



Development of Air Flow Rate Prediction Model Using Multiple Regression in VAV Terminal Unit

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Abstract: Accurate measurement of air flow rate is essential in automatic building control using the variable air volume (VAV) system. In order to solve the problems of the existing air flow measurement method and improve the accuracy of air flow control, this study developed a data-based multiple regression air flow prediction model. The independent variables used in the development of the predictive model were selected as the factors used for control and monitoring when operating with variable air flow rate in the existing air conditioning system. Data collection and correlation between independent variables and air flow rate of the terminal unit were analyzed. Using the IBM SPSS statistics version 25, an air flow rate prediction model was developed using multiple regression analysis. Reliability of model was evaluated by comparing the measured airflow. The relative error of -9.3% to 10.4% is shown when comparing the estimated air flow rate by the developed model with the measured air flow rate.

Keywords: variable air volume system; terminal unit; prediction model; air flow rate; multiple regression

1. Introduction

The air flow rate of variable air volume (VAV) terminal unit adjust the supply air flow rate and temperature based on the indoor load, ventilation requirement, and stratification [1–3]. Accurate measurement of air flow rate is essential in automatic building control using the VAV system. The air flow measurement method can generally be measured using a Pitot tube, a hot-wire anemometer, and a virtual airflow sensor [4].

Pitot-static tubes are the most commonly used methods for measuring air volume in buildings [5]. However, Pitot-static tubes have the disadvantage of low accuracy at low speeds [6].

The hot-wire anemometer can measure the air volume with high accuracy even at low speeds. However, in the wind speed measurement standard using a hot air anemometer, the sensor should be installed by dividing the duct evenly, and about 4 to 20 measurement points are required [7]. If a hot-wire anemometer is installed to measure the air volume, a problem of installation cost may occur due to multiple measurement points.

To improve the problems of these physical sensors, Kim [8] proposed a virtual air flow sensor for the terminal unit using a mathematical model. The air flow rate of the terminal unit was predicted using the in-situ performance curve of the damper. In addition, the factors affecting the air volume of the terminal unit were analyzed. It was confirmed that the air flow rate of the terminal unit was affected by the differential pressure of the damper as well as the speed of the supply fan. The virtual air flow sensor was developed using the supply fan speed and damper opening rate, which can be easily obtained from the existing control system. However, the mathematical model has the disadvantage that it takes a lot of effort and cost [9]. Therefore, it is necessary to derive factors affecting the prediction results and to use data-based prediction using statistical method [10].

The statistical method, which is one of the black box methods, can derive a prediction model using real data [11]. In addition, even though the variables used in the black box model have no physical meaning, the relationship between input and output is derived using statistical methods. The statistical methods used for the development of prediction model in building are linear [12], multiple [13], polynomial [14], logistic regression [15], and partial least squares [16].

In this study, a predictive model for the air flow rate was developed to secure the measurement stability of the VAV terminal unit. In order to predict the air flow rate, the factors used for control and monitoring when the existing heating, ventilation & air conditioning (HVAC) system is operated using the variable air volume system were selected as variables, and data collection and correlation analysis of the air flow rate of the terminal unit were performed. In addition, a predictive model for the air flow rate was developed using multiple regression analysis, and the reliability of the model was evaluated through comparison with the air flow rates measured by the hot-wire anemometer.

2. Collection of Air Flow Rate Data of the VAV Terminal Unit

2.1. Test Set-Up

Airflow rate prediction model tests were performed using the HVAC test-bed. The HVAC system in test-bed serves an office and lecture room. The test system is a VAV terminal unit with reheating coil in VAV system. The air handling unit (AHU) was equipped with a cooling coil, heating coil, and supply and return fan with a variable frequency drive (VFD). The VAV terminal unit consists of a damper, an actuator, a reheating coil, a valve, an air flow sensor, and a supply temperature sensor. In order to supply variable air flow rate, it is automatically controlled in conjunction with an indoor temperature sensor. In addition, monitoring, automatic control, and data collection are possible through building automation system (BAS). Table 1 shows the specification of test-bed [8] and Figure 1 shows the schematic diagram of experimental system.

