

Article

A Comparative Analysis of Measured and Simulated Data of PV Rooftop Installations Located in Poland

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Abstract: In recent years, photovoltaics (PVs) is the main driver of the renewable energy market growth in Poland. The number of photovoltaic installations, most of which are rooftop prosumer systems, is consistently growing. Therefore, the determination of the applicability and feasibility of photovoltaic systems under different climate conditions is of great significance. This study presents the performance analysis of four prosumer photovoltaic installations situated in the Eastern part of Poland, Lublin Voivodeship. The influence of various tilt angles, ranging from 19° to 40°, and azimuths (south, east, south–east, and east–west) on the final yield have been determined under one year of operation (2022). The average yearly final yield was found to be 1022 kWh·kW⁻¹, with the highest value obtained for the installation oriented towards the south, equal 1079 kWh·kW⁻¹. Then, the PV systems were simulated by the use of four specialized photovoltaic software: DDS-Cad 16, PVGIS 5.2, PVSOL premium 2022, and the PVWatts Calculator 8.2.1. A comparative analysis of the measured and simulated data in terms of the final yield was carried out. The data obtained from PVGIS and PVSOL demonstrated the highest degree of overall alignment of 92% and 91%, respectively. The most significant underestimation was noticed for the DDS-Cad software, which was equal to 77%. The most accurate predictions stand out for the system oriented to the south, while the weakest was found for the E–W installation.

Keywords: photovoltaics; PV system; PV installation; rooftop system; final yield; PVSOL software; DDS-Cad software; PVGIS software; PVWatts software



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1. Introduction

In recent years, technological development, population growth, improvements in the standards of living, and, thus, an enhanced demand for electricity have contributed to a significant increase in energy consumption. In addition, it is expected that this energy demand will increase by approximately 25% by 2050 [1]. However, fossil fuel combustion, which is still the most commonly used energy production process, has a negative impact on the environment. It is predicted that the fossil fuel share in the electricity mix will decrease from the present 59% to 12% by 2050 [1]. Nowadays, the coal share in gross energy production in Poland is approximately 70% [2,3]. All these factors have raised concerns about air pollution, the emission of greenhouse gases (GHGs), climate change, and the depletion of non-renewable resources. Nonetheless, the energy policy of the European Union (EU), and, thus, Poland, has recently been focused on the decarbonization process and energy transition. Climate neutrality by 2050 is a long-term worldwide strategy that assumes zero net emissions of GHGs into the atmosphere, counteracting climate change and its related negative effects. One of the main goals, which was claimed in the Paris Agreement [4], is to limit the increase of the average global temperature to 1.5 °C above pre-industrial levels. Poland's National Energy and Climate Plan for the years 2021–2030 (NECP PL) [5] was developed in 2019 in accordance with Regulation (EU) 2018/1999 of the European Parliament and of the Council of 11 December 2018 on the Governance of the Energy Union and Climate Action [6]. The main objective of the NECP PL is to achieve a

7% reduction of GHG emissions compared to the level in 2005 and 21–23% of the renewable energy source (RES) share in gross final energy consumption by 2030, to decrease primary energy consumption by 23% compared to the PRIMES 2007 predictions, and to reduce the coal share in electricity generation by 56–60%. Nonetheless, the European Commission proposed, in 2021, a new GHG reduction target equal to 17.7% [7], and, in May 2022, new RES targets by 2030 that would increase them to 45%, as a part of the REPowerEU plan [8]. The use of renewable energy in gross energy generation in Poland reached the value of 27.8% in 2021, while the 10-year increase ratio was equal to 9.9% [2]. According to The Institute for Renewable Energy data, the increase in the capacity of PV systems in EU countries in 2022 compared to 2021 was equal to 22%, while, for Poland, it was 61%. It is important to mention that about 70% of photovoltaic systems installed in Poland belong to prosumers [9]. Taking into consideration all regulations and national renewable energy subsidy programs, such as “My Electricity” [10,11], further growth in the photovoltaic sector is predicted [12].

All these aforementioned factors force researchers to thoroughly scrutinize the potential of photovoltaics, and, thus, assess its suitability, in various locations. Numerous scientific papers are devoted to the performance of PV systems located in Europe under real outdoor conditions. Gaglia et al. [13] presented a detailed analysis of a photovoltaic system consisting of multicrystalline modules (mc-Si) located in Athens, Greece during the summer and winter periods. The system was oriented towards the south with a tilt angle equal to 20°. The efficiency of the system under real outdoor conditions was found to be lower than the value obtained for standard test conditions (STCs). The analysis of two rooftop systems located in Trieste, Italy is presented in the work of Micheli et al. [14]. The orientations of the analyzed installations were south with a tilt angle of 10°, and south–west with an inclination equal to 30°. Due to favorable irradiations in the selected location, the yearly final yields (Y_f) were determined to be 1400 kWh·kW⁻¹ and 1277 kWh·kW⁻¹, respectively. Another performance measurement and analysis were conducted in south-eastern Italy by Congedo et al. [15]. The analyzed system is divided into two subfields, both of which consist of monocrystalline modules (mono-Si), and is installed on the parking shelter with the azimuth towards the south and tilt angles of 3° and 15°. The values of the average monthly yield ranged from 97.88 kWh·kW⁻¹ in December to 184.73 kWh·kW⁻¹ in June. Several studies were also carried out for the photovoltaic system located in Polish conditions. Sarniak [16] presented research about the prosumer photovoltaic installation for a single-family house located in Poland (52°48′ N, 19°67′ E). The installation, made of polycrystalline modules with a nominal power of 270 W, is oriented towards the south with a tilt angle of 22°. The yearly final yield was found to be 1072.9 kWh·kW⁻¹. A comprehensive review of nine photovoltaic systems, all of which are located in south-eastern Poland, is presented in the work of Gulkowski [17]. The study of the azimuth’s and the tilt angle’s influence on the final yield ratios was carried out over nearly one year of systems operation, from November 2020 to October 2021. The average final yield was 990.2 kWh·kW⁻¹ for all systems. Depending on the PV system, the highest Y_f value was found to be 1102.9 kWh·kW⁻¹, and the lowest one was equal to 868.8 kWh·kW⁻¹. The analysis of one year of operation (2019) of a polycrystalline system located in the city of Lublin, Poland was performed in the work of Zdyb and Szalas [18]. The analyzed installation was a low-angle tilted flat-rooftop system with a power capacity of 15 kW. The obtained results indicated that the final yield was close to 1100 kWh·kW⁻¹. An overview of the free-standing installation, located in Lublin Voivodeship (51°51′ N latitude), in which four types of photovoltaic modules were examined, including mc-Si, is presented in [19]. The installation is oriented towards the south with an inclination of 34°. The presented data pertain to four years of operation, from 2015 to 2018. The average value of the final yield was found to be 1038.89 kWh·kW⁻¹, ranging from 936 kWh·kW⁻¹ for 2017 to 1130.54 kWh·kW⁻¹ for 2018. In addition, various studies have been published on energy potential analysis under different outdoor conditions and locations by the use of specialized computer software. Haffaf et al. [20] presented the analysis of a 2.4 kW photovoltaic system, situated in France (47°43′ N, 7°18′ E); this

work has also been simulated by the use of PVGIS, PV Watts, and HOMER software. The performance simulations were also carried out via PVSOL, PVGIS, SolarGIS, and SISIFO in the work of Dondaryia et al. [21], in which performance prognosis was performed for a 6.4 kW on-grid installation made of monocrystalline modules facing south with a tilt angle of 23° placed in India. Akpolat et al. [22] presented an analysis of the feasibility and applicability of on-grid photovoltaic systems in Turkey by the use of PVSOL software. A comparative comparison of predictions obtained from PVGIS, PVSOL, and PVWatts for a 6.4 kW rooftop system, situated in Cyprus, is provided in the work of Kassem et al. [23]. The simulations (PVSOL and PVsyst) were also used by Mubarak et al. [24] to examine various azimuths and tilt angles to increase self-consumption for an installation placed in Hannover (Germany). The measured data was compared with the simulated one. Kurz and Nowak [25] used PVSOL software to determine the profitability of a 5.25 kW prosumer installation, taking into consideration self-consumption and the payback time, situated in Bydgoszcz in central Poland.

