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Manipulatable Interface Electric Field and Charge Transfer in a 2D/2D Heterojunction Photocatalyst via Oxygen Intercalation

Minyeong Je^{1,2}, Eun Seob Sim², Jungwook Woo², Heechae Choi^{1,*} and Yong-Chae Chung^{2,*}

- ¹ Theoretical Materials & Chemistry Group, Institute of Inorganic Chemistry, University of Cologne, Greinstr. 6, 50939 Cologne, Germany; mje@uni-koeln.de
- ² Division of Materials Science and Engineering, Hanyang University, 222 Wangsimni-ro, Seongdong-gu, Seoul 04763, Korea; ses1691@gmail.com (E.S.S.); dkdlfjqmdb20@gmail.com (J.W.)
- * Correspondence: h.choi@uni-koeln.de (H.C.); yongchae@hanyang.ac.kr (Y.-C.C.)

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Abstract: Charge separation is the most important factor in determining the photocatalytic activity of a 2D/2D heterostructure. Despite the exclusive advantages of 2D/2D heterostructure semiconductor systems such as large surface/volume ratios, their use in photocatalysis is limited due to the low efficiency of charge separation and high recombination rates. As a remedy for the weak interlayer binding and low carrier transport efficiency in 2D/2D heterojunctioned semiconductors, we suggested an impurity intercalation method for the 2D/2D interface. PtS₂/C₃N₄, as a prototype heterojunction material, was employed to investigate the effect of anion intercalation on the charge separation efficiency in a 2D/2D system using density functional theory. With oxygen intercalation at the PtS₂/C₃N₄ interface, a reversed and stronger localized dipole moment and a built-in electric field were induced in the vertical direction of the PtS₂/C₃N₄ interface. This theoretical work suggests that the anion intercalation method can be a way to control built-in electric fields and charge separation in designs of 2D/2D heterostructures that have high photocatalytic activity.

Keywords: density functional theory; photocatalytic water splitting; graphitic carbon nitrides; platinum disulfides; 2D/2D heterostructure; intercalation

1. Introduction

With the increasing energy demand, energy conversion and storage are important key factors to meet the demands of humans. At the same time, the energy crisis and environmental pollution problems come one after another because the burning of fossil fuels produces a huge amount of CO_2 . Therefore, renewable energy sources have received intensive attention as an alternative to non-renewable fossil fuels [1–3]. Solar energy conversion to hydrogen and hydrocarbon fuels using photocatalysts are considered to be a very promising renewable energy resources [4,5], however, eco-friendly hydrogen production from solar energy is only 5% of the total commercial hydrogen production [6]. To increase hydrogen production by renewable energy sources, the semiconductor-based photocatalyst has received considerable interest in water splitting and pollutant degradation, such as CO_2 reduction [7,8]. However, the most widely used photocatalysts such as metal oxide and precious metals are limited because of the high cost and the band gap within the ultraviolet region [9–11]. Therefore, semiconductor photocatalysts require a suitable photocatalytic system for efficient charge separation for electron-hole pairs [12–14].

Graphitic carbon nitrides (C_3N_4) have attracted attention for hydrogen and oxygen evolution as a water splitting photocatalyst due to their low cost, easy fabrication, and high chemical and thermal stability [11,15,16]. In particular, the band gap of C_3N_4 (2.70 eV) is appropriate for a photocatalyst



because it covers both water reduction and oxidation [17]. However, C_3N_4 shows poor photocatalytic efficiency induced by the fast recombination of the electron-hole pairs. Thus, to solve these problems, many studies have been conducted using a wide variety of modification strategies such as co-catalyst incorporation, 2D/2D heterostructures, and impurity doping [18–21].

Among the various modification strategies in the photocatalyst, the fabrication of 2D/2D heterojunctions based on monolayer 2D materials has been demonstrated as an effective approach toward high performance photocatalysts. However, due to the large interface region, 2D/2D heterojunctions often exhibit a high charge mobility and low charge recombination rates [22]. To solve this problem, many researchers are trying to find a 2D/2D heterostructure with the appropriate photocatalytic system. In the case of $C_3N_4/2D$ heterostructures, it was found that the photocatalytic systems such as Z-scheme and type-II vary according to the types of materials [23,24]. Therefore, using density functional theory (DFT), systematic research focusing on the rational design and construction of $C_3N_4/2D$ interface is necessary for readers to better understand the principles of 2D photocatalysts.