Category		Specification	
Category			
		Air flow (CMH)	12,000
	Supply fan	Static pressure (mmAq)	92
		Power (kW)	5.5
AHU	Return fan	Air flow (CMH)	9600
		Static pressure (mmAq)	35
		Power (kW)	3.7
	Cooling	Capacity (kW)	170
Air-cooled		Power consumption (kW)	46.5
Heat pump		Capacity (kW)	156
	Tleating	Power consumption (kW)	45.6
VAV Terminal unit	Rated air flow rat	1360	
	Capacity of rehea	4000	

Table 1. Summary of test system.



Figure 1. Schematic diagram of experimental system.

2.2. Data Collection

The operational data of the HVAC system were collected for prediction of the air flow rates of the terminal unit. The data collected for analysis used for the control and monitoring of the VAV terminal unit [8] were the data of six factors: supply fan speed, supply air static pressure, differential pressure of the supply fan, differential pressure of damper, damper position, and air flow rate. As for air flow rates, since the airflow sensor installed in the VAV terminal unit had low accuracy, the data of air flow rates were obtained by measuring the air velocity with a hot-wire anemometer and converting the measured values into air flow rates. In this study, the differential pressure sensor in damper, VFD of the supply fan, damper actuator in VAV terminal unit, and hot-wire anemometer were used for data collection of the air flow rate prediction model in VAV terminal unit. The data were measured at 1 min intervals from the BAS. Hot-wire anemometers were installed and measured using ASTM D3464-96 [7]. In addition, another measurement sensor collected data through the BAS.

Before data collection, the standard uncertainty of the hot air anemometer was calculated using Equation (1). After fixing the damper opening rate of the air volume terminal unit (60%), the fan speed was changed (21, 23, and 25 Hz), and the measurements were repeated five times each. The results indicate that the air velocity showed 0.004–0.005 m/s of uncertainty and the air flow rate showed 2.4–3.1 CMH of uncertainty. These values represent less than 1% uncertainty.

$$U = \frac{s}{\sqrt{n}} \tag{1}$$

The data of the other five factors were collected in real time through the BAS, and a total of 1184 sets of data were collected. Precisely, 75% (888 sets) of the collected data were used as the training data set and 25% (296 sets) were used as the validation data set to conduct multiple regression analysis. The training and validation data sets were classified by random extraction. Table 2 shows the specifications of measurement sensors used to collect data and the ranges of the collected data. Figure 2 shows the measured air flow rates and differential pressure of the VAV terminal unit. In the case of the air flow rates of the VAV terminal unit, it can be seen that the differential pressure of the VAV terminal unit varies even at the same air flow rate and it is thought to be influenced by the supply fan speed.

Measurement Point	Measuring Equipment	Accuracy	Full Scale	Measurement Data Range
Fan speed	VFD	0.1 Hz	60 Hz	18.9–25.6 Hz
Static pressure	Static pressure sensor	1 Pa	1000 Pa	98–162 Pa
Differential pressure of supply fan	Differential pressure sensor	1 Pa	500 Pa	124–225 Pa
Differential pressure of VAV terminal unit damper	Differential pressure sensor	1 Pa	500 Pa	56–159 Pa
Damper position	Damper actuator	0.1%	100%	48.6-69.4
Airflow rate of VAV terminal unit	Hot-wire anemometer	0.015 m/s	50 m/s	0.65–1.33 m/s (287–587 CMH)

Table 2. Summary of measured data and equipment.



Figure 2. Relationship between differential pressure and airflow rate of variable air volume (VAV) terminal unit.