Due to the increasing interest in renewable energy sources, and, thus, photovoltaic energy sources, many PV systems are installed all over the world. Nonetheless, the efficiency of photovoltaic installations is influenced by numerous factors, including climatic conditions which are strongly correlated with their locations. The performance of the installation can be determined on the basis of experimental data and by predictions obtained from specialized software. However, to the author's best knowledge, a limited number of publications provide a comparison between measured data and values obtained from simulations. An even smaller quantity of works present the simulation results obtained from more than one simulation software. Nonetheless, the highest degree of alignment is required in order to obtain the most realistic and reliable results under different experimental conditions. The objective of this work is to present the analysis of the final yield of four photovoltaic installations located in Lublin Voivodeship, Poland, for 2022. The systems are characterized by different orientations (south, east, south–east, and east–west) and tilt angles. In addition, four types of specialized photovoltaic software, namely, DDS-Cad 16, PVGIS 5.2, PVSOL premium 2022, and the PVWatts Calculator 8.2.1, were used to simulate the investigated PV installations. A thorough analysis of the measured data and simulations is provided, with an in-depth comparison of other authors' results presented in the literature.

2. Materials and Methods

2.1. Study Size Characteristics

Four grid-connected installations were selected for this case study, located on the rooftops of various households in eastern Poland, specifically in the Lublin Voivodeship. According to the Köppen-Geiger classification, the Lubelskie region is characterized by a warm temperate climate, fully humid with warm summers (Cfb) [26]. The region has good sun exposure, which equals 1123 kWh/m²/year. Furthermore, based on the Polish standard PN-EN 12831:2006 [27], the Lublin region is located in the third climate zone with an average outdoor temperature of 7.6 °C. The installations are situated near each other, as shown in Figure 1, and, therefore, operate in the same climatic conditions. The longitude and latitude of PV1–PV4 installations are 52.65° N 23.03° E, 51.77° N 22.63° E, 51.69° N 23.22° E, and 51.29° N 22.52° E, respectively.

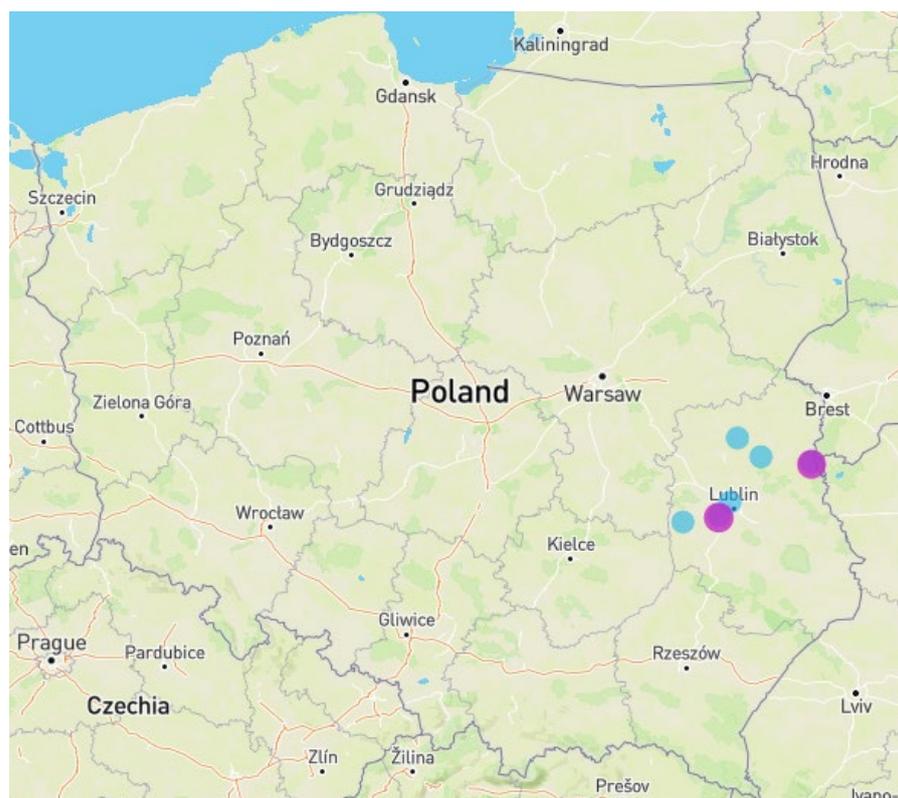


Figure 1. Localization of selected PV installations (blue dots) and weather stations (magenta dots) on Poland map.

The analyzed installations were commissioned in recent years: PV1 in June 2020, PV2 in October 2020, PV3 in November 2019, and PV4 in March 2021. The PV1 is a flat-roof system with an inclination of 19° and azimuth of 145° . It is composed of 23 series-connected PV modules with a nominal power of 310 Wp. PV2, PV3, and PV4 are rooftop systems with PV modules mounted vertically, parallel to the rooftop. The nominal output of PV2 system is 5.28 kW, and it is composed of 16 modules, each with a nominal power of 330 Wp. The orientation is 102° , while the tilt angle is 35° . The PV installation of the 3rd case study consists of 22 series-connected modules, each with a nominal power of 285 Wp, facing south (175°) at an inclination of 40° . The last PV system (PV4) faces east–west and is composed of 12 PV generators, each with a power of 325 Wp, tilted at an angle of 32° . The setup is divided into 2 maximum power point trackers (MPPts), with 6 and 5 series-connected modules on each tracker, facing east and west, respectively. It is important to mention that the tilt angles of PV installation are close to the optimal tilt angle for Poland, which is about 35° . This tilt angle allows photovoltaic modules to capture the optimal amount of solar irradiation. Since the installations are mounted on the roofs of real households, they are cleaned naturally with rainfall, and no additional cleaning methods are implemented. The detailed data about analyzed systems can be found in Table 1. Information about modules and inverters in standard test conditions (STC; $T = 25^\circ\text{C}$, $G = 1000\text{ W/m}^2$, AM 1.5) is presented in Tables 2 and 3, respectively. Monocrystalline modules were used in each installation, with efficiency ranging from 18.90% to 19.60%. All of the installations were made of 2 strings, each connected to a different MPP tracker. The inverters, which main role is to convert the DC (direct current) to AC (alternating current), have an efficiency no smaller than 98%. The schematic diagrams of analyzed PV1–PV4 systems is presented in Figure A1, Appendix A.

Table 1. Technical parameters of analyzed PV systems.

PV System	Azimuth [°]	Tilt Angle [°]	PV Module			Nominal Power of System [kW]
			Manufacturer	Type	Power [Wp]	
PV1	145	19	Risen Energy (Ningbo, China)	RSM-60-6-310M	310	7.13
PV2	102	35	Risen Energy	RSM-120-6-330M	330	5.28
PV3	175	40	Sharp (Sakai City, Japan)	NU-AC310	310	6.20
PV4	78/258	32	Q-Cells SE (Seoul, South Korea)	Q.PEAK DUO-G5 325	325	3.58

Table 2. Configuration of analyzed PV systems.

PV System	Inverter's Manufacturer	Inverter Model	Number of Modules [pcs.]	Configuration	
PV1	SOFARSOLAR Co. (Shenzhen, China)	8.8KTL-X	23	1 string/1st tracker	11 pcs.
				1 string/2nd tracker	12 pcs.
PV2	SOFARSOLAR Co.	4.4KTL-X	16	1 string/1st tracker	8 pcs.
				1 string/2nd tracker	8 pcs.
PV3	SOFARSOLAR Co.	5.5KTL-X	20	1 string/1st tracker	10 pcs.
				1 string/2nd tracker	10 pcs.
PV4	SOFARSOLAR Co.	SOFAR 3KTLM-G2	11	1 string/1st tracker	6 pcs.
				1 string/2nd tracker	5 pcs.

