



A Marine Gas Turbine Fault Diagnosis Method Based on Endogenous Irreversible Loss

Yunpeng Cao *[®], Junqi Luan, Guodong Han, Xinran Lv and Shuying Li

College of Power and Energy Engineering, Harbin Engineering University, Harbin 150001, China; luanjunqi@hrbeu.edu.cn (J.L.); hanguodong@hrbeu.edu.cn (G.H.); 13664504988@hrbeu.edu.cn (X.L.); lishuying@hrbeu.edu.cn (S.L.)

* Correspondence: caoyunpeng@hrbeu.edu.cn

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Abstract: When a malfunction occurs in a marine gas turbine, its thermal efficiency will decrease slightly, and the gas path fault is often difficult to distinguish. In order to solve this problem, based on the second law of thermodynamics, the endogenous irreversible loss (EIL) model of the marine gas turbine is established, and the exergy loss analysis under normal conditions is carried out to verify the accuracy of the model. The fault diagnosis of gas turbine gas path based on EIL is proposed, and a simulation experiment conducted on a three-shaft marine gas turbine demonstrated that the proposed approach can detect and isolate gas path fault accurately under different operating conditions and environments.

Keywords: gas turbine; gas path; fault diagnosis; endogenous irreversible loss

1. Introduction

A gas turbine is a complex thermal system. Its operation process is a cross-coupled thermodynamic process. When a certain component fails, it often causes the performance degradation of the entire equipment and even catastrophic consequences. The high-speed airflow passage composed of several components of the gas turbine is collectively referred to as the gas path. Since the turbine is required to inhale a large amount of air during operation, the air often contains salt ingested particles, moisture, and other corrosive substances, which may cause damage to the interior of the turbine. These gas path components are subject to wear, corrosion, fouling, and other external damage, which in turn causes the performance of the gas turbine to decrease [1,2]. Therefore, it is necessary to find a way to accurately monitor the gas path failure.

In recent years, many gas path fault diagnosis methods have been proposed to assess gas turbine health status, such as nonlinear gas path analysis [3–5], rule-based fuzzy expert system [6,7], Bayesian hierarchical models [8,9], neural networks [10–12], genetic algorithm [13,14], multiple-model method [15,16], and exergy analysis [17]. Gas path analysis is an inversely mathematical problem to obtain the deviation of component performance parameters over gas path measured variables. Most case studies show that artificial intelligence methods, such as artificial neural networks, Bayesian hierarchical models, and fuzzy expert systems, may effectively isolate the faulty components but not easily assess the severity of the fault [18].

The model-based approach is an analytical redundancy approach that diagnoses the fault based on the residual signal between the measurements and the gas turbine's mathematical model. Kalman filter is a typical model-based approach and is widely used in gas path fault diagnosis [18]. However, model-based approaches require accurate gas turbine mathematical models, and their reliability decreases as system complexity increases. Meanwhile, when a gas path fault occurs, the parameter change may be extremely weak and difficult to monitor. It is a new idea and direction to diagnose the gas path of gas turbine based on the exergy loss [19–25]. According to the second law of thermodynamics, we know that the exergy efficiency is an important indicator to measure the irreversibility of the work of the thermal system. The exergy loss is an actual loss in the process of energy conversion. Therefore, it is more suitable to describe the function of a thermal system. And when the fault occurs, the change of the exergy loss is greater than the rest of the thermal parameters, which can improve the sensitivity of the diagnosis. In recent years, on the basis of exergy research, some scholars have proposed the concept of thermoeconomic [26–29], not only based on the second law of thermodynamics, but also introduced the basic ideas of system engineering, optimization theory, and decision theory, capable of analyzing complex energy systems.

When a gas turbine fault occurs, the exergy loss of the gas turbine is divided into exogenous irreversible loss and endogenous irreversible loss (EIL) [30–32]—where the EIL can better characterize the impact of the gas turbine component itself, and the complicated coupling relationship of gas turbines and the EIL of internal sources may also change when other components fail. Therefore, the use of the EIL for fault diagnosis is the key research content of this paper.

At present, most of the fault diagnosis based on the exergy balance analysis principle of gas turbines is on industrial single-shaft or two-shaft gas turbines, while there are few studies on marine three-shaft gas turbines. Furthermore, the coupling relationship of the three-shaft marine gas turbine is more complicated. The operating environment of the marine gas turbine is more complicated and harsh than the industrial gas turbine, and the operating conditions are more variable. A new fault diagnosis method suitable for the marine three-shaft gas turbine is urgently needed.

In this regard, we have conducted the following research. In Section 2, the EIL models of the marine gas turbine under healthy and faulty are established. In Section 3, the diagnosis process based on the EIL is established. In Section 4, taking marine three-shaft gas turbine as the object, a fault diagnosis algorithm based on EIL is proposed, which is used for the verification of the algorithm under the condition of typical gas path fault.