3. Derivation of a Predictive Model for Air Flow Rates of the VAV Terminal Unit Using Multiple Regression Analysis

Multiple regression analysis was used for the operational data of the HVAC system to predict the air flow rate of the VAV terminal unit. Briefly, 1185 sets of the operational data of the HVAC system obtained by measurements and air flow rate data were used as variables. Equation (2) shows the relationships between the dependent variable (the air flow rate of the VAV terminal unit) and independent variables (the supply fan speed, supply air static pressure, differential pressure of the supply fan, differential pressure of the VAV terminal unit, and damper position) revealed by multiple regression analysis. In this case, it is assumed that the error term follows a normal distribution with mean 0 and variance σ^2 .

$$Q = \beta_0 + \beta_1 \overline{\omega} + \beta_2 P_s + \beta_3 P_{dp,sf} + \beta_4 P_{dp,damper} + \beta_5 \alpha + \varepsilon$$
(2)

For multiple regression analysis, an airflow prediction model was derived using the IBM SPSS Statistics version 25.

3.1. Derivation of Predictors of Air Flow Rates of the VAV Terminal Unit

When operating the VAV terminal unit in the HVAC system, it is controlled through factors related to the air flow rate, and the related factors are monitored as the air flow rate changes. In order to predict the air flow rates of the VAV terminal unit, the factors used for control and monitoring during the operation of the VAV terminal unit were set as variables. Table 3 shows the symbols and descriptions of the variables.

Variable Symbols	Explanation
$\overline{\omega}$	Fan speed
Ps	Static pressure
P _{dp,sf}	Differential pressure of supply fan
P _{dp,damper}	Differential pressure of VAV terminal unit damper
α	Damper position

Table 3. Summary of variables.

Statistical analysis was conducted to determine whether the selected variables can be used in the predictive model for the air flow rate. Scatter analysis and correlation analysis were performed to examine correlations among variables. The results of scatter analysis and correlation analysis are shown in Figure 3 and Table 4, respectively. Static pressure ($R^2 = 0.2796$) was shown to have a stronger correlation with the air flow rate compared to other variables. The other variables were correlated with the air flow rate in the order of the differential pressure of the VAV terminal unit ($R^2 = 0.1953$), differential pressure of the supply fan ($R^2 = 0.1816$), damper position ($R^2 = 0.1688$), and supply fan speed ($R^2 = 0.1430$). Table 2 shows the correlations between the air flow rate and independent variables. As the air flow rate increases, each of the independent variables increases, showing that there is a positive correlation between the air flow rate and each independent variables showed a high correlation (p < 0.05). Scatter plot and correlation analysis confirmed that all the independent variables were correlated with the air flow rate, indicating that they can be used as the predictors of the air flow rate.

Person correlation coefficient Air flow rate p-value (two-tailed)	0.378 0.000 888	0.529 0.000 888	0.426 0.000	0.442 0.000	0.411 0.000
Air flow rate <i>p</i> -value (two-tailed)	0.000 888	0.000	0.000	0.000	0.000
N	888	888			
IN		000	888	888	888
600 550 500 1000 450 450 350 300 250 R2=0.143		600 550 (HIW) 450 910 400 350 300 250	teratelation of the state of th	The for the function of the second	**************************************
15 20 25 30 Fan speed (Hz)		75	95 S	115 135 15 tatic pressure (pa)	5 175

Table 4. Correlation analysis result.

(a) Fan Speed.

(b) Static Pressure

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Figure 3. Cont.





(d) Differential Pressure of VAV TB Damper



(c) Differential Pressure of Supply Fan



(e) Damper Position

600

Figure 3. Scatter plot of air flow rate.

3.2. Development of a Predictive Model for Air Flow Rates of the VAV Terminal Unit Using Multiple **Regression Analysis**

A multiple regression analysis was conducted with the variables showing relationships with the air flow rate which can be utilized in predicting the air flow rates of the VAV terminal unit. A predictive model was developed using data obtained by measurements and monitoring. Prior to the development of the prediction model, a variable selection process was carried out to find the variables to be included in the regression model that could best explain the patterns of variations of the air flow rate. Among variable selection methods, we used the forward selection method, which is to enter variables one by one in descending order of importance in terms of the contribution to the model, starting with a regression model with only constant terms. It is the method of building a model by sequentially selecting the variables that make the largest contribution to the regression model, and once a variable has been selected, it continues to remain in the model. In selecting the variables, the *p*-value for entry into the model was 0.05, while the *p*-value for removal was 0.1. Table 5 shows the variables for each model derived from the forward selection method. Five models were derived by adding variables one by one in a stepwise manner in descending order of importance in terms of contribution to the model and examining whether the *p*-value was below the criterion.

