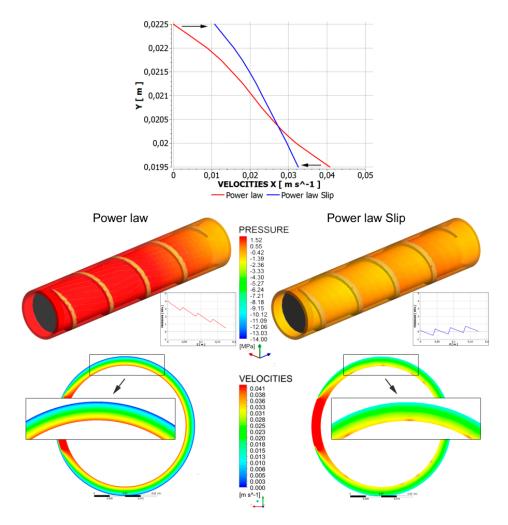
Research on the starve fed single screw extrusion was much more limited. Wilczyński et al. based on the polymer melting studies [59,127] developed the first, and, up to now, the only available computer model of this process SSEM-Starve [128]. This model was later extended to non-conventional screw configurations [205,206], and to the extrusion of polymer blends [233,234]. Recently, the global model GSEM (Global Screw Extrusion Model) was developed, which allows the modeling of single screw extrusion both in the flood fed and starve fed mode [205].

When modeling polymer extrusion, it is generally assumed that there is no slippage at the fluid/solid interface, and flowing materials in the screw extruders and dies adhere to the wall. However, there are several materials like filled polymers (e.g., wood polymer composites), elastomers, polymers like poly(vinyl chloride) and high-density polyethylene, and polymer suspensions, which exhibit wall slippage under certain conditions.

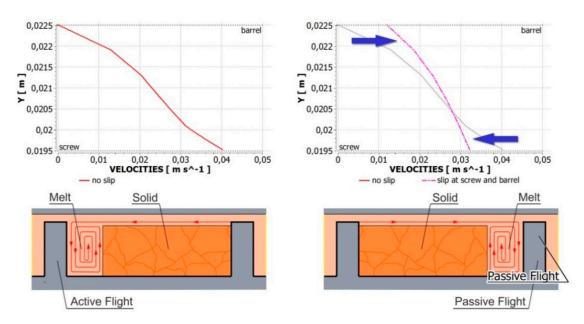
The phenomenon of wall slippage was studied first by Mooney [235]. Afterward, several studies were performed to answer how best to consider wall slippage when designing extruders. An extensive review on this subject was presented by Potente et al. [236]. Worth and Parnaby [237] presented an analysis of the effects of the wall slip on the extrusion throughput and power consumption for a one-dimensional isothermal Newtonian flow, and reported that power consumption in the extruder is reduced as a result of wall slippage. Meijer and Verbraak [238] performed two-dimensional Newtonian isothermal analysis, and showed an influence of slip on the velocity profiles and pumping characteristics

of the extruder. Lawal and Kalyon [239,240] developed an analytical model describing single-screw extrusion of viscoplastic fluids with different slip coefficients at screw and barrel. Kalyon et al. [241] as well as Malik et al. [183] studied numerically co-rotating twin-screw extrusion with wall slippage at the barrel and screws. Potente and his co-workers, e.g., [236,242–246] performed very extensive studies on modeling single-screw extrusion with slip effects, both analytically and numerically, by calculating the pressure/throughput and drive power behavior, as well as the melt temperature development in single-screw extrusion of wall-slipping polymers. Several studies were performed on modeling the flow of wall slipping polymers in the dies, e.g., by Ferras et al. [247], Hatzikiriakos and Mitsoulis [248], and Gupta [249].

Recently, Lewandowski and Wilczyński [250,251] performed an extensive fully three-dimensional non-Newtonian FEM study on the polymer melt flow with slip effects in the single-screw extruder to design the screw/die pumping characteristics, which may be implemented into the composite model of the process. An analysis was performed for the flow of polymers with slip effects both in the screw (on the screw and barrel surfaces) and in the die. An example of simulation is depicted in Figure 10, which shows slipping at the screw/barrel surfaces. A possible melting mechanism changing, as reported in the literature [65,66], is depicted in Figure 11. The molten material may accumulate at the passive flight of the screw, which is not consistent with the Tadmor mechanism of melting.



**Figure 10.** Screw flow simulations: pressure/velocity distributions for the power law model at slip/no slip conditions [251].



**Figure 11.** Slip effects and melting: (**a**) velocity distribution without a slip, and with slipping, and (**b**) possible melting mechanisms.

Currently, it is established that extrusion of wall-slipping polymers results in the reduction of the die pressure, and the screw characteristics changing, which affects the operating point of the extruder, and results in the global modeling of extrusion of wall-slipping polymers. This requires developing models both for the screw (plasticating unit) and for the extrusion die.

When modeling polymer extrusion, it is also generally assumed that flowing materials in the screw extruders and dies have no yield stress. However, it is well known that many materials have a yield stress, e.g., filled polymers, composites, and blood, paints, cosmetics, and foodstuffs such as margarine, mayonnaise, butter, and ketchup. These materials were first described by Bingham [252], and, later, a number of works related to viscoplastics were reviewed by Bird et al. [253] and Mitsoulis [254].

Compared to fundamental studies on the viscoplastic flows, much less research was devoted to the viscoplastic flows in the extrusion process. Laval and Kalyon [239,240] first developed analytical models of the single-screw extrusion of viscoplastic fluids described by the Herschel-Bulkley model. Later, Kalyon et al. [241] presented a combined experimental and finite element study of the flow and heat transfer in twin-screw extrusion of concentrated suspensions using the Herschel-Bulkley model.

Recently, Lewandowski and Wilczyński [251,255] performed an extensive fully three-dimensional non-Newtonian FEM modeling study on the viscoplastic flows in the single-screw extruder to design the screw/die pumping characteristics, which may be implemented into the composite model of the process. An analysis was performed for the flow with yield stress effects both in the screw and in the die. An example of simulation is depicted in Figure 12 where the flat velocity profile in the central part of the flow may be seen for some yield stresses.

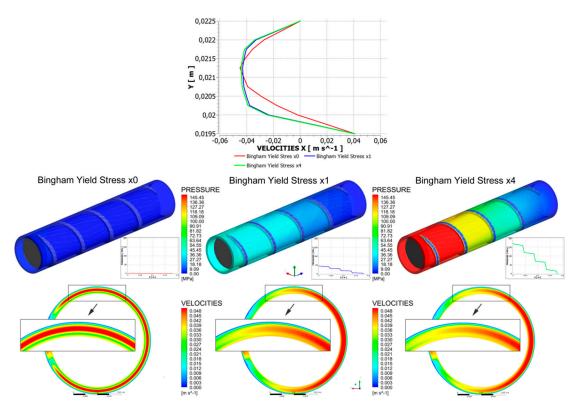


Figure 12. Screw flow simulations: pressure/velocity distributions for Bingham model [251].

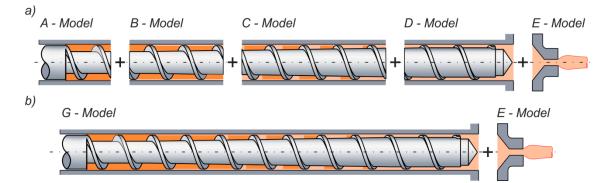
## 4. Global Modeling of the Extrusion Process

Extrusion is a continuous process of co-operation of the extruder (screw) and the die. Physical phenomena occurring in the extruder determine the flow in the extrusion die and vice versa. The flow in the die determines the phenomena occurring in the extruder. Any change in the processing conditions in the extruder causes a change in the processing conditions in the die and vice versa. Modeling of the extrusion process cannot be limited to the modeling of flow in the extruder and must include the extrusion die.

The term global modeling means modeling the interacting phenomena occurring in the extruder and the die, which entails modeling the extruder/die system (or screw/die system).

The classical global modeling of the extrusion process is based on the separate models for each section of the screw, i.e., solid transport section, melting and pre-melting sections, and melt flow section, and the global model consists of these elementary models (Figure 13). In this case, the computations are performed step-by-step in the elementary segments of the screw, and the output process parameters from the current segment are the input parameters for the next one.

Global modeling requires the use of a computation algorithm appropriate for a given type of extrusion. For classical (flood fed) extrusion, the forward scheme of computation is suitable. In this case, the flow rate of the material is not known, and is the result of the screw/die co-operation and must be determined in multiple iterative computations. For extrusion with starvation, the backward scheme of computation is applied, i.e., the inverse computation algorithm since the pressure profile is not continuous in this scenario, and there is no continuous flow rate/pressure relation. In this case, the flow rate is established and equal to the flow rate of the material metered by the dosing device (Figure 14).



**Figure 13.** Modeling concepts: (**a**) classical modeling: A—solid conveying model, B—pre-melting model, C—melting model, D—melt conveying model, E—die flow model, (**b**) continuum modeling: G—continuous model.

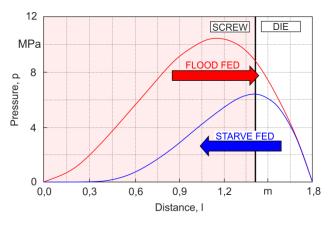
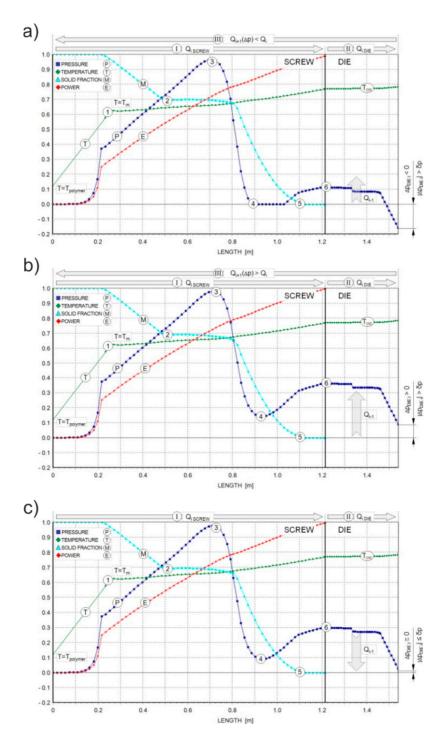


Figure 14. A forward scheme of computations for flood fed extrusion, and a backward scheme of computations.