2. EIL Model of Gas Turbine

Slight changes in performance parameters may cause changes in multiple thermal parameters of marine gas turbines under different operating conditions. Slight changes in thermal parameters are difficult to identify, causing problems with diagnostic difficulties. On the basis of the second law of thermodynamics, the use of exergy balance has better sensitivity for fault diagnosis of marine gas turbine gas paths.

This section introduces the exergy balance analysis method and establishes its physical structure and productive structure by analyzing the working principle of the marine gas turbine. Then, based on the nonlinear model of the marine gas turbine [33], the EIL model of marine gas turbine is established.

2.1. EIL Analysis of Gas Turbine

The exergy analysis method is based on the second law of thermodynamics, which provide a method to measure the actual performance and identify the causes of thermodynamic losses. Since the energy of different forms has mutual conservation of mass and qualitative difference, the two properties are different. As a physical quantity for evaluating energy value, exergy is a physical quantity that reflects both the "mass" and "quantity" of energy. In various forms of energy, such as mechanical energy, electrical energy, etc. which can all be converted into heat energy, the theoretical conversion efficiency is close to 100%, and this kind of energy that can be converted infinitely is called exergy, which is recorded as *B*.

Exergy loss occurs in any actual process, that is, a portion of the fuel exergy is lost during the production process. Using the definition of fuel and product, the process component exergy balance can be expressed as:

$$F = P + I \tag{1}$$

where *F* represents the component fuel, *P* which represents the component product, and *I* represents the loss of exergy of the component.

Therefore, fuel consumption is also related to the EIL of the process (exergy loss), which can be characterized by the unit consumption *k*.

$$k = F/P \tag{2}$$

When a gas path fault occurs in a marine gas turbine, the exergy must change. The changed part is composed of endogenous irreversible loss (EIL) and exogenous irreversible loss. The EIL can characterize the impact of fault for the marine gas turbine unit itself better. At the same time, due to the complex coupling relationship of the gas turbine, the EIL may also change greatly when other components fail. Compared with the other thermodynamic parameters for fault diagnosis, the EIL for fault diagnosis increases its sensitivity, and the number of parameters used is reduced, which simplifies the complexity of diagnosis. Thus, it is a new research direction.

According to the definition of "fuel-product" [34,35], in the normal condition, the product of the former component is the fuel of the latter component, and the rest is the exergy loss. When the component fault occurs, it causes additional exergy loss of the component, i.e., ΔP , and the required fuel also increases, i.e., ΔF .

Due to the complex coupling relationship of gas turbines, the "fuel-products" between the various components are linked. Taking two components as an example in Figure 1:



(b) Fault condition

Figure 1. Production relationship between fuel in normal/fault condition.

The expression is:

$$F_1 = P_1 + I_1, F_2 = P_2 + I_2, P_1 = F_2$$
(3)

The unit loss means that the exergy loss can be expressed as:

$$I = F - P = (k - 1)P$$
(4)

The total differential of equation (4) is expressed as:

$$dI = P^0 dk + (k-1)dP \tag{5}$$

It can be seen that the exergy loss consists of two components; one is the EIL, and the other is the exogenous irreversible loss. Since the EIL can accurately reflect the changes in the operating characteristics of the equipment unit, and to some extent exclude the influence of other equipment units, it is suitable as a feature for equipment failure.

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The EIL due to the change in component unit consumption is:

$$MF = P^0 \Delta k \tag{6}$$

2.2. Physical Structure and Productive Structure of the Marine Gas Turbine

In order to exergy balance analysis, a marine gas turbine is divided into several components or process components. A process component is a functional component that has a production purpose corresponding to a real device. However, the process component is not necessarily a specific physical structure device, and different devices can be combined into one process component, or one physical structure device can be further decomposed into several process components.

The productive structure model is to facilitate the analysis of the physical structure of the system and the depreciation of each flow. The structural characteristics of the marine gas turbine were analyzed in Figure 2. It can be seen that the air (0) is compressed by the low-pressure compressor (LC) to generate the low-pressure air (1) and then continues to be compressed by the high-pressure compressor (HC) to generate high-pressure air (2). The high-pressure air (2) and the fuel (10) are fully mixed and burned in the combustion chamber (CC) to form high temperature and high-pressure gas (3). The gas (3) enters the high-pressure turbine to expand to do work, the generated energy (8) drives the high-pressure compressor to rotate, and the expanded gas (4) enters the low-pressure turbine (LC) for further expansion, the energy (9) generated by low-pressure turbine drives the low-pressure compressor to rotate. Finally, the expanded gas (5) enters the power turbine (PT) to continue to expand to do work, the generated energy (6) drives the generator(G) to generate electricity (7), and the exhaust (11) is discharged into the atmosphere. According to the energy flow and mass flow described in Figure 2, the physical structure of the gas turbine is shown in Figure 3.



Figure 2. The layout of a marine three-shaft gas turbine.



Figure 3. The physical structure of the marine three-shaft gas turbine.