Table 6 shows the results of multiple regression analysis used to derive the predictive model for the air flow rate. The adjusted R^2 value representing the explanatory power of the predictive model was found to be 0.809 for Model 5, 0.806 for Model 4, and 0.796 for Model 3; thus, Model 5 has the highest explanatory power, followed by Model 4 and Model 3. The Durbin–Watson statistic, a test used for detecting autocorrelation in the residuals from regression analysis, was 1.989, which is close to 2, indicating that there is no correlation between error terms.

Model	Inputted Variables	Removed Variables	Variable Selection Method
1	P _s	_	Forward selection method (standard: $F \le 0.05$)
2	<i>P</i> _s , α	_	Forward selection method (standard: $F \le 0.05$)
3	$P_s, \alpha, \overline{\omega}$	_	Forward selection method (standard: $F \le 0.05$)
4	$P_s, \alpha, \overline{\omega}, P_{dp,sf}$	_	Forward selection method (standard: $F \le 0.05$)
5	$P_s, \alpha, \overline{\omega}, P_{dp,sf}, P_{dp,damper}$	_	Forward selection method (standard: $F \le 0.05$)

Table 5. Inputted and removed variables in the models.

Table 6.	Multiple	regression	analysis.

Model	R	R ²	Adjusted R ²	Std. Error of the Estimate	Durbin-Watson
1	0.529	0.280	0.279	55.85907	
2	0.844	0.713	0.712	35.27255	
3	0.892	0.796	0.796	29.73047	
4	0.898	0.807	0.806	28.99591	
5	0.900	0.810	0.809	28.71909	1.989

Table 7 shows the analysis results of coefficients of the regression models and Table 8 shows the results of ANOVA of the air flow rate prediction model. In the case of Model 3, the air flow rate increases as the supply air static pressure, damper position, and differential pressure of the supply fan increase, but the air flow rate decreases as the supply fan speed and differential pressure of the VAV terminal unit increase. The results of ANOVA revealed that the prediction model was statistically significant with a *p*-value of 0.000 (p < 0.05) for all models. The overall analysis results such as the explanatory power of the model and the *p*-value indicate that Model 5 is the optimal model for predicting the air flow rate of the VAV terminal unit.

		Unstandardized Coe	fficients	Standardized Coefficients		n Valua
widdei		В	Std. Error	β	- t	<i>p</i> -value
1	Constant	245.807	10.606		23.176	0.000
1	Ps	1.527	0.082	0.529	18.542	0.000
	Constant	-493.680	21.304		-23.173	0.000
2	Ps	2.300	0.056	0.796	40.969	0.000
	α	10.960	0.300	0.711	36.565	0.000
	Constant	-184.040	24.239		-7.593	0.000
3	Ps	4.209	0.111	1.457	37.928	0.000
5	α	11.148	0.253	0.723	44.093	0.000
	$\overline{\omega}$	-25.339	1.332	-0.717	-19.018	0.000
	Constant	186.004	59.268		3.138	0.000
4	Ps	3.551	0.145	1.230	24.481	0.000
	α	10.968	0.248	0.711	44.227	0.000
	$\overline{\omega}$	-58.260	5.007	-1.649	-11.636	0.000
	P _{dp,sf}	2.658	0.390	1.144	6.809	0.000

Table 7. Coefficients of the models.

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Model		Unstandardized Coefficients		Standardized Coefficients	L	u Value
		В	Std. Error	β	- t	p-value
5	Constant	282.927	62.967		4.493	0.000
	P_s	6.028	0.600	2.087	10.054	0.000
	α	9.203	0.482	0.597	19.092	0.000
	$\overline{\omega}$	-57.703	4.961	-1.633	-11.632	0.000
	P _{dp,sf}	2.599	0.387	1.119	6.715	0.000
	P _{dp,damper}	-2.596	0.610	-0.899	-4.255	0.000

Table 7. Cont.

