



Article Density Functional Theory Study of CuAg Bimetal Electrocatalyst for CO₂RR to Produce CH₃OH

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Abstract: Converting superfluous CO_2 into value-added chemicals is regarded as a practical approach for alleviating the global warming problem. Powered by renewable electricity, CO_2 reduction reactions (CO_2RR) have attracted intense interest owing to their favorable efficiency. Metal catalysts exhibit high catalytic efficiency for CO_2 reduction. However, the reaction mechanisms have yet to be investigated. In this study, CO_2RR to CH_3OH catalyzed by CuAg bimetal is theoretically investigated. The configurations and stability of the catalysts and the reaction pathway are studied. The results unveil the mechanisms of the catalysis process and prove the feasibility of CuAg clusters as efficient CO_2RR catalysts, serving as guidance for further experimental exploration. This study provides guidance and a reference for future work in the design of mixed-metal catalysts with high CO_2RR performance.

Keywords: CuAg bimetal; CO₂RR; pathway; theoretical study



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1. Introduction

The increasing emissions of greenhouse gases such as CO_2 and CH_4 into the air fuels the greenhouse effect and the concomitant global warming. The increase of the concentration of CO_2 has the greatest impact on rising global temperatures. Owing to its important environmental and economic repercussions, reducing carbon emissions without affecting social and economic development has become one of the most urgent problems in China.

Before now, numerous strategies have been developed to reduce the concentration of CO_2 in the atmosphere, such as CO_2 capture and storage [1], absorption [2], and chemical conversion [3–6]. In recent years, the conversion of CO_2 into a variety of economically valuable chemicals has emerged as a promising technology [7,8]. In this regard, electrochemical CO_2 reduction (CO_2RR) stands out because of its high value-added products (including ethanol and methanol) and its favorable conversion efficiency [9–13]. Among the various catalysts for CO_2RR , copper (Cu) is widely used because of its abundance and ambient-environment working conditions; however, its limited activity and selectivity has hindered further development [14–18]. Consequently, recent research efforts have been devoted to enhancing its catalytic performance by adjusting catalyst properties such as particle size [19], shape [20–22], and grain boundary [23].

As a result, more attractive Cu-based bimetallic CO₂RR catalysts with enhanced activity and selectivity have been discovered [24–28]. Thus, Kim et al. [29] reported a CuAu catalyst demonstrating high CO selectivity (~80%) in an overpotential of ~200 mV. Zhang et al. [30] fabricated a CuPd nanoalloy with a twofold enhancement in Faradaic efficiency for CO₂RR to methane compared with Cu alone. Sarfraz et al. [31] reported a stable CuSn catalyst exhibiting a Faradaic efficiency for CO₂RR to CO greater than 90%

and a current density of -1.0 mA cm⁻² at -0.6 V vs. a reversible hydrogen electrode (RHE). Chungseok et al. [32] reported on the performance of a CuAg nanowire. The Cu-Ag interface of the CuAg nanowire significantly improved the selectivity of CO₂ reduction to CH₄, with a maximum Faraday efficiency (FE) of 72% production at -1.17 V (relative to an RHE). Nevertheless, studies on Cu bimetallic catalysts inducing CO₂RR to alcohol are scarce, and a more fundamental understanding is required for the rational design of Cu-based catalysts in this field.

After much research, significant progress has been made in CO₂RR, especially in experimental studies. However, traditional experimental methods have inherent limitations, including blindness, workload, time, and resource waste. Nowadays, quantum chemistry and molecular dynamic simulations are widely used for calculating and simulating chemical systems as a technique to understand and predict behaviors at the molecular level [33–37]. Combining computational chemistry predictions with experimental investigation is a highly efficient methodology for accelerating the investigation of CO₂RR. In electrocatalysis research, the density functional theory (DFT) is widely used to analyze possible reaction path energy changes, reaction mechanisms, and catalyst materials for special reactions, such as CO₂RR, NRR, ORR, and so on [38]. CH₃OH is one of the most important chemicals used as a green fuel or the intermediate of reactions. It can be directly used in energy conversion systems such as methanol fuel cells or internal combustion engines, due to its relatively high energy density.