Simulation schemes for flood fed single-screw extrusion are relatively well known [210–216]. In this case, the modeling proceeds from the hopper to the die, according to the forward scheme of calculations (Figure 14), and the extrusion operating point is searched, which defines the extrusion flow rate and die pressure. The flow rate is not known, and results from the extruder/die co-operation. Computations start for some presumed flow rate, e.g., equal to the drag flow rate, and solid conveying, melting, melt conveying, and die flow are simulated. The calculated pressure at the die exit is compared to the atmospheric pressure. The computation is achieved when both pressures are equal. Otherwise, the presumed flow rate is modified and computations are iteratively repeated until the convergence is reached. A scheme of such computations is depicted in Figure 15. The arrows indicate the direction of computations, which are forward computations in the screw (I) and die (II) sections, and a backward step (III) to repeat computations for the new flow rate.

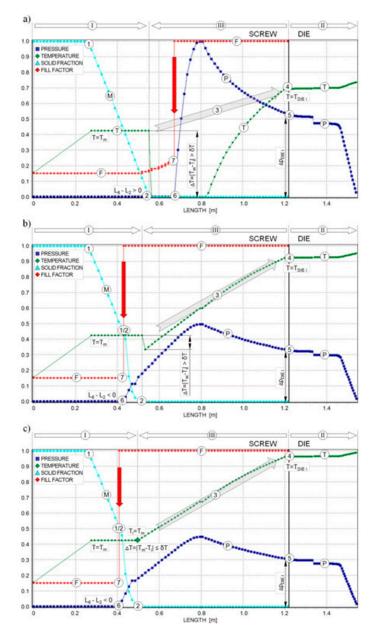
In the case depicted in Figure 15, the computations are repeated for a modified presumed flow rate, and, after hundreds of iterations, the convergence is reached (Figure 15c).



**Figure 15.** Scheme of computation for flood fed single screw extrusion: (a)  $\Delta p_{die} < 0$ , (b)  $\Delta p_{die} > 0$ , (c)  $|\Delta p_{die}| < \delta_p$ , 1—start of melting, 2—start of compression section, 3—pressure max, 4—end of pressure drop, 5—end of melting, 6—pressure at screw exit (die inlet), *Q*—flow rate,  $Q_{i+1}$ —next iteration flow rate, p—pressure,  $\Delta p_{die}$ —die pressure at die exit,  $\delta_p$ —accuarcy of pressure computation, *T*—temperature,  $T_m$ —melting point,  $T_{die}$ —die melt temperature, *M*—solid fraction (melting), *E*—power consumption.

Simulation schemes for starve fed single-screw extrusion are much less known [128,205,206]. In this case, the modeling requires an inverse approach. The flow rate is known, and is equal to the feeding rate. However, since the screw is not completely filled with the polymer, the computations cannot be processed from the hopper to the die. In this case, the die pressure is computed first for a presumed polymer melt temperature. Then, the pressure gradient along the screw is computed using

the screw pumping characteristics. When the pressure falls to zero, the starvation begins and the screw filling is computed. The calculated temperature at the end of melting is compared to the melting point, and the computation is achieved when both temperatures are equal. Otherwise, the presumed melt temperature is modified and computations are iteratively repeated until the convergence is reached. A scheme of such computations is depicted in Figure 16. The arrows indicate the direction of calculations, such as forward calculations in the melting (I) and die (II) sections, and backward calculations in the melting the melting (II) and die (III) sections.



**Figure 16.** Computation scheme: (**a**) one-stage melting mechanism, computation discrepancy, (**b**) two-stage melting mechanism, computation discrepancy, (**c**) computation convergency: (I), forward computations in the melting section, (II) forward computations in the die section, (III), backward computations in the melt conveying section, (*M*), melting (*SF*), (*F*), filling (fill factor), (*T*), temperature, (*P*), pressure, (1), start of melting, (2) end of melting, (3) transfer of computations to the die, (4) start of die melt temperature computation, (5) start of die pressure computation, (6) zero pressure location, (7) beginning of filling computation (partly filled region starts),  $\Delta P_{\text{DIEi}}$ , die pressure,  $T_{\text{DIEi}}$ , presumed melt temperature,  $T_{\text{m}}$ , melting point, *i*, number of iterations,  $\Delta T = |T_{\text{m}} - T_{\text{i}}|$ , convergency checking, and  $\delta T$ , computation accuracy [206].

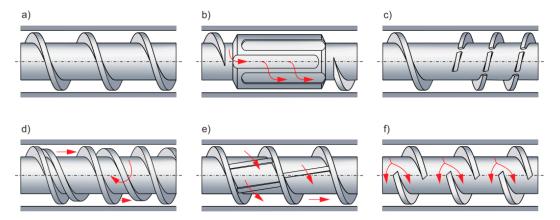
In the case depicted in Figure 16, the computations are repeated for a modified presumed exit temperature, and the second stage of melting appears (Figure 16b). Thus, the computation scheme gets much more complicated since the location of the transition partially/fully filled screw has to be determined. At this location, the second stage of melting starts, and the second melting mechanism is included into the computations. After hundreds of iterations, the convergence is reached (Figure 16c).

Using this inverse computation approach, the authors developed the composite models for closely intermeshing counter-rotating twin-screw extruders [229,231,232]. This was also applied by other researchers for co-rotating twin-screw extruders [222,226,227]. However, those composite models using one-stage melting models were much simpler in execution. Moreover, the location of the melting regions was not computed but specified previously in those cases.

# 5. Future Concepts

In the extrusion process, both single-screw extrusion and twin-screw extrusion (co-rotating and counter-rotating), flood fed or starve fed, the modeling of polymer melting consists of performing an experiment to get to know the melting mechanism, then proposing the physical model of this mechanism, and, lastly, developing the mathematical model. Thus, these models are not overall models, and are limited to the specific extrusion method.

These models are also not general in nature because of the material being processed. For example, melting of polymers that exhibit slippage during the flow does not follow the Tadmor model because the molten material does not accumulate at the active flight of the screw, but flows toward the passive flight. These models are also not general in view of the operating and geometrical parameters of the process. For example, the melting mechanism may vary substantially depending on the screw geometry (Figure 17) as well as on the screw speed.

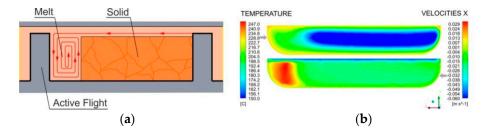


**Figure 17.** Conventional and non-conventional screw configurations: (**a**) conventional section, (**b**) Maddock section, (**c**) mixing section, (**d**) Maillefer section, (**e**) Barr section, and (**f**) Rheotoc section.

In conclusion, the currently available extrusion models are not general in nature due to limitations of the extrusion type, specific material, and specific operating and geometrical conditions of the process. Therefore, the question arises whether it is possible to solve the problem of global modeling of the extrusion process without referring to the specific solid/melt flow mechanism, which is determined by the extrusion method, the material type, and the process conditions.

So far, there is no global model of the extrusion process, which would not be limited in this range. Therefore, the concept may be proposed to solve this problem on the basis of fluid mechanics using CFD (Computational Fluids Dynamics) computation procedures.

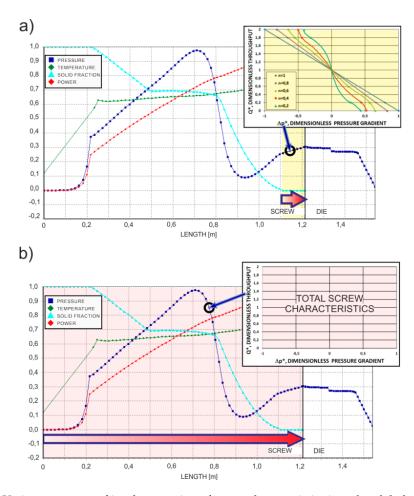
Instead of the specific solid/melt flow mechanism assumed, the polymer flow in the extrusion process can be simulated by solving the conservation equations of mass, motion, and energy along with a polymer constitutive equation, which was proposed by some researchers for the melting section [100–105]. An example of such computations is depicted in Figure 18.



**Figure 18.** Example of modeling: (**a**) geometrical model of the melting mechanism, and (**b**) temperature and velocity distribution in the cross-section of the screw channel.

This novel approach based on solving the conservation equations without an assumed polymer flow mechanism seems to be very promising for the future work on modeling the extrusion process, even though it requires very large computational capabilities.

The global modeling of the extrusion process, however, requires iterative computations to define the process operating point, and the question arises regarding how to implement the continuum computations into the global model of the process. This might be solved by developing a novel concept of the total (continuous) screw characteristics, which is schematically depicted in Figure 19, similarly to the screw pumping characteristics valid for the melt flow region [128,203,205,206], which are shown in Figure 9.



**Figure 19.** Various concepts of implementation of screw characteristics into the global model of the extrusion process: (a) screw pumping characteristics implemented into the melt region, (b) total (continuous) screw characteristics implemented into the entire area of the screw. Example of modeling.

The most promising approach would be the coupled DEM/CFD modeling. Very recently, a coupling between EDEM, a DEM software, and OpenFOAM, which is an open-sourced computational fluid dynamics CFD software, has been developed and is now under testing. The initial version of this coupling allows for momentum transfer between EDEM and OpenFOAM, with a heat transfer capability to be implemented. The coupling overcomes one of the common limitations with DEM/CFD coupled simulations, namely that particles must be smaller in volume than the mesh cells they occupy, which allows for a wide range of application types that were previously not possible.

## 6. Conclusions

An issue of global modeling of polymer extrusion was reviewed and discussed, which includes modeling for solid conveying, melting, and melt flow, as well as co-operation of the screw/die system.