Model		Sum of Squares	df (Degree of Freedom)	Mean Square	F	<i>p</i> -Value
	Regression	1072719.660	1	1072719.660	343.794	0.000
1	Residual	2764528.688	886	3120.236		
	Total	3837248.347	887			
	Regression	2736173.060	2	1368086.530	1099.613	0.000
2	Residual	1101075.287	885	1244.153		
	Total	3837248.347	887			
3	Regression	3055880.057	3	1018626.686	1152.422	0.000
	Residual	781368.290	884	883.901		
	Total	3837248.347	887			
	Regression	3094854.876	4	773713.719	920.252	0.000
4	Residual	742393.471	883	840.763		
	Total	3837248.347	887			
5	Regression	3109787.186	5	621957.437	754.084	0.000
	Residual	727461.161	882	824.786		
	Total	3837248.347	887			

4. Validation of the Predictive Model for Air Flow Rates of the VAV Terminal Unit

To conduct validation of the model derived through multiple regression analysis, 296 data sets for validation among the collected data were used. In order to validate the performance of the prediction model for the air flow rate through the comparison with the performance of a conventional hot-wire anemometer, the relative error was calculated using Equation (2).

$$e = \frac{Q_{meas} - Q_{pred}}{Q_{meas}} \tag{3}$$

The range of the input and dependent variables used in validation are shown in Table 9. The predicted air flow rates obtained using the prediction model ranged from 291 to 530 CMH. As a result of comparing the values with the air flow rates measured by the hot-wire anemometer, the relative error ranged from -9.3% to 10.4%, as shown in Figure 4.

Table 9. Comparison of measured data, prediction airflow rate, and relative error.

Number of Verification Data Sets	ω	P_s	$P_{dp,sf}$.	P _{dp,damper}	а	Q _{meas}	Qpred	Relative Error (%)
296	19–25.6	98–161	124–225	88–157	44-67.9	291-560	291–530	-9.3 to 10.4



Figure 4. Comparison of measured and predicted air flow rate.

5. Conclusions

In this study, a prediction model for the air flow rate was developed using multiple regression analysis to secure the measurement stability of the VAV terminal unit. The data collected by measurement and monitoring during the operation of the VAV terminal unit were used as the variables for development of the prediction model, and statistical analysis was conducted to determine the relationships between each of the variables and the air flow rate. Correlation and scatter analysis were used to derive the variables that have a significant correlation with the air flow rate and thus can be used for the prediction of air flow rates. Then, a prediction model for the air flow rate was developed by multiple regression analysis, and the validation of the developed prediction model was carried out. Static pressure was found to have the strongest correlation with the air flow rate, followed by the differential pressure of the VAV terminal unit, differential pressure of the supply fan, damper position, and supply fan speed in descending order, and the prediction model using the five variables was found to be the optimal model for prediction of air flow rates. The validation results of the prediction model for air flow rates showed a relative error of less than 10% compared with measured air flow rates. The results of this study showed the potential applicability of a predictive model for air flow rates of the VAV terminal unit in future studies such as development of the control technology for the minimum air flow rate of the VAV terminal unit.

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Nomenclature

U	Standard uncertainty
S	Standard deviation
п	Number of measurements
е	Relative error
P _{dp,damper}	Differential pressure of VAV terminal unit damper (Pa)
P _{dp,sf}	Differential pressure of supply fan (Pa)
P_s	Static pressure (Pa)

Q	Airflow rate of VAV terminal unit (CMH)
Qmeas	Measured air flow rate (CMH)
Qpred	Predicted air flow rate (CMH)
α	Damper opening ratio (%)
$\beta_0, \beta_1, \beta_2, \beta_3, \beta_4, \beta_5$	Regression coefficients
$\overline{\omega}$	Fan speed (Hz)
ε	Error

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