Table 3. Modules' and inverters' detailed data.

PV System	Module Parameters							Inverter Parameters			
	P_{MAX} [Wp]	V_{OC} [V]	V_{MPP} [V]	I_{SC} [A]	I_{MPP} [A]	η [%]	β [%/°C]	AC Power [kW]	Max DC Voltage [V]	MPP Voltage Range [V]	η [%]
PV1	310	40.60	33.40	9.86	9.28	18.90	−0.29	8.80	1000	300–840	98.3
PV2	330	40.30	34.05	10.30	9.70	19.60	−0.29	4.40	1000	190–840	98.0
PV3	310	40.82	33.18	9.89	9.35	18.90	−0.273	5.50	1000	240–840	98.0
PV4	325	40.40	33.65	10.14	9.66	19.30	−0.28	3.00	600	230–520	98.0

2.2. Calculation of Final Yield

To evaluate the performance of the photovoltaic system, several important parameters must be calculated using data obtained during operation. This allows for a comparison of PV installation in a specific geographic area. The output power data were collected by inverters' monitoring software, Solarman Smart 1.7.1, in a time interval of 5 min. The final yield ($Y_{f,m}$) value can be defined as daily, monthly, or annual energy output (E_{AC}) divided by the rated peak power ($P_{PV,rated}$) of the photovoltaic system measured at standard test conditions according to Equation (1) [28,29]. Thus, the value of the monthly final yield ($E_{AC,m}$) can be calculated as shown in Equation (2) where $E_{AC,d}$ is the daily final yield and N is a number of days of the month. The daily final yield can be determined according to Equation (3), where $P_{AC,i}$ is the i -th recorded value of the output AC power, and τ_i is the i -th time interval.

$$Y_{f,m} = \frac{E_{AC,m}}{P_{PV,rated}} \left[\text{kWh} \cdot \text{kW}^{-1} \right] \quad (1)$$

$$E_{AC,m} = \sum_{d=1}^N E_{AC,d} \quad (2)$$

$$E_{AC,d} = \sum_{i=1}^k P_{AC,i} \cdot \tau_i \quad (3)$$

2.3. Performance Analysis Using Selected Photovoltaic Software

To compare the energy yields of the PV1–PV4 installations, specialized computer software was used to conduct thorough simulations. DDS-Cad, PVSOL, PVWatts Calculator,

and PVGIS software were utilized to simulate all installations, allowing for monthly and yearly solar energy yield predictions based on input data. Detailed information about software is depicted in Table 4. All relevant information, including module working parameters, inverter specifications, number of modules, and photovoltaic system configurations, was carefully mapped. Additionally, the orientation and tilt angles of the modules were taken into consideration.

Table 4. Detailed information about designing software.

Feature	DDS-Cad	PVSOL	PVGIS	PVWatts Calculator
Solar radiation database	Meteonorm	Meteonorm	PVGIS-SARAH/PVGIS-SARAH2/PVGIS-ERA5	NSRDB/SWERA/IWEC
PV product database	Very complex with the possibility to expand	Very complex with the possibility to expand	No	No
PV module input data	Very detailed	Very detailed	Basic	Basic
Inverter input data	Very detailed	Very detailed	No	Basic
Design of PV system	Yes	Yes	No	No
3D visualization	Advanced	Basic	No	No
Energy output simulations	Yes	Yes	Yes	Yes
Shadows simulations	Yes	Yes	No	No
Output data report	Very detailed	Very detailed	Basic	Basic
Availability	Licensed	30-days free version/licensed	Online tool	Online tool
Fee	Not free of charge	Free/Not free of charge	Free of charge	Free of charge

2.3.1. DDS-Cad

DDS-Cad is an advanced software for the comprehensive design of photovoltaic installations integrated with the building, as well as PV farms [30]. Additionally, this software enables the effective design of not only photovoltaic installations but also electrical, sanitary, heating, ventilation, and air-conditioning installations. However, in this case study, only the photovoltaic functions were used. With the use of this software, full design documentation can be created, including results of calculations, 2D and 3D drawings, and final reports with monthly and yearly energy yields. Firstly, it is necessary to create a building model based on DWG, PDF, or JPG file. This prototype can be easily transformed into a three-dimensional model, on which the photovoltaic installation is based. To create a model of the PV system, input data such as localization, azimuth, rooftop characteristics, and detailed information about module working parameters are required. The implemented Polysyn Inside software is used to carry out the solar system simulations based on the parameters of the inverters and the proposed configuration of the system. The important part of designing in DDS-Cad software is sizing the cables and planning the cables' route. For simulations, climate data are taken from Meteonorm 8 software for the selected locations. The final report contains detailed information about the components and working parameters of the designed installation. The visualizations of four installations made by DDS-Cad software are shown in Figure 2.

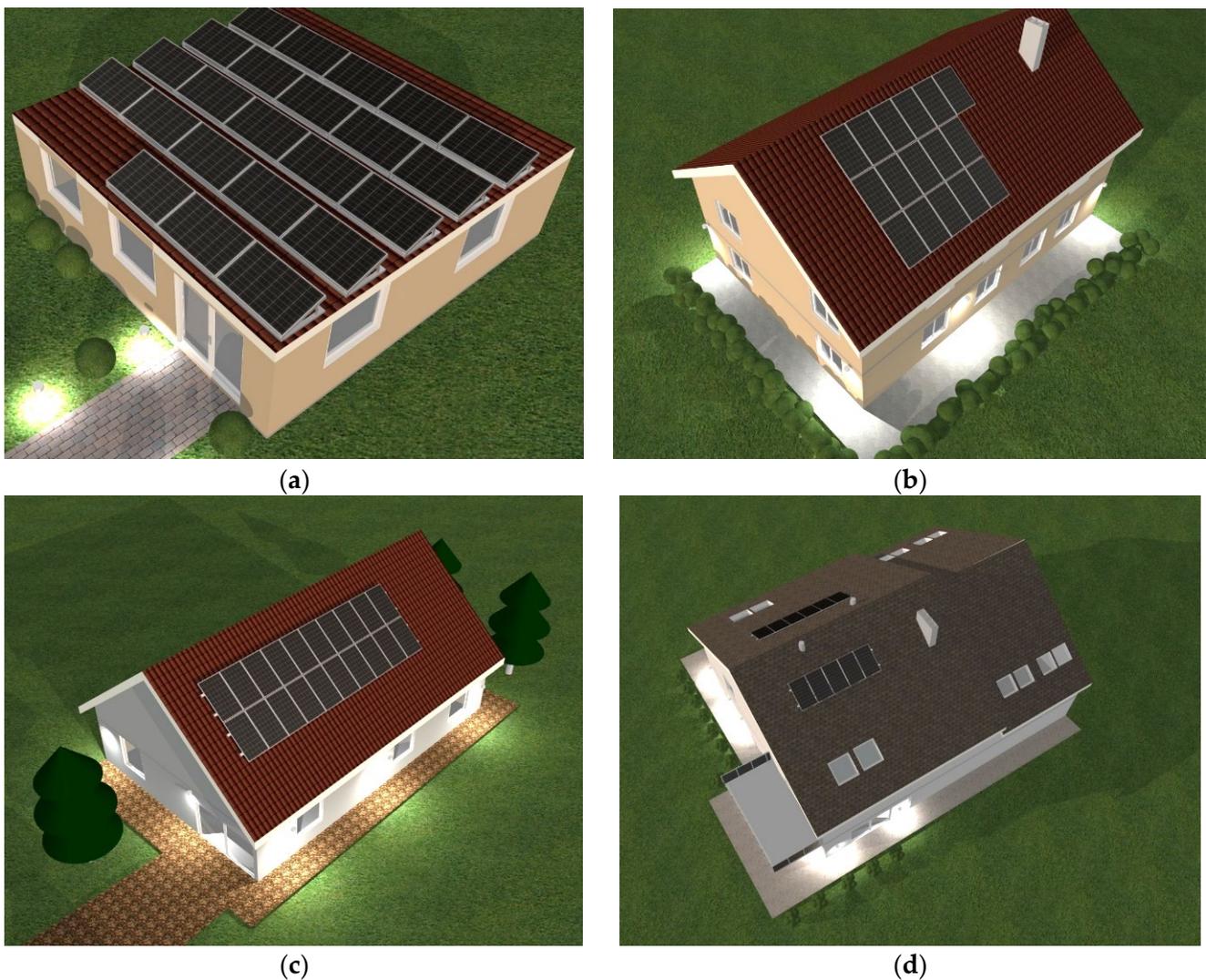


Figure 2. Visualization made with the use of DDS-Cad software of (a) PV1 system; (b) PV2 system; (c) PV3 system; and (d) PV4 system.