The charge separation is a very important factor for photocatalytic water splitting [25,26]. In particular, in 2D/2D heterostructures for photocatalyst systems, the driving force for charge separation is the energy level difference of the electrons and holes built by the band alignment of the heterostructure [27–29]. In other words, if the exchange of electrons and holes between the two layers is more active, it is more effective to separate the charge at the interface. However, charge flow across the two layers is restricted in 2D/2D heterostructures because the nature of its interface is commonly a van der Waals (vdW) interaction [30]. This indicates that 2D/2D heterostructures still suffer from low efficiency in charge separating and transferring oriented charges [31,32]. According to previous studies, it is reported that charge separation at interfaces of vdW heterostructures can be promoted through impurity intercalation [30,33]. This means that impurity intercalation will play an important role when a 2D heterostructure strategy is adopted in PtS₂/C₃N₄ heterostructures for increasing photogeneration of electron-hole pairs throughout its lifetime. Among the various impurity atoms, O as the impurity for intercalation was chosen because it does not influence the structure of $g-C-_3N_4$, but improves the charge separation [34,35]. Therefore, it must be confirmed that it is possible to use a PtS₂/O/C₃N₄ heterostructure as a photocatalyst through a theoretical approach.

Among the various 2D materials, transition metal dichalcogenide (TMD) is widely used as a co-catalyst in a photocatalyst due to its hydrogen evolution reaction (HER) ability and the ease of controlling its electronic properties [36–39]. C_3N_4 /TMD heterostructures such as C_3N_4 /MoS₂ and C_3N_4 /SnS₂ afford a high photocatalytic activity [40–42]. Group-10 TMD has been reported as a potentially promising photocatalyst, electrocatalyst, and opto-electronic device because of its unique properties [43–45]. Lattice mismatches must be considered in the heterostructure because they are associated with compressive or tensile stress, affecting the electronic properties [46,47]. Among the Group-10 TMDs, platinum disulfides (PtS₂) showed a low lattice mismatch between 2 × 2 C_3N_4 and PtS₂. In addition, PtS₂ has recently been reported to have shown good HER performance and to have the appropriate band gap of 1.8 eV for a photocatalyst [44]. Thus, PtS₂ was chosen to avoid other effects such as corrugation, and to see only the effects of the O-intercalation.

Herein, the effect of O-intercalation in the PtS_2/C_3N_4 heterostructure was investigated through density functional theory (DFT) calculations. After O-intercalation at the interface, the charge redistribution trend changed. Due to the changed dipole moment by the electron acceptance between the surface and the O, the direction of the built-in electric field was reversed. The amount of charge transfer increased due to the increase in the strength of the built-in electric field at the interface. In addition, charge separation efficiency was improved as O-intercalation increased. PtS_2/C_3N_4 is a suitable photocatalyst for water splitting because the reduction and oxidation stability is strong. However, $PtS_2/O/C_3N_4$ is not suitable for photocatalytic water splitting since its reduction stability is weak. From these results, it is expected that the desired direction of the built-in electric field and the charge separation efficiency can be obtained if the ratio of anion intercalation can be properly controlled.

2. Results and Discussion

As the impurity intercalation of the heterostructure, O atoms were chosen because previous studies have reported that the photocatalytic performance of monolayer C_3N_4 is enhanced by O doping [48]. To theoretically examine the stability of the PtS_2/C_3N_4 heterostructure after doping, the intercalation energy (E_{int}) of the $PtS_2/Ox/C_3N_4$ heterostructure was calculated using Equation (1):

$$E_{int} = \frac{1}{n} \left[E(PtS_2/Ox/C_3N_4) - E\left(\frac{PtS_2}{C_3N_4}\right) - \frac{n}{2}E_{O_2} \right] \ (x = 1.8, \ 3.6, \ 5.4, \ 7.1\%)$$
(1)

