



Communication A Machine Learning Approach for Segmentation and Characterization of Microtextured Regions in a Near- α Titanium Alloy

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Abstract: The development of automated segmentation and quantitative characterization of microtextured regions (MTRs) from the complex heterogeneous microstructures is urgently needed, since MTRs have been proven to be the critical issue that dominates the dwell-fatigue performance of aerospace components. In addition, MTRs in Ti alloys have similarities to microstructures encountered in other materials, including minerals and biomaterials. Meanwhile, machine learning (ML) offers new opportunities. This paper addresses segmentation and quantitative characterization of MTRs, where an ML approach, the Gaussian mixture models (GMMs) coupled with density-based spatial clustering of applications with noise (DBSCAN) clustering algorithms, was employed in order to process the orientation data acquired via EBSD in the Matlab environment. Pixels with orientation information acquired through electron backscatter diffraction (EBSD) are divided and colored into several "classes" (MTRs) within the defined *c*-axis misorientations (i.e., 25°, 20°, 15°, 10°, and 5°), the precision and efficacy of which are verified by the morphology and pole figure of the segmented MTR. An appropriate range of *c*-axis misorientations for MTR segmentation was derived, i.e., 15~20°. The contribution of this innovative technique is compared with previous studies. At the same time, the MTRs were statistically characterized in the global region.

Keywords: titanium alloys; microtextured regions; machine learning; dwell-fatigue; EBSD

1. Introduction

A heterogeneous microstructure that consists of microtextured regions (MTRs) in near- α titanium alloys is hard to characterize, but microtextured regions are believed to be the prominent issue determining the dwell-fatigue performance of aerospace components [1–3]. MTRs are characterized as regions where the majority of α particles share similar crystallographic orientations, facilitating the nucleation and propagation of dwell-fatigue cracks [4–6]. Accordingly, it is essential to correlate the MTRs' factors (i.e., size, morphology, orientation, etc.) with the dwell-fatigue performance [7]. Therefore, the precise quantitative characterization of MTRs should be developed urgently and has been the primary focus of existing research.

A general and global method for the characterization of microstructures containing MTRs was a rough approach to analyzing MTRs which was applied in the early decades of this area of research [8,9]. This process yields statistical results on the crystallographic orientation for the α phase over the global region, which, however, cannot effectively feature the local MTRs. Therefore, the method of rectangulating the regions with MTRs on the global region was developed to describe and analyze MTRs more precisely [10–12]. Germain et al. investigated the formation mechanism of macrozones (i.e., MTRs framed



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). by rectangles) in near- α titanium alloys during the manufacturing process, and various band-like macrozones with different orientations were observed [11]. The developed method was able to characterize the orientation of MTRs, but it cannot identify information about the morphology and size of MTRs. Then, a more precise and detailed solution to segmenting MTRs from the obtained electron backscatter diffraction (EBSD) data was devised, based on inverse pole figure maps [13-15]. These studies lacked a clear basis for segmenting MTRs and relied on manual selection of MTRs, which cannot characterize MTRs quantitatively, automatically, and precisely. Additionally, the latest studies have introduced an essential criteria for defining MTRs, where the α particles in an MTR should have their *c*-axis orientation alignment within a specific angle of $\sim 25^{\circ}$, i.e., the *c*-axis misorientations of the α particles in an MTR are less than ~25° [16,17]. However, the suitable range of *c*-axis misorientations for MTR segmentation has not been derived. Machine learning (ML) has demonstrated its capability for heterogeneous image segmentation, but it has yet to make a breakthrough in materials science [18–21]. Unsupervised ML applied in heterogeneous image segmentation is usually more scalable and adaptable, i.e., Gaussian mixture models (GMMs) coupled with density-based spatial clustering of applications with noise (DBSCAN) clustering algorithms are the common methods that can be adapted and optimized according to defined materialogical criteria (i.e., c-axis misorientations in this case) [22–24].

The present study addresses the segmentation and characterization of MTRs in a near- α titanium alloy, where Ti6242 was employed as the object, based on the ML approach using the updated crystallographic criteria cited above. The ML approach, the GMMs coupled with DBSCAN, was employed to process the orientation data acquired by EBSD in a Matlab environment. The effects of segmentation at different *c*-axis misorientations (i.e., 25°, 20°, 15°, 10°, and 5°) were compared, and an appropriate range of *c*-axis misorientations for MTR segmentation was determined. The precision of the segmentation technique using the ML approach proposed here is compared with previous studies that segmented manually. Finally, the MTRs were statistically characterized in the global region (i.e., 3 mm × 3 mm).

2. Experiments and Methods

The as-received Ti6242 (Ti-6.02Al-2.11Sn-4.14Zr-2.03Mo-0.12O-0.08Si-0.02Fe) was sampled at the center of a billet. The sampled region was mechanically polished and then electro-polished in a solution (HClO₄: C₄H₉OH: CH₃OH = 3:15:32 in volume). EBSD analysis was performed on a section parallel to the rolling direction using the EDAX-TSL, USA, Oxford Nordlys X-max and Oxford Instruments HKL A/S 2007. The step size for the EBSD scan was 2 μ m, and the scan performed at a 20 kV accelerating voltage with an inclination angle of 70 degrees.