In this study, we theoretically designed a series of CuAg bimetallic clusters and investigated their feasibility as catalysts for CO_2RR to methanol according to the DFT. Considering that Ag nanoparticles have been previously shown to act as nucleation seeds for CuAg particles [39], we selected the most stable Ag cluster as a basis for the design of CuAg clusters with different configurations. Then, the CO_2 adsorption behavior on different sites was evaluated. Finally, the reaction pathway was fully studied to determine the optimal CuAg cluster configuration. This work sought to experimentally study a series of CuAg bimetallic cluster catalysts and establish a screening mechanism to calculate the catalytic activity of reducing CO_2RR to CH_3OH . This work can serve as guidance for further experimental exploration.

2. Results and Discussion

2.1. Study on the Stability of the Ag Clusters

In contrast with Ag_1 and Ag_2 clusters, which exhibit only one structure, different isomers appear when the number of Ag atoms (n) is $n \ge 3$. In this case, the most stable configuration among these isomers must be screened. For n = 3, there are two isomers, i.e., linear and triangular, with similar bond lengths according to the calculation. By comparing their total energy and binding energy (Table S1), it was found that the binding energy of the triangular isomer is lower than that of its linear counterpart. Therefore, the most stable structure of the Ag_3 cluster is a flat regular triangle; its optimized structure is shown in Figure S1.

When n = 4, Ag_4 exhibits five isomeric structures (Figure S2), among which the most stable is a flat rhombus. For n = 5, the most stable configuration is a plane isosceles trapezoid composed of three triangles. Moreover, when n = 6, a two-dimensional close-packed shape composed of four triangles has the lowest binding energy and is therefore the most stable. Surprisingly, these selected structures are all planar (the corresponding calculation results can be found in Supplementary Information).

Figure 1 depicts the most stable Ag_n cluster structures for n = 1-6. The relationship between the stability of the six clusters and the number of Ag atoms is analyzed in Figure 2. As can be seen, the binding energy (E_B) has a downward trend, indicating that the total energy required for cluster binding decreases as the number of atoms increases. However, since the number of Ag atoms differs between clusters, the overall E_B cannot be used to compare their stability, and the average binding energy (E_b) needs to be introduced. The calculated values of E_b are shown in Table S5. It was found that E_b decreases with the increase of n, reaching the smallest value (indicative of the highest cluster stability) for n = 6. Therefore, the Ag₆ clusters were selected for the following experiments.



Figure 1. Most stable configurations of Ag_n (n = 1–6) clusters: (a) Ag_1 ; (b) Ag_2 ; (c) Ag_3 ; (d) Ag_4 ; (e) Ag_5 ; (f) Ag_6 .



Figure 2. Variation of binding energy and average binding energy with the number of Ag atoms.

2.2. Study on the Stability of the CuAg Clusters

The selected Ag₆ clusters were doped with Cu atoms, and the changes in parameters such as bond length, bond angle, and stability after doping were examined. When doped with a Cu atom, the resulting Cu₁Ag₅ cluster has two kinds of isomers. The specific structures are shown in Figure 3. Although the two structures have symmetry, the addition of Cu changes the structure of the Ag cluster, which loses its regular triangle structure. Calculation of the total energy and average binding energy of the two structures (Table S6) revealed that structure *a* is relatively stable in comparison to structure *b*. According to the method mentioned above, the most stable configurations of the Cu_{6-n}Ag_n (n = 1–5) clusters shown in Figure 4 were obtained.

The HOMO and LUMO values of the six structures in Figure 4 were simulated and calculated. Figure 5 shows that the E_{LUMO} decreases after doping with Cu, indicating that the presence of the Cu atoms enhances the electron-accepting ability of the Ag clusters. Moreover, the E_{HOMO} of the bimetallic clusters decreases after Cu doping, indicating that the addition of Cu atoms reduces the electron-donating ability. The ΔE value is not significantly changed by Cu doping, and the ΔE of Cu₅Ag₁ is the smallest, which suggests that the electron transfer is the fastest in this cluster.



Figure 3. Isomeric structure of Cu_1Ag_5 clusters: (a) Cu is the tip position; (b) Cu is the middle position.



Figure 4. Most stable configuration of $Cu_{6-n}Ag_n$ (n = 1–6) clusters: (a) Cu_5Ag_1 ; (b) Cu_4Ag_2 ; (c) Cu_3Ag_3 ; (d) Cu_2Ag_4 ; (e) Cu_1Ag_5 ; (f) Ag_6 .



Figure 5. Frontier molecular orbital energy level and ΔE of the Cu_{6-n}Ag_n cluster: (a) Cu₅Ag₁, (b) Cu₄Ag₂, (c) Cu₃Ag₃, (d) Cu₂Ag₄, (e) Cu₁Ag₅, and (f) Ag₆.