where $E_{PtS_2/O_x/C_3N_4}$, E_{PtS_2/C_3N_4} , and E_{O_2} are the total energy of the PtS₂/O_x/C₃N₄, the PtS₂/C₃N₄ heterostructure and the O₂, respectively. The n is the number of O atoms in the heterostructure. The E_{int} of the PtS₂/O_{1.8%}/C₃N₄ heterostructure was -1.78 eV. The optimized configuration of the PtS₂/O_x/C3N4 heterostructure is shown Figure S1. The E_{int} of all considered PtS₂/O_x/C₃N₄ heterostructures is shown in Table S1. Based on these results, we can infer that the PtS₂/O_{1.8%}/C₃N₄ heterostructure is energetically stable. This means that the O atoms remain captured between the C₃N₄ and PtS₂ layers, rather than diffusing between the layers and recombining to yield O₂ or H₂O gas. The calculated interface binding energy (E_b) of the PtS₂/C₃N₄ and the PtS₂/O_{1.8%}/C₃N₄ heterostructures was 12.5 and 10 meV/Å², which was close to the typical vdW-binding energy (13–21 meV/Å²) in previous works [49,50]. Hence, the PtS₂/C₃N₄ and PtS₂/O_{1.8%}/C₃N₄ heterostructure.

To explore the charge separation after the O-intercalation in the PtS_2/C_3N_4 heterostructure, the charge density difference and planar-averaged charge density difference of the PtS_2/C_3N_4 and $PtS_2/O_X/C_3N_4$ (X = 1.8, 3.6, 5.4, 7.1 %) heterostructures were calculated. The charge density difference iso-surface can be evaluated with Equation (2):

$$\Delta \rho(z) = \rho_{total} - \left(\rho_{C_3N_4} + \rho_{PtS_2}\right) - \rho_O \tag{2}$$

where ρ_{total} , $\rho_{C_3N_4}$, ρ_{PtS_2} , and ρ_X denote the charge densities of the PtS₂/C₃N₄ or PtS₂/O_X/C₃N₄ heterostructure, the monolayer C₃N₄, the monolayer PtS₂, and the O atom, respectively. It is defined as Equation (3):

$$\Delta Q(z) = \int_{-\infty}^{z} \Delta \rho(z') dz'$$
(3)

The charge density difference and planar charge density difference of the PtS_2/C_3N_4 and the $PtS_2/O_{1.8\%}/C_3N_4$ heterostructures is shown in Figure 1a. The charge density difference iso-surface plots are shown in the inset in Figure 1a. The yellow and sky blue colors indicate the electron accumulation and depletion regions, respectively. The red line of Figure 1a indicates that the planar-averaged charge density difference of the C_3N_4/PtS_2 (left) and the $PtS_2/O_{1.8\%}/C_3N_4$ (right) heterostructures along the Z direction exhibited charge redistribution. In both the PtS_2/C_3N_4 and the $PtS_2/O_{1.8\%}/C_3N_4$ heterostructures, the charge redistribution mainly occurred around the PtS₂/C₃N₄ heterostructure interface and the charge transferred from the C_3N_4 to the PtS₂ layer in the heterostructure. However, in the case of the PtS_2/C_3N_4 heterostructure, little charge transfer showed between the C_3N_4 and PtS_2 . (Figure 1a) This indicates that the PtS_2/C_3N_4 heterostructure shows a low efficiency of separation of photogenerated electron-hole pairs, like other 2D/2D heterostructures [31,51]. Due to the O-intercalation, the $PtS_2/O_{1.8\%}/C_3N_4$ heterostructure effectively boosts the charge separation, better than that of the PtS_2/C_3N_4 heterostructure. The charge transferred from the PtS_2 to the C_3N_4 layer at the interface of the $PtS_2/O_{1.8\%}/C_3N_4$ heterostructure, unlike in the PtS_2/C_3N_4 heterostructure. In addition, in the other O concentration, the direction of charge transfer was the same, and the amount of charge transfer increased (Figure S2). From these results, this study confirmed the impurity intercalation effect on the amount and direction of charge transfer.

(a)

∆ p (10⁻¹ e/Å)

0.2

0.1

0.0

-0.1



-0.2 12 14 16 10 18 20 10 12 14 16 18 20 Z (Å) Z (Å) (b) Built-in E field (10⁶ V/cm) 6.0 Dipole 0.10 5.0 4.0 0.00 3.0 moment 2.0 0.10 1.0 0.0 -1.0 Ð 0.30 -1.5 0 1.8 3.6 5.4 7.1 Oxygen concentration (%)

Figure 1. The charge density difference and planar-averaged electron density difference for the (a) PtS_2/C_3N_4 (**left**) and $PtS_2/O_{1.8\%}/C_3N_4$ (**right**) heterostructures. The yellow and cyan color indicate charge accumulation and depletion, respectively. The iso-values are 0.005 eV/Å³. The purple, yellow, blue, gray, and red colors denote the Pt, S, N, C, and O atoms, respectively. (b) The built-in electric field and dipole moment of the $PtS_2/O_3/V_4$ (X = 0, 1.8, 3.6, 5.4, 7.1%) heterostructure.