Then, the data acquired through EBSD were processed for MTR segmentation in the Matlab environment with Matlab software version R2020b, as shown in Figure 1, and the details are described as follows: The crystallographic orientation of each pixel is specified by three Euler Bunge angles $[\varphi_1, \Phi, \varphi_2]$. The third Euler, φ_2 , relates only to orientation about the hexagonal crystal *c*-axis, the direction of which is determined from Euler angles φ_1 and Φ , and the corresponding rotation matrix *g* relates the crystal reference orientation to the specimen coordinate system:

$$g = \begin{bmatrix} \cos \varphi_1 & -\sin \varphi_1 \cos \Phi & \sin \varphi_1 \sin \Phi \\ \sin \varphi_1 & \cos \varphi_1 \cos \Phi & -\cos \varphi_1 \sin \Phi \\ 0 & \sin \Phi & \cos \Phi \end{bmatrix}$$
(1)



Figure 1. Workflow of the data processing for MTR segmentation.

Then, the input *c*-axis orientation *x* can be characterized as:

$$x = g \cdot C_0 \tag{2}$$

where C_0 is $[0, 0, 1]^T$, which is parallel to the *z*-axis of the specimen coordinate system. The *x* is a standard unit vector typically consistent with a Gaussian mixture distribution. In MTR segmentation, *x* is employed as the observation vector. The segmented region can be viewed as a single Gaussian model of the same form, with each model being independent of the others. The entire global region is a GMM fused by multiple single Gaussian models of varying weight.

$$P(x|w_k,\mu_k,\sum_k) = \sum_{k=1}^K w_k f(x|\mu_k,\sum_k)$$
(3)

where *K* denotes the number of GMM components and w_k is the mixture weight, which indicates the proportion of the single Gaussian model in the mixture model. $f(x|\mu_k, \sum_k)$ is the distribution of the Gaussian component *k*, whose function expression is shown in Formula (4):

$$f(x|\mu_k, \sum_k) = \frac{1}{\sqrt{(2\pi)^3 |\sum_k|}} e^{-\frac{1}{2}(x-\mu_k)^T \sum_k -1(x-\mu_k)}$$
(4)

where μ_k is the mean vector, \sum_k is the covariance matrix, and $\sum_k {}^{-1}$ is the inverse matrix of \sum_k . Thus, the GMM is constructed. Thereafter, the DBSCAN clustering algorithm is used for classification under the defined threshold (i.e., *c*-axis misorientation here), initializing the GMM, and determining the value of *K* in the GMM as well. The Euclidean distance in DBSCAN between any two neighboring vectors, x_i and x_j , is given by Formula (5). When defining various *c*-axis misorientations θ (i.e., 25° , 20° , 15° , 10° , and 5°) and the correspond-

ing critical Euclidean distance D_{θ} (shown in Formula (6)), the number of components in the GMM (*K*, i.e., the number of "classes") can be determined.

$$D(\mathbf{x}_{i}, \mathbf{x}_{j}) = \left(\sum_{n=1}^{3} \left| \mathbf{x}_{i}^{(n)} - \mathbf{x}_{j}^{(n)} \right|^{2} \right)^{1/2}$$
(5)

$$D_{\theta} = 2\sin\frac{\theta}{2} \tag{6}$$

The expectation maximization (EM) algorithm is then used to maximize the likelihood function $L(w_k, \mu_k, \sum_k)$ and estimate the other parameters (i.e., w_k, μ_k , and \sum_k) in the GMM to obtain the probability that each pixel belongs to each "class". Eventually, the category with the highest probability is chosen to be the "class" to which the pixel belongs. This process is repeated until all pixels are classified into various "classes". In other words, pixels in a featured zone with *c*-axis misorientations within the defined θ were classified as an MTR. Each MTR was then colored and visualized to be distinguished from the others. Consequently, the MTRs were segmented and characterized. The likelihood function is shown in Formula (7).

$$L\left(\boldsymbol{w}_{k},\boldsymbol{\mu}_{k},\boldsymbol{\sum}_{k}\right) = \ln\prod_{k=1}^{K}P\left(\boldsymbol{x}|\boldsymbol{w}_{k},\boldsymbol{\mu}_{k},\boldsymbol{\sum}_{k}\right)$$
(7)

3. Results and Discussion

3.1. MTR Segmentation

Figure 2 shows the colored and segmented MTRs of the Ti6242 sample according to the defined *c*-axis misorientations using the ML approach, where Figure 2a shows the IPF map of MTRs obtained via EBSD and Figure 2b–f depict the segmented MTRs based on the GMMs coupled with DBSCAN within the defined *c*-axis misorientation, i.e., 25° , 20° , 15° , 10° , and 5° . Figure 2a displays the sampled region with significant band-like MTRs along the RD direction, which are, however, difficult to differentiate and characterize. Figure 2b–f show the segmentation and coloring results of Ti6242 MTRs according to the defined *c*-axis misorientation. From the segmented results, the morphology of MTRs within the *c*-axis misorientation of 25° is rough (i.e., Figure 2b); it is too refined within 10° and 5° (i.e., Figure 2e,f), however. The morphology of segmented MTRs within the *c*-axis misorientations of 20° and 15° shown in Figure 2c,d is appropriate compared with the morphology in Figure 2a. To further compare and quantify the effect of segmentation, as well as to get an effective range of *c*-axis misorientations for MTR segmentation, a small featured zone, framed by the blue dotted line shown in Figure 3a, was measured in detail.