As can be seen from Figure 3, the marine gas turbine is divided into six components: The low-pressure compressor, the high-pressure compressor, the combustor, the high-pressure turbine, the low-pressure turbine, and the power turbine. The generator connected to the power turbine belongs to the gas turbine. The process of physical flow is shown by the arrow, and there are 11 physical flows between components and the environment.

From the physical structure, we can establish the productive structure of the marine gas turbine, as shown in Figure 4. There are two fuels in the low-pressure compressor, one is F_1 which is supplied by the product P_5 that is produced by the low-pressure turbine, and the other is flow 0, and its exergy is equal to 0. The product of the low-pressure compressor is exergy flow P_1 . The fuel F_2 of the high-pressure compressor comes from the product of high-pressure turbine P_4 , and its product is exergy flow P_2 . The fuel of the combustor is fossil fuel F_3 , and its product is P_3 . We can see from Figure 3, the expansion gas is not fully expanded in the high-pressure turbine; it also enters low-pressure turbine and the power turbine to continue to expand, so a junction point "J" to present the sum of useful

product P_1 , P_2 , and P_3 , and a breakpoint "B" to present the relationship that product divided into three fuel flows, F_4 enters into high-pressure turbine, F_5 enters into low-pressure turbine, and F_6 enters into power turbine. P_6 is the product of the power turbine and is also the fuel of generator. It can be seen from Figure 4, the productive structure indicates a detailed analysis of the "production" and "consumption" processes of the marine gas turbine.



Figure 4. Productive structure of the marine three-shaft gas turbine.

2.3. EIL Model of Components

The establishment of the productive structure makes the resource allocation of the marine gas turbine represented graphically. According to the productive structure, the "fuel" and "product" of each process component were analyzed. The EIL model of the marine gas turbine can be established according to the productive structure.

2.3.1. EIL Model of Compressors

The compressor is one of the main components of the gas turbine, which uses the mechanical energy supplied by the low-pressure turbine to continuously compress and deliver the gas. For compressor simulation modeling, compressor characteristics are particularly important. It is necessary to obtain the flow and efficiency by converting the speed and pressure ratio. The enthalpy and entropy of equipment inlet and outlet are functions of temperature, which can be obtained by fitting equation, so as to calculate the exergy of equipment inlet and outlet.

The calculation equation of the EIL of the low-pressure compressor is:

$$MF_1 = P_1(\frac{F_1'}{P_1'} - \frac{F_1}{P_1}) \tag{7}$$

$$P_1 = h_1 - h_0 - T_0(s_1 - s_0) \tag{8}$$

$$F_1 = \frac{1}{2} J_{LCLT} \omega^2 \tag{9}$$

where h_1 is the outlet enthalpy of the low-pressure compressor and s_1 is the outlet entropy of the low-pressure compressor. MF_1 is the EIL of the low-pressure compressor, F'_1 is the fuel and P'_1 is the product of the low-pressure compressor in a fault condition, F_1 and P_1 are the fuel and the product of low-pressure compressor in normal condition.

The calculation equation of the EIL of the high-pressure compressor is:

$$MF_2 = P_2 \left(\frac{F_2'}{P_2'} - \frac{F_2}{P_2}\right) \tag{10}$$

$$P_2 = h_2 - h_0 - T_0(s_2 - s_0) - [h_1 - h_0 - T_0(s_1 - s_0)]$$
(11)

$$F_2 = \frac{1}{2} J_{HCHT} \omega^2 \tag{12}$$

where MF_2 is the EIL of high-pressure compressor, F'_2 is the fuel and P'_2 is the product of high-pressure compressor in a faulty condition, F_2 is the fuel and P_2 is the product of high-pressure compressor in normal condition.

2.3.2. EIL Model of the Combustion Chamber

The role of the combustion chamber is to mix the high-pressure air from the high-pressure compressor with the fuel injected by the fuel nozzle and burn it, then convert the chemical energy contained in the fuel into heat energy, forming high-temperature gas to enter the high-pressure turbine for work.

When there is a chemical imbalance between substance (logistics) and environment, its chemical exergy should be calculated. Although when the fuel in the environmental condition is in thermal balance with the environment, there is still chemical imbalance, so it can react with oxygen in the air to release the chemical energy of the fuel. The approximate calculation equation of liquid fuel exergy:

$$B_{xl} = 0.975 \Delta H_h \tag{13}$$

where ΔH_h is the high calorific value of the fuel, (kJ/kg).

The calculation equation of the EIL of the combustion chamber is:

$$MF_3 = P_3(\frac{F'_3}{P'_3} - \frac{F_3}{P_3})$$
(14)

$$P_3 = h_3 - h_0 - T_0(s_3 - s_0) - [h_2 - h_0 - T_0(s_2 - s_0)]$$
(15)

$$F_3 = 0.975 \Delta H_u f \tag{16}$$

$$f = \frac{G_f}{G_{Bin}} \tag{17}$$

where MF_3 is the EIL of the combustion chamber, F'_3 is the fuel and P'_3 is the product of combustion chamber in a fault condition, F_3 is the fuel and P_3 is the product of the combustion chamber in normal condition.

