## Supplementary Materials: Hierarchical sparse nonnegative matrix factorization for hyperspectral unmixing with spectral variability

## Tatsumi Uezato <sup>1,†</sup>, Mathieu Fauvel <sup>2</sup> and Nicolas Dobigeon <sup>1,3,\*</sup>

<sup>1</sup> This report provides complementary results in support of the paper [1]. Section 1 conducts

<sup>2</sup> an sensibility analysis of the proposed algorithm with respect to key parameters. Section 2 reports

<sup>3</sup> additional quantitative results for experiments conducted on the synthetic data sets SIM1 and SIM2

4 corrupted by a noise with a lower signal-to-noise-ratio (SNR).

## 5 1. Parameter sensitivity analysis

- <sup>6</sup> The sensitivity of the proposed HSNMF algorithm with respect (w.r.t.) the parameters  $S_1$  and
- $\lambda_a$  is illustrated in Fig. S1 in term of accuracy of abundance estimation (RMSE). As expected, a large
- \* value (i.e.,  $\approx$  10) of  $\lambda_a$  leads to poor estimates of the abundances by imposing too much sparsity. For
- the SIM1 data set, a large value of  $S_1$  results to bad esimation mainly because the clustering step fails.
- <sup>10</sup> On the other hand, for the SIM2 data set, the HSNMF algorithm seems to be less sensitive w.r.t. the
- <sup>11</sup> parameters. This can be explained by the fact this data set contains a large number of prototypal
- <sup>12</sup> endmember spectra.



**Figure S1.** Sensitivity analysis of the proposed HSNMF w.r.t. the parameters  $\lambda_a$  and  $S_1$ .

## 13 2. Results obtained from a low SNR scenario

In [1], experiments are conducted with a noise level chosen as SNR = 30dB. Hereafter, we report 14 results obtained for a wose case scenario by imposing a noise level of SNR= 20dB. Tables S1 and S2 15 provide the quantitative results for the SIM1 and SIM2 data sets, respectively. For SIM1 in this low 16 SNR scenario, HSNMF performs better than compared methods except EBE-MEMM in terms of RMSE, 17 SAM and JD. The good performance of EBE-MEMM can be explained by the fact this method is able to 18 extract a larger number of endmember spectra within each class, thus reducing the impact of noise 19 during the multiple endmember unmixing process. For SIM2, the proposed HSNMF outperforms 20 other compared methods in terms of RMSE, SAM and JD. This shows that HSNMF is robust to low 21 SNR when endmember variability is large. 22

	C-SunSAL	ELMM	MEMMs	EBE-FL	EBE-MEMM	HSNMF
RMSE	0.0865	0.0377	0.0288	0.0432	0.0198	0.024
RE	0.0433	0.0226	0.0434	0.0293	0.0336	0.0345
SAM	0.0374	0.0311	0.0367	0.0214	0.0210	0.0229
JD	0.7132	0.6147	0.1287	0.5678	0.1037	0.1079
Time	0.085	92.2889	2.6762	5.574	4.7082	19.0501

**Table S1.** SIM1 (SNR= 20dB) – Quantitative results (best values in bold).

Table S2. SIM2 (SNR= 20dB) – Quantitative results (best values in bold).

0	C-SunSAL	ELMM	MEMMs	EBE-FL	EBE-MEMM	HSNMF
RMSE	0.2036	0.1502	0.112	0.1854	0.1125	0.044
RE	0.0598	0.0331	0.057	0.058	0.0564	0.0387
SAM	0.0767	0.0618	0.0759	0.0623	0.0743	0.0337
JD	0.5491	0.5266	0.1712	0.5009	0.1698	0.0947
Time	0.2479	237.3549	18.4855	4.4852	19.1069	606.1786

23

24 1. Uezato, T.; Fauvel, M.; Dobigeon, N. Hierarchical sparse nonnegative matrix factorization for hyperspectral

<sup>25</sup> unmixing with spectral variability. *Remote Sensing* **submitted**.