As the built-in electric field at the interface makes an important contribution to charge separation (drifted charge separation) and other charge separation pathways in semiconductors, it must be conceivable [52,53]. In general, the direction of a built-in electric field is induced by the dipole moment [54,55]. Thus, the dipole moment and built-in electric field of the PtS₂/C₃N₄ and the PtS₂/O_X/C₃N₄ heterostructures were calculated, as shown in Figure 1b. Using Equation (3), the dipole moment (μ) is given by Equation (4)

$$\mu = \int_{-\infty}^{\infty} z \Delta Q(z) dz \tag{4}$$

where z indicates the z-axis distance. In Figure 1b, the red line denotes the dipole moment. The μ value decreases as O-intercalation increases and the direction of μ is reversed. As the oxygen is inserted, the direction and strength of the μ changes because the electrons on the surface of the PtS₂ move to the O, resulting in the surface of the PtS₂ having a positive charge. This result indicates that the change in dipole moment is caused by the acceptance of electrons occurring between the PtS₂ layer and the O, regardless of the interaction between the O and the C₃N₄ layer. From these results, it can be predicted that a similar dipole moment change will occur due to electron acceptance between the surface and the anion if the other anion as well as the O are inserted into the 2D/2D heterostructure. Next, a built-in

electric field was generated at the PtS_2/C_3N_4 and the $PtS_2/O_X/C_3N_4$ heterostructure. Thus, the built-in electric field was calculated as Equation (5):

$$\mathbf{E} = \int_{-\infty}^{z} \frac{\Delta \rho(z')}{\varepsilon_0} dz' \tag{5}$$

where E and ε_0 are the built-in electric field, the charge density, and the vacuum permittivity, respectively. $\Delta\rho$ is the charge density difference obtained in Equation (2). The built-in electric field of the PtS₂/C₃N₄ heterostructure (-1.11×10^6 V/cm) was smaller than that of the PtS₂/O_{1.8%}/C₃N₄ heterostructure (1.64×10^6 V/cm). In addition, the direction of the built-in electric field was reversed after O-intercalation in the C₃N₄/PtS₂ heterostructure. As the amount of O-intercalation in the PtS₂/C₃N₄ heterostructure increased, the strength of the built-in electric field increased (Figure 2b). As shown in Figure 2b, as O-intercalation increased, the intensity of the dipole moment and the built-in electric field increased linearly. From these results, it can be inferred that the direction of the built-in electric field indicates that a powerful electrostatic field existed perpendicular to the interface direction. Thus, it can be predicted that the PtS₂/O_X/C₃N₄ heterostructure will show increased photocatalytic activity because the driving force for charge separation provided by the built-in electric field is consequently enhanced, thus leading to significantly increased photocatalytic activity.



Figure 2. The band structure of (**a**) the PtS_2/C_3N_4 and (**b**) the $PtS_2/O_{1.8\%}/C_3N_4$ heterostructure, respectively. The contribution of each layer in the band structure of the PtS_2/C_3N_4 heterostructure with or without O-intercalation. The percentages of the contributions of each layer are marked in a different color. The Fermi level was set to zero.

The optimized band structure of the PtS₂/C₃N₄ and the PtS₂/O_{1.8%}/C₃N₄ with various O concentration heterostructures was calculated to confirm the photocatalytic activity (Figure 2). Considering that, in general, the PBE approach underestimates the band gaps (E_g), this study used a band structure calculated using the HSE06 method to increase the reliability in the following analyses. The contribution of each layer in the conduction band minimum (CBM) and valence band maximum (VBM) of the PtS₂/C₃N₄ and the PtS₂/O_{1.8%}/C₃N₄ heterostructure was investigated as shown in Figure 3. Since it is generally known that the trends of hybrid functional calculations and normal DFT calculations are not very different, the contribution of each layer in the CBM and the VBM was verified using the band structure of the PBE approach [56]. The contributions of each layer in the PtS₂/O_{3.6%}/C₃N₄ heterostructures are shown in Figure S3. The C₃N₄ layer in the PtS₂/C₃N₄ heterostructure largely contributed to the VBM, whereas the CBM was dominated by the