2.3.2. PVSOL

PVSOL software is used for designing and simulating various types of photovoltaic systems, such as on-grid and off-grid systems, including rooftop installations, solar power plants, and electric vehicle charging stations [31]. To design a PV installation, detailed information about the installation type and localization must be provided. It is possible to use cadastral or satellite maps, as well as architectural plans. Then, based on the modules' working parameters, the photovoltaic installation can be sized, taking into consideration the roof structure. The three-dimensional model assists in precisely determining shading areas to avoid a reduction in energy yield. The system configuration is selected based on detailed information about the inverter. The source of the climate data is Meteonorm software. All technical details and simulation results are compiled in the final project report.

2.3.3. PVGIS

PVGIS stands for Photovoltaic Geographical Information System [32], which provides information about solar radiation and estimates the energy generation potential of the designed photovoltaic installation. The tool has three main parts dedicated to solar radiation and temperature, the performance of the photovoltaic installation, and a typical meteorological year (TMY). The analysis is possible for locations in Europe, Africa, and, partially, in Asia and America. The software provides data of monthly, daily, and hourly

average values of radiation and temperature. Additionally, the Typical Meteorological Year tool enables generation of a set of meteorological data (such as global horizontal irradiance, diffuse horizontal irradiance, air pressure, wind speed, and wind direction) for every hour of the year. Based on input data, including photovoltaic module technology, the nominal power of the PV system, system losses, tilt angle, and azimuth, the user can calculate the long-term average energy output from a grid-connected or off-grid system, as well as tracking PV systems. The results can be presented in the report or CSV format.

2.3.4. PVWatts Calculator

PVWatts Calculator is an online tool provided by NREL (US National Renewable Energy Laboratory, Golden, CO, USA) [33], used for predicting the performance of photovoltaic systems connected to the grid. Based on the location and the physical characteristics of the photovoltaic system, the simulation of the global annual energy production of PV systems is carried out. Despite the fact that PVWatts Calculator makes assumptions about detailed parameters of PV components, general information about the system is required, such as array type, system losses, tilt and the azimuth of the installation, inverter efficiency, ground coverage ratio, or albedo. It is important to highlight that the software only works for typical crystalline silicon or thin-film modules. The solar resource data are provided by the NREL National Solar Radiation Database (NSRDB) for locations that are covered by this database, while Solar and Wind Energy Resource Assessment Programme (SWERA) and The ASHRAE International Weather for Energy Calculations Version 1.1 (IWECC) are used for the rest of the world.

3. Results and Discussion

3.1. Weather Data Analysis

The climatic data were analyzed in terms of the outside temperature, irradiation, wind speed, and humidity for the year 2022. The minimum and maximum values of the temperature (T), wind speed (V), and humidity (HU) can be found in Table 5. The T , V , and HU data were acquired from the Institute of Meteorology and Water Management (IMGW) for the Lublin Radawiec weather station [34]. The data were collected every 10 min daily. The measurements of the global horizontal irradiance (GHI) were carried out with the use of a Kipp & Zonen pyranometer, CMP11 model, in the Wlodawa weather station [34]. The data were collected every minute. The locations of the weather stations are shown in Figure 1.

Table 5. The minimum and maximum values of the temperature, wind speed, and humidity in 2022 at the selected site (Lublin Radawiec weather station).

Month	T_{min} [°C]	T_{max} [°C]	V_{min} [m/s]	V_{max} [m/s]	HU_{min} [%]	HU_{max} [%]
January	−11.9	9.00	0.3	14.0	51	100
February	−6.3	9.50	0.3	12.0	42	100
March	−11.0	18.00	0.1	9.8	21	100
April	−3.9	18.00	0.1	9.6	28	100
May	0.5	26.30	0.1	11.8	24	100
June	6.0	34.00	0.1	9.0	4	100
July	8.5	33.30	0.1	21.3	4	98
August	9.8	31.20	0	9.9	25	98
September	3.7	22.30	0	8.2	28	98
October	−0.5	21.50	0	10.2	45	99
November	−7.6	14.40	0.2	5.0	57	99
December	−16.0	7.10	0	9.7	64	99

Figure 3a depicts the average outside temperature and global horizontal irradiation. The outside temperature gradually rose from January to August, with significant temperature drops in July, reaching an average value of 20.75 °C. In the second half of the year, average temperature values decreased, reaching the lowest value of −0.44 °C in

December. The selected area in 2022 was characterized by favorable irradiance conditions with the highest irradiation observed in June with the value of 206.73 kWh/m^2 . The winter months received the lowest irradiation, reaching a minimum value which was equal to 15.49 kWh/m^2 in December. It is important to highlight that March and April were characterized by remarkably similar irradiation. The registered value in March was 106.65 kWh/m^2 , while, in April, it was 107.64 kWh/m^2 . The average humidity and wind speed recorded at this weather station are depicted in Figure 3b. The highest average monthly wind speeds occurred during winter, particularly in January (4.53 m/s) and February (4.08 m/s), while the lowest appeared in August with a value of 1.93 m/s . In general, the selected location exhibits humidity levels exceeding 70%, peaking in November (90.83%) and dipping to its lowest value of 63.47% in March.

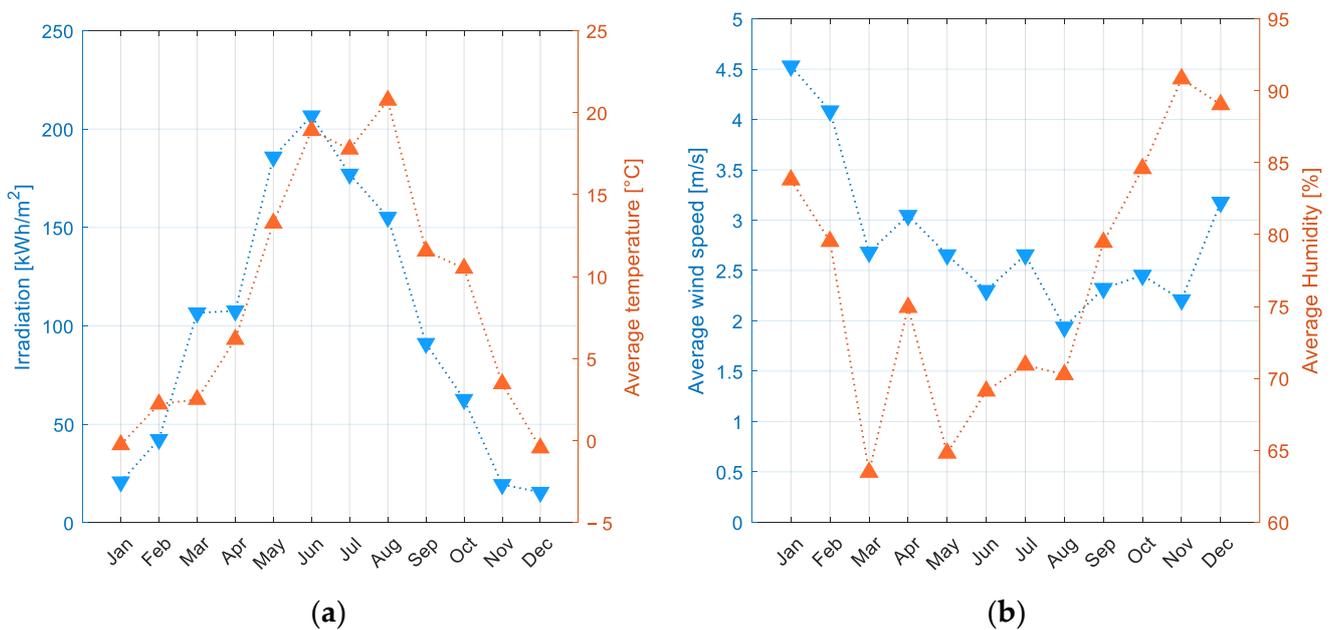


Figure 3. (a) Global horizontal irradiation and outside temperature; and (b) average wind speed and humidity in 2022 in the selected site.