2.3. Study on the CO₂ Adsorption Stability of the CuAg Clusters

Table 1 lists the values of the first four atoms with the largest absolute Fukui index of the six cluster structures. Because some clusters have symmetry, the Fukui indices of atoms

Site Site Site Value Site Value Configuration Value Value +0.237-0.228-0.204а Cu (4/6) Ag (1) Cu (4/6) Ag (1) +0.175+0.276-0.229-0.185+0.183b Cu (6) Ag (1/4) Cu (6) Ag (1/4) -0.217Ag (1) +0.233Ag (4/6) +0.221-0.219С Ag (1) Ag (4/6) d +0.238-0.252+0.211-0.182Ag (1) Ag (4/6) Ag (4/6) Ag (1) Ag (1/4) -0.252+0.241+0.210-0.206e Ag (6) Ag (1/4) Ag (6) f Ag (1/4/6) -0.234Ag (1/4/6) -0.231Ag (2/3/5) +0.103Ag (2/3/5) -0.102

that are structurally axisymmetric are equal. CO_2 is easily adsorbed on atoms with small Fukui (-) values because the structure is stable after adsorption; therefore, cluster catalysts with small Fukui indices would exhibit enhanced CO_2 activation.

Table 1. Fukui indices of CuAg clusters.

CO₂ adsorption proceeds mainly by two processes, i.e., single-site adsorption and dual-site adsorption. For the Cu₅Ag₁ cluster, the absolute Fukui value (–) of the silver atom at position 1 is the largest, and CO₂ adsorption is therefore preferred at this site. The specific stable structure after adsorption is shown in Figure 6, and the bond lengths, bond angles, and energies of the Cu₅Ag₁–CO₂ structure are summarized in Table 2. In double-site adsorption, comparison of the C–O bond length before and after adsorption reveals that two C–O bonds of CO₂ elongate and the third shortens in structures *a* and *c*. In contrast, the two bond lengths of CO₂ in structures *a* and *c* are more conducive to inducing CO₂ reduction to alcohols. Then, by comparing the adsorption energy of structures *a* and *c*, it can be concluded that structure *a* is the best for double-site adsorption of CO₂.



Figure 6. Isomers of the Cu₅Ag₁–CO₂ adsorption structure (\mathbf{a} – \mathbf{c}) are dual-site adsorption, while (\mathbf{d} , \mathbf{e}) are single-site adsorption.

Isomers	∠ 01CO2/ °	$d_{C-O1}/Å$	$d_{C-O2}/Å$	E _{CuAg-CO2} /Ha	E_{obs}/eV
а	175.605	1.264	1.449	-13,589.920	-0.555
b	171.015	1.330	1.332	-13,589.911	-0.299
с	177.676	1.270	1.469	-13,589.905	-0.1439
d	170.699	1.322	1.332	-13,589.911	-0.301
e	173.680	1.335	1.346	-13,589.906	-0.163

Table 2. Bond lengths, bond angles, and energies of the Cu₅Ag₁–CO₂ structures.

For single-site adsorption, the CO_2 bond length in structure *d* does not change significantly, whereas the change in structure *e* is more obvious, indicating a higher probability of CO_2 activation when C atoms are adsorbed on Cu_5Ag_1 .

Similarly, the best adsorption configurations for double-site adsorption and singlesite adsorption were obtained for the other clusters, as shown in Figures 7 and 8. The calculation results show that the adsorption method, the CO_2 activation degree, and the overall stability after adsorption are different between clusters.



Figure 7. Optimal CO₂ adsorption structure in the Cu_nAg_{6-n} cluster (n = 1–6) for dual-site adsorption: (a) Cu₅Ag₁; (b) Cu₄Ag₂; (c) Cu₃Ag₃; (d) Cu₂Ag₄; (e) Cu₁Ag₅; (f) Ag₆.



Figure 8. Optimal CO₂ adsorption structure in the Cu_nAg_{6-n} cluster (n = 1–6) for single-site adsorption: (a) Cu₅Ag₁; (b) Cu₄Ag₂; (c) Cu₃Ag₃; (d) Cu₂Ag₄; (e) Cu₁Ag₅; (f) Ag₆.