It can be seen from the productive structure in Figure 4 that there are three exergy flows after the combustion chamber: The product P_3 , the product of low-pressure compressor P_1 (Flow 1), and the product of high-pressure compressor P_2 (Flow 2). Therefore, the product at the junction point "J" is the sum of these three products, $P_J = P_1 + P_2 + P_3 = h_3 - h_0 - T_0(s_3 - s_0)$, and the product $P_J = P_3$ is the fuel of breakpoint "B", and it is divided into F_4 , F_5 , and F_6 . They are the fuel of the high-pressure turbine, and power turbine, respectively.

2.3.3. EIL Model of Turbines

The turbine is a kind of rotary machinery that transforms gas heat energy into mechanical energy. There are many similarities between a turbine and a compressor. The marine gas turbine has a high-pressure turbine, a low-pressure turbine, and a power turbine, whose functions are to drive the high-pressure compressor, the low-pressure compressor, and output load, respectively.

The turbine and compressor are the same turbomachinery, which exchanges energy with airflow, so they have many similarities. The enthalpy and entropy of the turbine inlet and outlet can also be obtained by fitting the equation, and then the exergy of inlet and outlet can be obtained.

As a gas turbine, the power turbine converts energy into mechanical work, which is used to drive the turbomachinery with external load (propeller, motor, etc.). Therefore, $P_6 = W_{net}$. The gas at the

outlet of the low-pressure turbine is expanded for the last time in the power turbine to output external mechanical power and exhaust gas. For the exhaust, this paper considers that there is no waste heat boiler and other devices, the exhaust is discharged to the atmospheric environment, and this energy is considered to be 0.

In addition, for the P_4 and P_5 flows in the productive structure diagram, they are the energy that the low-pressure turbine and the high-pressure turbine drive the low-pressure compressor and the high-pressure compressor to rotate. Both of these energies are mechanical energy. All mechanical energy is available energy.

The calculation equation of the EIL of the high-pressure turbine is:

$$MF_4 = P_4(\frac{F'_4}{P'_4} - \frac{F_4}{P_4})$$
(18)

$$P_4 = \frac{1}{2} J_{HCHT} \omega^2 \tag{19}$$

$$F_4 = h_3 - h_0 - T_0(s_3 - s_0) - [h_4 - h_0 - T_0(s_4 - s_0)]$$
(20)

where MF_4 is the EIL of high-pressure turbine, F'_4 is the fuel and P'_4 is the product of high-pressure turbine in a fault condition, F_4 is the fuel and P_4 is the product of high-pressure turbine in normal condition.

The calculation equation of the EIL of the low-pressure turbine is:

$$MF_5 = P_5(\frac{F'_5}{P'_5} - \frac{F_5}{P_5})$$
(21)

$$P_5 = \frac{1}{2} J_{LCLT} \omega^2 \tag{22}$$

$$F_5 = h_4 - h_0 - T_0(s_4 - s_0) - [h_5 - h_0 - T_0(s_5 - s_0)]$$
(23)

where MF_5 is the EIL of the low-pressure turbine, F'_5 is the fuel and P'_5 is the product of low-pressure turbine in a fault condition, F_5 is the fuel and P_5 is the product of low-pressure turbine in normal condition.

The calculation equation of the EIL of power turbine is:

$$MF_6 = P_6(\frac{F'_6}{P'_6} - \frac{F_6}{P_6})$$
(24)

$$P_6 = W_{net} \tag{25}$$

$$F_6 = h_6 - h_0 - T_0(s_6 - s_0) \tag{26}$$

where MF_6 is the EIL of power turbine, F'_6 is the fuel and P'_6 is the product of power turbine in a faulty condition, F_6 and P_6 are the fuel and product of power turbine in normal condition.

The change of unit exergy consumption reflects the change of component exergy efficiency, which defines the internal EIL of the equipment. This index is a problem that needs to be explored for the variation law of the equipment in case of failure and the variation law under the influence of multiple boundary conditions. This problem will be discussed in detail in Section 4.

2.4. Gas Turbine Exergy Loss Analysis Under Normal Conditions

First, the correlation matrix is introduced. The correlation matrix is the matrix connecting each exergy flow and each component in the system. If the system includes *m* component and *n* exergy flow, its correlation matrix is $A(m \times n)$, and its element a_{ij} is expressed by the following method. When the exergy flow is input into the component *i*, it is recorded as $a_{ij} = 1$; when the exergy flow is output from the component, it is recorded as $a_{ij} = -1$; when neither input nor output, it is recorded

as $a_{ij} = 0$. Through the correlation matrix, the characteristics of the whole system can be described. After introducing the correlation matrix, the exergy balance of the system can be written as

$$A \times E = I \tag{27}$$

where *E* is the exergy flow vector $[0, P_1, P_2, F_3, P_J, B_3, F_5, F_6, F_4, F_1, F_2, P_6]$; *I* is the exergy loss $[I_1, I_2, ..., I_{12}]$ of each component. Through the correlation matrix *A* and exergy flow direction *E* obtained from the above equations, and through exergy balance expression, exergy loss *I* is obtained, where *A* is as shown in the equation.