3.2. Analysis of Energy Output

Figure 4a depicts the measured and simulated values of the monthly final yield (Y_f) for the PV1 installation with an azimuth of 145° , and a tilt angle equal to 19° . The data were gathered over one year of operation (2022). PV system production ranges from $6.94 \text{ kWh}\cdot\text{kW}^{-1}$ in December to $173.21 \text{ kWh}\cdot\text{kW}^{-1}$ in June. The annual energy production was $1043.17 \text{ kWh}\cdot\text{kW}^{-1}$. Similar values were observed in the paper of Zdyb and Szalas [18] in which the photovoltaic installation operating in Lublin, Poland was analyzed. It is important to emphasize that both installations are situated in nearly the same location. The PV array with a tilt angle of 14° is oriented to the south. The annual final yield of the mc-Si installation was noticed to be $1098 \text{ kWh}\cdot\text{kW}^{-1}$, with the value of the final yield in June equal to $179.11 \text{ kWh}\cdot\text{kW}^{-1}$. In the work of Gulkowski [17], several photovoltaic installations, located in the Lublin area, were analyzed, one of which faced south-east with a tilt angle of 25° . The presented hybrid system was made of monocrystalline modules with an efficiency of 17.7% ; however, every two modules were connected to SolarEdge power optimizers. The annual final yield was determined to be $978.1 \text{ kWh}\cdot\text{kW}^{-1}$. In the work of Sarniak [16], the 22° -tilted rooftop photovoltaic installation, oriented towards the south and located in central Poland, was analyzed. The value of the average annual yield was $1072.9 \text{ kWh}\cdot\text{kW}^{-1}$.

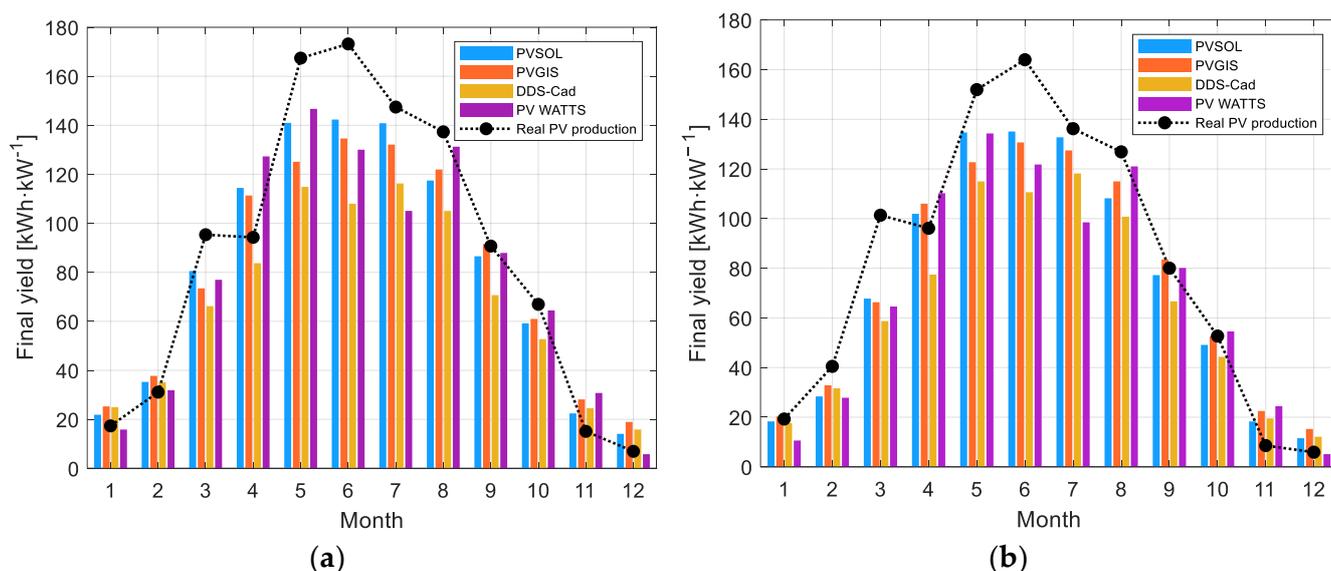


Figure 4. The measured and simulated values of the monthly final yield of the (a) PV1 system; and (b) PV2 system.

A bell-shaped curve can be observed, indicating a trend of lower energy production during winter and significantly higher production in the summer months. We can see that 77.68% of the annual yield was produced from April to September. Similar observations can also be found in papers [16–18]. The same trend can be seen in data gathered from the PVSOL and PVGIS simulations, while some deviations are observed in June for the DDS-Cad software, and, in June and July, for the PVWatts Calculator. During the winter time, the gathered Y_f values from computer software closely approximate the measured data, with negligible differences observed specifically in January, February, November, and December. In sunny months, especially in June, the measured values are moderately higher than the simulated ones. Energy production values gathered from PVSOL and PVGIS software are highly accurate, whereas data determined by DDS-Cad and the PVWatts Calculator are underestimated. The least amount of accuracy was noticed in the DDS-Cad predictions. The average measured monthly final yield is $86.93 \text{ kWh}\cdot\text{kW}^{-1}$, while the values obtained by PVSOL, PVGIS, DDS-Cad, and the PVWatts Calculator are $81.34 \text{ kWh}\cdot\text{kW}^{-1}$, $80.10 \text{ kWh}\cdot\text{kW}^{-1}$, $68.16 \text{ kWh}\cdot\text{kW}^{-1}$, and $79.5 \text{ kWh}\cdot\text{kW}^{-1}$, respectively.

The results obtained for the PV2 installation, characterized by an azimuth of 102° and a tilt angle of 35° , are presented in Figure 4b. As was mentioned before, the tilt angle is optimal for Polish conditions; however, the azimuth significantly deviates from the optimal one. The energy production varied from $5.9 \text{ kWh}\cdot\text{kW}^{-1}$ to $163.97 \text{ kWh}\cdot\text{kW}^{-1}$ with the lowest value registered in December 2022 and the highest in June 2022. The energy yield values in March were higher than in April, which was also observed in PV1's operation. This can be explained by the relatively high irradiation registered in March, closely comparable to April, while the average outside temperature in March was significantly lower than in April. The final yield factor was calculated to be $983.36 \text{ kWh}\cdot\text{kW}^{-1}$, with 77% of the energy produced in the summer period (from April to September). The significant decrease in the final yield value, compared to PV1, can be explained by the unfavorable azimuth orientation. Nonetheless, the trend demonstrating the final yield factor corresponds to both the PV1 and PV2 systems. In the paper [17], the system located in the Lublin region, consisting of 20 mono-Si PV modules tilted at 30° and oriented at 135° , obtained a value of the annual final yield equal to $895.7 \text{ kWh}\cdot\text{kW}^{-1}$. In the work of Olczak [35], the operation of photovoltaic installations located in the Mazowieckie Voivodeship in Poland ($52^\circ 03' \text{ N}$ latitude) was examined. The installation's azimuth is 140° with an inclination of 30° . The PV array consists of 10 monocrystalline modules (440 Wp), separated into three subfields,

all of which are connected to microinverters. The final yield of the presented system was $995 \text{ kWh}\cdot\text{kW}^{-1}$, which is comparable in value to that obtained for PV2.