PtS₂ layer in the C_3N_4/PtS_2 heterostructure (Figure 2a). In addition, this phenomenon was maintained despite the amount the O-intercalation increased in the PtS_2/C_3N_4 heterostructure (Figure 2b and Figure S3). The PtS_2/C_3N_4 heterostructure with and without O-intercalation had staggered gap structures, resulting in Z-scheme or type-II systems. The reason for the difference of heterostructure type is due to the difference in the direction and strength of the built-in electric field caused by the difference in charge redistribution occurring by O-intercalation. From these results, it can be inferred that the electrons and holes will move differently in the PtS_2/C_3N_4 and the $PtS_2/O_X/C_3N_4$ heterostructures when visible-light irradiation is absorbed.



Figure 3. The CBM and VBM potential versus the normal hydrogen electrode of the PtS_2/C_3N_4 and the $PtS_2/O_X/C_3N_4$ (X = 1.8, 3.6, 5.4, 7.1%) heterostructures using the HSE06 method. E means the built-in electric field.

The band edge position of the PtS_2/C_3N_4 and the $PtS_2/O_x/C_3N_4$ heterostructures, which is another important factor that determines the performance of photocatalytic water splitting of a semiconductor, was calculated to confirm the redox capability of the PtS_2/C_3N_4 and the $PtS_2/O_x/C_3N_4$ heterostructures. The potential level vs. the normal hydrogen electrode (NHE) was converted from the vacuum potential level ($E_{vacuum votential level}$) using Equation (6) [57]:

$$E_{\text{potential level vs NHE}} = E^e - E_{\text{vacuum potential level}}$$
(6)

where E^e is the energy of the free electrons at the hydrogen scale ($E^e = -4.44 eV$) and $E_{vacuum potential level}$ is obtained by the planar-averaged electrostatic potential. To achieve water splitting on the semiconductor, the CBM potential is more negative than the H⁺/H₂ reduction potential (0.0 eV), and the VBM potential is more positive than the H₂O/O₂ oxidation potential (1.23 eV). Figure 3 shows the charge transfer and band edge position of the PtS₂/C₃N₄ and the PtS₂/O_x/C₃N₄ heterostructures. The band edge position of the CBM (VBM) potential in the C₃N₄/PtS₂ heterostructure was -0.56 (1.66 eV), which was more negative (positive) than the H⁺/H₂ reduction (O₂/H₂O oxidation) potential. Based on the direction of the built-in electric field, in the case of the PtS₂/C₃N₄ heterostructure, the electrons in the CBM of the PtS₂ could transfer to the VBM of the C₃N₄ to combine with holes. In addition, the electrons in the CBM of the C₃N₄ were used to reduce H⁺ to H₂, and the holes in the VBM of the C₃N₄ were used to reduce H⁺ to H₂. Through this result, it can be inferred that the PtS₂/C₃N₄ heterostructure showed a Z-scheme. In the case of the PtS₂/O_X/C₃N₄ heterostructure, the electrons transferred from the CBM of the C₃N₄ to the CBM of the PtS₂ and the VBM holes of the PtS₂ transferred into the VBM of the CBM C_3N_4 structure. Thus, H^+/H_2 reduction and O_2/H_2O oxidation occurred in the CBM of the PtS₂ and the VBM of the C_3N_4 . In the density of states, there was no defect level caused by O in the energy gap of the PtS₂ and the C_3N_4 (Figure S4). In the case of the C_3N_4 layer, the energy gap increased as O was inserted at the interface of the PtS_2/C_3N_4 heterostructure. On the other hand, the energy gap of the PtS_2 layer decreased. Due to the decreased energy gap of the PtS_2 , the CBM of the PtS_2 was lower than the O_2/H_2O oxidation potential. Given the decreased energy gap of the PtS₂, the CBM of the PtS₂ was lower than the O_2/H_2O oxidation potential. As the monolayer C_3N_4 and monolayer PtS_2 had an indirect band gap, C_3N_4 and PtS_2 exhibited similar photo absorption efficiency. However, after the intercalation of O at the interface of the heterostructure, the strength of photo absorption in the PtS_2 with a decreased energy gap will increase. From these results, it can be inferred that the strength of photo absorption in the PtS₂ will be stronger than that of the C_3N_4 when visible-light irradiation is absorbed. The CBM level was located about 0.09 eV under the H^+/H_2 reduction potential. Using the thermal energy at room temperature (0.026 eV), the possibility of H^+/H_2 reduction occurring in the $PtS_2/O_{1.8\%}/C_3N_4$ heterostructure was approximately 3%. Thus, it was found that the O-intercalation in the PtS_2/C_3N_4 heterostructures not only enhanced the separation of photogenerated electron-hole pairs, but also changed the direction of the built-in electric field, resulting in the determination of the heterostructure type.