2.4. Pathway Study on CO₂RR to CH₃OH

The mechanism of the CO₂ reduction reaction is still unclear, and further experimental and theoretical research is needed. Recently, the reaction pathway of CO₂ hydrogenation reduction to CH₃OH has been studied [40,41]. Figure 9 depicts the preferred reaction mechanism of CO₂ hydrogenation to obtain CH₃OH; thus, this route was selected to study the catalytic effect of the CuAg clusters. The specific reaction intermediates are CO₂*, HCOO*, HCOOH*, H₂COOH*, TS4, CH₂O*, TS5, CH₃O*, and CH₃OH.



Figure 9. Reaction pathway of CO₂ hydrogenation to CH₃OH.

The Gibbs free energy (Δ G) of the reactions involving intermediates, reactants, and products was calculated at 298.15 K, using the CO₂ reactant as a benchmark. The results are shown in Table S16. Similarly, the adsorption structures of all products, intermediates, reactants, and catalysts were simulated according to the previous calculation structure. Structure optimization and Δ G calculation were performed using the same method.

The calculated energy values of the Cu_5Ag_1 cluster are listed in Table S17, and the corresponding ladder diagram is shown in Figure 10. It can be seen that in the absence of a catalyst, the ΔG of the intermediates gradually rises, and the energy difference between CO_2 and CH_3OH is 389.422 eV, which indicates that the reaction is not spontaneous under normal conditions.



Reaction Progress

Figure 10. Energy diagram of CO₂ hydrogenation to CH₃OH catalyzed by the Cu₅Ag₁ cluster.

When the Cu₅Ag₁ catalyst is added, the ΔG of the intermediate decreases compared with that obtained without the catalyst, indicating that the cluster has a certain degree of catalytic activity for the CO₂ reduction reaction. After adding the Cu₅Ag₁ cluster, the difference between the energy of the CH₃OH product and that of CO₂ is only 84.709 eV. Compared with the results without a catalyst, although ΔG is reduced by about four times, it is still positive, indicating that the reaction cannot proceed spontaneously in the presence of Cu₅Ag₁. Therefore, it can be concluded that the Cu₅Ag₁ cluster has a catalytic effect on the reaction, albeit a small one.

The energy ladder diagram of the Cu₄Ag₂ cluster reduction is shown in Figure 11. Certain catalytic activity on CO₂RR was detected for the Cu₄Ag₂ cluster by comparing the Δ G of each intermediate and the blank control data. Specifically, the catalyst decreases the Δ G of each intermediate, this decrease being the largest in HCOO* and TS4. In the absence of a catalyst, CO₂ has the lowest Δ G in all the pathways, but this trend changes after adding Cu₄Ag₂. For the CH₃OH product, after adding the Cu₄Ag₂ catalyst, Δ G decreases by 259.869 eV. Therefore, the Cu₄Ag₂ catalyst can induce the formation of CH₃OH to some extent, reducing the reaction energy barrier and softening the reaction conditions. However, the Δ G of CH₃OH is still positive, indicating that the catalytic effect of the cluster is not ideal.



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Figure 11. Energy diagram of CO₂ hydrogenation to CH₃OH catalyzed by the Cu₄Ag₂ cluster.

The calculation results of the Cu₃Ag₃ cluster are shown in Figure 12. It was found that after the addition of the Cu₃Ag₃ cluster catalyst, the ΔG of the CO₂ hydrogenation route undergoes a major change. In the absence of a catalyst, the energy of the intermediates gradually rises, whereas this trend is reversed after adding the Cu₃Ag₃ catalyst. The catalyst reduces the ΔG of most of the intermediates in the entire path, among which HCOO^{*}, H₂COOH^{*}, and CH₃O^{*} exhibit the largest decrease, indicating that the catalyst can promote the formation of the three intermediates. However, the ΔG of the transition state TS4 is higher by about 23 eV than that obtained without catalysis, which suggests that the bimetallic Cu₃Ag₃ cluster could not promote the formation of TS4. For the CH₃OH product, after adding the Cu₃Ag₃ cluster catalyst, the ΔG of CH₃OH decreases by 152.792 eV, indicating that the catalyst can effectively reduce the energy barrier of the reaction path. However, since the ΔG of the intermediate product increases, the catalytic effect of the Cu₃Ag₃ cluster on CO₂RR is not significant either.



Reaction Progress

Figure 12. Energy diagram of CO₂ hydrogenation to CH₃OH catalyzed by the Cu₃Ag₃ cluster.