It was observed that the basis of computer extrusion models are still the early models of solid conveying and polymer melting, and no significant progress has been made in recent years. Extrusion modeling using a discrete element method (DEM) for solid conveying, and computational fluid dynamics (CFD) for polymer melting may be promising in this respect.

It was also observed that the extrusion models are generally limited to neat polymers. When modeling the polymer extrusion, it is assumed that there is no slippage at the fluid/solid interface, and flowing materials in the screw extruders and dies adhere to the wall. It is also assumed that flowing materials have no yield stress. However, there are many materials like filled polymers (e.g., wood polymer composites) that have a yield stress and exhibit wall slippage under certain conditions.

Limitations of the traditional approach to modeling based on an assumed polymer solid/melt flow mechanism were presented, and the novel continuous concept of global modeling based on solving the conservation equations without an assumed polymer flow mechanism was proposed. A concept of the total (continuous) screw characteristics was discussed to solve the problem of implementing the continuum computations into the global model of the process. Promising progress in coupled DEM/CFD modeling was indicated.

Author Contributions: Conceptualization, K.W. Methodology, K.W. Software, A.N. Validation, A.L., K.J.W., and K.B. Investigation, A.N., A.L., K.J.W., and K.B. Writing—original draft preparation, K.W. Writing—review and editing, K.W. Visualization, A.N., A.L., K.J.W., and K.B. Supervision, K.W.

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflict of interest.

#### References

- 1. McKelvey, J.M. Polymer Processing; John Wiley & Sons Inc.: New York, NY, USA, 1962; ISBN 978-0471584438.
- Tadmor, Z.; Klein, I. Engineering Principles of Plasticating Extrusion; Van Nostrand Reinhold, Co.: New York, NY, USA, 1970; ISBN 978-0442156350.
- 3. White, J.L. Rubber Processing; Hanser Publishers: Munich, Germany, 1995; ISBN 978-3446166004.
- White, J.L.; Potente, H. Screw Extrusion. Science and Technology; Hanser Publishers: Munich, Germany, 2003; ISBN 978-3-446-19624-7.
- 5. Tadmor, Z.; Gogos, C.G. *Principles of Polymer Processing*, 2nd ed.; John Wiley & Sons Inc.: New York, NY, USA, 2006; ISBN 978-0-471-38770-1.
- White, J.L.; Kim, E.K. Twin Screw Extrusion. Technology and Principles, 2nd ed.; Hanser Publishers: Munich, Germany, 2010; ISBN 978-1569904718.
- Hensen, F.; Knappe, W.; Potente, H. Handbuch der Kunststoff-Extrusiontechnik. Grundlagen; Carl Hanser Verlag: Munich, Germany, 1989; ISBN 978-3446143395.
- 8. Rauwendaal, C. *Polymer Extrusion*, 5th ed.; Carl Hanser Verlag: Munich, Germany, 2014; ISBN 978-1-56990-516-6.
- 9. Campbell, G.A.; Spalding, M.A. *Analyzing and Troubleshooting Single-Screw Extruders*; Carl Hanser Verlag: Munich, Germany, 2013; ISBN 978-3-446-41371-9.

- 10. Chung, C.I. *Extrusion of Polymers. Theory and Practice*, 2nd ed.; Carl Hanser Verlag: Munich, Germany, 2010; ISBN 978-1-569-904596.
- 11. Agassant, J.F.; Avenas, P.; Carreau, P.J.; Vergnes, B.; Vincent, M. *Polymer Processing. Principles and Modelling*, 2nd ed.; Carl Hanser Verlag: Munich, Germany, 2017; ISBN 978-1-56990-605-7.
- 12. Agassant, J.F.; Andersen, P.G.; Anderson, P.D.; Ban, K.; Bousmina, M.; Bumm, S.H.; Canedo, E.L.; Elemans, P.H.M.; Feke, D.L.; Feng, L.-F.; et al. *Mixing and Compounding of Polymers. Theory and Practice*, 2nd ed.; Manas-Zloczower, I., Ed.; Carl Hanser Verlag: Munich, Germany, 2009; ISBN 978-3-446-40773-2.
- 13. Osswald, T.; Hernandez-Ortiz, J.P. *Polymer Processing. Modeling and Simulation*; Carl Hanser Verlag: Munich, Germany, 2006; ISBN 978-3-446-40381-9.
- 14. Fisher, E.G. Extrusion of Plastics, 1st ed.; Iliffe Books Ltd.: London, UK, 1958.
- 15. Bergen, J.T.; Bernhardt, E.C.; Beyer, C.S.; Carley, J.F.; Cash, F.M.; Dahl, R.B.; Darnell, W.H.; Hearst, T.M.; Kovach, G.P.; Marshall, D.I.; et al. *Processing of Thermoplastic Materials*; Bernhardt, E.C., Ed.; Reinhold Publishing Corporation: New York, NY, USA, 1959.
- 16. Schenkel, G. Kunststoff-Extrudertechnik; Carl Hanser Verlag: Munich, Germany, 1963.
- 17. Pearson, J.R.A. Mechanical Principles of Polymer Melt Processing; Pergamon Press: Oxford, UK, 1966.
- 18. Fenner, R.T. Extruder Screw Design; Iliffe Books Ltd.: London, UK, 1970.
- 19. Torner, R.V. Grundprozesse der Verarbeitung von Polymeren; VEB Deutscher Verlag: Leipzig, Germany, 1974.
- 20. Middleman, S. Fundamentals of Polymer Processing; McGraw-Hill: New York, NY, USA, 1977; ISBN 978-0070418516.
- 21. Potente, H. Auslegen von Schneckenmaschinen Baureihen; Carl Hanser Verlag: Munich, Germany, 1981; ISBN 978-3446133846.
- 22. Pearson, J.R.A.; Crochet, M.J.; Walters, K.; Tanner, R.I.; Fenner, R.T.; Richardson, S.M.; Denn, M.M.; Petrie, C.J.S.; Kistler, S.F.; Scriven, L.E.; et al. *Computational Analysis of Polymer Processing*; Pearson, J.R.A., Richardson, S.M., Eds.; Elsevier Publisher: London, UK, 1983; ISBN 978-94-009-6634-5.
- 23. Barone, M.R.; Forger, R.D.; Bernhardt, E.C.; Tucker, C.L.; Kamal, M.R.; Michael, E.R.; Lee, C.-C.; Castro, J.M.; Richardson, S.M.; Güceri, S.I.; et al. *Fundamentals of Computer Modeling for Polymer Processing*; Tucker, C.T., Ed.; Hanser Publishers: New York, NY, USA, 1989; ISBN 978-3446147041.
- 24. Rao, N.S. Computer Aided Design of Plasticating Screws: Programs in Fortran and Basic; Hanser Publishers: New York, NY, USA, 1986; ISBN 978-1569900826.
- 25. Erwin, L.; Elmendorp, J.J.; Tucker, C.L.; Rauwendaal, C.; Dreiblatt, A.; Eise, K.; Jansen, L.P.B.M.; Nichols, R.; Manas-Zloczower, I.; Kearney, M.R.; et al. *Mixing in Polymer Processing*; Rauwendaal, C., Ed.; M. Dekker: New York, NY, USA, 1991; ISBN 978-0824785215.
- 26. Bernhardt, E.C.; Bertacchi, G.; Crochet, M.J.; Debbaut, B.; Harms, R.; Mitsoulis, E.; O'Brien, K.T.; Rao, N.S.; Vlachopoulos, J.; Silvi, N.; et al. *Computer Modeling for Extrusion and Other Continuous Polymer Processes*; O'Brien, K.T., Ed.; Hanser Publishers: New York, NY, USA, 1992; ISBN 978-1569900680.
- 27. Baird, D.G.; Collias, D.I. *Polymer Processing: Principles and Design*; Butterworth-Heinemann: Oxford, UK, 1995; ISBN 978-0750691055.
- 28. Kohlgrüber, K. *Co-Rotating Twin-Screw Extruders;* Hanser Publisher: New York, NY, USA, 2008; ISBN 978-1569904220.
- 29. Vlachopoulos, J. Polymer Rheology and Extrusion; McMaster University: Hamilton, ON, Canada, 2011.
- 30. Hopmann, C.; Michaeli, W. *Extrusion Dies for Plastics and Rubber*, 4th ed.; Hanser Publisher: New York, NY, USA, 2016; ISBN 978-1-56990-623-1.
- 31. Martelli, F. *Twin–Screw Extruders: A Basic Understanding;* Van Nostrand Reinhold Co.: New York, NY, USA, 1983; ISBN 978-146-841-466-0.
- 32. Todd, D.B. Plastics Compounding; Carl Hanser Verlag: Munich, Germany, 1998; ISBN 978-344-615-861-0.
- 33. Kramer, W.; Stewart, E.; Martin, C.; Griff, A.; Wagner, J.R.; Fisher, T.; Smith, D.; Stoughton, P.; Morgan, C.; Hovis, G.; et al. *The SPE Guide on Extrusion Technology and Troubleshooting*; Wagner, J.R., Vlachopoulos, J., Eds.; Society of Plastic Engineers: Brookfield, CT, USA, 2001; ISBN 978-097-221-592-3.
- 34. Darnell, W.H.; Mol, E.A.J. Solids Conveying in Extruders. SPE J. 1956, 20, 20–29.
- 35. Schneider, K. Der Fördervorgang in der Einzugszone eines Extruders. Ph.D. Thesis, Rheinisch-Westfälische Technische Hochschule Aachen, Aachen, Germany, October 1968.
- Tadmor, Z.; Broyer, E. Solids Conveying in Screw Extruders—Part I: A Modified Isothermal Model. *Polym.* Eng. Sci. 1972, 12, 12–24. [CrossRef]