Considering the generally used synthesis conditions of C_3N_4 , the possibility of O intercalation in the PtS_2/C_3N_4 heterostructure was examined theoretically. The relationship between the equilibrium constants (K_p) for reactions and temperatures was considered based on the thermodynamic energy of intercalation formation. The main reactions occurring in the $PtS_2/O/C_3N_4$ heterostructure can be written as follows:

(1) O₂ gas

$$PtS_2/C_3N_4 + \frac{1}{2}O_2(g) \to PtS_2/O/C_3N_4$$

(2) H₂O gas

$$PtS_2/C_3N_4 + H_2O(g) \rightarrow PtS_2/O/C_3N_4 + H_2(g)$$

The Gibbs energy for interaction is described in Equation (7):

$$\Delta G_f = G_{PtS_2/O/C_3N_4} - G_{PtS_2/C_3N_4} + \sum n_O \mu_O \tag{7}$$

where $G_{PtS_2/O/C_3N_4}$, $G_{PtS_2/O/C_3N_4}$, n_O , and μ_O denote the Gibbs energy of the PtS_2/O/C_3N_4 heterostructure, the Gibbs energy of the PtS_2/C_3N_4 heterostructure, the coefficient atoms in the chemical equation, and the chemical potential of atoms, respectively. In the case of μ_O , it can be written as Equation (8):

$$\mu_i = \mu^0(T) + k_B T ln\left(\frac{p_i}{p^0}\right) \tag{8}$$

where μ^0 , k_B , T, p^0 , and p_i are the standard chemical potential ($p_0 = 1$ bar), Boltzmann constant, temperature, standard partial pressure, and partial pressure, respectively. The standard chemical potential values were taken from the JANAF-NIST thermochemical table [53]. Using Equation (2) and Equation (6), the Gibbs energy for intercalation can be expressed as Equation (9):

$$\Delta G_f = \Delta E_{DFT} + \Delta \mu_0(T, P_0) + k_B T ln(K_p)$$
(9)

where ΔE_{DFT} and K_p are the change in total energies of the DFT and the equilibrium constant, respectively. Hence, K_p is defined as Equation (10):

$$K_p = e^{\left(\frac{\Delta G_f - \Delta E_{DFT} - \Delta \mu_0(T, P_0)}{k_B T}\right)}$$
(10)

To consider the concentration of O-intercalation, the Boltzmann distribution is given by Equation (11)

$$\frac{x_p}{x_i} = e^{\left(\frac{G_i - G_p}{k_B T}\right)} = e^{\left(\frac{\Delta G_f}{k_B T}\right)}$$
(11)

where x_p , x_i , G_p , and G_i denote the molar fraction of pristine and intercalation, and Gibbs free energy of pristine and intercalation in the PtS₂/C₃N₄ heterostructure, respectively.

Using Equations (10) and (11), K_p is given by Equation (12)

$$K_p = \frac{x_p}{x_i} \cdot e^{\left(\frac{-\Delta E_{DFT} - \Delta \mu_0(T, P_0)}{k_B T}\right)}$$
(12)

The calculated K_p was plotted for varying temperatures (Figure 4). It is known that C_3N_4 exhibits good crystallinity under the synthesis conditions between 873 and 973 K [58]. Therefore, to exclude other factors that affect the photocatalytic activity, other than O-intercalation, the temperature range for K_P was set from 800 K to 1000 K. When O_2 gas is used as the reactant gas, the partial pressure of the O_2 gas must be 2.83×10^{21} atm at 800 K and 5.60×10^{18} atm at 1000 K in order to insert 1 at% O. However, these partial pressures are much higher than the practical processing capabilities of synthesis devices. When H_2 o is the reactant gas for O-intercalation in the PtS₂/C₃N₄ heterostructure, the partial pressure of the H₂ should be controlled between 6.3×10^{-7} atm and 3.9×10^{-6} atm, which is a feasible range in synthesis devices. Through this result, it is expected that the PtS₂/O/C₃N₄ heterostructure can be synthesized using H₂O gas as the reactant gas.