Figure 13 shows the energy ladder diagram of CO_2RR to CH_3OH after adding the bimetallic Cu_2Ag_4 cluster catalyst. The ΔG of all intermediates and products decreases significantly. Compared with the results of the reaction without a catalyst, the ΔG values of all intermediates and reactants decrease directly from positive to negative, indicating that the hydrogenation of CO_2 to CH_3OH can occur spontaneously in the presence of the Cu_2Ag_4 catalyst. Therefore, the Cu_2Ag_4 cluster displays sufficient catalytic activity on the CO_2RR to CH_3OH .



Reaction Progress

Figure 13. Energy diagram of CO₂ hydrogenation to CH₃OH catalyzed by the Cu₂Ag₄ cluster.

The catalytic effect of the cluster doped with one Cu atom is shown in Figure 14. From the overall diagram, it can be deduced that the cluster has a good catalytic effect, because the ΔG of the six intermediates is lower than that of CO₂. However, the ΔG of the TS5 intermediate is higher than that of CO₂, and the ΔG of TS5 is positive. Focusing on the

CH₃OH product, it can be seen that the ΔG of CH₃OH after the addition of the catalyst does not differ much from that of CO₂; the difference is only 23.456 eV. This indicates that the reaction is more favorable after adding Cu₁Ag₅. Therefore, the Cu₁Ag₅ cluster can promote the reaction of CO₂ to CH₃OH, but the overall catalytic effect is not as significant as that of Cu₂Ag₄.



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Figure 14. Energy diagram of CO₂ hydrogenation to CH₃OH catalyzed by the Cu₁Ag₅ cluster.

Next, we analyzed the catalytic effect of a pure silver cluster Ag_6 . The specific calculation results are shown in Figure 15. The reaction pathway with the Ag_6 cluster is completely different from those of the bimetallic catalysts, and no catalytic effect on CO_2RR is observed. The energy barrier that needs to be overcome after adding the catalyst Ag_6 cluster is higher than the energy barrier present when no catalyst has been added, indicating that the pure metal Ag_6 cluster catalyst would require more severe reaction conditions and would destabilize the intermediates. The Ag_6 cluster cannot promote the formation of the intermediates in the CO_2RR to CH_3OH .



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Figure 15. Energy diagram of CO₂ hydrogenation to CH₃OH catalyzed by the Ag₆ cluster.

The energy ladder diagrams of the bimetallic CuAg clusters and the pure metal Ag₆ cluster can be directly compared in Figure 16. It can be seen that the Δ G value of the path is higher for Ag₆ than for the CuAg clusters, indicating that the energy barrier that needs to be overcome for the reaction to proceed is the highest, and the catalytic effect of Ag₆ is the worst. This result demonstrates that Cu doping can indeed increase the catalytic activity of the clusters, which is further confirmed by the experimental results of single-site adsorption of CO₂ (the corresponding data can be found in the supporting information).



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Figure 16. Energy diagram of CO₂ hydrogenation to CH₃OH catalyzed by the CuAg clusters.

By comparing the catalytic activity of the doped bimetallic clusters, it was found that the ΔG of intermediates and the product obtained with Cu₂Ag₄ exhibits the largest decrease among the clusters, and the ΔG of all the intermediates decreases to negative values. This shows that the Cu₂Ag₄ catalyst can significantly improve the stability of the reaction intermediates, thereby facilitating their generation and promoting the spontaneous progress of the reaction. Therefore, among all the catalysts, Cu₂Ag₄ exhibits the best catalytic activity.

3. Models and Methods

This study primarily used the DMol³ module in the Materials Studio software (version 2017), employing spin-polarized DFT to draw the structure, optimize the cluster structure, and calculate the energy. The parameters were set as follows: Functional function selects generalized gradient approximation and Perdew–Burke–Ernzerhof (PBE), the maximum iteration in energy calculation was 1000 times, and "Use symmetry" was selected. In the electronic module, the integration accuracy and self-consistent field (SCF) tolerances were both set to medium. In the basis set, double numerical plus polarization (DNP) was selected, and the basis file was set to 4.4. In the SCF module, the maximum SCF expansion was set to 1000 times, with "Use smearing to tail" checked. In the solvent module, the "Use COSMO solution environment" was set to "water".

Before designing the CuAg bimetallic cluster catalyst, the method by which it will be determined whether the catalyst itself is stable should be clarified. The binding energy E is calculated by quantification, and the formula is as follows (1)–(3).