	0	-1	0	0	0	0	0	0	0	1	0	0
	0	0	-1	0	0	0	0	0	0	0	1	0
	0	0	0	1	-1	0	0	0	0	0	0	0
<u> </u>	0	0	0	0	0	0	0	0	1	0	-1	0
А —	0	0	0	0	0	0	1	0	0	-1	0	0
	0	0	0	0	0	0	0	1	0	0	0	-1
	0	1	1	0	1	-1	0	0	0	0	0	0
	0	0	0	0	0	1	-1	-1	-1	0	0	0

Thus, the EIL of each component can be obtained. According to the above equations, a gas turbine EIL model is established, which will be verified in Section 4.

3. Gas Path Fault Diagnosis Method Based on EIL

The traditional gas path fault diagnosis method is based on the first law of thermodynamics, which detects the malfunction of the component by the deviation of gas path measured variables. It can be from Figure 3, the components are interrelated, that is, result in the strong coupling effect for measured variables and the fault may not be effectively identified [18]. EIL is based on the second law of thermodynamics, which is from a comprehensive sight of the system to detect efficiency deviations and identify the causes of performance degradation, and may solve the parameter coupling problem of traditional gas path analysis method. A gas path fault diagnosis algorithm based on EIL is proposed, and its fault diagnosis process is shown in Figure 5, which consists the following steps:



Figure 5. Fault diagnosis process of the marine gas turbine in operation.

Step 1: The measured temperature variables T' were acquired from the monitoring and control system of the marine gas turbine, where $T' = [T'_1, T'_2, T'_4, T'_5, T'_6]$, T'_1 is the outlet temperature of low-pressure compressor, T'_2 is the outlet temperature of high-pressure compressor, T'_4 is the outlet temperature of low-pressure turbine, T'_5 is the outlet temperature of low-pressure turbine, T'_6 is the outlet temperature of low-pressure turbine, T'_6 is the outlet temperature of power turbine. The *Load* is the power output of the gas turbine; in this paper, we use the operating points to present the rated power. T_0 and P_0 are the environment parameters.

Step 2: The measured temperature variables T under the normal condition are estimated by the healthy estimation model that is established by back a propagation neural networks [33]. For the gas turbine healthy estimation model, the inputs are the environment parameters (T_0 , P_0) and *Load*.

Step 3: The endogenous irreversible loss *MF* of the gas turbine components under given conditions are calculated by the EIL model, which is presented in Section 2.

Step 4: The EIL model output describes the characteristics of the gas turbine under normal condition and different faulty conditions, and the diagnostic rule was obtained by statical analysis. Therefore, in this paper, a gas path fault reasoning algorithm is proposed, and its flowchart is shown in Figure 6.



Figure 6. The flowchart of the fault reasoning algorithm.

In this process, when the endogenous irreversible loss *MF* input, Rule 0 is used to detect whether the current condition is normal or not. If it is Y, the output $C_0 = 1$, and the current condition is normal. If it is N, it indicates that there is a fault, $C_0 = 0$, and then the following n diagnostic rules will be executed in parallel. For example, if the MF complies with Rule 1, then the diagnostic result of Ruel 1 is $C_1 = 1$, or else if all other rule output is 0, then the current condition is the first fault.

4. Results and Discussion of Fault Diagnosis

In this section, taking a marine three-shaft gas turbine as an example, the simulation results of the EIL under typical gas path fault are obtained, and then a simulation case was carried out to verify the fault diagnosis method based on EIL.

4.1. Exergy Loss Analysis of Marine Gas Turbine Under Normal Condition

The marine three-shaft gas turbine was divided into eight process groups, including six components and two virtual process groups. According to the productive structure of a marine three-shaft gas turbine, the marine gas turbine EIL model was established in MATLAB/Simulink, and the step size of the model was 0.2 s. The exergy loss of each process component under different operating conditions were calculated. In this simulation case, $T_0 = 20 \text{ °C } P_0 = 101.325 \text{ kPa}$, and *Load* was set to 0.5, 0.6, 0.7, 0.8, and 0.9, respectively, where 0.6 means 60% of rated power. Simulation results of exergy loss of marine three-shaft gas turbine components are shown in Table 1, and the unit is kilojoules per kilogram (kJ/kg).