The PV2 system was also carefully mapped and then simulated using specialized software. The predicted values for the winter period closely approximate the measured ones, while, during the summer months, the real values surpass those obtained from simulations. The result with the highest accuracy is PVGIS software with the final yield value of $895.04 \text{ kWh}\cdot\text{kW}^{-1}$, followed closely by the PVSOL result, which is $883.19 \text{ kWh}\cdot\text{kW}^{-1}$. The predicted values of Y_f presented from the PVWatts Calculator are slightly lower and are equal to $853.03 \text{ kWh}\cdot\text{kW}^{-1}$. The most significant deviation can be seen from DDS-Cad software with the prediction of $772.54 \text{ kWh}\cdot\text{kW}^{-1}$. The PVSOL software's predictions are better in the summer period, while PVGIS demonstrates better alignment in the winter months. It is important to note that all predicted values were underestimated compared to the measured data.

The PV3 system is oriented towards the south with an inclination of 40° . Those parameters are closely approximated to the optimal ones from Poland, which are a south azimuth and tilt angle of $35\text{--}36^\circ$. The highest results were obtained in June, equating to $157.01 \text{ kWh}\cdot\text{kW}^{-1}$, and the lowest ones were in December, with a value of $14.02 \text{ kWh}\cdot\text{kW}^{-1}$. The bell-shaped curve can be seen from the measured values, with a small deviation in April, which is shown in Figure 5a. However, this deviation was also present in the operation of PV1 and PV2. The annual final yield was found to be $1079.44 \text{ kWh}\cdot\text{kW}^{-1}$ with 71% of the energy produced in the sunnier half of the year. Similar values were revealed in the work of Zdyb and Gulkowski [19]. The subfield, consisting of polycrystalline modules, obtained the average annual final yield of $1038.89 \text{ kWh}\cdot\text{kW}^{-1}$. The efficiency of the pc-Si modules was 15.4%, while that of monocrystalline used in PV3 was 18.9%, which is likely why the obtained Y_f value is slightly lower than for PV3. The results indicate that 75% of the energy is produced in sunny months. The predictions of Y_f , obtained by selected software, indicate a slightly better fit compared to the PV1 and PV2 systems. The greatest conformity can be seen in May for the PVWatts Calculator and in July for PVSOL. Nonetheless, the best predictions were computed by PVGIS, followed closely by PVSOL, with average annual final yields of $89.03 \text{ kWh}\cdot\text{kW}^{-1}$ and $88.39 \text{ kWh}\cdot\text{kW}^{-1}$, respectively, while the value obtained from the measured data was $89.95 \text{ kWh}\cdot\text{kW}^{-1}$. The DDS-Cad software provided underestimated results by approximately 25%. The deviation in the trend of the bell-shaped curve can be seen in April when the measured values are lower than the predictions.

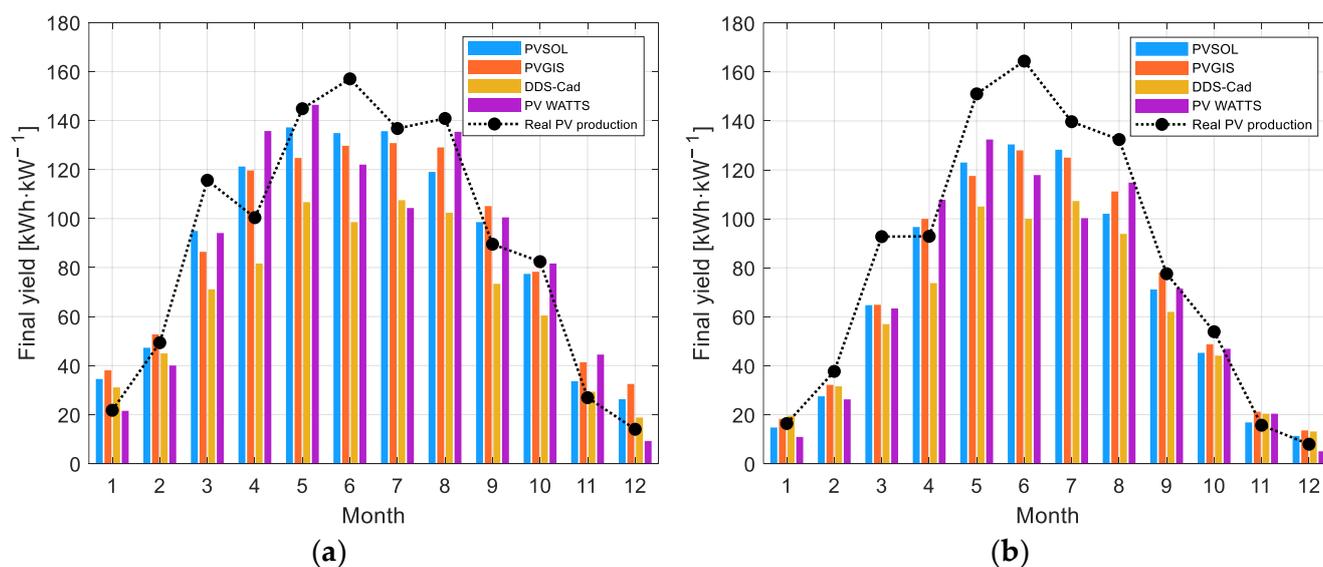


Figure 5. The measured and simulated values of monthly final yield of (a) PV3 system; and (b) PV4 system.

The last photovoltaic system (PV4) is oriented east–west with a tilt angle of 32° . Six series-connected modules face west, while the other five are oriented eastward. Figure 5b depicts the final energy yield obtained from both subfields. Low values of Y_f were registered during the winter months, reaching a minimum in December with a value equal to $7.92 \text{ kWh}\cdot\text{kW}^{-1}$. The operation of the system in the summer months resulted in a 77% energy production with a peak observed in June with a value of $164.44 \text{ kWh}\cdot\text{kW}^{-1}$. The annual final yield was determined to be $982.29 \text{ kWh}\cdot\text{kW}^{-1}$. In a bell-shaped trend of energy production, the deviation is visible in April. However, the energy production values in March and April were remarkably similar and were equal to $92.73 \text{ kWh}\cdot\text{kW}^{-1}$ and $92.84 \text{ kWh}\cdot\text{kW}^{-1}$, respectively. In the work of Gulkowski [17], an east–west-oriented photovoltaic system was also analyzed. The presented PV array, located in the Lublin Voivodeship, is composed of 12 series-connected monocrystalline modules with half-cut technology, which were inclined at 30° . The efficiency of the modules was 18.7%. The author declared the final yield to be $868.8 \text{ kWh}\cdot\text{kW}^{-1}$. All simulations for the PV4 system were carefully made, taking into consideration the east–west configuration of the system. The predictions received from specialized software were significantly underestimated, particularly in the summer months and March. The worse conformity can be seen in May, June, and July. The simulated data obtained from PVGIS software were the closest to the measured values; nonetheless, the average difference was about 13% with the predicted final yield value of $858.63 \text{ kWh}\cdot\text{kW}^{-1}$. PVSOL indicates slightly worse alignment ($Y_f = 831.87 \text{ kWh}\cdot\text{kW}^{-1}$), closely followed by the PVWatts Calculator ($Y_f = 817.60 \text{ kWh}\cdot\text{kW}^{-1}$). The predictions presented by DDS-Cad were underestimated by approximately 25%.

The boxplot of the measured daily final yield values in each month of 2022 with the average computed values is presented in Figure 6a for the PV1 system, and for the PV2 in Figure 6b. The interquartile ranges are considerably higher for the summer months, which is correlated with the variability in energy production. In the case of PV1, the wide interquartile ranges of daily yields were observed from March to September, with the widest distribution registered in April. Nonetheless, the daily highest values were obtained for June, while the daily final yield varied from $1.3 \text{ kWh}\cdot\text{kW}^{-1}$ to $8.50 \text{ kWh}\cdot\text{kW}^{-1}$ with a median equal to $7.16 \text{ kWh}\cdot\text{kW}^{-1}$. The narrowest interquartile range was registered in December with a median of $0.3 \text{ kWh}\cdot\text{kW}^{-1}$. The highest average energy output value was found in June, equal to $6.21 \text{ kWh}\cdot\text{kW}^{-1}$, while the lowest was for December ($0.35 \text{ kWh}\cdot\text{kW}^{-1}$). The average daily energy production values obtained from simulations in most cases largely aligned with the middle 50% of the measured data. The underestimation is clearly visible, especially in May and June, while an opposite scenario can be observed in November and December.