- 37. Tadmor, Z.; Broyer, E. Solids Conveying in Screw Extruders—Part II: A Modified Non-Isothermal Model. *Polym. Eng. Sci.* **1972**, *12*, 376–378. [CrossRef]
- 38. Campbell, G.A.; Dontula, N. Solids Transport in Extruders. Int. Polym. Proc. 1995, 10, 30–35. [CrossRef]
- 39. Hyun, K.S.; Spalding, M.A.; Hinton, C.E. Theoretical and Experimental Analysis of Solids Conveying in Single-Screw Extruders. *J. Reinf. Plast. Compos.* **1997**, *16*, 1210–1219. [CrossRef]
- Chung, C.I. Maximum Pressure Developed by Solid Conveying Force in Screw Extruders. *Polym. Eng. Sci.* 1975, 15, 29–34. [CrossRef]
- 41. Chung, C.I. Conveying in Screw Extruders. SPE-J. 1970, 26, 33–44.
- 42. Spalding, M.A.; Hyun, K.S. Coefficients of Dynamic Friction as a Function of Temperature, Pressure, and Velocity for Several Polyethylene Resins. *Polym. Eng. Sci.* **1995**, *35*, 557–563. [CrossRef]
- Leßmann, J.-S.; Weddige, R.; Schöppner, V.; Porsch, A. Modelling the Solids Throughput of Single Screw Smooth Barrel Extruders as a Function of the Feed Section Parameters. *Int. Polym. Proc.* 2012, 27, 469–477. [CrossRef]
- 44. Trippe, J.; Schöppner, V. Modeling of Solid Conveying Pressure Throughput Behavior of Single Screw Smooth Barrel Extruders under Consideration of Backpressure and High Screw Speeds. *Int. Polym. Process.* **2018**, *33*, 486–496. [CrossRef]
- 45. Fang, S.; Chen, L.; Zhu, F. Studies on the Theory of Single Screw Plasticating Extrusion. Part II: Non-Plug Flow Solid Conveying. *Polym. Eng. Sci.* **1991**, *31*, 1117–1122. [CrossRef]
- 46. Pohl, T.C.; Potente, H. Simulation and Analyses of the Polymer-Pellet-Flow into the First Section of a Single Screw. *SPE ANTEC Tech. Papers* **2001**, *59*, 185–189.
- 47. Moysey, P.A.; Thompson, M.R. Investigation of Solids Transport in a Single-Screw Extruder Using a 3-D Discrete Particle Simulation. *Polym. Eng. Sci.* **2004**, *44*, 2203–2215. [CrossRef]
- 48. Moysey, P.A.; Thompson, M.R. Modelling the Solids Inflow and Solids Conveying of Single-Screw Extruders Using the Discrete Element Method. *Powder Technol.* **2005**, *153*, 95–107. [CrossRef]
- 49. Moysey, P.A.; Thompson, M.R. Determining the Collision Properties of Semi-Crystalline and Amorphous Thermoplastics for DEM Simulations of Solids Transport in an Extruder. *Chem. Eng. Sci.* **2007**, *62*, 3699–3709. [CrossRef]
- 50. Moysey, P.A.; Thompson, M.R. Discrete Particle Simulations of Solids Compaction and Conveying in a Single-Screw Extruder. *Polym. Eng. Sci.* **2008**, *48*, 62–73. [CrossRef]
- 51. Carrot, C.; Guillet, J.; May, J.F.; Puaux, J.-P. Modeling of the Conveying of Solid Polymer in the Feeding Zone of Intermeshing Co-Rotating Twin Screw Extruders. *Polym. Eng. Sci.* **1993**, *33*, 700–708. [CrossRef]
- 52. Bawiskar, S.; White, J.L. Solids Conveying and Melting in a Starve Fed Self-wiping Co-Rotating Twin Screw Extruder. *Int. Polym. Proc.* **1995**, *10*, 105–110. [CrossRef]
- 53. Potente, H.; Melisch, U.; Palluch, K.P. A Physico-Mathematical Model for Solids Conveying in Co-Rotating Twin Screw Extruders. *Int. Polym. Proc.* **1996**, *11*, 29–41. [CrossRef]
- 54. Wong, A.C.-Y.; Liu, T.; Zhu, F. Solid Transportation in the Feeding Zone of Intermeshing Co-rotating Twin-Screw Extruders. *J. Polym. Res.* **2000**, *7*, 135–147. [CrossRef]
- 55. Doboczky, Z. Theoretische and wirkliche Ausstoßleistung der Doppelschnecken Extruder. *Plastverarbeiter* **1965**, *16*, 395–400.
- 56. Wilczyński, K.; White, J.L. Experimental Study of Melting in an Intermeshing Counter-Rotating Twin Screw Extruder. *Int. Polym. Proc.* **2001**, *16*, 257–262. [CrossRef]
- 57. Maddock, B.H. A Visual Analysis of Flow and Mixing in Extruder Screws. *SPE ANTEC Tech. Papers* **1959**, 15, 383.
- 58. Street, L.F. Plastifying Extrusion. Intern. Plast. Eng. 1961, 1, 289–296.
- 59. Wilczyński, K.; Lewandowski, A.; Wilczyński, K.J. Experimental Study for Starve-Fed Single Screw Extrusion of Thermoplastics. *Polym. Eng. Sci.* 2012, *52*, 1258–1270. [CrossRef]
- Tadmor, Z. Fundamentals of Plasticating Extrusion. I. A Theoretical Model for Melting. *Polym. Eng. Sci.* 1966, 6, 185–190. [CrossRef]
- 61. Marshall, D.I.; Klein, I. Fundamentals of Plasticating Extrusion. II. Experiments. *Polym. Eng. Sci.* **1966**, *6*, 191–197. [CrossRef]
- 62. Tadmor, Z.; Duvdevani, I.J.; Klein, I. Melting in Plasticating Extruders Theory and Experiments. *Polym. Eng. Sci.* **1967**, *7*, 198–217. [CrossRef]

- 63. Tadmor, Z.; Klein, I. *Computer Programs for Plastic Engineers*; Reinhold Book Corporation: New York, NY, USA, 1968.
- 64. Kacir, L.; Tadmor, Z. Solids Conveying in Screw Extruders. Part III: The Delay Zone. *Polym. Eng. Sci.* **1972**, 12, 387–395. [CrossRef]
- 65. Menges, G.; Klenk, K.P. Melting and Plasticating of Unplasticized PVC Powder in the Screw Extruder. *Kunststoffe* **1967**, *57*, 598–603.
- 66. Mennig, G. Observations Made in the Extrusion of Wall-Slipping Rigid PVC. Kunststoffe 1981, 71, 359–362.
- 67. Dekker, J. Improved Screw Design for the Extrusion of Polypropylene. Kunststoffe 1976, 66, 5–7.
- Donovan, R.C. A Theoretical Melting Model for Plasticating Extruders. *Polym. Eng. Sci.* 1971, 11, 247–257. [CrossRef]
- 69. Edmondson, I.R.; Fenner, R.T. Melting of Thermoplastics in Single Screw Extruders. *Polymer* **1975**, *16*, 49–56. [CrossRef]
- 70. Cox, A.P.D.; Fenner, R.T. Melting Performance in the Single Screw Extrusion of Thermoplastics. *Polym. Eng. Sci.* **1980**, *20*, 562–571. [CrossRef]
- 71. Lindt, J.T. A Dynamic Melting Model for a Single-Screw Extruder. *Polym. Eng. Sci.* **1976**, *16*, 284–290. [CrossRef]
- 72. Lindt, J.T. Pressure Development in the Melting Zone of a Single-Screw Extruder. *Polym. Eng. Sci.* **1981**, *21*, 1162–1166. [CrossRef]
- 73. Elbirli, B.; Lindt, J.T.; Gottgetreu, S.R.; Baba, S.M. Mathematical Modeling of Melting of Polymers in a Single-Screw Extruder. *Polym. Eng. Sci.* **1984**, *24*, 988–999. [CrossRef]
- 74. Lindt, J.T.; Elbirli, B. Effect of the Cross-Channel Flow on the Melting Performance of a Single-Screw Extruder. *Polym. Eng. Sci.* **1985**, *25*, 412–418. [CrossRef]
- 75. Shapiro, J.; Halmos, A.L.; Pearson, J.R.A. Melting in Single Screw Extruders. *Polymer* **1976**, *17*, 905–918. [CrossRef]
- 76. Halmos, A.L.; Pearson, J.R.A.; Trottnow, R. Melting in Single Screw Extruders. *Polymer* **1978**, *19*, 1199–1216. [CrossRef]
- 77. Vermeulen, J.R.; Gerson, P.M.; Beek, W.J. The Melting of a Bed of Polymer Granules on a Hot Moving Surface. *Chem. Eng. Sci.* **1971**, *26*, 1445–1455. [CrossRef]
- 78. Pearson, J.R.A. On the Melting of Solids Near a Hot Moving Interface, with Particular Reference to Beds of Granular Polymers. *Int. J. Heat Mass Tran.* **1976**, *19*, 405–411. [CrossRef]
- 79. Mount, E.M.; Watson, J.G.; Chung, C.I. Analytical Melting Model for Extrusion: Melting Rate of Fully Compacted Solid Polymers. *Polym. Eng. Sci.* **1982**, *22*, 729–737. [CrossRef]
- 80. Potente, H. An Analytical Model of Partial and Thorough Melting in Single-Screw Extruders. *Int. Polym. Proc.* **1991**, *6*, 297–303. [CrossRef]
- 81. Ingen Housz, J.F.; Meijer, H.E.H. The Melting Performance of Single Screw Extruders. *Polym. Eng. Sci.* **1981**, 21, 352–359. [CrossRef]
- Ingen Housz, J.F.; Meijer, H.E.H. The Melting Performance of Single Screw Extruders. II. *Polym. Eng. Sci.* 1981, 21, 1156–1161. [CrossRef]
- 83. Elbirli, B.; Lindt, J.T.; Gottgetreu, S.R.; Baba, S.M. Mathematical Modeling of Melting of Polymers in Barrier-Screw Extruders. *Polym. Eng. Sci.* **1983**, *23*, 86–94. [CrossRef]
- 84. Amellal, K.; Elbirli, B. Performance Study of Barrier Screws in the Transition Zone. *Polym. Eng. Sci.* **1988**, *28*, 311–320. [CrossRef]
- 85. Han, C.D.; Lee, K.Y.; Wheeler, N.C. A Study on the Performance of Barrier-Screw Extruders. *Polym. Eng. Sci.* **1991**, *31*, 831–841. [CrossRef]
- 86. Rauwendaal, C. Extruder Screws with Barrier Sections. Polym. Eng. Sci. 1986, 26, 1245–1253. [CrossRef]
- Gaspar-Cunha, A.; Covas, J.A. The Plasticating Sequence in Barrier Extrusion Screws Part I: Modeling. *Polym. Eng. Sci.* 2014, 54, 1791–1803. [CrossRef]
- 88. Gaspar-Cunha, A.; Covas, J.A. The Plasticating Sequence in Barrier Extrusion Screws Part II: Experimental Assessment. *Polym. Plast. Technol.* **2014**, *53*, 1456–1466. [CrossRef]
- 89. Grünschloß, E. A New Style Single Screw Extruder with Improved Plastification and Output Power. *Int. Polym. Proc.* **2002**, *17*, 291–300. [CrossRef]
- Grünschloß, E. A Powerful Universal Plasticating System for Single-Screw Extruders and Injection-Molding Machines. *Int. Polym. Proc.* 2003, 18, 226–234. [CrossRef]