Operating Condition	LC	НС	CC	HT	LT	РТ	J	В
0.5	16.59	15.62	247.15	69.59	16.45	169.75	0	0
0.6	17.21	15.98	257.84	73.51	17.14	182.69	0	0
0.7	18.17	16.34	267.89	77.26	17.78	196.20	0	0
0.8	18.86	16.78	277.04	80.72	18.39	209.21	0	0
0.9	19.61	17.05	285.58	83.95	18.97	221.68	0	0

Table 1. Simulation results of exergy loss of marine three-shaft gas turbine components.

It can be seen from the Table 1 that the exergy losses of components are different under the same operating condition, the exergy loss of combustion chamber is the highest, which is because the exergy loss is very large in the combustion process, and the exergy loss of power turbine is also relatively high. Therefore, the simulation results are in accordance with the thermodynamic law. The degree of exergy loss for a component only increases slightly with the increase of operating conditions, which indicates that exergy loss can be used to characterize the impact of faults on components more stable, and this advantage is helpful for fault isolation. The junction point and breakpoint are virtual components, then the exergy loss of them is 0.

4.2. Fault Reasoning Rules of the Typical Gas Path Fault Conditions

4.2.1. Simulation of Gas Turbine EIL Under Fault Condition

The magnitude of the EIL is mainly related to the fault of the system itself, and many scholars regard it as an important condition of fault isolation. Therefore, the variation law of the EIL under the complex boundary conditions, which is the combination of environment temperature and operating conditions, was studied and analyzed on the marine gas turbine EIL model, and the EIL reasoning rule of typical gas path fault is obtained.

A total of 35 boundary conditions were set in Figures 7 and 8, consisting of five operating conditions (0.5–0.9) and seven temperature conditions (0–30 °C, 5 °C steps). The simulation step of the exergy balance simulation model was set to 0.2 s and simulation time set to 1050 s, that is, 5250 simulation experiments were performed for a typical fault condition, and 11 typical fault conditions, including normal condition and 10 fault conditions, are shown in Table 2.



Figure 7. The setting of operating conditions.



Figure 8. The setting of environment temperature.

Case	LC		HC		HT		LT		PT	
	$\Delta \eta_{LC}$	ΔG_{LC}	$\Delta \eta_{HC}$	ΔG_{HC}	$\Delta \eta_{HT}$	ΔG_{HT}	$\Delta \eta_{LT}$	ΔG_{LT}	$\Delta \eta_{PT}$	ΔG_{PT}
<i>C</i> ₀	0	0	0	0	0	0	0	0	0	0
C_1	-5	0	0	0	0	0	0	0	0	0
C_2	0	-5	0	0	0	0	0	0	0	0
C_3	0	0	-5	0	0	0	0	0	0	0
C_4	0	0	0	-5	0	0	0	0	0	0
C_5	0	0	0	0	-5	0	0	0	0	0
C_6	0	0	0	0	0	-5	0	0	0	0
C_7	0	0	0	0	0	0	-5	0	0	0
C_8	0	0	0	0	0	0	0	-5	0	0
C_9	0	0	0	0	0	0	0	0	-5	0
C_{10}	0	0	0	0	0	0	0	0	0	-5

Table 2. Typical fault models of marine gas turbine.

In Table 2, C_i represents a kind of component fault state. Where C_0 represents normal condition, C_1 represents a 5% decrease in low-pressure compressor efficiency, C_2 represents a 5% decrease in low-pressure compressor flow, C_3 represents a 5% decrease in high-pressure compressor efficiency, C_4 represents a 5% decrease in high-pressure compressor flow, C_5 represents a 5% decrease in high-pressure turbine efficiency, and C_6 represents 5% decreases in high-pressure turbine flow, C_7 represents a 5% decrease in low-pressure turbine efficiency, C_8 represents a 5% decrease in low-pressure turbine flow, C_9 represents a 5% decrease in power turbine efficiency, and C_{10} represents a 5% decrease in power turbine flow.

4.2.2. Variation Law of Component EIL Under Typical Fault Condition

It can be seen from Figure 5 that there are six temperature-measured variables in the gas turbine monitoring and control system. Therefore, there are four component EIL that can be monitored in practice, that is the low-pressure compressor, the high-pressure compressor, the low-pressure turbine, and the power turbine. The fault factors were implanted in the EIL model to get the distribution of the EIL of each component. Based on the typical fault simulation result in Section 4.2.1, the variation laws of the four component EIL results are shown in Figure 9.



⁽d) EIL range of power turbine

Figure 9. Distribution law of the EIL of various systems under marine gas turbine failure.

The maximum value, minimum value, and standard deviation of each component EIL under typical fault condition were obtained. Take C_1 (5% decrease in low-pressure compressor efficiency) as an example, the maximum value, minimum value, and standard deviation of the EIL under 35 boundary conditions are shown in Table 3.

Parameter	LC	НС	LT	РТ
MF_max	6.48	0.01	0.11	13.16
MF_min	5.38	-0.38	-0.04	9.50
MF_std	0.27	0.02	0.01	0.50

Table 3. The variation law of the EIL under typical fault condition C_1 .