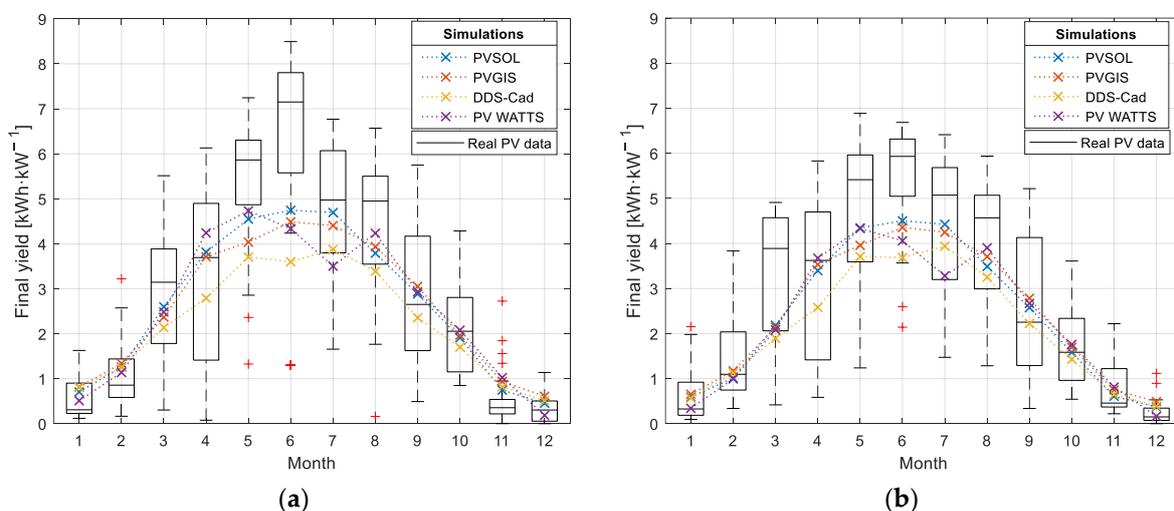


Figure 6. The measured and average simulated values of daily final yields of (a) PV1 system; and (b) PV2 system.

The daily final yield values obtained for PV2 were lower compared to those registered for PV1. It can be explained by the nonoptimal azimuth of the photovoltaic system. The highest daily value of $6.88 \text{ kWh}\cdot\text{kW}^{-1}$ was registered in May; however, the interquartile range representing June is the highest. The values for June are characterized by a concentrated distribution represented by the value of the first quartile equal to $5.05 \text{ kWh}\cdot\text{kW}^{-1}$ and the third one of $6.32 \text{ kWh}\cdot\text{kW}^{-1}$. It is important to highlight that the median values for May, June, and July are close to each other, and equal to $5.41 \text{ kWh}\cdot\text{kW}^{-1}$, $5.93 \text{ kWh}\cdot\text{kW}^{-1}$, and $5.07 \text{ kWh}\cdot\text{kW}^{-1}$, respectively. However, taking into consideration the mean value, the highest one was in June ($5.46 \text{ kWh}\cdot\text{kW}^{-1}$), while May and July obtained the lower values, $4.9 \text{ kWh}\cdot\text{kW}^{-1}$ and $4.39 \text{ kWh}\cdot\text{kW}^{-1}$, respectively. The average simulated daily energy production values exhibit the same trend observed for PV1 with a substantial drop in July for the PVWatts Calculator predictions. However, it is important to mention that the simulations are underestimated only for June, and slightly overestimated for December.

The daily final yield distributions for PV3 and PV4 are presented in Figure 7a,b, respectively. The PV3 system, which is characterized by an almost optimal azimuth and tilt angle, obtained wider interquartile ranges compared to the other installations. The values obtained for the winter months (January, February, November, and December, especially) are spread out over a larger range. The highest registered daily value of the final yield was $6.97 \text{ kWh}\cdot\text{kW}^{-1}$ in May, which is very close to the value obtained, also in May, for the PV2 system. The highest median and mean values were calculated in June, and they equal $5.49 \text{ kWh}\cdot\text{kW}^{-1}$ and $5.23 \text{ kWh}\cdot\text{kW}^{-1}$, respectively. The best correlation between the simulations and measured data can be seen in October, in which only the DDS-Cad predictions are underestimated and they are slightly below the interquartile range.

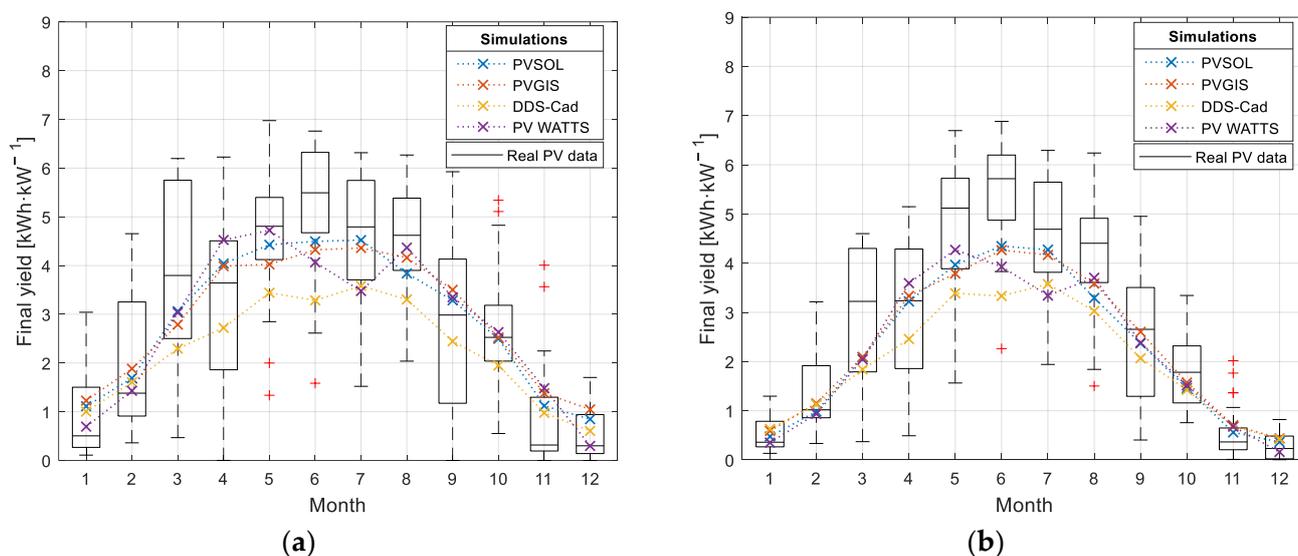


Figure 7. The measured and average simulated values of daily final yields of (a) PV3 system; and (b) PV4 system.

The same trends can be observed in the results obtained for the PV4 installation. The highest values of the daily final yield were obtained in May, which is characterized by the first quartile equal to $4.87 \text{ kWh}\cdot\text{kW}^{-1}$ and the third one of $6.19 \text{ kWh}\cdot\text{kW}^{-1}$. The median value was equal to $5.72 \text{ kWh}\cdot\text{kW}^{-1}$. The calculated mean values were in the range of $0.29 \text{ kWh}\cdot\text{kW}^{-1}$ for December to $5.48 \text{ kWh}\cdot\text{kW}^{-1}$ for June. The simulation made for the PV4 system is underestimated for four summer months, especially for June; however, the predictions for the winter months indicate the highest degree of alignment with the real data. The closest simulation values, within all predictions made for the PV2–PV4 systems, were obtained for October.