- 91. Chung, C.I.; Choi, M.; Yoon, D.; Gunning, L.; Grünschloß, E. Performance of a HELIBAR Extruder Using a Grooved Barrel. *SPE ANTEC Tech. Papers* **2009**, *2*, 1192–1196.
- 92. Jin, X.-M.; Jia, M.-Y.; Xue, P.; Cai, J.-C.; Pan, L.; Yu, D.-Q. Study on the Melting Performance of Single Screw Extruder with Grooved Melting Zone and Barr Screw. *J. Mater. Process. Tech.* **2014**, *12*, 2834–2842. [CrossRef]
- 93. Avila-Alfaro, J.A.; Grünschloß, E.; Epple, S.; Bonten, C. Analysis of a Single Screw Extruder with a Grooved Plasticating Barrel—Part I: The Melting Model. *Int. Polym. Proc.* **2015**, *30*, 284–296. [CrossRef]
- 94. Kettemann, J.; Avila-Alfaro, J.A.; Bonten, C. Analysis of a Single-Screw Extruder with a Grooved Plasticizing Barrel—Experimental Investigation. *Int. Polym. Proc.* **2019**, *34*, 143–150. [CrossRef]
- 95. Liu, T.; Wong, A.C.-Y.; Zhu, F. Prediction of Screw Length Required for Polymer Melting and Melting Characteristics. *Int. Polym. Proc.* 2001, *16*, 113–123. [CrossRef]
- 96. Zhu, F. Extrusion Theory and Application; China Light Industry Press: Beijing, China, 2001.
- 97. Noriega, M.D.P.; Osswald, A.T.; Ferrier, N. In Line Measurement of the Polymer Melting Behavior in Single Screw Extruders. *J. Polym. Eng.* **2004**, *24*, 557–578. [CrossRef]
- Wang, D.; Min, K. In-Line Monitoring and Analysis of Polymer Melting Behavior in an Intermeshing Counter-Rotating Twin-Screw Extruder by Ultrasound Waves. *Polym. Eng. Sci.* 2005, 45, 998–1010. [CrossRef]
- Aigner, M.; Praher, B.; Kneidinger, C.; Miethlinger, J.; Steinbichler, G. Verifying the Melting Behavior in Single-Screw Plasticization Units Using a Novel Simulation Model and Experimental Method. *Int. Polym. Proc.* 2014, 29, 624–634. [CrossRef]
- 100. Yu, H.; Xu, B.; Wu, H.; Turng, L.-S.; Wang, M. A Visualization of Flow Patterns of Viscoelastic Fluid Partially Filled in a Co-Rotating Nontwin Screw Extruder. *Polym. Eng. Sci.* **2019**, *59*, E24–E32. [CrossRef]
- Viriyayuthakorn, M.; Kassahun, B. A Three Dimensional Model for Plasticating Extrusion Screw Design. SPE-ANTEC Tech. Papers 1985, 30, 81–84.
- Syrjala, S. A New Approach for the Simulation of Melting in Extruders. *Int. Commun. Heat Mass* 2000, 27, 623–634. [CrossRef]
- 103. Altinkaynak, A.; Gupta, M.; Spalding, M.A.; Crabtree, S.L. Melting in a Single Screw Extruder: Experiments and 3D Finite Element Simulations. *Int. Polym. Proc.* **2011**, *26*, 182–196. [CrossRef]
- 104. Hopmann, C.; Kremer, C.; Grammel, S. Predicting the Melting Behavior Within a Single Screw Extruder Using 3D FVM simulation. In Proceedings of the Polymer Processing Society 28th Annual Meeting (PPS-28), Pattaya, Thailand, 11–15 December 2012.
- Kazmer, D.O.; Grosskopf, C.M.; Venoor, V. Vortical Fountain Flows in Plasticating Screws. *Polymers* 2018, 10, 823. [CrossRef]
- Lewandowski, A.; Wilczyński, K. General Model of Polymer Melting in Extrusion Process. *Polimery* 2018, 63, 444–452. [CrossRef]
- 107. Todd, D.B. Melting of Plastics in Kneading Blocks. SPE ANTEC Tech. Papers 1992, 39, 2528–2536. [CrossRef]
- 108. Sakai, T. The Development of On-line Techniques and Novel Processing Systems for the Monitoring and Handling of the Evolution of Microstructure in Nonreactive and Reactive Polymer Systems. *Adv. Polym. Technol.* 1995, 14, 277–290. [CrossRef]
- Gogos, C.G.; Tadmor, Z.; Kim, M.H. Melting Phenomena and Mechanisms in Polymer Processing Equipment. *Adv. Polym. Technol.* 1998, 17, 285–305. [CrossRef]
- Qian, B.; Gogos, C.G. The Importance of Plastic Energy Dissipation (PED) to the Heating and Melting of Polymer Particulates in Intermeshing Co-Rotating Twin-Screw Extruders. *Adv. Polym. Technol.* 2000, 19, 287–299. [CrossRef]
- Qian, B.; Todd, D.B.; Gogos, C.G. Plastic Energy Dissipation and its Role on Heating/Melting of Single-Component Polymers and Multi-Component Polymer Blends. *Adv. Polym. Technol.* 2003, 22, 85–95. [CrossRef]
- 112. Potente, H.; Melisch, U. Theoretical and Experimental Investigations of the Melting of Pellets in Co-Rotating Twin-Screw Extruders. *Int. Polym. Proc.* **1996**, *11*, 101–108. [CrossRef]
- Bawiskar, S.; White, J.L. Melting Model for Modular Self Wiping Co-Rotating Twin Screw Extruders. *Polym. Eng. Sci.* 1998, *38*, 727–740. [CrossRef]
- 114. Vergnes, B.; Delacour, M.L.; Souveton, G.; Bouvier, J.M. A Study of Polymer Melting in a Co-Rotating Twin Screw Extruder. In Proceedings of the International Polymer Processing Society 15th Annual Meeting (PPS-15), Hertogenbosch, The Netherlands, 31 May–4 June 1999.