From Figure 9, it can clearly be seen that the distribution range of the EIL of each component is unique when different faults occurred. Therefore, it is feasible to use the EIL for fault detection and isolation of the marine three-shaft gas turbine.

4.2.3. Gas Path Fault Reasoning Rules

Firstly, the false alarm rate *Fr* and missing alarm rate *Mr* are introduced as fault diagnosis criteria.

$$Fr = \frac{M}{R - T} \times 100\%$$
⁽²⁸⁾

$$Mr = \frac{N}{T} \times 100\%$$
⁽²⁹⁾

where *M* is the number of the false alarm, *N* is the number of missing alarm, *T* is the number of experiment samples for each fault pattern, and *R* is the total number of experiment samples.

It is necessary to judge whether there is a fault in the system. When there is no fault, the EIL of the marine gas turbine component should be zero in theory. However, in practice, due to the noise, the EIL of the system is not zero, but a very small number close to zero. Therefore, for the reasoning rule of the normal condition, the setting of the threshold value of the EIL needs to be discussed.

$$\cap abs(MF_i) < X \tag{30}$$

where *i* represents the components of the marine gas turbine, and *X* represents the value of the threshold. Suppose *X* equals 0.1, 0.2, 0.3, 0.4, and 0.5 respectively, and the false alarm rate and missing alarm rate are shown in Table 4, respectively.

X	F _r	M_r
0.1	6.52%	0.04%
0.2	5.84%	0%
0.3	5.48%	0%
0.4	5.12%	0.04%
0.5	4.880%	0.08%

Table 4. Relationship between the threshold and diagnostic criteria.

It can be seen from the table that the false alarm rate F_r has a slight downward trend with increasing the threshold, while the missing alarm rate M_r is zero when X equals 0.2 or 0.3.

On the basis of the gas path fault diagnosis method introduced in Section 3, according to the EIL distribution of components under 10 typical fault conditions in Figure 9, the fault reasoning rules are shown in Table 5.

Number	Condition	Fault Vector
Rule 0	$0 \le \left MF(i) \right < 0.3$	[10000000000]
Rule 1	$5.38 \le MF_{LC} \le 6.48$	$[0\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]$
Rule 2	$\begin{array}{rcl} 0.001 < MF_{LC} \leq 0.77 & \& & 0.001 < MF_{PT} \leq 1.55 \\ \& -0.07 \leq MF_{HC} \leq 0.01 \end{array}$	$[0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 0]$
Rule 3	$4.40 \le MF_{HC} \le 5.29$	$[0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0]$
Rule 4	$\begin{split} MF_{LC} &\leq -0.001 \& 0.64 \leq MF_{HC} \leq 1.11 \\ \& -0.04 \leq MF_{LT} \leq 0.01 \& 0.63 \leq MF_{PT} \leq 1.70 \end{split}$	$[0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0]$
Rule 5	$9.67 \le MF_{PT} \le 13.16$	$[0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0]$
Rule 6	$\begin{split} MF_{LC} &> 0.001 & MF_{HC} < -0.001 \\ \& & -3.92 \leq MF_{LT} \leq -2.67 & -4.23 \leq MF_{PT} \leq -1.96 \end{split}$	[00000010000]
Rule 7	$3.67 \le MF_{LT} \le 4.36$	$[0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ 0]$
Rule 8	$\begin{split} MF_{LC} < -0.001 & \& & MF_{HC} < -0.001 \\ \& & -1.43 \leq MF_{LT} \leq -1.08 & -6.05 \leq MF_{PT} \leq -2.50 \end{split}$	$[0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0]$
Rule 9	$16.30 \le MF_{PT} \le 26.21$	$[0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0]$
Rule 10	$\begin{array}{rrr} 0.43 < MF_{LC} < 1.50 & \& & -0.05 < MF_{HC} \leq 0.22 \\ \& & 1.51 < MF_{LT} \leq 2.01 & \& & 1.77 < MF_{PT} \leq 3.77 \end{array}$	[00000000001]

Table 5. Fault reasoning rules of the marine three-shaft gas turbine.

According to Figure 6, IF and ELSE-IF logic statements are used to fault reasoning, and the fault diagnosis result is expressed in the fault vector *C*.

4.3. Fault Diagnosis of Marine Gas Turbine

In this section, using the marine gas turbine model to present the actual marine gas turbine [33], which was established in Matlab/Simulink, and the simulation method is the fourth-order ode14x (extrapolation with fixed time step), the simulation step is 0.2 s. In the test case, the gas turbine works under the transient condition, the operating condition is increased from 0.5 to 0.9 in 500 s with the variable environment temperature that is between 0 and 30 °C, as shown in Figures 10 and 11.



Figure 10. The operating condition setting of marine gas turbine.



Figure 11. The ambient temperature setting of marine gas turbine.