3.1. The Cluster Stability and CO₂ Adsorption Structure Data Analysis

To calculate the binding energy E_B , find the total energy after the final step of convergence is successful in the calculation result file, and bring the total energy into Formula (1). For Ag clusters, the smaller the binding energy is, the more stable the structure is.

$$E_B = E_{Agn} - \mathbf{n} \times E_{Ag} \tag{1}$$

The smaller the average binding energy (E_b) of each atom, the lower the stored energy and the more stable the structure of the whole cluster. The average binding energy of the Ag cluster is found using Formula (2), and that of the CuAg metal cluster is found using Formula (3).

$$E_b = E_{Agn} / n - E_{Ag} \tag{2}$$

$$E_b = [E_{CuAg} - \mathbf{n} \times E_{Ag} - (6 - \mathbf{n}) \times E_{Cu}]/6$$
(3)

The adsorption energy $E_{CuAg-CO_2}$ is obtained from Formula (4). The smaller the adsorption energy, the more stable the overall structure after adsorption and the greater the change in the C–O bond length, indicating that the catalyst has a better degree of CO₂ activation.

$$E_{ads} = E_{CuAg-CO_2} - E_{CuAg} - E_{CO_2} \tag{4}$$

3.2. Data Analysis of CO₂ Hydrogenation Reduction Path

At 298.15 K, the Gibbs free energy of reacting all monomers is based on CO₂, and the respective ΔG is obtained. The two sets of ΔG data calculated with and without the catalyst were made into an energy ladder diagram to analyze the catalytic effect of CuAg clusters.

3.3. The HOMO, LUMO and ΔE *of the Cluster*

The highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbitals (LUMO) eigenvalues, the HOMO-LUMO gap, and the Fukui function are the most commonly used parameters to estimate the performance of a designed catalyst. The HOMO represents the highest occupied molecular orbital. The higher the E_{HOMO} , the easier it is for CuAg clusters to give electrons. The LUMO represents the lowest unoccupied molecular orbital. The lower the E_{LUMO} , the easier it is for CuAg clusters to obtain electrons. The magnitude of the energy band gap value ($\Delta E = E_{\text{LUMO}} - E_{\text{HOMO}}$) governs the electron transfer rate in the CuAg cluster. The smaller the ΔE , the faster the electron transfer rate between the HOMO and LUMO orbitals.

3.4. Calculation of the Fukui Index of Atoms in the Cluster

The smaller the Fukui (-) value of an atom, the more easily the atom is attacked by a Lewis base; the larger the Fukui (+) of the atom, the more easily the atom is attacked by a Lewis acid. Because CO₂ is a Lewis base, the smaller the Fukui (-) value, the more stable the structure will be after CO₂ adsorption. The better the degree of activation of the cluster catalyst to CO₂, the more easily the atom becomes the best adsorption site for CO₂.

4. Conclusions

On the basis of quantum chemistry theory, the stability of pure Ag metal clusters and bimetallic CuAg clusters and the CO₂ adsorption activity and catalytic effect of the CuAg clusters on the CO₂ hydrogenation to CH₃OH were analyzed by energy calculation and optimization of the constructed structures. The following conclusions were obtained: The most stable configurations of Ag_n (n = 1–6) metal clusters are planar. The stability of the configurations increases with the symmetry. When the adsorption site and adsorption mode of CO₂ on the cluster catalyst are different, the degree of activation of the catalyst and the stability after the adsorption of CO₂ are also different. Doping Cu atoms in the Ag cluster can improve the catalytic activity toward CO₂ hydrogenation to CH₃OH, with the Cu₂Ag₄ cluster

affording the best results. This theoretical study provides guidance and a reference for future work in the design of mixed-metal catalysts with high CO₂RR performance.

Based on theoretical calculations, the relationship between a catalyst's structure, composition, and catalytic CO_2RR activity is constructed, which can be used to guide the preparation of the catalyst and better study the reaction path and mechanism of CO_2RR synthesis of CH_3OH . This has important theoretical and practical significance for promoting research and development of catalytic CO_2RR synthesis of CH_3OH . This article establishes a database for future research and further guides the experimental study of catalysts for reducing CO_2 to CH_3OH . In future studies, theoretical research will be used in the catalytic CO_2RR to produce alcohols, methane, formic acid, and formaldehyde.

Supplementary Materials: The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/catal14010007/s1.

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