- 115. Vergnes, B.; Souveton, G.; Delacour, M.L.; Ainser, A. Experimental and Theoretical Study of Polymer Melting in a Co-rotating Twin Screw Extruder. *Int. Polym. Proc.* **2001**, *16*, 351–362. [CrossRef]
- Zhu, L.; Narh, K.A.; Geng, X. Modeling of Particle-Dispersed Melting Mechanism and its Application in Corotating Twin-Screw Extrusion. J. Polym. Sci. B Polym. Phys. 2001, 39, 2461–2468. [CrossRef]
- 117. Janssen, L.P.B.M. *Twin Screw Extrusion*; Elsevier Scientific Pub. Co.: Amsterdam, The Netherlands, 1978; ISBN 978-0444416292.
- Lim, S.; White, J.L. Flow Mechanisms, Material Distributions and Phase Morphology Development in a Modular Intermeshing Counter-Rotating Twin Screw Extruder of Leistritz Design. *Int. Polym. Proc.* 1994, 9, 33–45. [CrossRef]
- Cho, J.W.; White, J.L. Melting and Blending in a Modular Co-Rotating/Counter-Rotating Twin Screw Extruder. *Int. Polyrn Proc.* 1996, 11, 21–28. [CrossRef]
- 120. Wilczyński, K.; White, J.L. Melting Model for Intermeshing Counter-Rotating Twin-Screw Extruders. *Polym. Eng. Sci.* **2003**, *43*, 1715–1726. [CrossRef]
- Wang, D.; Min, K. Experiments and Analysis of Effect of Calender Gaps on Melting of PVC Powders in an Intermeshing Counter-Rotating Twin-Screw Extruder. *Int. Polym. Proc.* 2006, 21, 17–23. [CrossRef]
- 122. Wilczyński, K.; Lewandowski, A.; Wilczyński, K.J. Experimental Study of Melting of LDPE/PS Polyblend in an Intermeshing Counter-Rotating Twin Screw Extruder. *Polym. Eng. Sci.* **2012**, *52*, 449–458. [CrossRef]
- Lopez-Latorre, L.; McKelvey, J.M. Melting and Pressurization in Starve Feed Extrusion. *Adv. Polym. Technol.* 1984, 3, 355–364. [CrossRef]
- 124. Isherwood, D.P.; Pieris, R.N.; Kassatly, J. The Effect of Metered Starve Feeding on the Performance of a Small Extruder. *J. Eng. Ind.* **1984**, *106*, 132–136. [CrossRef]
- 125. Strand, S.R.; Spalding, M.A.; Hyun, S.K. Modeling of the Solids-Conveying Section of a Starve Fed Single Screw Plasticating Extruder. *SPE ANTEC Tech. Papers* **1992**, *38*, 2537–2541.
- 126. Thompson, M.R.; Donoian, G.; Christiano, J.P. Melting Mechanism of a Starved-Fed Single-Screw Extruder for Calcium Carbonate Filled Polyethylene. *Polym. Eng. Sci.* **2000**, *40*, 2014–2026. [CrossRef]
- 127. Wilczyński, K.; Nastaj, A.; Wilczyński, K.J. Melting Model for Starve Fed Single Screw Extrusion of Thermoplastics. *Int. Polym. Proc.* 2013, 28, 34–42. [CrossRef]
- 128. Wilczyński, K.J.; Nastaj, A.; Lewandowski, A.; Wilczyński, K. A Composite Model for Starve Fed Single Screw Extrusion of Thermoplastics. *Polym. Eng. Sci.* **2014**, *54*, 2362–2374. [CrossRef]
- 129. Wilczyński, K.; Nastaj, A.; Lewandowski, A.; Wilczyński, K.J.; Buziak, K. Experimental Study for Extrusion of Polypropylene/Wood Flour Composites. *Int. Polym. Proc.* **2015**, *30*, 113–120. [CrossRef]
- 130. Wilczyński, K.J.; Buziak, K. Study on the Flow of Wood Plastic Composites in the Starve Fed Single Screw Extrusion. *Polimery* **2017**, *62*, 680–685. [CrossRef]
- 131. Wilczyński, K.J.; Lewandowski, A.; Wilczyński, K. Experimental Study of Melting of Polymer Blends in a Starve Fed Single Screw Extruder. *Polym. Eng. Sci.* **2016**, *56*, 1349–1356. [CrossRef]
- 132. Donovan, R.C.; Thomas, D.E.; Leversen, L.D. An Experimental Study of Plasticating in a Reciprocating-Screw Injection Molding Machine. *Polym. Eng. Sci.* **1971**, *11*, 353–360. [CrossRef]
- 133. Donovan, R.C. A Theoretical Melting Model for a Reciprocating-Screw Injection Molding Machine. *Polym. Eng. Sci.* **1971**, *11*, 361–368. [CrossRef]
- 134. Donovan, R.C. The Plasticating Process in Injection Molding. Polym. Eng. Sci. 1974, 14, 101–111. [CrossRef]
- 135. Lipshitz, S.D.; Lavie, R.; Tadmor, Z. A Melting Model for Reciprocating Screw Injection-Molding Machines. *Polym. Eng. Sci.* **1974**, *14*, 553–559. [CrossRef]
- 136. Potente, H.; Schulte, H.; Effen, N. Simulation of Injection Molding and Comparison with Experimental Values. *Int. Polym. Proc.* **1993**, *8*, 224–235. [CrossRef]
- 137. Potente, H.; Bornemann, M. Non-Isothermal Model for the Drive Power Calculation of Single-screw Plasticating Units. *Int. Polym. Proc.* 2008, 23, 345–350. [CrossRef]
- 138. Iwko, J.; Steller, R.; Wróblewski, R.; Kaczmar, J. Experimental Verification of Computer Model for Polymer Plastication Process in Injection Molding. *Polimery* **2015**, *60*, 644–656. [CrossRef]
- 139. Iwko, J.; Steller, R.; Wróblewski, R. Experimentally Verified Mathematical Model of Polymer Plasticization Process in Injection Molding. *Polymers* **2018**, *10*, 968. [CrossRef]
- Fernandes, C.; Pontes, A.J.; Viana, J.C.; Nóbrega, J.M.; Gaspar-Cunha, A. Modeling of Plasticating Injection Molding—Experimental Assessment. *Int. Polym. Proc.* 2014, 29, 558–569. [CrossRef]

- 141. Wilczyński, K.; Narowski, P. Simulation Studies on the Effect of Material Characteristics and Runner Layout Geometry on the Filling Imbalance in Geometrically Balanced Injection Molds. *Polymers* 2019, 11, 639. [CrossRef] [PubMed]
- 142. Rowell, H.S.; Finlayson, D. Screw Viscous Pumps. Engineering 1928, 126, 249.
- 143. Carley, J.F.; Mallouk, R.S.; McKelvey, J.M. Simplified Flow Theory for Screw Extruders. *Ind. Eng. Chem.* **1953**, 45, 974–978. [CrossRef]
- 144. Maillefer, C. Etude Theorique et Experimentale sur le Fonctionnement des Boudineuses. Ph.D. Thesis, University of Lausanne, Lausanne, Switzerland, 1952.
- 145. Carley, J.F.; Strub, R.A. Basic Concepts of Extrusion. Ind. Eng. Chem. 1953, 45, 970–974. [CrossRef]
- 146. Squires, P.H. Screw Extruder Pumping Efficiency. SPE J. 1958, 14, 24–30.
- 147. Booy, M.L. Influence of Channel Curvature on Flow, Pressure Distribution, and Power Requirements of Screw Pumps and Melt Extruders. *Polym. Eng. Sci.* **1963**, *3*, 176–185. [CrossRef]
- 148. Squires, P.H. Screw Extrusion—Flow Patterns and Recent Theoretical Developments. *Polym. Eng. Sci.* **1964**, *4*, 7–16. [CrossRef]
- 149. Mallouk, R.S.; McKelvey, J.M. Power Requirements of Melt Extruder. *Ind. Eng. Chem.* **1953**, 45, 987–989. [CrossRef]
- 150. Maddock, B.H. Effect of Wear on the Delivery Capacity of Extruder Screw. SPE J. 1959, 15, 433-434.
- 151. Kroesser, F.W.; Middleman, S. The Calculation of Screw Characteristics for the Extrusion of Non-Newtonian Melts. *Polym. Eng. Sci.* **1965**, *5*, 230. [CrossRef]
- 152. Middleman, S. Flow of Power Law Fluids in Rectangular Ducts. Trans. Soc. Rheol. 1965, 9, 83–93. [CrossRef]
- 153. Colwell, R.E.; Nickolls, K.R. The Screw Extruder. Ind. Eng. Chem. 1959, 51, 841–843. [CrossRef]
- 154. Griffith, R.M. Fully Developed Flow in Screw Extryders. Theoretical and Experimental Study. *Ind. Eng. Chem. Fundam.* **1962**, *1*, 180–187. [CrossRef]
- 155. Zamodits, H.J.; Pearson, J.R.A. Flow of Polymer Melts in Extruders. Part I. The Effect of Transverse Flow and of a Superposed Steady Temperature Profile. *Trans. Soc. Rheol.* **1969**, *13*, 357–385. [CrossRef]
- 156. Fenner, R.T. The Design of Large Hot Melt Extruders. *Polymer* **1975**, *16*, 298–304. [CrossRef]
- 157. Elbirli, B.; Lindt, J.T. A Note on the Numerical Treatment of the Thermally Developing Flow in Screw Extruders. *Polym. Eng. Sci.* **1984**, 24, 482–487. [CrossRef]
- 158. Lindt, J.T. Flow of a Temperature Dependent Power-Law Model Fluid Between Parallel Plates: An Approximation for Flow in a Screw extruder. *Polym. Eng. Sci.* **1989**, *29*, 471–478. [CrossRef]
- 159. Spalding, M.A.; Dooley, J.; Hyun, K.S.; Strand, S.R. Three-Dimensional Numerical Analysis of a Single-Screw Extruder. *SPE ANTEC Tech. Papers* **1993**, *39*, 1533–1541.
- Lawal, A.; Kalyon, D.M. Nonisothermal Model of Single Screw Extrusion of Generalized Newtonian Fluids. Numer. Heat Transf. A Appl. 1994, 26, 103–121. [CrossRef]
- 161. Syrjala, S. On the Analysis of Fluid Flow and Heat Transfer in the Melt Conveying Section of a Single-Screw Extruder. *Numer. Heat Transf. A Appl.* **1999**, *35*, 25–47. [CrossRef]
- Syrjala, S. Numerical Simulation of Nanisothermal Flow of Polymer Melt in a Single-Screw Extruder. *Numer. Heat Transf. A Appl.* 2000, *37*, 897–915. [CrossRef]
- 163. Ilinca, F.; Hétu, J.-F. Three-Dimensional Finite Element Solution of the Flow in Single and Twin-Screw Extruders. *Int. Polym. Proc.* 2010, 25, 275–286. [CrossRef]
- 164. Pachner, S.; Löw-Baselli, B.; Affenzeller, M.; Miethlinger, J. A Generalized 2D Output Model of Polymer Melt Flow in Single-Screw Extrusion. *Int. Polym. Proc.* **2017**, *32*, 209–216. [CrossRef]
- 165. Marschik, C.; Roland, W.; Löw-Baselli, B.; Miethlinger, J. A Heuristic Method for Modeling Three-Dimensional Non-Newtonian Flows of Polymer Melts in Single-Screw Extruders. J. Non Newton Fluid 2017, 248, 27–39. [CrossRef]
- 166. Marschik, C.; Roland, W.; Miethlinger, J. A Network-Theory-Based Comparative Study of Melt-Conveying Models in Single-Screw Extrusion: A. Isothermal Flow. *Polymers* **2018**, *10*, 929. [CrossRef] [PubMed]
- 167. Polychronopoulos, N.D.; Vlachopoulos, J. Computer Flow Simulation of Moffatt Eddies in Single Screw Extrusion. *Int. Polym. Proc.* 2018, 33, 662–668. [CrossRef]
- 168. Erdmenger, R. Mehrwellen-Schnecken in der Verfahrenstechnik. *Chem. Ing. Tech.* **1964**, *36*, 175–185. [CrossRef]
- 169. Erdmenger, R. Schneckenmaschinen fur die Hochviskos-Verfahrenstechnik; Bayer AG: Leverkusen, Germany, 1978.
- 170. Booy, M.L. Geometry of Fully Wiped Twin-Screw Equipment. Polym. Eng. Sci. 1978, 18, 973–984. [CrossRef]