Figure 4. The K_{ps} of the $PtS_2/O_X/C_3N_4$ (X = 1, 5, 10, 50%) heterostructure expressed depending on the temperature for fabrication.

3. Calculation Method

All DFT calculations were performed with the Vienna Ab initio package (VASP) [59,60]. The interactions between the valence and core electrons were described using the projector augmented wave (PAW) method [61]. A generalized gradient approximation (GGA) with the Perdew–Burke–Ernzerhof (PBE) functional was employed for the plane-wave expansion with a cutoff energy of 500 eV [62,63]. Brillouin zones were sampled with a Monkhorst–Pack k-point grid of $2 \times 2 \times 1$ in the 4×4 PtS₂/C₃N₄ heterostructure with O-intercalation [64]. The energy convergence criteria in the self-consistent field were set to 10^{-5} eV. All geometry structures were fully relaxed until the Hellman–Feynman forces achieved a range of 0.02 eV Å⁻¹. The Methfessel–Paxton smearing scheme was applied with a smearing width of 0.1 eV [65]. To avoid the artifact of a neighboring periodic image, the size of the vacuum region in the z direction was set to a value larger than 20 Å. The vdW correction was considered with Grimme's DFT-D3 (BJ) scheme to accurately describe the interaction between the C₃N₄ and PtS₂

layers [66]. The band gap of the PtS₂/C₃N₄ and PtS₂/O_X/C₃N₄ (X = 1.8, 3.6, 5.4, 7.1%) heterostructures were determined by the hybrid functional (HSE06) with $\alpha = 0.2$ [67].

4. Conclusions

This study demonstrated that anion intercalation in a 2D/2D heterostructure is an effective way to manipulate the direction and strength of the built-in electric fields and dipole moments. The direction of the vertical built-in electric field in the PtS_2/C_3N_4 heterostructure can be reversed with O-intercalation at the interface, as the O-atom bound to the PtS_2 accepts electrons and induces a local dipole moment in the opposite direction. When the O-intercalation density increased, the intensities of the electric field and dipole moment increased nearly linearly. It was also noticeable that the band edge levels in the PtS_2 and the C_3N_4 significantly shifted with different O-intercalation amounts. Hence, this anion intercalation method can be widely used for 2D/2D heterojunction photocatalysts for effective control of charge separation aspects and redox reactivities.

Supplementary Materials: The following are available online at http://www.mdpi.com/2073-4344/10/5/469/s1, Figure S1: The stable configuration of the PtS₂/O_x/C₃N₄ heterostructure (x = (a) 1.8, (b) 3.6, (c) 5.4, and (d) 7.1%). The purple, yellow, blue, gray, and red color denote the Pt, S, N, C, and O atoms, respectively, Figure S2: The charge density difference and planar-averaged electron density difference for the PtS₂/O_{3.6%}/C₃N₄, PtS₂/O_{5.4%}/C₃N₄, PtS₂/O_{5.4%}/C₃N₄, heterostructures. The purple, yellow, blue, gray, and red atoms indicate Pt, S, N, C, and O, respectively. The yellow and cyan areas indicate charge accumulation and depletion, respectively. The iso-values are 0.005 eV/Å³, Figure S3: The band structure of the PtS₂/O_{3.6%}/C₃N₄, PtS₂/O_{5.4%}/C₃N₄, and PtS₂/O_{7.1%}/C₃N₄ heterostructures. The percentages of the contributions of each layer are marked in a different color. The Fermi level was set to zero, Figure S4: The projected density of states in the PtS₂/O_x/C₃N₄ (x = 0, 1.8, 3.6, 5.4, 7.1%) heterostructure. The black, blue, and red line indicate the PtS₂ layer, C₃N₄ layer, and O atom in the PtS₂/O_x/C₃N₄ heterostructure. The Fermi level (vertical black dotted line) was set to zero, Table S1: The intercalation energy of the PtS₂/O_x/C₃N₄ heterostructure (x = 1.8, 3.6, 5.4, 7.1%).

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