Suppose gas turbine works in 30 s under normal condition C_0 , then a fault occurred for 20 s. Ten typical faulty conditions C_1, C_2, \dots, C_{10} occurred separately in sequence. The fault simulation setting is shown in Figure 12. Therefore, the total number of test samples is 2501, the number of normal test samples is 1001, and the number of test samples for each fault is 150.



Figure 12. Settings of simulation fault.

The measured variables under the normal condition are on-line estimate by the healthy estimation model, then using the EIL model to calculate the EIL of each component under this test case, and the results of the EIL are shown in Figure 13.



Figure 13. Component EIL change of marine gas turbine under simulated fault.

Figure 13 shows the change process of the EILs of the low-pressure compressor, high-pressure compressor, low-pressure turbine, and power turbine, and the EIL will change abruptly at the moment of gas path fault implantation.

Finally, the *MFs* of component EIL input the fault reasoning algorithm. Rule 0 is used to detect the current status of the marine gas turbine, whether it is normal or not. The diagnosis result is μ_0 , 1 represents the normal condition, and 0 represents the faulty condition. When a fault is detected, ten typical fault reasoning rules execute in parallel to isolate which fault occurred, the fault reasoning results are $\mu_1 \sim \mu_{10}$, which is the value of element C_1, \dots, C_{10} of fault vector *C*. The fault reasoning results are shown in Figure 14, and it shows that the marine gas turbine diagnosis method based on EIL can diagnose the gas path fault correctly. The EIL has good sensitivity to the gas path fault, the reasoning rule will change in time when the hypothesis fault occurred. At the same time, through experiments, it is found that missing alarms generally occur at the switching time of normal condition and fault condition, so the fault detection time is introduced, which is the product of the time step and the missing alarm. The false alarm, missing alarm, and detection time are shown in Table 6.



Figure 14. Diagnosis results of the marine gas turbine system.

Mode	Т	R-T	\boldsymbol{M}	N	False Alarm Rate	Missing Alarm Rate	Detection Time
<i>C</i> ₀	1001	1500	12	16	0.08%	1.60%	0.8 s (max)
C_1	150	2351	0	3	0.00%	2.00%	0.6 s
C_2	150	2351	1	8	0.04%	5.33%	1.6 s
C_3	150	2351	0	0	0.00%	0.00%	0 s
C_4	150	2351	0	11	0.00%	7.33%	2.2 s
C_5	150	2351	15	12	0.64%	8.00%	2.4 s
C_6	150	2351	0	12	0.00%	8.00%	2.4 s
C_7	150	2351	20	7	0.85%	4.67%	1.4 s
C_8	150	2351	0	22	0.00%	14.67%	4.4 s
C_9	150	2351	1	1	0.04%	0.67%	0.2 s
C_{10}	150	2351	0	20	0.00%	13.33%	4 s

Table 6. Results of false alarm, missing alarm, and detection time.

In Table 6, the total number of experiment samples *R* is 2501. The performance of fault detection of the proposed gas path fault diagnosis method based on EIL can be seen from the false alarm rate and missing alarm rate of normal condition C_0 , the number of normal condition experiment samples is 1001, the number of false alarm is 12, and the number of missing alarm is 16, so the false alarm rate is 0.08% and the missing alarm rate is 1.6%. When the marine gas turbine returns to normal condition, the maximum detection time needs 4 time steps, that is, 0.8 s. The simulation results show that the performance of the gas path fault diagnosis method can detect fault quickly and accurately.

The performance of fault isolation of the proposed gas path fault diagnosis based on EIL can be seen from the false alarm rate and missing alarm rate of the fault condition C_1, C_2, \ldots, C_{10} . Although the missing alarm rate is slightly higher, the proposed gas path fault diagnosis method can isolate fault accurately. The false alarm rate is less than 1% which shows that the diagnostic reasoning rules based on EIL are robust under complex operating conditions and environments.

The missing alarm of C_8 and C_{10} is high, because the transition time from the normal condition to fault condition of the marine gas turbine model is long in the simulation test.

5. Conclusions

In this paper, a gas path fault diagnosis method based on EIL has been presented to detect and isolate the gas path faults of marine gas turbines. The EIL of component models were established to characterize exergy loss under the normal condition and typical gas path fault condition. The EIL is sensitive to gas path fault, and it is not affected by the change of operating condition and environment. Therefore, the diagnostic reasoning rules based on EIL are robust, and are helpful for detecting and isolating gas path faulty components.

Simulation case studies on a three-shaft marine gas turbine were conducted, and the performance of the proposed method for the detection and isolation of typical gas path fault was analyzed. The simulation results show that the proposed EIL-based gas path fault diagnosis method detect and isolate gas path fault accurately.

In this paper, the feasibility of the gas path fault diagnosis based on EIL was verified by single gas path fault. In the future, we will improve the performance of the proposed method under transient process. Furthermore, we will continually evaluate the multiple gas path fault diagnosis performance of the proposed method and also study hybrid diagnostic approaches combining EIL with artificial intelligence algorithms.

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