- 171. Booy, M.L. Isothermal Flow of Viscous Liquids in Corotating Twin Screw Devices. *Polym. Eng. Sci.* **1980**, 20, 1220–1228. [CrossRef]
- 172. Denson, C.D.; Hwang, B.K. The Influence of the Axial Pressure Gradient on Flow Rate for Newtonian Liquids in a Self Wiping, Co-Rotating Twin Screw Extruder. *Polym. Eng. Sci.* **1980**, *20*, 965–971. [CrossRef]
- 173. Szydłowski, W.; White, J.L. An Improved Theory of Metering in an Intermeshing Corotating Twin-Screw Extruder. *Adv. Polym. Technol.* **1987**, *7*, 177–183. [CrossRef]
- 174. White, J.L.; Szydłowski, W. Composite Models of Modular Intermeshing Corotating and Tangential Counter-Rotating Twin Screw Extruders. *Adv. Polym. Technol.* **1987**, *7*, 419–426. [CrossRef]
- 175. Tayeb, J.; Vergnes, B.; Della Valle, G. Theoretical Computation of the Isothermal Flow Through the Reverse Screw Element of a Twin Screw Extrusion Cooker. *J. Food Sci.* **1988**, *53*, 616–625. [CrossRef]
- 176. Tayeb, J.; Vergnes, B.; Della Valle, G. A Basic Model for a Twin-Screw Extruder. J. Food Sci. 1989, 54, 1047–1056. [CrossRef]
- 177. Wang, Y.; White, J.L. Non-Newtonian Flow Modelling in the Screw Regions of an Intermeshing Corotating Twin Screw Extruder. *J. Non Newton. Fluid* **1989**, *32*, 19–38. [CrossRef]
- 178. Wang, Y.; White, J.L.; Szydłowski, W. Flow in a Modular Intermeshing Co-Rotating Twin Screw Extruder. *Int. Polym. Proc.* **1989**, *4*, 262–269. [CrossRef]
- 179. Chen, Z.; White, J.L. Dimensionless Non-Newtonian Isothermal Simulation and Scale-up Considerations for Modular Intermeshing Corotating Twin Screw Extruders. *Int. Polym. Proc.* **1991**, *6*, 304–310. [CrossRef]
- White, J.L.; Chen, Z. Simulation of Non-Isothermal Flow in Modular Co-Rotating Twin Screw Extrusion. *Polym. Eng. Sci.* 1994, 34, 229–237. [CrossRef]
- Potente, H.; Ansalh, J.; Wittemeier, R. Throughput Characteristics of Tightly Intermeshing Co-rotating Twin Screw Extruders. *Int. Polym. Proc.* 1990, *5*, 208–216. [CrossRef]
- 182. Todd, D.B. Drag and Pressure Flow in Twin Screw Extruders. Int. Polym. Proc. 1991, 6, 143–147. [CrossRef]
- 183. Malik, M.; Kalyon, D.M.; Golba, J.C., Jr. Simulation of Co-Rotating Twin Screw Extrusion Process Subject to Pressure-Dependent Wall Slip at Barrel and Screw Surfaces: 3D FEM Analysis for Combinations of Forwardand Reverse-Conveying Screw Elements. *Int. Polym. Proc.* 2014, 29, 51–62. [CrossRef]
- 184. Durin, A.; De Micheli, P.; Nguyen, H.-C.; David, C.; Valette, R.; Vergnes, B. Comparison between 1D and 3D Approaches for Twin-Screw Extrusion Simulation. *Int. Polym. Proc.* **2014**, *29*, 641–648. [CrossRef]
- 185. Bravo, V.L.; Hrymak, A.N.; Wright, J.D. Numerical Simulation of Pressure and Velocity Profiles in Kneading Elements of a Co-Rotating Twin Screw Extruder. *Polym. Eng. Sci.* **2000**, *40*, 525–541. [CrossRef]
- Martin, C. Twin Screw Extruders as Continuous Mixers for Thermal Processing: A Technical and Historical Perspective. AAPS Pharm. Sci. Tech. 2016, 17, 3–19. [CrossRef]
- 187. Martin, C. A Typical Twin Screw Extrusion Compounding Systems for Polyolefins. In Proceedings of the SPE International Polyolefins Conference, Houston, TX, USA, 26 February–1 March 2017.
- 188. Utracki, A. Simulation of Co-Rotating Fully Intermeshing Twin-Screw Compounding Extruders. In Proceedings of the SPE International Polyolefins Conference, Houston, TX, USA, 26 February–1 March 2017.
- Martin, C. Optimum Twin Screw Extrusion Process Designs for PLA formulations. In Proceedings of the PPS Americas Regional Conference, Boston, MA, USA, 5–9 November 2018.
- 190. Nakayama, Y.; Takemitsu, H.; Kajiwara, T.; Kimura, K.; Takeuchi, T.; Tomiyama, H. Improving Mixing Characteristics with a Pitched Tip in Kneading Elements in Twin-Screw Extrusion. *AIChE J.* 2018, 64, 1424–1434. [CrossRef]
- 191. Kimura, Y.; Chaudhary, A.K.; Spalding, M.A. Twin-Screw Extrusion of Polyethylene. In *Handbook of Industrial Polyethylene and Technology*; Spalding, M.A., Chatterjee, A.M., Eds.; Scrivener Publishing LLC: Beverly, MA, USA, 2018; pp. 357–380. ISBN 978-111-915-976-6.
- 192. Kiesskalt, S. Untersuchungen an einer Kapsel Pumpe. VDI Zeitschr. 1927, 71, 453.
- 193. Montelius, C.O.J. Der Kogelige Danske Videnscabernes Selscabs Skrifter. Teknist Tidskaift. 1933, 6, 61–63.
- 194. Doboczky, Z. Einschnecke–Doppelschnecke. Plastverarbeiter 1965, 16, 57-67.
- 195. Janssen, L.P.B.M.; Mulders, L.H.R.M.; Smith, J.M. A Model from the Output of the Pump Zone of the Double Screw Processor or Extruder. *Plastics Polym.* **1975**, *43*, 93–98.
- 196. Speur, J.A.; Mavridis, H.; Vlachopoulos, J.; Janssen, L.P.B.M. Flow Patterns in the Calender Gap of a Counterrotating Twin Screw Extruder. *Adv. Polym. Technol.* **1987**, *7*, 39–48. [CrossRef]
- 197. White, J.L.; Adewale, A. A Unified View of Modeling Flow in Counter-rotating Twin Screw Extruders. *Int. Polym. Proc.* **1993**, *8*, 210–217. [CrossRef]

- 198. Li, T.; Manas-Zloczower, I. Flow Field Analysis of an Intermeshing Counter-Rotating Twin Screw Extruder. *Polym. Eng. Sci.* **1994**, *34*, 551–558. [CrossRef]
- 199. Kajiwara, T.; Nagashima, Y.; Nakano, Y.; Funatsu, K. Numerical Study of Twin-Screw Extruders by Three-Dimensional Flow Analysis-Development of Analysis Technique and Evaluation of Mixing Performance for Full Flight Screws. *Polym. Eng. Sci.* **1996**, *36*, 2142–2152. [CrossRef]
- 200. Hong, M.-H.; White, J.L. Fluid Mechanics of Intermeshing Counter-Rotating Twin Screw Extruders. *Int. Polym. Proc.* **1998**, *13*, 342–346. [CrossRef]
- 201. Hong, M.H.; White, J.L. Simulation of Flow in an Intermeshing Modular Counter-Rotating Twin Screw Extruder: Non-Newtonian and Non-Isothermal Behavior. *Int. Polym. Proc.* **1999**, *14*, 136–143. [CrossRef]
- 202. Schneider, H.-P. The Historical Development of the Counter-Rotating Twin-Screw Extruder. *Kunstoffe Plast. Eur.* **2005**, *1*, 1–6.
- 203. Wilczyński, K.; Lewandowski, A. Study on the Polymer Melt Flow in a Closely Intermeshing Counter-Rotating Twin Screw Extruder. *Int. Polym. Proc.* 2014, *29*, 649–659. [CrossRef]
- 204. ANSYS Inc. ANSYS Polyflow, CDF for Extrusion, Forming and Molding; ANSYS Inc.: Canonsburg, PA, USA, 2019.
- 205. Wilczyński, K.J.; Lewandowski, A.; Nastaj, A.; Wilczyński, K. Modeling for Starve Fed/Flood Fed Mixing Single-Screw Extruders. *Int. Polym. Proc.* 2016, *31*, 82–91. [CrossRef]
- 206. Wilczyński, K.J.; Lewandowski, A.; Nastaj, A.; Wilczyński, K. A Global Model for Starve-Fed Nonconventional Single-Screw Extrusion of Thermoplastics. *Adv. Polym. Technol.* **2017**, *36*, 23–35. [CrossRef]
- 207. Ariffin, A.; Ahmad, M.S.B. Review: Single Screw Extruder in Particulate Filler Composite. *Polym. Plast. Technol.* **2011**, *50*, 395–403. [CrossRef]
- 208. Wilczyński, K.; Nastaj, A.; Lewandowski, A.; Wilczyński, K.J. Multipurpose Computer Model for Screw Processing of Plastics. *Polym. Plast. Technol.* **2012**, *51*, 626–633. [CrossRef]
- 209. Teixeira, C.; Gaspar-Cunha, A.; Covas, J.A. Flow and Heat Transfer Along the Length of a Co-rotating Twin Screw Extruder. *Polym. Plast. Technol.* **2012**, *51*, 1567–1577. [CrossRef]
- Klein, I.; Klein, R.J. The SPR System of CAE Software. In *Computer Modeling for Extrusion and Other Continuous Polymer Processes*; O'Brien, K.T., Ed.; Hanser Publishers: New York, NY, USA, 1992; pp. 103–252. ISBN 978-1569900680.
- Agur, E.E.; Vlachopoulos, J. Numerical Simulation of a Single-Screw Plasticating Extruder. *Polym. Eng. Sci.* 1982, 22, 1084–1094. [CrossRef]
- 212. Potente, H.; Hanhart, W.; Schöppner, V. Potential Applications for Computer-aided Extruder Design. *Int. Polym. Proc.* **1993**, *8*, 335–344. [CrossRef]
- Potente, H.; Hanhart, W.; Reski, T. Design and Processing Optimization of Extruder Screws. *Polym. Eng. Sci.* 1994, 34, 937–945. [CrossRef]
- 214. Sebastian, D.H.; Rakos, R. Extrusion Process Analysis with PASS. In *Computer Modeling for Extrusion and Other Continuous Polymer Processes*; O'Brien, K.T., Ed.; Hanser Publishers: New York, NY, USA, 1992; pp. 331–448. ISBN 978-1569900680.
- 215. Wilczyński, K. A Computer Model for Single-Screw Plasticating Extrusion. *Polym. Plast. Technol.* **1996**, *35*, 449–477. [CrossRef]
- 216. Wilczyński, K. Single Screw Extrusion Model for Plasticating Extruders. *Polym. Plast. Technol.* **1999**, *38*, 581–608. [CrossRef]
- 217. Fukase, H.; Kunio, T.; Shinya, S.; Nomura, A. A Plasticating Model for Single-Screw Extruders. *Polym. Eng. Sci.* **1982**, *22*, 578–586. [CrossRef]
- 218. Zawadsky, E.; Karnis, J. Mathematical Model of a Single-Screw Plasticating Extruder. *J. Rheol. Acta* **1985**, *24*, 556–565. [CrossRef]
- 219. Vincelette, A.R.; Guerrero, C.S.; Carreau, P.J.; Lafleur, P.G. A Model for Single-Screw Plasticating Extruders. *Int. Polym. Proc.* **1989**, *4*, 232–241. [CrossRef]
- 220. Amellal, K.; Lafleur, P.G. Computer Simulation of Conventional and Barrier Screw Extruders. *Plast. Rubber Compos. Process.* **1993**, *19*, 227–239.
- 221. Wilczyński, K.; Buziak, K.; Wilczyński, K.J.; Lewandowski, A.; Nastaj, A. Computer Modeling for Single-Screw Extrusion of Wood-Plastic Composites. *Polymers* **2018**, *10*, 295. [CrossRef]
- 222. Bawiskar, S.; White, J.L. A Composite Model for Solid Conveying, Melting, Pressure and Fill Factor Profiles in Modular Co-Rotating Twin Screw Extruders. *Int. Polym. Proc.* **1997**, *12*, 331–340. [CrossRef]