Figure 3 measures a representative MTR segmented under various *c*-axis misorientations, where Figure 3a,b show the morphology of the segmented MTR, and Figure 3c presents the pole figures. The results show that when the *c*-axis misorientation decreases from 25° to 5°, the length (of the long axis) of the MTR decreases from ~1800 μ m to ~400 μ m. The strength of the microtexture, on the other hand, increases from ~20.2 to ~53.7. As one may have noticed, 15° is a threshold, beyond which (i.e., at 15° or 20°) the length of the MTR and microtexture strength start to vary gently with *c*-axis misorientations. Therefore, 15~20° could be employed as an appropriate range of *c*-axis misorientations for MTR segmentation.



Figure 2. IPF map of EBSD zone (**a**), segmentation and coloring results of Ti6242 MTRs according to the defined *c*-axis misorientations: 25° (**b**), 20° (**c**), 15° (**d**), 10° (**e**), and 5° (**f**). The blue dotted frame is a feature zone, shown in detail in Figure 3.

The contribution of the segmentation technique using the ML approach here is compared with previous studies, which segmented manually [11,14]. In this study, MTRs were segmented according to the *c*-axis misorientation (i.e., 15° in Figure 4), where the ML approach, the GMMs coupled with DBSCAN, was employed to process the orientation data acquired via EBSD in the Matlab environment. In terms of the segmentation effect, the MTRs segmented using the ML approach (this work) has a more precise morphology and a clearer boundary. As reflected in the pole figure, a single, strong texture peak of the MTR is obtained in this work, compared with the multiple peaks of various intensities obtained in previous studies [11,14], which conducted the segmentation manually. In summary, the segmentation technique using the ML approach here is more effective.

3.2. Characterization of MTRs

After segmenting the MTRs, statistical characterization of the MTRs' features (i.e., length, high aspect ratio, and orientation) in Ti6242 was conducted, which will provide essential data when investigating dwell-fatigue [4–7]. Figure 5a depicts the segmentation of MTRs from the global region, and Figure 5c depicts MTRs with long-axis lengths exceeding 200 μ m (approximately 10 average alpha particles) being separated. Figure 5d,e show the statistical results of the length and high aspect ratio of the MTRs presented in Figure 5c, where the mean value of length is 581.9 μ m and the mean value of the high aspect ratio is 2.8. Furthermore, the *c*-axis orientation of each MTR is determined by solving the mean vector μ_k in the GMM of the ML approach, as shown in Figure 5c. Additionally, the statistical distribution of angles of the MTRs' *c*-axis to RD is described (Figure 5f).

Figure 3. A representative MTR segmented under different *c*-axis misorientations: segmented MTR (**a**), the MTR in IPF (**b**), and pole figures (**c**).

Figure 4. Comparison of the effectiveness and precision of MTR characterization between previous studies and this work [11,14]. The macrozone IV is an MTR framed with rectangles.

Figure 5. Statistical characterization of MTRs: segmentation and coloring of "classes" (**a**), non-MTR regions (**b**), schematic of orientation in each MTR (**c**), statistics and fitting of length (**d**) and high aspect ratio (**e**) of MTRs, and distribution of angles of MTRs' *c*-axis to RD (**f**). The grey hexagonal prism in (**c**) represents the orientation of each MTR, and W1 and L1 represent the width and length of the MTR, respectively.

4. Conclusions

This work proposes a novel automatic approach for segmenting MTRs in a Ti6242 billet based on *c*-axis misorientation, where an ML approach, the GMMs coupled with DBSCAN, was employed to process the orientation data acquired via EBSD in the Matlab environment. Millions of pixels with orientation information are divided and colored into several "classes" within the defined *c*-axis misorientation (i.e., 25° , 20° , 15° , 10° , and 5°), the precision and efficacy of which are verified by the morphology and pole figure of the segmented MTR. An appropriate range of *c*-axis misorientations for MTR segmentation was derived, i.e., $15\sim20^{\circ}$. Compared with the approaches employed in previous studies, the segmentation technique using the ML approach proposed here is more effective. In terms of segmentation effect, the MTR segmented using this ML approach has a more precise morphology and a clearer boundary. As shown in the pole figure, a single, strong texture peak of an MTR is obtained in this work, compared with the multiple peaks of various intensities obtained in previous studies. At the same time, the MTRs were statistically characterized in the global region to provide essential data for investigating dwell-fatigue.

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