A comparison of the measured and simulated annual values of the final yield factors for the analyzed systems is presented in Table 6. As can be seen, all performed simulations are underestimated compared to the measured values. However, the best overall fit was obtained for the PV3 system, which has the closest approximated azimuth and tilt angle to the optimal ones from Poland. The degree of alignment was 99%, 98%, and 96% for PVGIS, PVSOL, and the PVWatts Calculator, respectively. The predictions carried out by DDS-Cad corresponded to the measured values in 77%. The data obtained for PV4 (east–west system) demonstrated the weakest alignment, since the degree of fit was 87%, 84%, 83%, and 74% for PVGIS, PVSOL, the PVWatts Calculator, and DDS-Cad, respectively.

Table 6. The measured and simulated values of yearly final yields.

PV System	Y_f^{real}	Y_f^{PVSOL}	Y_f^{PVGIS}	$Y_f^{DDS-Cad}$	$Y_f^{PVWATTS}$
	[kWh·kW ⁻¹]				
PV1	1043.16	976.06	961.23	817.88	954.01
PV2	983.36	879.85	891.66	772.58	853.03
PV3	1079.45	1055.60	1068.37	826.14	1035.41
PV4	982.30	829.45	853.82	728.74	817.32

4. Conclusions

A comparative analysis of the measured data and simulations for four photovoltaic systems was carried out. The photovoltaic installations, all of which are located in the Lublin Voivodeship, Poland, with various orientations (S, E, SE, and E–W) and tilt angles, were analyzed. The data were collected during one year of operation (2022). The prediction of the energy yield while designing the photovoltaic installation is crucial, and, nowadays, is required to complement the project. Four different commercially available software tools, namely, DDS-Cad, PVSOL, the PVWatts Calculator, and PVGIS, were used to execute the simulations, and, thus, obtain information about the monthly and yearly energy yield based on input data. A comparative comparison between various software energy outputs and real production data is essential to gain knowledge about the accuracy and reliability of the performed simulations.

The annual final yield of the PV1, PV2, PV3, and PV4 system was 1043.16 kWh·kW⁻¹, 983.36 kWh·kW⁻¹, 1079.45 kWh·kW⁻¹, and 982.30 kWh·kW⁻¹, respectively. Therefore, the average value for the photovoltaic system located in this area was 1022.07 kWh·kW⁻¹ during the measurement period. The obtained results can be compared with the range of values reported for Poland, especially in the Lublin Voivodeship. The highest final yield ratio was obtained for PV3, which is oriented towards the south and the tilt angle was close to optimal for Poland, while the lowest one was for the east–west system (PV4). It is important to highlight that the results obtained for the PV2 system, which is oriented towards the east (102°), were very close to those for PV4. A wide range of daily yields, approximately 77% of the total energy yield, was registered in the sunny months, which is consistent with other authors' results. The winter months demonstrated low values of energy generation, which is related to the relatively short day, and, thus, small number of sunshine hours, in the location under study. The summer half of the year is characterized by a wide range of daily final yields, e.g., values from 1.24 kWh·kW⁻¹ to 6.89 kWh·kW⁻¹ were registered in May for PV2.

The predictions computed by simulation software were compared with the measured data. The results indicated that simulations perform the highest degree of alignment in the winter months, while, for the summer months, they are significantly underestimated. The predictions for June demonstrated underestimation in all analyzed cases. However, it is worth mentioning that the results of the simulations are applicable not only to the Poland case study but also to other locations with similar latitudes, such as Germany, the Netherlands, and Belgium.

The data obtained from PVGIS simulations present the best fit, with an average of 92% compared to real values, despite the lack of the possibility to enter detailed information about PV modules or inverters. This is closely followed by the simulation made by PVSOL with an average 91% degree of alignment. Relatively close to the measured values were also predictions computed by the PVWatts Calculator, which demonstrate 89% of alignment. DDS-Cad is the software that underestimates the most and shows the least degree of matching, about 77%. In addition, DDS-Cad predictions do not indicate a bell-shaped curve trend of energy production, since a considerable drop can be seen in June for all analyzed installations.

Future work is going to include a comparative analysis of the higher number of PV real-system data located not only in the east–south but also in other sites of Poland, with the results obtained from prediction software.

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Conflicts of Interest: The author declares no conflict of interest.

Appendix A

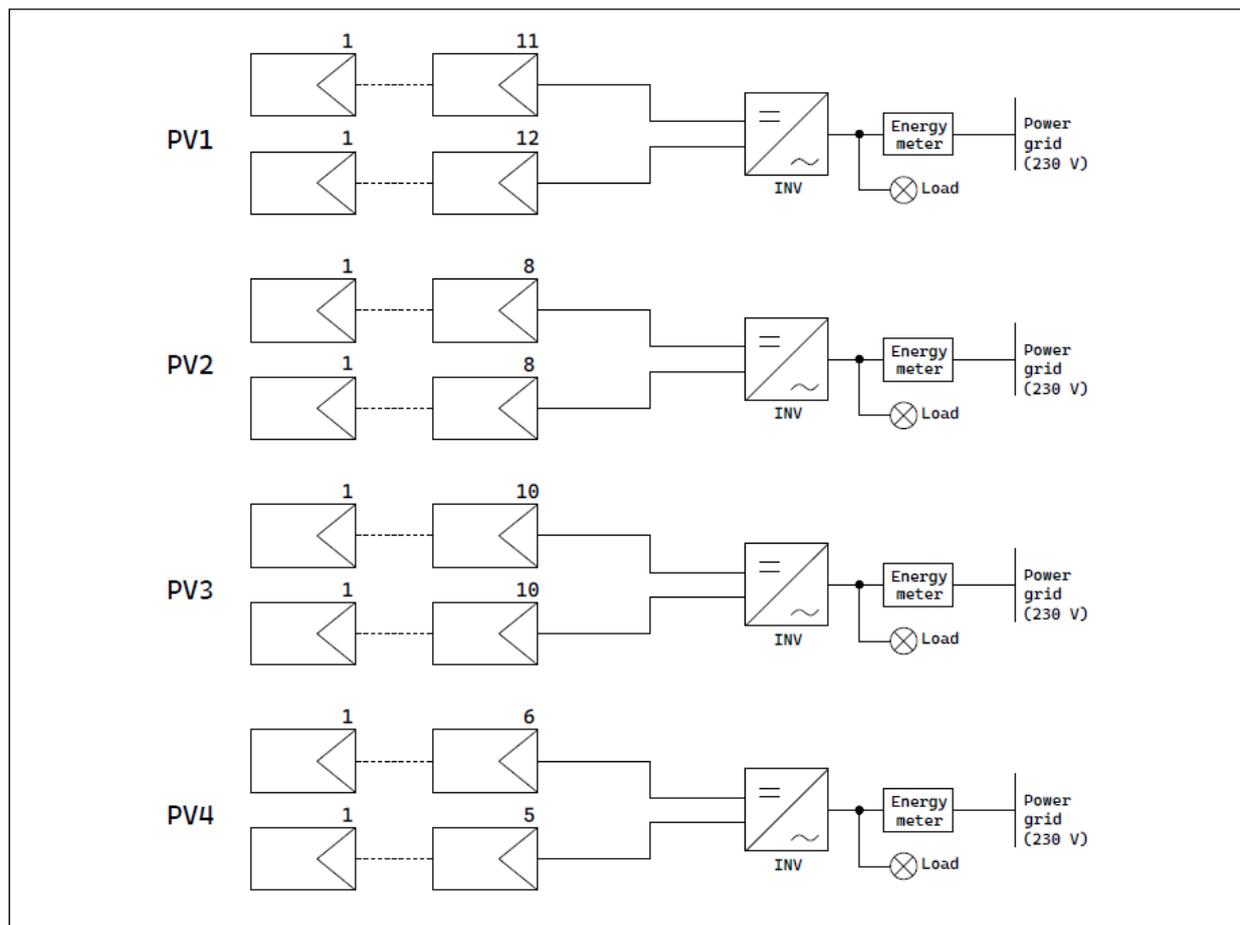


Figure A1. Schematic diagram of analyzed PV1–PV4 systems.

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