- 223. White, J.L.; Kim, B.-J.; Bawiskar, S.; Keum, J.M. Development of a Global Computer Software for Modular Self-Wiping Corotating Twin Screw Extruders. *Polym. Plast. Technol.* **2001**, *40*, 385–405. [CrossRef]
- 224. White, J.L.; Keum, J.; Jung, H.; Ban, K.; Bumm, S. Corotating Twin-Screw Extrusion Reactive Extrusion-Devolatilization Model and Software. *Polym. Plast. Technol.* **2006**, *45*, 539–548. [CrossRef]
- 225. Potente, H.; Ansalh, J.; Klarholz, B. Design of Tightly Intermeshing Co-Rotating Twin Screw Extruders. *Int. Polym. Proc.* **1994**, *9*, 11–25. [CrossRef]
- 226. Potente, H.; Bastian, M.; Flecke, J. Design of a Compounding Extruder by Means of the SIGMA Simulation Software. *Adv. Polym. Technol.* **1999**, *18*, 147–170. [CrossRef]
- 227. Vergnes, B.; Valle, G.D.; Delamare, L. A Global Computer Software for Polymer Flows in Corotating Twin Screw Extruders. *Polym. Eng. Sci.* **1998**, *38*, 1781–1792. [CrossRef]
- 228. Canedo, E.L. Computer Simulation of Plastics Compounding Operations in Twin-Screw Extruders. *SPE ANTEC Tech. Papers* **1999**, *45*, 310–316.
- Wilczyński, K.; Jiang, Q.; White, J.L. A Composite Model for Melting, Pressure and Fill Factor Profiles in a Metered Fed Closely Intermeshing Counter-Rotating Twin Screw Extruder. *Int. Polym. Proc.* 2007, 22, 198–203. [CrossRef]
- 230. Jiang, Q.; White, J.L.; Yang, J. A Global Model for Closely Intermeshing Counter-Rotating Twin Screw Extruders with Flood Feeding. *Int. Polym. Proc.* 2010, 25, 223–235. [CrossRef]
- 231. Wilczyński, K.; Nastaj, A.; Lewandowski, A.; Wilczyński, K.J. Modeling of the Polymer Melt Flow in a Twin Screw Counter-Rotating Extrusion Process. Part II. Simulation and Experimental Studies—Verification of the Adopted Model. *Polimery* **2011**, *56*, 45–50. [CrossRef]
- Lewandowski, A.; Wilczyński, K.J.; Nastaj, A.; Wilczyński, K. A Composite Model for an Intermeshing Counter-Rotating Twin-Screw Extruder and its Experimental Verification. *Polym. Eng. Sci.* 2015, 55, 2838–2848. [CrossRef]
- 233. Wilczyński, K.J.; Nastaj, A.; Wilczyński, K. A Computer Model for Starve-Fed Single-Screw Extrusion of Polymer Blends. *Adv. Polym. Technol.* **2018**, *37*, 2142–2151. [CrossRef]
- 234. Wilczyński, K.; Buziak, K.; Nastaj, A.; Lewandowski, A.; Wilczyński, K.J. Modeling for Single Screw Extrusion of Wood Plastic Composites. In Proceedings of the Polymer Processing Society Conference (PPS2015), Graz, Austria, 21–25 September 2015; p. 170.
- 235. Mooney, M. Explicit Formulas for Slip and Fluidity. J. Rheol. 1931, 2, 210–222. [CrossRef]
- 236. Potente, H.; Bornemann, M.; Kurte-Jardin, M. Analytical Model for the Throughput and Drive Power Calculation in the Melting Section of Single Screw Plasticizing Units Considering Wall-Slippage. *Int. Polym. Proc.* **2009**, *24*, 23–30. [CrossRef]
- 237. Worth, R.A.; Parnaby, J.; Helmy, H.A. Wall Slip and its Implications in the Design of Single Screw Melt-Fed Extruders. *Polym. Eng. Sci.* **1977**, *17*, 257–265. [CrossRef]
- 238. Meijer, H.E.H.; Verbraak, C.P.J.M. Modeling of Extrusion with Slip Boundary Conditions. *Polym. Eng. Sci.* **1988**, *28*, 758–771. [CrossRef]
- Lawal, A.; Kalyon, D.M.; Yilmazer, U. Extrusion and Lubrication Flows of Viscoplastic Fluids with Wall Slip. Chem. Eng. Commun. 1993, 122, 127–150. [CrossRef]
- 240. Lawal, A.; Kalyon, D.M. Single Screw Extrusion of Viscoplastic Fluids Subject to Different Slip Coefficients at Screw and Barrel Surfaces. *Polym. Eng. Sci.* **1994**, *34*, 1471–1479. [CrossRef]
- 241. Kalyon, D.M.; Lawal, A.; Yazici, R.; Yaras, P.; Railkar, S. Mathematical Modeling and Experimental Studies of Twin-Screw Extrusion of Filled Polymers. *Polym. Eng. Sci.* **1999**, *39*, 1139–1151. [CrossRef]
- 242. Potente, H.; Ridder, H. Pressure/Throughput Behavior of a Single-Screw Plasticising Unit in Consideration of Wall Slippage. *Int. Polym. Proc.* 2002, *17*, 102–107. [CrossRef]
- 243. Potente, H.; Ridder, H.; Cunha, R.V. Global Concept for Describing and Investigation of Wall Slip Effects in the Extrusion Process. *Macromol. Mater. Eng.* **2002**, *287*, 836–842. [CrossRef]
- 244. Potente, H.; Kurte, M.; Ridder, H. Influence of Non-Newtonian Behaviour on the Processing Characteristics of Wall-Slipping Materials. *Int. Polym. Proc.* 2003, *18*, 115–121. [CrossRef]
- Potente, H.; Kurte–Jardin, M.; Klus, S.; Timmermann, K. Two Dimensional Description of Pressure-Throughput Behaviour of Newtonian Materials Considering Wall Slippage Effects. *Int. Polym. Proc.* 2005, 20, 312–321. [CrossRef]

- 246. Potente, H.; Timmermann, K.; Kurte-Jardin, M. Description of the Pressure/Throughput Behavior of a Single-Screw Plasticating Unit in Consideration of Wall Slippage Effects for Non-Newtonian Material and 1-D Flow. *Int. Polym. Proc.* 2006, 21, 272–282. [CrossRef]
- 247. Ferras, L.L.; Nobrega, J.M.; Pinho, F.T.; Carneiro, O.S. Profile Extrusion Die Design: The Effect of Wall Slip. In Proceedings of the Polymer Processing Society 23rd Annual Meeting (PPS-23), Salvador, Brazil, 27–31 May 2007.
- 248. Hatzikiriakos, S.G.; Mitsoulis, E. Slip Effects in Tapered Dies. Polym. Eng. Sci. 2009, 49, 1960–1969. [CrossRef]
- 249. Gupta, M. Effect of Wall Slip on the Flow in a Flat Die for Sheet Extrusion. *SPE ANTEC Tech. Papers* **2011**, *57*, 1191–1196.
- 250. Lewandowski, A.; Wilczyński, K. Global Modeling of Single Screw Extrusion with Slip Effects. *Int. Polym. Proc.* **2019**, *34*, 81–90. [CrossRef]
- 251. Wilczyński, K.; Buziak, K.; Lewandowski, A.; Wilczyński, K.J.; Nastaj, A. Proceedings of the AIP 35th International Conference of the Polymer Processing Society, Izmir-Cesma, Turkey, 26–30 May 2019. in press.
- 252. Bingham, E.C. Fluidity and Plasticity; McGraw-Hill: New York, NY, USA, 1922.
- 253. Bird, R.B.; Dai, G.C.; Yarusso, B.J. The Rheology and Flow of Viscoplastic Materials. *Rev. Chem. Eng.* **1983**, *1*, 1–70. [CrossRef]
- 254. Mitsoulis, E. Flows of Viscoplastic Materials: Models and Computations. In *Rheology Reviews* 2007; Binding, D.M., Hudson, N.E., Keunings, R., Eds.; The British Society of Rheology: London, UK, 2007; pp. 135–178.
- 255. Lewandowski, A.; Wilczyński, K. Global Modeling for Single Screw Extrusion of Viscoplastics. *Int. Polym. Proc.* **2020**, *35*. in press.



© 2019 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).